

# LFV, R-parity, and invisible particles in rare decays with missing energy



Christopher Smith

# Introduction

*The goal of this talk:*

Characterization of some NP effects in the very rare decays

$$K \rightarrow \pi + \text{missing energy}$$

$$B \rightarrow (\pi, K, K^*) + \text{missing energy}$$

*The outline of this talk:*

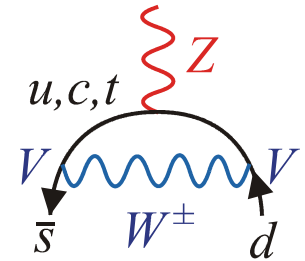
- I. *Observables & kinematics*
- II. *Lepton flavor violating effects*
- III. *Signals of R-parity violation*
- IV. *Very light invisible particles*

*Conclusion*

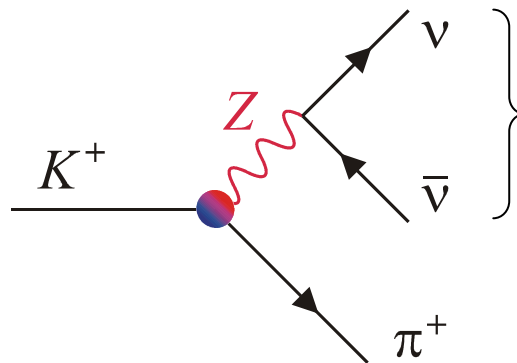
# I. Observables & Kinematics

A. The  $K \rightarrow \pi\nu\bar{\nu}$  decays

	SM ( $\times 10^{-11}$ )	Experiment
$K_L \rightarrow \pi^0 \nu\bar{\nu}$	$2.57^{+0.37}_{-0.37}$	$< 6.7 \cdot 10^{-8}$ E391a
$K^+ \rightarrow \pi^+ \nu\bar{\nu}(\gamma)$	$8.22^{+0.75}_{-0.75}$	$17.3^{+11.5}_{-10.5} \cdot 10^{-11}$ E787 E949



Only the pion is seen, whose energy is not fixed (three-body decay).

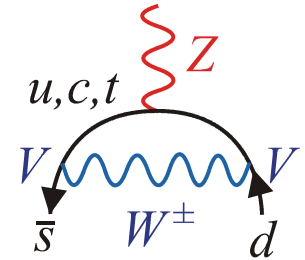


Missing "energy":  $z = (p_\nu + p_{\bar{\nu}})^2 / m_K^2$

Pion momentum:  $|\mathbf{p}_\pi| = \frac{m_K}{2} \lambda(1, z, r_\pi^2)$

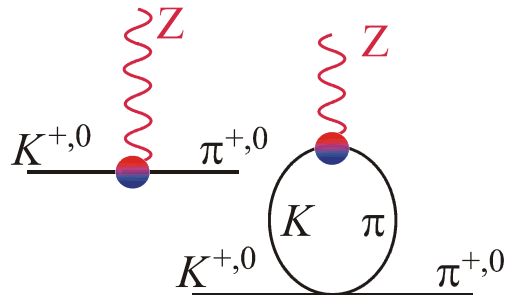
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Z penguin & W boxes lead to the interaction  $\bar{s} \gamma^\mu (1 - \gamma_5) d \otimes \bar{\nu} \gamma_\mu (1 - \gamma_5) \nu$ .

Hadronic matrix element:  $\langle \pi | \bar{s} \gamma^\mu d | K \rangle \approx f(z) (p_K + p_\pi)^\mu$ ,  $f(z) \approx \frac{1}{1 - z/m_{K^*}^2}$ ,

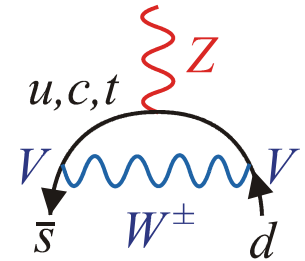


- $f(0) \approx 1$  (Ademollo-Gatto Theorem),
- Vector meson dominance away from zero.

Chiral & isospin corrections (partial NNLO) are estimated using  $K_{\ell 3}$  decays.

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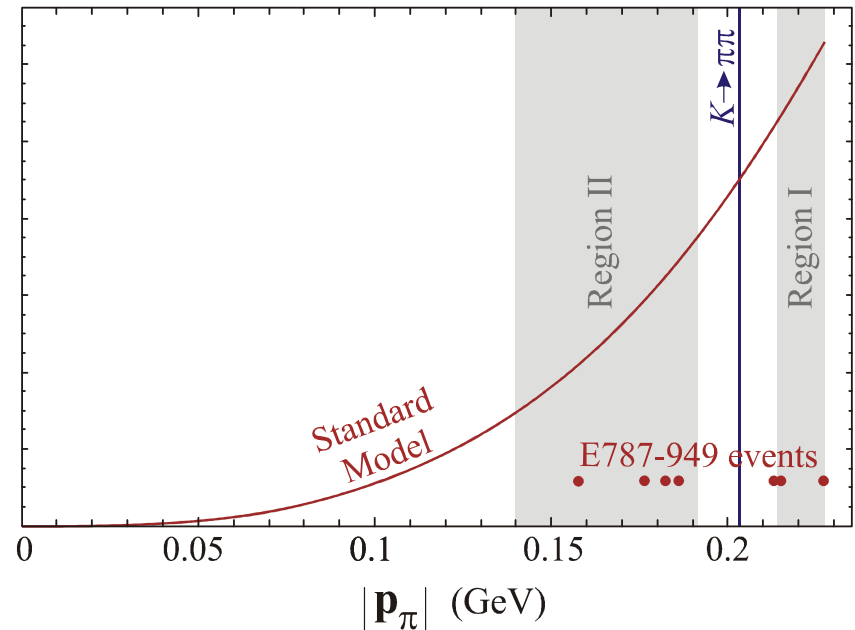
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The observable differential rate is

$$\frac{\partial \ln \Gamma}{dz} \sim \frac{|\mathbf{p}_\pi|^3}{m_K^3} |f(z)|^2$$

Essential for the necessarily aggressive background rejection.



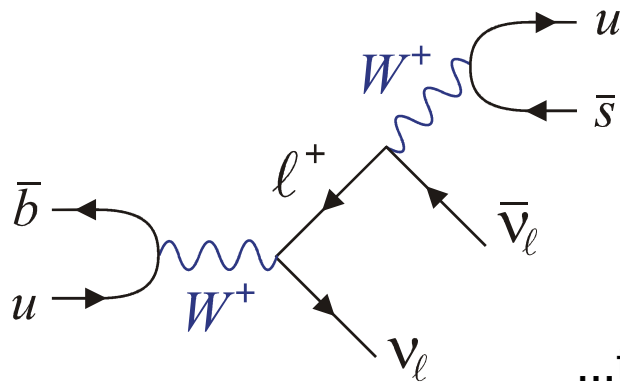
**Important messages:** V-A current assumed & kinematical range limited.

## B. The $B^+ \rightarrow (\pi^+, K^{(*)+}) \nu \bar{\nu}$ decays

Charged decays are intimately connected to  $B \rightarrow \bar{\nu}_\tau \tau [\rightarrow (\pi, K, K^*) \nu_\tau]$  .

See talk by J. Kamenik.

Tree-level dim-8 contributions to all charged  $\nu \bar{\nu}$  rare decays:



$$\sim G_F^2 V_{ub} V_{us}^* \times \frac{p_\ell^2}{p_\ell^2 - m_\ell^2 + im_\ell \Gamma_\ell} \times \bar{u}_\nu p_\ell (1 - \gamma_5) \nu_{\bar{\nu}}$$

...to be compared to the dim-6 penguin  $\sim G_F \alpha V_{tb} V_{ts}^*$  .

Hence, sizeable only for  $\ell = \tau$  which is kinematically allowed to be on-shell:

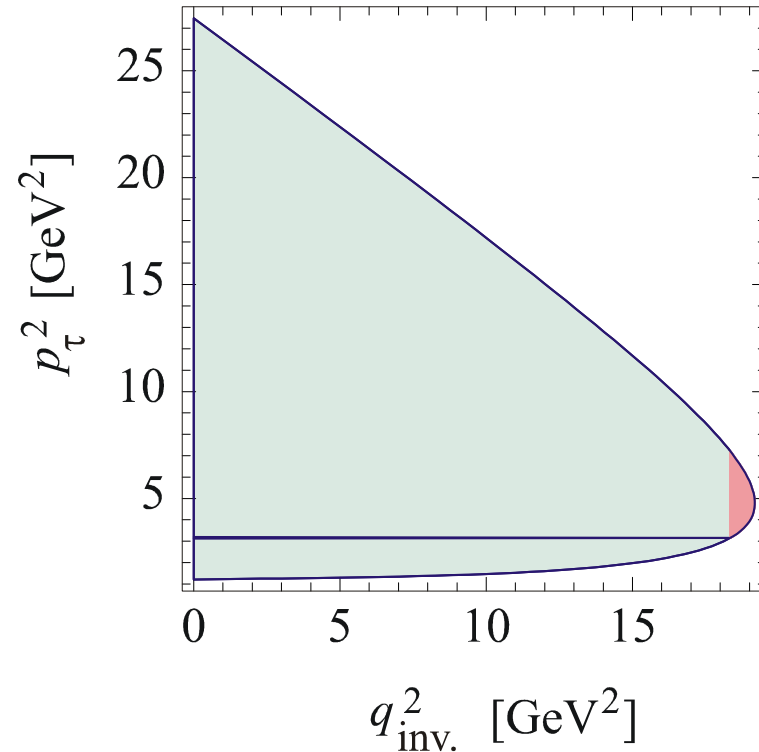
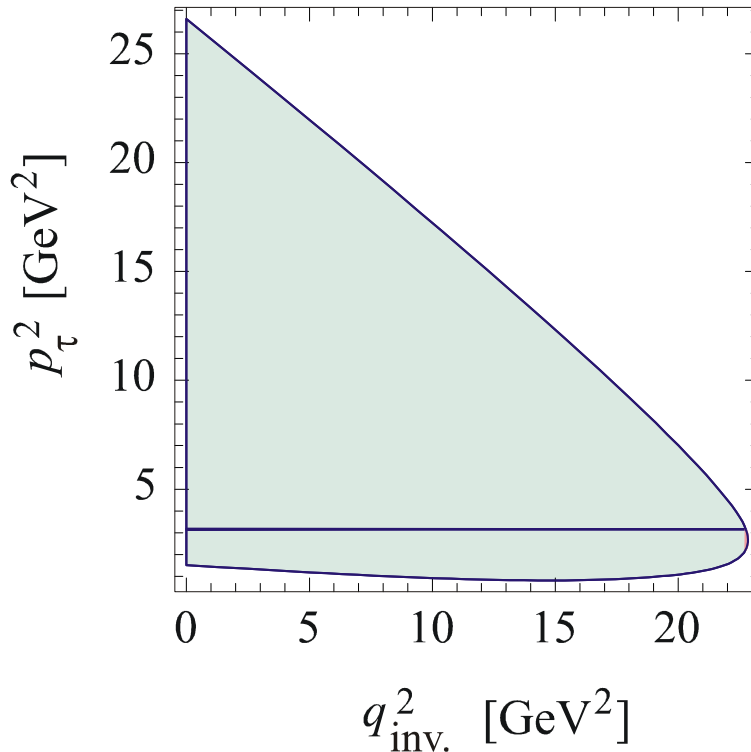
- *K decays*: Helicity suppression inactive  $\rightarrow$  negligible dim-10 effect.
- *B decays*: The  $\tau$  pole in  $\Gamma_\tau^{-1} \sim G_F^{-2}$  makes it potentially dominant.

(note the inverted CKM scaling of the pole and penguin)



*B. The  $B^+ \rightarrow (\pi^+, K^{(*)+})\nu\bar{\nu}$  decays*

*Entanglement:* the  $\tau$  pole runs over the whole missing energy range.



Note: the differential rates for the pole and loop have similar dependences on  $q^2$ .

*B. The  $B^+ \rightarrow (\pi^+, K^{(*)+})\nu\bar{\nu}$  decays*

$\times 10^{-6}$	$\tau$ pole	Direct SD	Ratio
$B^+ \rightarrow \pi^+\nu\bar{\nu}$	9.4(2.1)	0.16(4)	$SD / \tau = 2\%$
$B^+ \rightarrow K^+\nu\bar{\nu}$	0.61(13)	4.5(7)	$\tau / SD = 14\%$
$B^+ \rightarrow K^{*+}\nu\bar{\nu}$	1.2(3)	7.2(1.1)	$\tau / SD = 17\%$

$B^+ \rightarrow \nu_\tau \tau^+ [\rightarrow e\nu_e, \mu\nu_\mu]$  : Safe, no pollution from  $b \rightarrow (s, d)\nu\bar{\nu}$ .

$B^+ \rightarrow \nu_\tau \tau^+ [\rightarrow \pi^+\bar{\nu}_\tau]$  : 2% pollution by the direct  $b \rightarrow d\nu\bar{\nu}$  transition.

Any NP in  $b \rightarrow d\nu\bar{\nu}$  is essentially inaccessible.

$B^+ \rightarrow \nu_\tau \tau^+ [\rightarrow K^{(*)+}\bar{\nu}_\tau]$  : 600-700% apparent enhancement due to  $b \rightarrow s\nu\bar{\nu}$ .

Sensitive to NP through both  $B \rightarrow \nu_\tau \tau$  and  $b \rightarrow s\nu\bar{\nu}$ .

Alternatively:  $B^0 \rightarrow X_{s,d}^0 \nu\bar{\nu}$  or  $B_c^+ \rightarrow D_s^+ \nu\bar{\nu}$  induced purely by  $b \rightarrow (s, d)\nu\bar{\nu}$ .

Lepton flavor violating effects

*A. Effective operators for  $P \rightarrow P' \nu^I \bar{\nu}^J$  and  $P \rightarrow P' \ell^I \bar{\ell}^J$*

Assume the matter content is that of the SM:

$$Q = \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad U = u_R^\dagger, \quad D = d_R^\dagger, \quad L = \begin{pmatrix} \nu_L \\ \ell_L \end{pmatrix}, \quad E = \ell_R^\dagger$$

Five dimension-six gauge-invariant structures can be constructed:

$$\begin{array}{ccc} \bar{Q}\Gamma_i Q \otimes \bar{L}\Gamma^i L & \bar{Q}\Gamma_i Q \otimes E\Gamma^i \bar{E} & \bar{Q}\Gamma_i \bar{D} \otimes E\Gamma^i L \\ D\Gamma_i \bar{D} \otimes \bar{L}\Gamma^i L & D\Gamma_i \bar{D} \otimes E\Gamma^i \bar{E} & \end{array}$$

Contributes to  $P \rightarrow P' \nu^I \bar{\nu}^J$  and  $P \rightarrow P' \ell^I \bar{\ell}^J$ .

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Five dimension-six gauge-invariant structures can be constructed:

$$\mathcal{H}_{eff} = \frac{C^{IJKL}}{\Lambda_{NP}^2} \left( \begin{array}{cc} \bar{Q}^I \Gamma_i Q^J \otimes \bar{L}^K \Gamma^i L^L & \bar{Q}^I \Gamma_i Q^J \otimes E^K \Gamma^i \bar{E}^L \\ D^I \Gamma_i \bar{D}^J \otimes \bar{L}^K \Gamma^i L^L & D^I \Gamma_i \bar{D}^J \otimes E^K \Gamma^i \bar{E}^L \end{array} \quad \bar{Q}^J \Gamma_i \bar{D}^I \otimes E^K \Gamma^i L^L \right)$$

Contributes to  $P \rightarrow P' \nu^I \bar{\nu}^J$  and  $P \rightarrow P' \ell^I \bar{\ell}^J$ .

New Physics flavor puzzle: If all the  $C^{IJKL} \sim 1$ , then  $\Lambda_{NP} \gg 1$  TeV.

## B. What Minimal Flavor Violation can say

- The gauge interactions exhibit the  $U(3)^5$  flavor symmetry:

$$G_f = U(3)^5 = U(3)_Q \times U(3)_U \times U(3)_D \times U(3)_L \times U(3)_E$$

Chivukula,  
Georgi '87

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- The only sources of breaking are the fermionic Yukawa and mass terms:

$$\begin{aligned} \mathcal{L}_{matter} &= U\mathbf{Y}_u(QH) + D\mathbf{Y}_d(QH^*) + E\mathbf{Y}_e(LH^*) + N\mathbf{M}N + N\mathbf{Y}_\nu(LH) \\ &\rightarrow U\mathbf{Y}_u(QH) + D\mathbf{Y}_d(QH^*) + E\mathbf{Y}_e(LH^*) + (LH)^T \mathbf{Y}_\nu^T \mathbf{M}^{-1} \mathbf{Y}_\nu(LH) \end{aligned}$$

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- *Artificially invariance under  $G_f$*  created when the breaking terms are **spurions**.

With them, all the *effective operators are made invariant under  $G_f$*  .

Hall, Randall '90  
D'Ambrosio, Giudice,  
Isidori, Strumia '02



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- Artificially invariance under  $G_f$  created when the breaking terms are spurions.

- The spurions are frozen back to their physical values:

$$\text{Dirac masses: } \nu\mathbf{Y}_u = m_u V_{CKM}, \quad \nu\mathbf{Y}_d = m_d, \quad \nu\mathbf{Y}_e = m_e,$$

Hall, Randall '90  
D'Ambrosio, Giudice,  
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$$\text{Majorana masses: } \nu^2 \mathbf{Y}_\nu^T \mathbf{M}^{-1} \mathbf{Y}_\nu = U_{PMNS}^* \mathbf{m}_\nu U_{PMNS}^\dagger,$$

Cirigliano, Grinstein  
Isidori, Wise '05

Note:  $\mathbf{m}_\nu \sim 1\text{eV}$  with  $\mathbf{Y}_\nu \sim \mathcal{O}(1)$  when  $\mathbf{M} \sim 10^{13} \text{ GeV}$ .

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Casas, Ibarra '01,  
Pascoli, Petcov,  
Yaguna '03,...

$$\text{LFV spurion: } v^2 \mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu = M_R U_{PMNS} \mathbf{m}_\nu^{1/2} e^{2i\Phi} \mathbf{m}_\nu^{1/2} U_{PMNS}^\dagger, \quad \Phi^{IJ} = \varepsilon^{IJK} \phi_K.$$

*B. What Minimal Flavor Violation can say*

Chiral suppressions:

Quark transitions:	$\bar{Q}Q \rightarrow \bar{Q}^I (\mathbf{Y}_u^\dagger \mathbf{Y}_u)^{IJ} Q^J$	$\sim 1$
	$D\bar{D} \rightarrow D^I \mathbf{Y}_d^{II} (\mathbf{Y}_u^\dagger \mathbf{Y}_u)^{IJ} \mathbf{Y}_d^{\dagger JJ} \bar{D}^J$	$\sim \mathbf{m}_{d^I} \mathbf{m}_{d^J} / v^2$
	$DQ \rightarrow D^I \mathbf{Y}_d^{II} (\mathbf{Y}_u^\dagger \mathbf{Y}_u)^{IJ} Q^J$	$\sim \mathbf{m}_{d^I} / v$
Lepton transitions:	$\bar{L}L \rightarrow \bar{L}^I (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} L^J$	$\sim 1$
	$E\bar{E} \rightarrow E^I \mathbf{Y}_e^{II} (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} \mathbf{Y}_e^{\dagger JJ} \bar{E}^J$	$\sim \mathbf{m}_{\ell^I} \mathbf{m}_{\ell^J} / v^2$
	$EL \rightarrow E^I \mathbf{Y}_e^{II} (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} L^J$	$\sim \mathbf{m}_{\ell^I} / v$

So, the dominant operator is  $\bar{Q}^I (\mathbf{Y}_u^\dagger \mathbf{Y}_u)^{IJ} Q^J \otimes \bar{L}^I (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} L^J$  .

### C. Numerics (rough preliminary outline)

$$\frac{1}{\Lambda^2} \bar{Q}^I (\mathbf{Y}_u^\dagger \mathbf{Y}_u)^{IJ} Q^J \otimes \bar{L}^I (a_0 \mathbf{1} + a_1 \mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} L^J$$

*Lepton-flavor conserving:*

$$b \rightarrow s : |V_{tb}^* V_{ts}| \sim 10^{-2}, \quad b \rightarrow d : |V_{tb}^* V_{td}| \sim 10^{-3}, \quad s \rightarrow d : |V_{ts}^* V_{td}| \sim 10^{-4}$$

$$\text{So, for } \Lambda \lesssim 1 \text{ TeV, } \frac{\Gamma_{NP}^{LFC}}{\Gamma_{SM}} (P \rightarrow P' \nu^I \bar{\nu}^I, P' \ell^I \bar{\ell}^I) \lesssim 1.$$

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*Lepton-flavor violating:*

Since  $m_\nu \sim Y_\nu^2 / M$ , take  $M$  sufficiently large so that  $Y_\nu \sim \mathcal{O}(1)$ .

$$\text{But, } \mathbf{Y}_\nu \text{ is bounded by } \mathcal{H}_{\text{eff}} (\ell \rightarrow \ell' \gamma) = \frac{e}{\Lambda^2} E^I \mathbf{Y}_e^H (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{IJ} \sigma^{\mu\nu} L^J H^\dagger F_{\mu\nu}.$$

$$\text{So, conservatively, } (\mathbf{Y}_\nu^\dagger \mathbf{Y}_\nu)^{I \neq J} < 1\% \text{ for } \Lambda \lesssim 1 \text{ TeV, and } \frac{\Gamma_{NP}^{LFV}}{\Gamma_{NP}^{LFC}} \lesssim 10^{-4}.$$

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In other words, when  $I \neq J$ , MFV says:

$$Br_{NP}^{LFV} (K \rightarrow \pi \nu^I \bar{\nu}^J, \pi \ell^I \bar{\ell}^J) < 10^{-15}$$

$$Br_{NP}^{LFV} (B \rightarrow (\pi, K) \nu^I \bar{\nu}^J, (\pi, K) \ell^I \bar{\ell}^J) < 10^{-10}$$

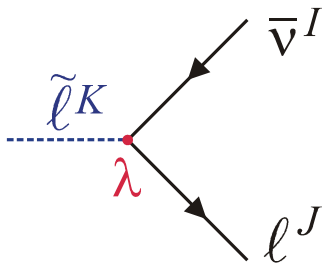
R-parity violation

A. The MSSM without R-parity

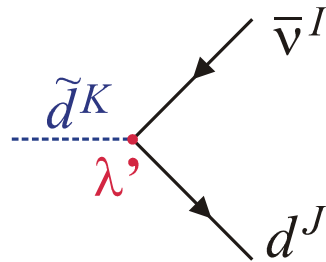
With scalar squarks & sleptons, renormalizable couplings can violate  $\mathcal{B}$  or  $\mathcal{L}$ :

$$\mathcal{W}_{RPV} = \underbrace{\mu'^I L^I H_d + \lambda^{IJK} L^I L^J E^K + \lambda'^{IJK} L^I Q^J D^K}_{\Delta\mathcal{L} = 1} + \underbrace{\lambda''^{IJK} U^I D^J D^K}_{\Delta\mathcal{B} = 1}$$

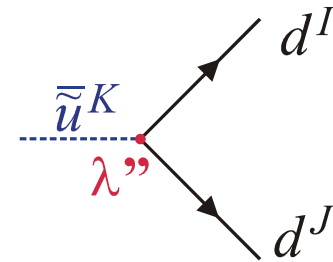
Dilepton currents:



Leptoquark currents:



Diquark currents:



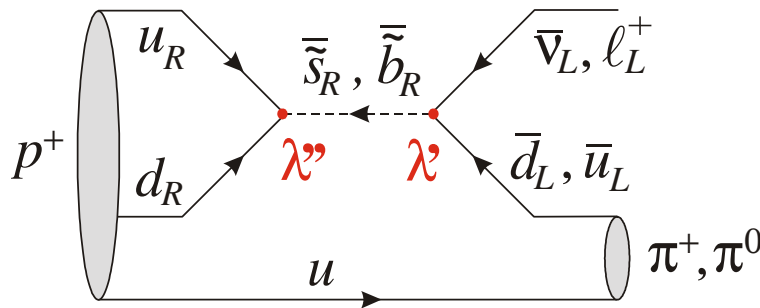


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With both  $\Delta\mathcal{L}$  and  $\Delta\mathcal{B}$ , *proton decay* (and associated) occurs at tree-level:



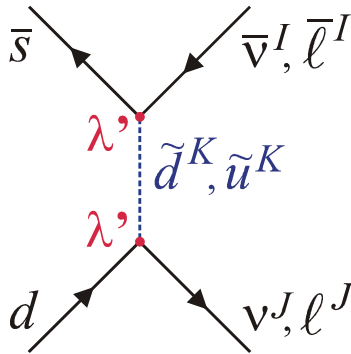
$$p \rightarrow \pi^+ \bar{\nu}_\ell, K^+ \bar{\nu}_\ell, \pi^0 \ell^+, \dots$$

$$n \rightarrow \pi^0 \bar{\nu}_\ell, K^0 \bar{\nu}_\ell, \pi^- \ell^+, \dots$$

But experimentally,  $\tau_{p^+} > 10^{30}$  years :  $\Gamma_{p^+} \sim \frac{m_p^5}{M_{\tilde{d}}^4} |\lambda'' \lambda'|^2 \Rightarrow |\lambda'' \lambda'| \leq 10^{-27}$  ?

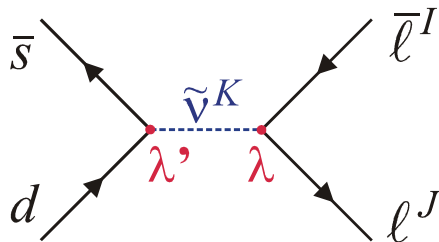
*B. Possible effects in rare decays*

Rare decays conserve both  $\mathcal{B}$  and  $\mathcal{L} \rightarrow$  Quadratic in the R-parity couplings.



Fermi-like  $V \pm A \otimes V - A$  effective couplings:

$$\bar{s}\gamma^\mu(1 \pm \gamma_5)d \otimes \begin{cases} \bar{\nu}\gamma_\mu(1 - \gamma_5)\nu \\ \bar{\ell}\gamma_\mu(1 - \gamma_5)\ell \end{cases}$$



Scalar-pseudoscalar effective couplings:

$$\bar{s}(1 \pm \gamma_5)d \otimes \bar{\ell}(1 \mp \gamma_5)\ell$$

The RPV couplings can induce quark & lepton flavor transitions, hence could contribute to all  $P \rightarrow P'\nu^I\bar{\nu}^J$  and  $P \rightarrow P'\ell^I\bar{\ell}^J$  decays.

C. What Minimal Flavor Violation can say

- The  $\mathcal{B}$  violating couplings can be constructed using  $\Delta\mathcal{B} = 0$  quark Yukawas:

$$\lambda^{IJK} = \epsilon^{LJK} (Y_u Y_d^\dagger)^{IL} \Rightarrow \lambda^{IJK} U^I D^J D^K \rightarrow \det(g_D^\dagger) \lambda^{IJK} U^I D^J D^K$$

$$\lambda^{IJK} = \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN} \Rightarrow \lambda^{IJK} U^I D^J D^K \rightarrow \det(g_Q^\dagger) \lambda^{IJK} U^I D^J D^K$$

...

- But  $\mathcal{L}$  violating couplings are strictly forbidden as long as  $m_\nu = 0$ :

The SU(3) combinatorics demands a spurion transforming like a **six**.

The only spurion available is the suppressed  $\Delta\mathcal{L} = 2$  Majorana mass term:

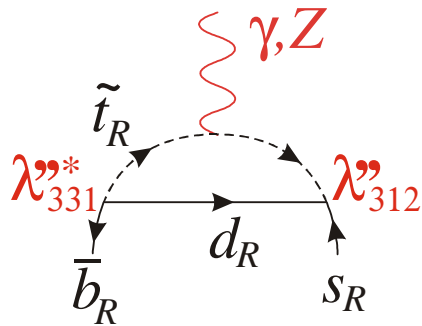
$$\Upsilon_\nu \equiv v_u Y_\nu^T M^{-1} Y_\nu \rightarrow g_L^* \Upsilon_\nu g_L^\dagger \sim \mathbf{6}_{SU(3)_L} \otimes \mathbf{1}_{SU(3)_E}$$

All  $\Delta\mathcal{L} = 1$  couplings are suppressed by neutrino masses.

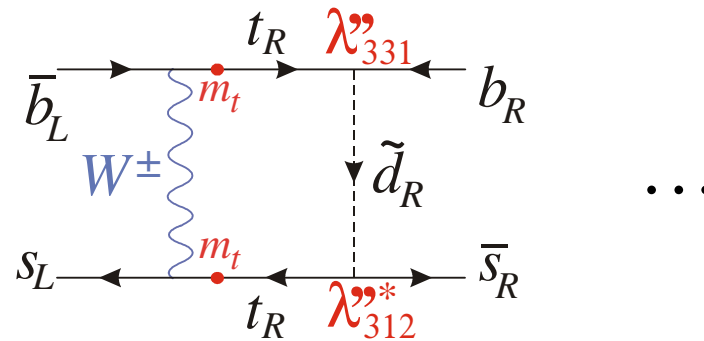
- These suppressions are sufficient to pass all the bounds from proton decay.

C. What Minimal Flavor Violation can say

- Since  $\Delta\mathcal{L}$  couplings are negligible, we turn to  $\Delta\mathcal{B}$  and *diquark currents*.
- Induce *new FCNC* at the loop level (nothing at tree level)



Chakraverty, Choudhury '01, ...



Barbieri, Masiero '86, Slavich '00, ...

- *With MFV*, these are *typically small* compared to the SM contributions:

$$\text{RPV: } b \rightarrow s : |\lambda''_{312} \lambda''^*_{331}| < 10^{-3}, \quad b \rightarrow d : |\lambda''_{312} \lambda''^*_{323}| < 10^{-5}, \quad s \rightarrow d : |\lambda''_{313} \lambda''^*_{323}| < 10^{-8}$$

$$\text{SM: } b \rightarrow s : |V_{tb}^* V_{ts}| \sim 10^{-2}, \quad b \rightarrow d : |V_{tb}^* V_{td}| \sim 10^{-3}, \quad s \rightarrow d : |V_{ts}^* V_{td}| \sim 10^{-4}$$

Very light invisible particles

## A. Flavor-based classification

New very light and neutral particles  $X$  coupled to the SM particles

Flavor-breaking:  $\{\bar{q}^I \Gamma q^J\} X$

Flavor-blind:  $\{\bar{q}^I \Gamma q^I\} X$

Able to induce the  $\Delta F = 1$  quark transition.

Needs  $W$  bosons for the weak transitions

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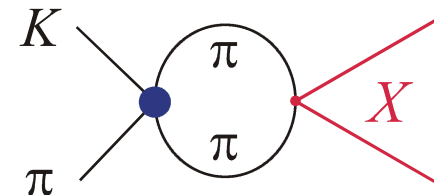
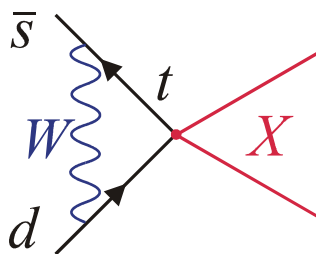
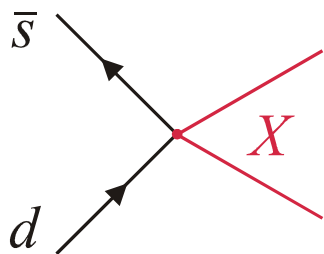
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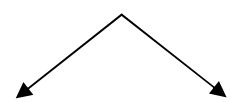
Heavy quarks:  
New FCNC

Light quarks:  
Long-distance effects



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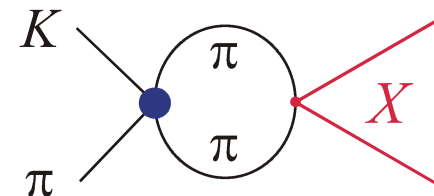
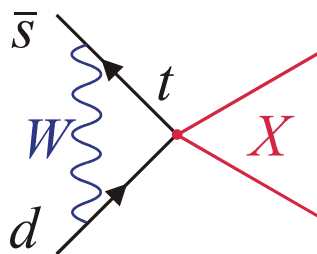
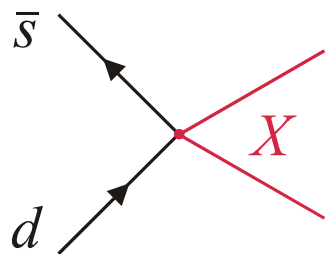
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$P \rightarrow P' X$  may be large,  
competitive with  $P \rightarrow P' \nu \bar{\nu}$ .

Flavor-blind searches with  
EWPO, quarkonium decay,...  
may be more sensitive.

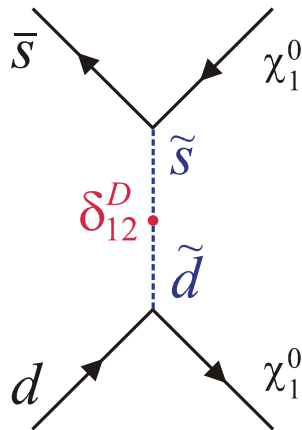
In all cases: The  $X$  mass range probed is limited by experimental requirements.



## B. Flavor-breaking scenario: Very light neutralinos

Dreiner et al '09

Beyond MFV, the flavor-breaking comes from squark mixings.



Effective couplings:

$$\bar{s} \gamma^\mu (1 \pm \gamma_5) d \otimes \bar{\chi} \gamma_\mu \gamma_5 \chi, \text{ tuned by } \delta_{LL}, \delta_{RR}.$$

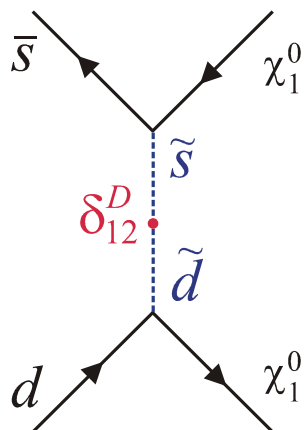
$$\bar{s} (1 \pm \gamma_5) d \otimes \bar{\chi} (1 \pm \gamma_5) \chi, \text{ tuned by } \delta_{LR}.$$

( Illustrated for  $K \rightarrow \pi \chi_1^0 \chi_1^0$ , but similar for  $B \rightarrow (\pi, K^{(*)}) \chi_1^0 \chi_1^0$  )

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Dreiner et al '09

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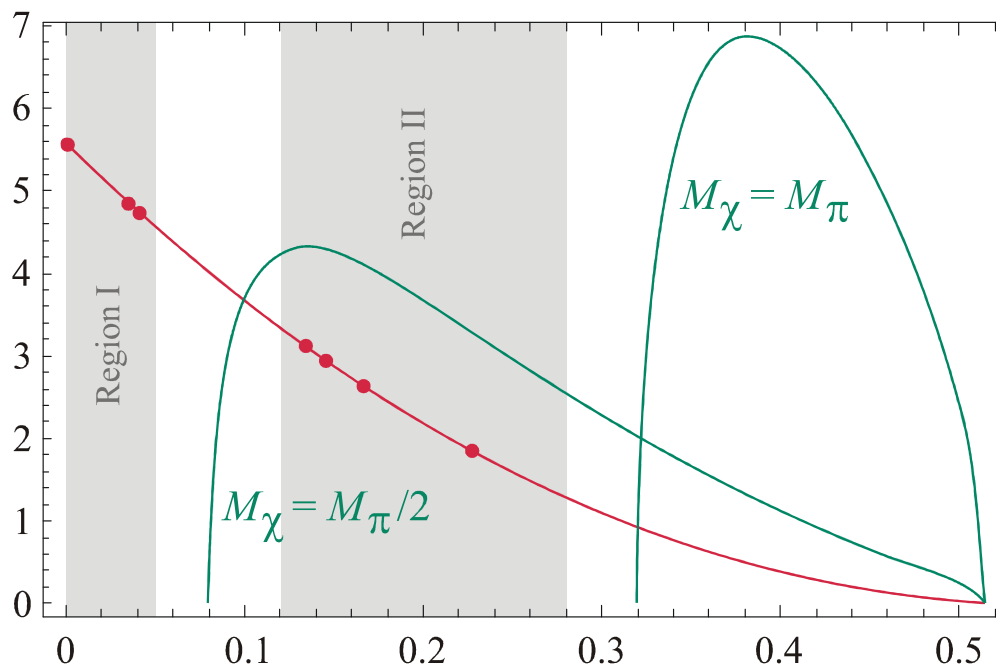


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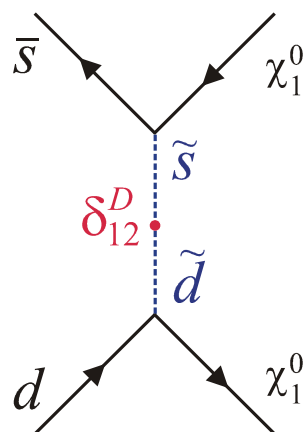
$$K^+ \rightarrow \pi^+ \chi_1^0 \chi_1^0$$



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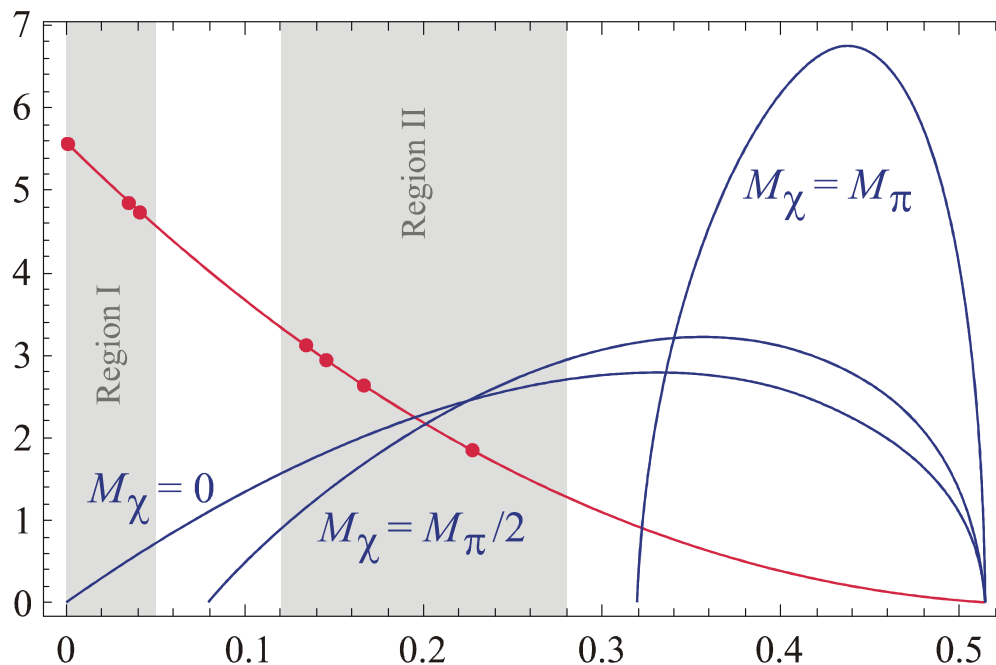
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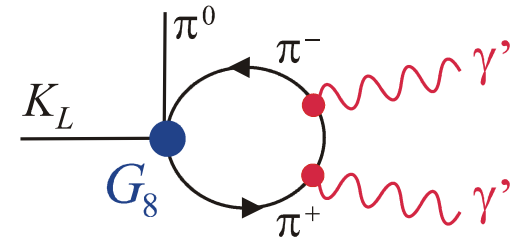
$$\bar{s}(1 \pm \gamma_5) d \otimes \bar{\chi}(1 \pm \gamma_5) \chi$$

$K^+ \rightarrow \pi^+ \chi_1^0 \chi_1^0$



### C. Flavor-blind scenario: Weakly-coupled new photon

$$\mathcal{L}_{\text{int}} = e' A'_\mu \left( \frac{2}{3} \bar{u} \gamma^\mu u - \frac{1}{3} \bar{d} \gamma^\mu d - \frac{1}{3} \bar{s} \gamma^\mu s \right)$$



**Problem 1:** The EW transition strongly suppresses the rate.

$$Br(K_L \rightarrow \pi^0 \gamma \gamma)^{\text{exp}} = 1.273(34) \times 10^{-6}$$

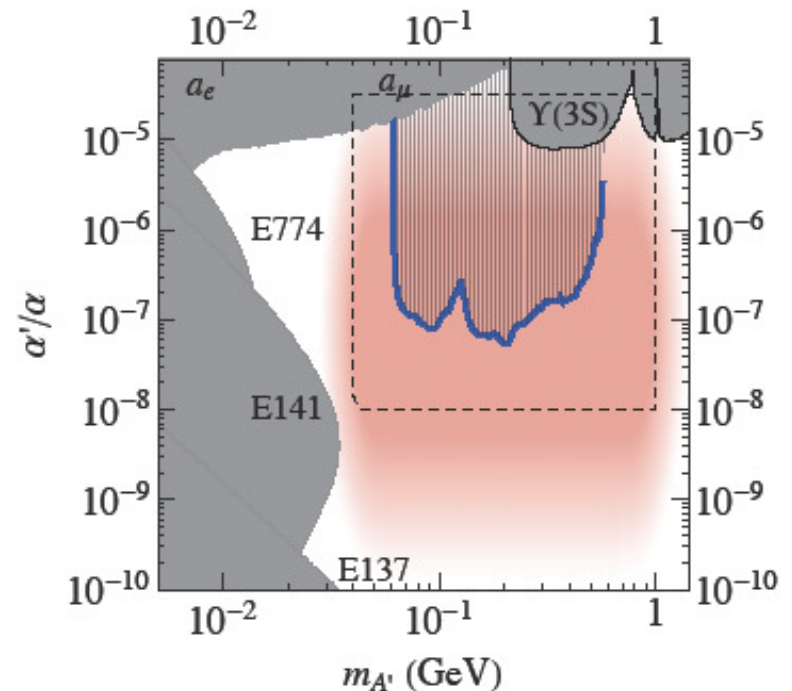
$$\rightarrow Br(K_L \rightarrow \pi^0 \gamma' \gamma') \approx \frac{\alpha'^2}{\alpha^2} \times 10^{-6}$$

A bound in the  $10^{-12}$  range means

$$\alpha' / \alpha < 10^{-3},$$

which is already excluded...

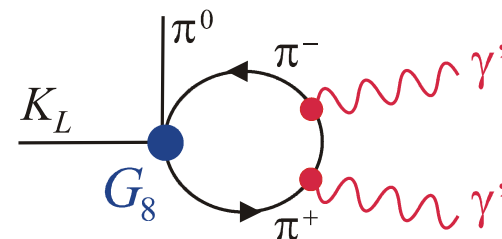
(Remember:  $Br(K_L \rightarrow \pi^0 \nu \bar{\nu})^{SM} \sim 10^{-11}$ )



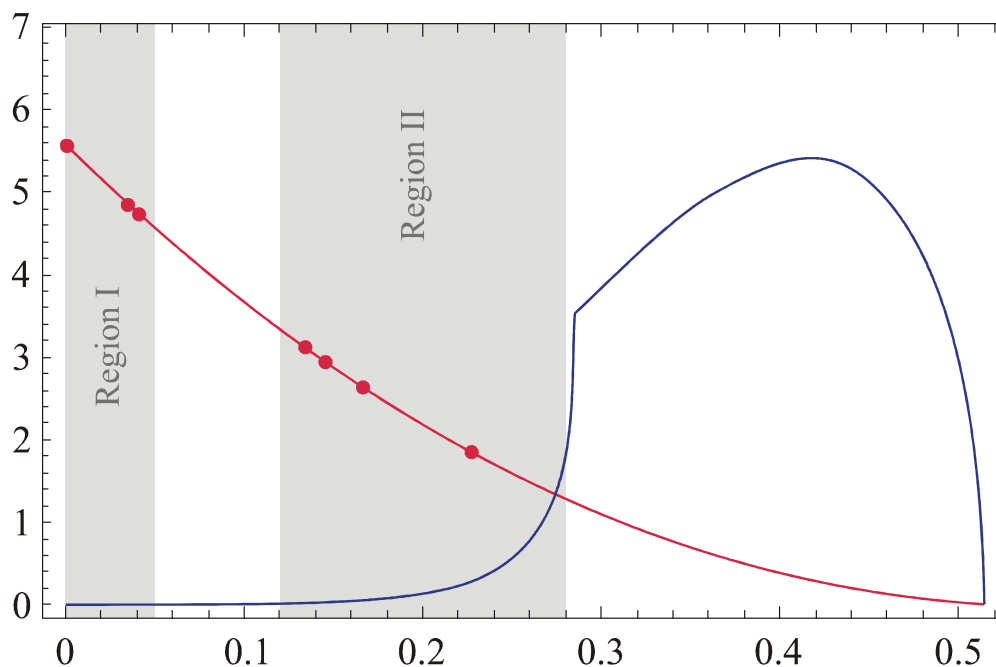
From Essig et al, ArXiv:1001.2557

*C. Flavor-blind scenario: Weakly-coupled new photon*

$$\mathcal{L}_{\text{int}} = e' A'_\mu \left( \frac{2}{3} \bar{u} \gamma^\mu u - \frac{1}{3} \bar{d} \gamma^\mu d - \frac{1}{3} \bar{s} \gamma^\mu s \right)$$



**Problem 2:** The LD dynamics strongly suppresses the rate below \$2\pi\$.



So there is very little sensitivity, no matter the mass of \$\gamma'\$.

Conclusion

With the very rare  $\nu\bar{\nu}$  modes one naturally probes several NP effects:

Lepton flavor violation:  $P \rightarrow P' \nu^I \bar{\nu}^J$

Within MFV,  $P \rightarrow P' \nu^I \bar{\nu}^J$  and  $P \rightarrow P' \ell^I \bar{\ell}^J$  are both tightly constrained by  $\ell^I \rightarrow \ell^J \gamma$ , making them too suppressed to be seen.

R-parity violation: Tree-level effects possible from  $\Delta\mathcal{L} = 1$  couplings.

Within MFV,  $\Delta\mathcal{L}$  couplings are negligible, and loop-level FCNC from  $\Delta\mathcal{B}$  couplings are very suppressed (except maybe for  $b \rightarrow s$ ).

New invisible states:  $P \rightarrow P' + \text{missing energy}$

Competitive bounds if these states have flavor-breaking interactions, or if they couple to top quarks (?), but not if they couple to light quarks.

*The main message:* Let's keep an open mind and *look for the unexpected!*