

Open questions in flavor physics

Paride Paradisi

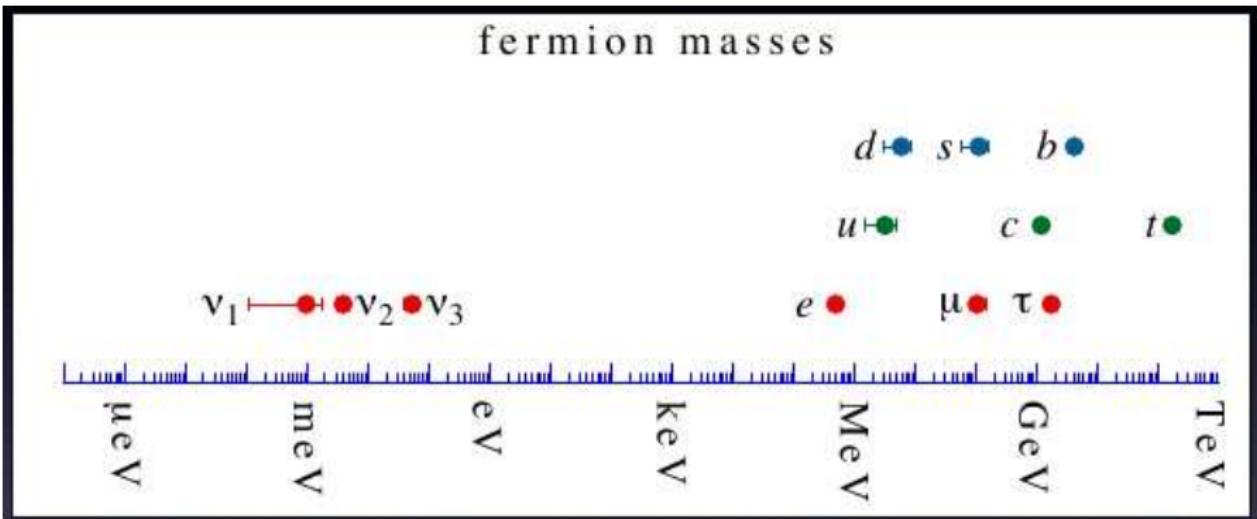


CKM 2010
Warwick, September 7, 2010

- ① Open questions
- ② The SM flavor puzzle
- ③ Messages from the B-factories and Tevatron
- ④ The NP flavor puzzle
- ⑤ “Flavor-test” of NP models: the case of SUSY
- ⑥ Flavor at the LHC

- ① Which is the underlying mechanism regulating the EWSB?
- ② Which is the connection between EWSB and flavor physics?
- ③ Are there new flavor symmetries beyond the puzzling fermion mass spectrum?
- ④ Are there new flavor violating interactions not governed by the SM Yukawas? That is, to which extent the MFV hypothesis is valid?
- ⑤ Do the new sources of CPV accounting for the BAU have an impact on flavor physics and/or EDMs?
- ⑥ Which is the role of flavor physics in the LHC era?
- ⑦ Do we expect to understand the (SM and NP) flavor puzzles through the interplay of flavor physics and the LHC?
- ⑧

The fermion mass puzzle



$$|V_{CKM}| \sim \begin{pmatrix} 1 & \lambda_c & \lambda_c^3 \\ \lambda_c & 1 & \lambda_c^2 \\ \lambda_c^3 & \lambda_c^2 & 1 \end{pmatrix}, \quad |V_{PMNS}| \simeq \begin{pmatrix} 0.79 - 0.86 & 0.50 - 0.61 & 0.0 - 0.2 \\ 0.25 - 0.53 & 0.47 - 0.73 & 0.56 - 0.79 \\ 0.21 - 0.51 & 0.42 - 0.69 & 0.61 - 0.83 \end{pmatrix}_{3\sigma}$$

Hierarchical

Anarchic / Tribimaximal

The fermion mass puzzle

- Quark/charged-lepton mass hierarchy

$$\begin{aligned} Y_t &\sim 1, \quad Y_c \sim 10^{-2}, \quad Y_u \sim 10^{-5} \\ Y_b &\sim 10^{-2}, \quad Y_s \sim 10^{-3}, \quad Y_d \sim 10^{-4} \\ Y_\tau &\sim 10^{-2}, \quad Y_\mu \sim 10^{-3}, \quad Y_e \sim 10^{-6} \end{aligned}$$

- Quark mixing angles hierarchy

$$|V_{us}| \sim 0.2, \quad |V_{cb}| \sim 0.04, \quad |V_{ub}| \sim 0.004 \quad (\delta_{KM} \sim 1)$$

- Neutrinos

$$\begin{aligned} \Delta m_{sol}^2 &= (7.9 \pm 0.3) \times 10^{-5} \text{ eV}^2, \quad |\Delta m_{atm}^2| = (2.6 \pm 0.2) \times 10^{-3} \text{ eV}^2, \\ \sin^2 \theta_{sol} &= 0.31 \pm 0.02, \quad \sin^2 \theta_{atm} = 0.47 \pm 0.07, \quad \sin^2 \theta_{e3} = 0_{-0.0}^{+0.08}, \end{aligned}$$

- Quark-Lepton complementarity: GUT + Flavor Symmetry? [Raidal '04]

$$\theta_{sol} + \theta_c \approx \frac{\pi}{4}, \quad \theta_{atm} + \theta_{23} \approx \frac{\pi}{4}$$

- SM gauge couplings

$$g_s \sim 1, \quad g \sim 0.6, \quad g' \sim 0.3, \quad \lambda_{\text{Higgs}} \sim 1$$

Flavor Physics within the SM

- $\mathcal{L}_{Kinetic+Gauge}^{\text{SM}} + \mathcal{L}_{Higgs}^{\text{SM}}$ has a large $U(3)^5$ global **flavour symmetry**

$$\mathbf{G} = \mathbf{U}(3)^5 = \mathbf{U}(3)_{\mathbf{u}} \otimes \mathbf{U}(3)_{\mathbf{d}} \otimes \mathbf{U}(3)_{\mathbf{Q}} \otimes \mathbf{U}(3)_{\mathbf{e}} \otimes \mathbf{U}(3)_{\mathbf{L}}$$

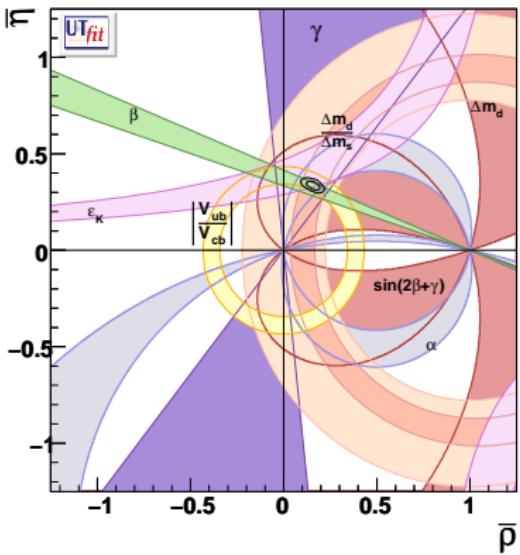
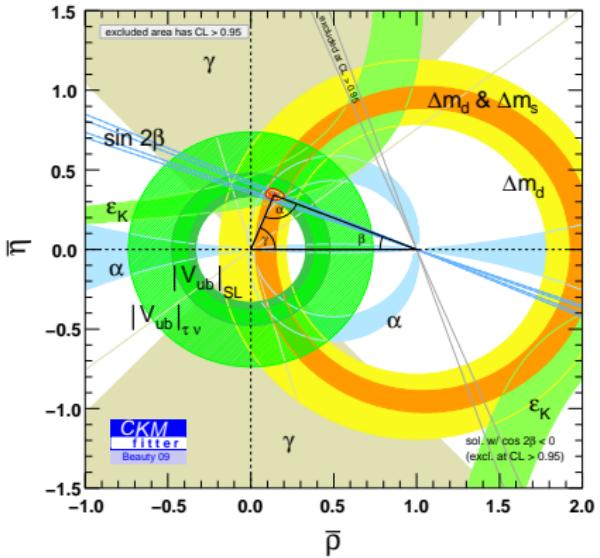
- $\mathcal{L}_{\text{Yukawa}} = \bar{Q}_L \mathbf{Y}_{\mathbf{D}} D_R \phi + \bar{Q}_L \mathbf{Y}_{\mathbf{U}} U_R \tilde{\phi} + \bar{L}_L \mathbf{Y}_{\mathbf{L}} E_R \phi + h.c$ break

$$\mathbf{G} \rightarrow \mathbf{U}(1)_{\mathbf{B}} \times \mathbf{U}(1)_{\mathbf{e}} \times \mathbf{U}(1)_{\mu} \times \mathbf{U}(1)_{\tau}$$

- **CKM matrix:** $\mathbf{Y}_{\mathbf{U}} = V_{CKM} \times \text{diag}(y_u, y_c, y_t)$ for $\mathbf{Y}_{\mathbf{D}} = \text{diag}(y_d, y_s, y_b)$

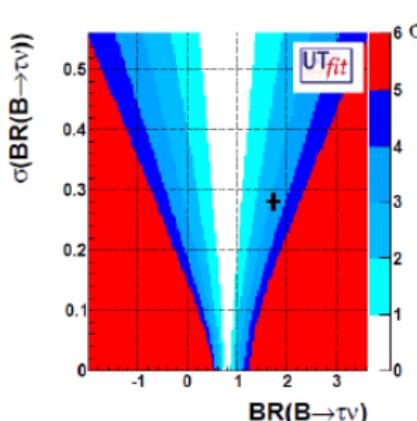
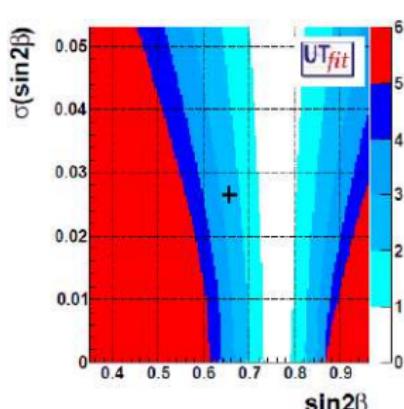
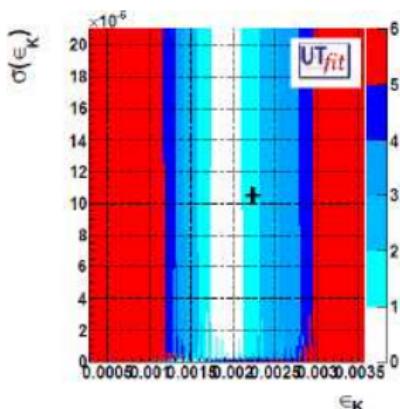
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{ts} & V_{tc} & V_{tb} \end{pmatrix} = \begin{pmatrix} n \leftarrow \frac{e^-}{\bar{\nu}} p & K \leftarrow \frac{\ell^-}{\bar{\nu}} \pi & B \leftarrow \frac{\ell^-}{\bar{\nu}} \pi \\ D \leftarrow \frac{\ell^-}{\bar{\nu}} \pi & D \leftarrow \frac{\ell^-}{\bar{\nu}} K & B \leftarrow \frac{\ell^-}{\bar{\nu}} D \\ B^0 \leftarrow \bar{B}^0 & B_s \leftarrow \bar{B}_s & t \leftarrow W b \end{pmatrix}$$

Messages from the B-factories



"Very likely, flavour and CP violation in FC processes are dominated by the CKM mechanism" (Nir)

UT tensions



- ① $\sim 6\%$ reduction of ϵ_K^{SM}
[Buras & Guadagnoli; BG & Isidori]
- ② smaller \hat{B}_K from
unquenched analyses
[Antonio et al. '08; Aubin et al. '10]
- ③ fit vs. exp. $\approx -1.7\sigma$

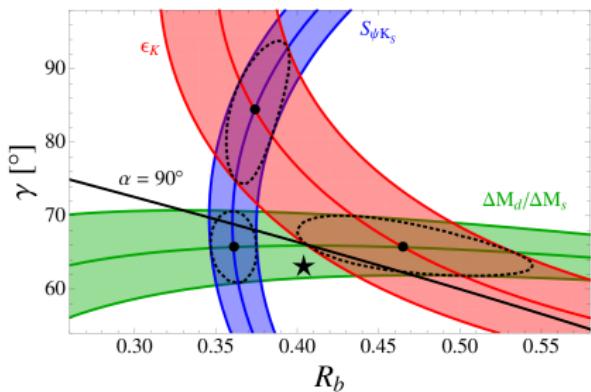
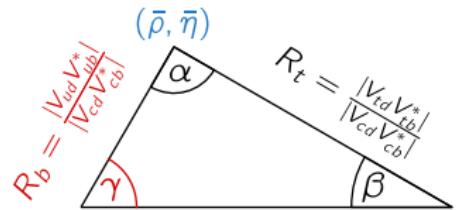
NEW: ϵ_K^{SM} @ NNLO QCD:
 $\sim +3\%$ [Brod & Gorbahn, '10]

- ① fit vs. exp. $\approx +2.6\sigma$
- ② $B(B \rightarrow \ell\nu)/\Delta M_d \sim (\sin \beta / \sin \gamma)^2 / \hat{B}_{B_d}$
- ③ fit vs. exp. $\approx -3.2\sigma$

Similar conclusions also by Lenz & Nierste + CKMfitter collaboration ('10)

UT tensions and NP

- “Tensions” in the UT analysis [Lunghi & Soni, Buras & Guadagnoli]
- Look at ϵ_K , $S_{\psi K_S}$, and $\Delta M_d/\Delta M_s$ in the R_b - γ plane from tree-level processes

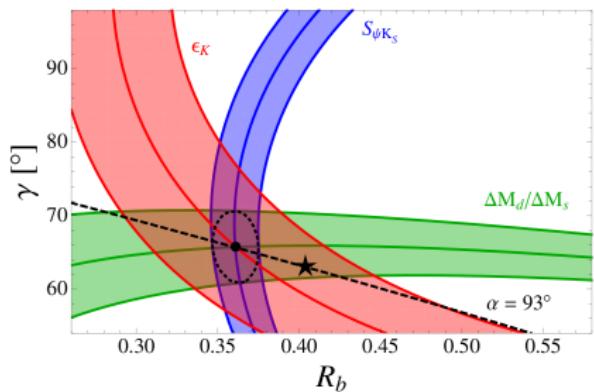


Altmannshofer et al. '09

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- Look at ϵ_K , $S_{\psi K_S}$, and $\Delta M_d/\Delta M_s$ in the R_b - γ plane from tree-level processes

$$R_t = \frac{|V_{td} V_{tb}^*|}{|V_{cd} V_{cb}^*|}$$
$$R_b = \frac{|V_{ud} V_{ub}^*|}{|V_{cd} V_{cb}^*|}$$

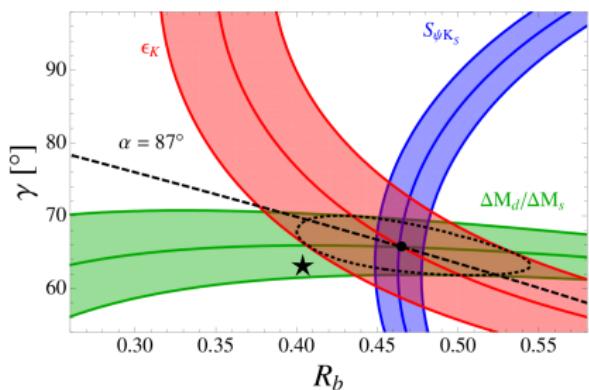


Possible solutions:

- +24% NP effect in ϵ_K

Altmannshofer et al. '09

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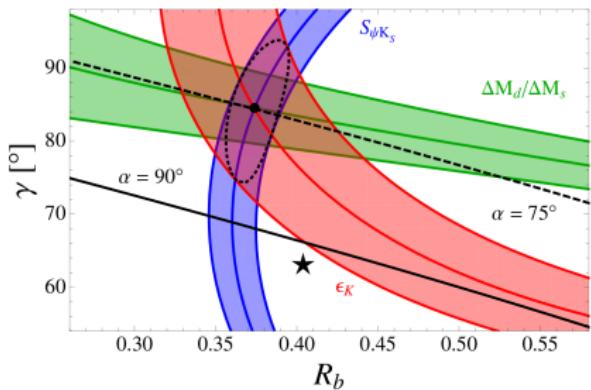
$R_t = \frac{|V_{td}V_{tb}^*|}{|V_{cd}V_{cb}^*|}$

$R_b = \frac{|V_{ud}V_{sb}^*|}{|V_{cd}V_{cb}^*|}$

Possible solutions:

- +24% NP effect in ϵ_K
- 6.5° NP phase in B_d mixing

- “Tensions” in the UT analysis [Lunghi & Soni, Buras & Guadagnoli]
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Altmannshofer et al. '09

Diagram illustrating the relationship between R_b and R_t in terms of CKM matrix elements:

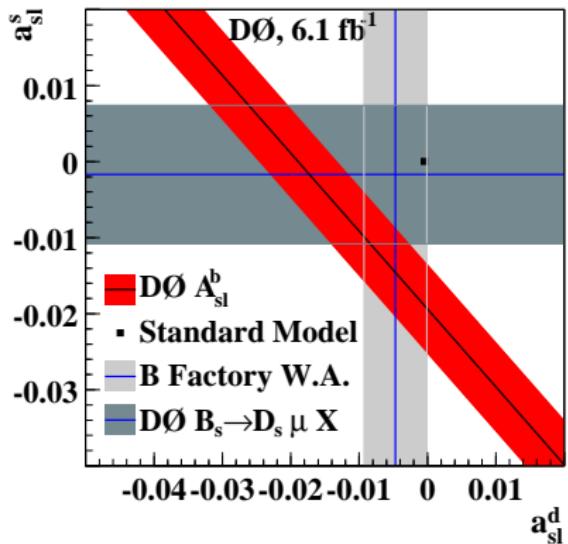
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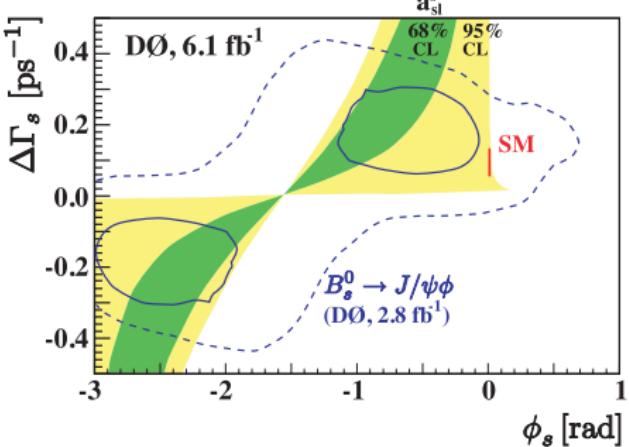
- +24% NP effect in ϵ_K
- 6.5° NP phase in B_d mixing
- 22% NP effect in $\Delta M_d/\Delta M_s$

CPV in B_s mixing (before ICHEP 2010)



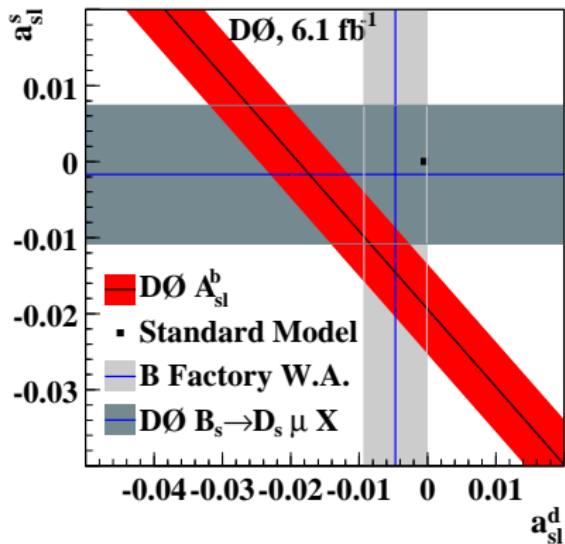
$$A_{SL}^q \equiv \frac{\Gamma(\bar{B}_q \rightarrow l^+ X) - \Gamma(B_q \rightarrow l^- X)}{\Gamma(\bar{B}_q \rightarrow l^+ X) + \Gamma(B_q \rightarrow l^- X)},$$

$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_{B_s})$$

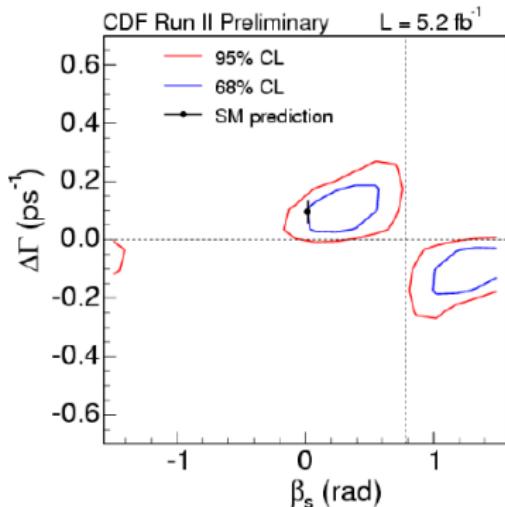


New Physics in the B_s mixing phase?

CPV in B_s mixing (after ICHEP 2010)



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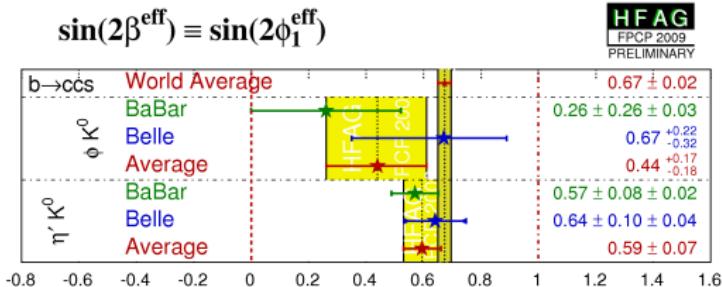
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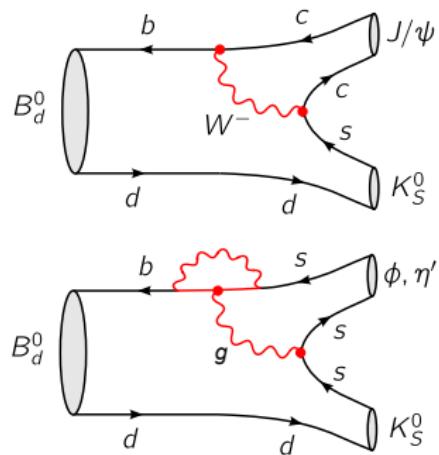
$\sin 2\beta_{\text{eff}}$ tensions

- In the SM, $(\sin 2\beta)_{\psi K_S} \approx (\sin 2\beta)_{\phi K_S} \approx (\sin 2\beta)_{\eta' K_S}$
- $B_d \rightarrow \psi K_S$ dominated by tree level, ϕK_S and $\eta' K_S$ are loop-induced

Data indicate $S_{\phi K_S} < S_{\eta' K_S} < S_{\psi K_S}$



[adapted from HFAG]



New physics in the decay amplitudes?

The SuperB will tell us...

The NP “scale”

- **Gravity** $\Rightarrow \Lambda_{\text{Planck}} \sim 10^{18-19} \text{ GeV}$
- **Neutrino masses** $\Rightarrow \Lambda_{\text{see-saw}} \lesssim 10^{15} \text{ GeV}$
- **Hierarchy problem:** $m_h^{\text{SM}}(\Lambda_{\text{NP}}^2) \sim M_W \Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$
- **Dark Matter** $\Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$
- **BAU**: evidence of CPV beyond SM
 - ▶ Electroweak Baryogenesis $\Rightarrow \Lambda_{\text{NP}} \lesssim \text{TeV}$
 - ▶ Leptogenesis $\Rightarrow \Lambda_{\text{see-saw}} \lesssim 10^{15} \text{ GeV}$
 - ▶



SM = effective theory at the EW scale

- Going BSM model-independently:

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d \geq 5} \frac{c_{ij}^{(d)}}{\Lambda_{NP}^{d-4}} O_{ij}^{(d)}$$

- ▶ $\mathcal{L}_{\text{eff}}^{d=5} = \frac{y_\nu^{ij}}{\Lambda_{\text{see-saw}}} L_i L_j \phi \phi$
- ▶ $\mathcal{L}_{\text{eff}}^{d=6}$ generates many FCNC operators

The NP flavor puzzle

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d=6} \frac{c_{ij}^{(6)}}{\Lambda_{NP}^2} O_{ij}^{(6)}$$

[Isidori, Nir, Perez '10]

Operator	Bounds on Λ (TeV)		Bounds on c_{ij} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \varepsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \varepsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4	5.7×10^{-8}	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	9.3×10^2	3.3×10^{-6}	1.0×10^{-6}	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	1.9×10^3	3.6×10^3	5.6×10^{-7}	1.7×10^{-7}	$\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$
$(\bar{b}_L \gamma^\mu s_L)^2$	1.1×10^2	1.1×10^2	7.6×10^{-5}	7.6×10^{-5}	Δm_{B_s}
$(\bar{b}_R s_L)(\bar{b}_L s_R)$	3.7×10^2	3.7×10^2	1.3×10^{-5}	1.3×10^{-5}	Δm_{B_s}

⇓

“Generic” FV sources at the TeV scale are excluded

- SM without Yukawa interactions: $U(3)^5$ global **flavour symmetry**

$$U(3)_u \otimes U(3)_d \otimes U(3)_q \otimes U(3)_e \otimes U(3)_L$$

- Yukawa interactions break this symmetry
- Proposal for any New Physics model:

Yukawa structures as the **only sources of flavour violation**



Minimal Flavour Violation [D'Ambrosio et al. '02]

Notice that MFV allows new “flavour blind”CPV phases!

[Kagan et al. '09] (model-independent)

[Ellis et al. '07] (SUSY)

[Colangelo et al., '08], [Smith et al. '09] (SUSY)

[Altmannshofer et al., '08,'09], [P.P & Straub, '09] (SUSY)

[Buras et al., '10,'10] (2HDM)

MFV & the NP flavor puzzle

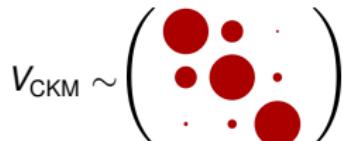
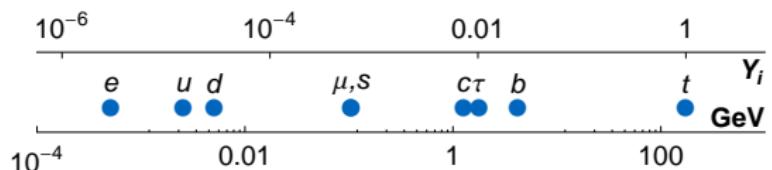
$$(c_{\text{MFV}}^{\Delta F=1})_{ij} \sim \textcolor{red}{V_{ti}^* V_{tj}}, \quad (c_{\text{MFV}}^{\Delta F=2})_{ij} \sim (\textcolor{red}{V_{ti}^* V_{tj}})^2$$

$\Delta F = 1, 2$ MFV operators	$\Lambda(\text{TeV})$	Observables
$H^\dagger \left(\overline{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} Q_L \right) (e F_{\mu\nu})$	6.1 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$\frac{1}{2} (\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L)^2$	5.9 TeV	$\epsilon_K, \Delta m_{B_d}, \Delta m_{B_s}$
$H_D^\dagger \left(\overline{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} T^a Q_L \right) (g_s G_{\mu\nu}^a)$	3.4 TeV	$B \rightarrow X_s \gamma, B \rightarrow X_s \ell^+ \ell^-$
$(\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (\overline{E}_R \gamma_\mu E_R)$	2.7 TeV	$B \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu^+ \mu^-$
$(\overline{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (e D_\mu F_{\mu\nu})$	1.5 TeV	$B \rightarrow X_s \ell^+ \ell^-$

Observable	Experiment	MFV prediction	SM prediction
$A_{CP}(B_s \rightarrow \psi \phi)$	[0.10, 1.44] @ 95% CL	0.04(5)	0.04(2)
$A_{CP}(B \rightarrow X_s \gamma)$	< 6% @ 95% CL	< 0.02	< 0.01
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	$< 1.8 \times 10^{-8}$	$< 1.2 \times 10^{-9}$	$1.3(3) \times 10^{-10}$
$\mathcal{B}(B \rightarrow X_s \tau^+ \tau^-)$	—	$< 5 \times 10^{-7}$	$1.6(5) \times 10^{-7}$
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$< 2.6 \times 10^{-8}$ @ 90% CL	$< 2.9 \times 10^{-10}$	$2.9(5) \times 10^{-11}$

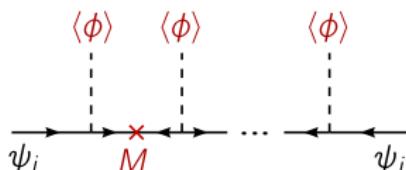
[D'Ambrosio et al. '02; Hurth et al. '08, Isidori, Nir & Perez '10]

SM vs. NP flavor puzzle



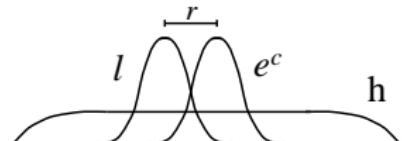
Froggatt-Nielsen '79: Hierarchies from SSB of a Flavour Symmetry

$$\epsilon = \frac{\langle \phi \rangle}{M} \ll 1 \Rightarrow Y_{ij} \propto \epsilon^{(a_i + b_j)}$$



Arkani-Hamed & Schmaltz '99: Hierarchies from Extra Dimensions

$x = \mu r$	1	2	3	4	5
$e^{-\frac{x^2}{2}}$	1	10^{-1}	10^{-2}	10^{-4}	10^{-6}
	λ_t	\dots			λ_e



The Gaussian wave functions of l and e^c overlap in an exponentially small region



Small Yukawa couplings without Symmetries

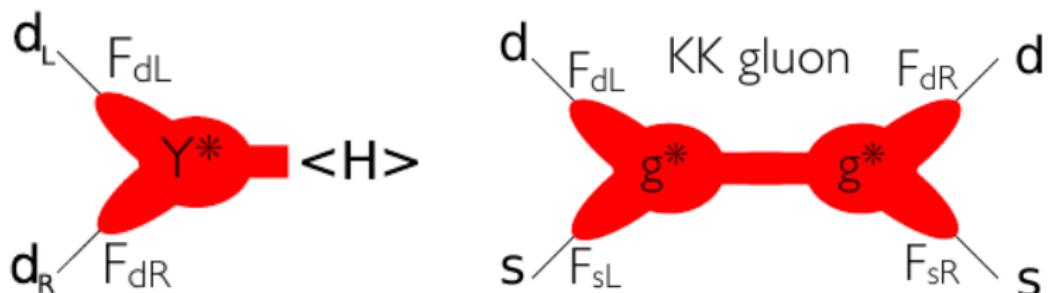
SM vs. NP flavor puzzle

- Flavor Models flavor protection

[Lalak, Pokorski & Ross '10]

Operator	$U(1)$	$U(1)^2$	$SU(3)$	MFV
$(\bar{Q}_L X_{LL}^Q Q_L)_{12}$	λ	λ^5	λ^3	λ^5
$(\bar{D}_R X_{RR}^D D_R)_{12}$	λ	λ^{11}	λ^3	$(y_d y_s) \times \lambda^5$
$(\bar{Q}_L X_{LR}^D D_R)_{12}$	λ^4	λ^9	λ^3	$y_s \times \lambda^5$

- RS flavor protection [Gerghetta & Pomarol, '99; Huber, '03; Agashe, Perez & Soni, '04]



$$m_d \sim v F_{d_L} Y^* F_{d_R}$$

$$(V_{CKM})_{ij} \sim F_{d_{L_i}} / F_{d_{L_j}}$$

$$(\epsilon_K)_{\text{RS-GIM}} \sim \frac{(g^*)^2}{M_{\text{KK}}^2} \frac{\mathbf{m}_d \mathbf{m}_s}{(v Y^*)^2}$$

[Csaki, Falkowski & Weiler, '08]

[Blanke, Buras, Duling, Gori, Weiler, '08]

Where to look for New Physics at the low energy?

- Processes very suppressed or even forbidden in the SM

- ▶ FCNC processes ($\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, $B_{s,d}^0 \rightarrow \mu^+\mu^-$, $K \rightarrow \pi\nu\bar{\nu}$)
- ▶ CPV effects in the electron/neutron EDMs, $d_{e,n}$...
- ▶ FCNC & CPV in $B_{s,d}$ decay/mixing & D mixing amplitudes

- Processes predicted with high precision in the SM

- ▶ EWPO as $\Delta\rho$, $(g-2)_\mu$
- ▶ LU in $R_M^{e/\mu} = \Gamma(K(\pi) \rightarrow e\nu)/\Gamma(K(\pi) \rightarrow \mu\nu)$

Flavor in the LHC era

[Isidori, Nir & Perez '10]

Observable	SM prediction	Theory error	Present result	Future error	Future Facility
$ V_{us} [K \rightarrow \pi \ell \nu]$	input	$0.5\% \rightarrow 0.1\%_{\text{Latt}}$	0.2246 ± 0.0012	0.1%	K factory
$ V_{cb} [B \rightarrow X_s \ell \nu]$	input	1%	$(41.54 \pm 0.73) \times 10^{-3}$	1%	Super- B
$ V_{ub} [B \rightarrow \pi \ell \nu]$	input	$10\% \rightarrow 5\%_{\text{Latt}}$	$(3.38 \pm 0.36) \times 10^{-3}$	4%	Super- B
$\gamma [B \rightarrow D K]$	input	$< 1^\circ$	$(70^{+27}_{-30})^\circ$	3°	LHCb
$S_{B_d \rightarrow \psi K}$	$\sin(2\beta)$	$\lesssim 0.01$	0.671 ± 0.023	0.01	LHCb
$S_{B_s \rightarrow \psi \phi}$	0.036	$\lesssim 0.01$	$0.81^{+0.12}_{-0.32}$	0.01	LHCb
$S_{B_d \rightarrow \phi K}$	$\sin(2\beta)$	$\lesssim 0.05$	0.44 ± 0.18	0.1	LHCb
$S_{B_s \rightarrow \phi \phi}$	0.036	$\lesssim 0.05$	—	0.05	LHCb
$S_{B_d \rightarrow K^* \gamma}$	$\text{few} \times 0.01$	0.01	-0.16 ± 0.22	0.03	Super- B
$S_{B_s \rightarrow \phi \gamma}$	$\text{few} \times 0.01$	0.01	—	0.05	LHCb
A_{SL}^d	-5×10^{-4}	10^{-4}	$-(5.8 \pm 3.4) \times 10^{-3}$	10^{-3}	LHCb
A_{SL}^s	2×10^{-5}	$< 10^{-5}$	$(1.6 \pm 8.5) \times 10^{-3}$	10^{-3}	LHCb
$A_{CP}(b \rightarrow s \gamma)$	< 0.01	< 0.01	-0.012 ± 0.028	0.005	Super- B
$\mathcal{B}(B \rightarrow \tau \nu)$	1×10^{-4}	$20\% \rightarrow 5\%_{\text{Latt}}$	$(1.73 \pm 0.35) \times 10^{-4}$	5%	Super- B
$\mathcal{B}(B \rightarrow \mu \nu)$	4×10^{-7}	$20\% \rightarrow 5\%_{\text{Latt}}$	$< 1.3 \times 10^{-6}$	6%	Super- B
$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$	3×10^{-9}	$20\% \rightarrow 5\%_{\text{Latt}}$	$< 5 \times 10^{-8}$	10%	LHCb
$\mathcal{B}(B_d \rightarrow \mu^+ \mu^-)$	1×10^{-10}	$20\% \rightarrow 5\%_{\text{Latt}}$	$< 1.5 \times 10^{-8}$	[?]	LHCb
$A_{FB}(B \rightarrow K^* \mu^+ \mu^-)_{q_0^2}$	0	0.05	(0.2 ± 0.2)	0.05	LHCb
$B \rightarrow K \nu \bar{\nu}$	4×10^{-6}	$20\% \rightarrow 10\%_{\text{Latt}}$	$< 1.4 \times 10^{-5}$	20%	Super- B
$ q/p _{D-\text{mixing}}$	1	$< 10^{-3}$	$(0.86^{+0.18}_{-0.15})$	0.03	Super- B
ϕ_D	0	$< 10^{-3}$	$(9.6^{+8.3}_{-9.5})^\circ$	2°	Super- B
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	8.5×10^{-11}	8%	$(1.73^{+1.15}_{-1.05}) \times 10^{-10}$	10%	K factory
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	2.6×10^{-11}	10%	$< 2.6 \times 10^{-8}$	[?]	K factory
$R^{(e/\mu)}(K \rightarrow \pi \ell \nu)$	2.477×10^{-5}	0.04%	$(2.498 \pm 0.014) \times 10^{-5}$	0.1%	K factory
$\mathcal{B}(t \rightarrow c Z, \gamma)$	$\mathcal{O}(10^{-13})$	$\mathcal{O}(10^{-13})$	$< 0.6 \times 10^{-2}$	$\mathcal{O}(10^{-5})$	$LHC (100 \text{ fb}^{-1})$

The soft-sector contains a huge number of FV and/or CPV parameters: natural $O(1)$ values for these parameters are excluded by the exp. data

Flavor problem: solutions

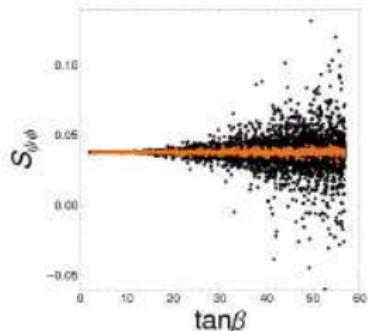
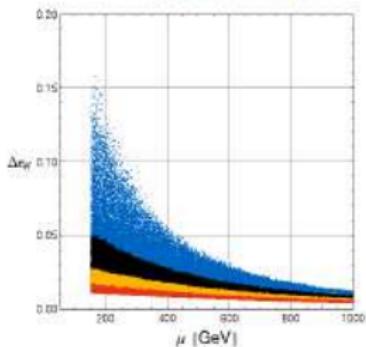
- ① **Decoupling:** $m_{SUSY} \gg \text{TeV}$, the hierarchy problem is (partly) reintroduced
- ② **Degeneracy:** sfermion masses nearly degenerate, e.g. gauge mediation, flavour models, MFV...
- ③ **Alignment:** quark and squark mass matrices aligned [Nir & Seiberg '93]

CP problem: solutions

- ① Degeneracy & Alignment do not solve the CP problem as flavor blind phases are allowed
- ② **CPV from flavor effects** \Rightarrow EDMs suppressed by small mixing angles
- ③ Hp in flavor models: CP spontaneously broken in the flavor sector by flavon VEVs [Nir & Rattazzi '96]
- ④ Applying the same idea to MFV: CPV only from MFV-compatible terms breaking the flavour blindness [P.P & Straub, '09]

① Kaon mixing

- The mixing amplitude M_{12}^K has no sensitivity to the new flavor blind phases
- Still, $\epsilon_K \propto \text{Im}(M_{12}^K)$ can get a positive NP contribution up to 15%
- But only for a very light SUSY spectrum:
 $\mu, m_{\tilde{t}_1} \simeq 200 \text{ GeV}$

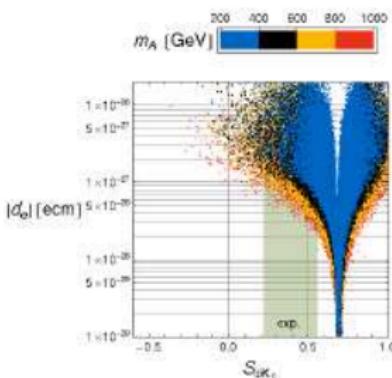
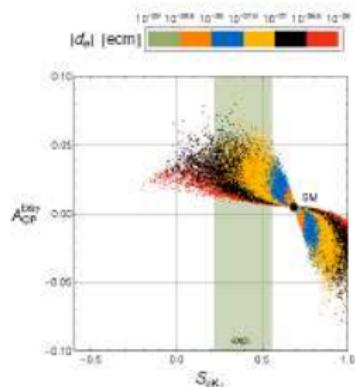
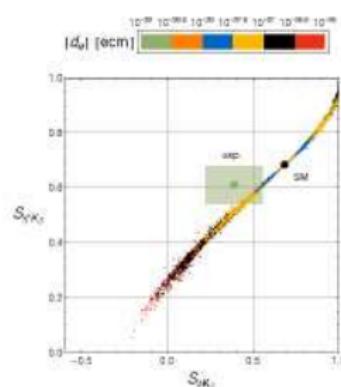


② B_d and B_s mixing

- Leading NP contributions to $M_{12}^{d,s}$ are insensitive to the new phases of a FBMSSM.
(at least for moderate $\tan\beta$...)
- For large $\tan\beta$, the constraint from $b \rightarrow s\gamma$ does not allow for sizeable effects
- $S_{\psi K_S}$ and $S_{\psi\phi}$ are SM like ($S_{\psi\phi} \simeq 0.03 - 0.05$)

[Altmannshofer, Buras & P.P., '08]

MSSM with MFV and “flavour blind” phases



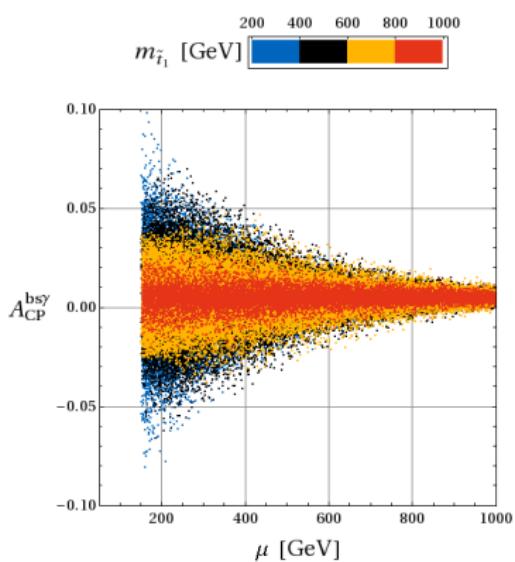
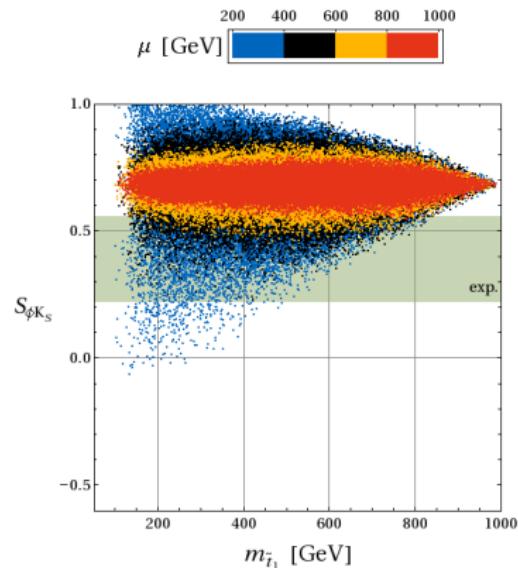
- CP violating $\Delta F = 0$ and $\Delta F = 1$ dipole amplitudes can be strongly modified
- $S_{\phi K_S}$ and $S_{\eta' K_S}$ can simultaneously be brought in agreement with the data
- sizeable and correlated effects in $A_{CP}^{bsn} \simeq 1\% - 6\%$
- lower bounds on the electron and neutron EDMs at the level of $d_{e,n} \gtrsim 10^{-28} \text{ ecm}$
- large and correlated effects in the CP asymmetries in $B \rightarrow K^+ \mu^+ \mu^-$
(WA, Ball, Bharucha, Buras, Straub, Wick)

- the leading NP contributions to $\Delta F = 2$ amplitudes are not sensitive to the new phases of the FBMSSM
- CP violation in meson mixing is SM like
- i.e. small effects in $S_{\psi\phi}$, $S_{\psi K_S}$ and ϵ_K
- in particular: $0.03 < S_{\psi\phi} < 0.05$

A combined study of all these observables and their correlations constitutes a very powerful test of the FBMSSM

[Altmannshofer, Buras & P.P., '08]

Implications for direct searches of SUSY particles



- $S_{\phi K_S} \simeq 0.4$ implies $\mu \lesssim 600$ GeV and $m_{\tilde{t}_1} \lesssim 700$ GeV
- $A_{CP}^{bs\gamma} \gtrsim 2\%$ implies $\mu \lesssim 600$ GeV and $m_{\tilde{t}_1} \lesssim 800$ GeV

[Altmannshofer,Buras & P.P., '08]

Abelian vs. Non-abelian flavor models

- Non-abelian models predict \approx degenerate 1st & 2nd sfermion masses
 - ▶ Suppressed contributions to $1 \leftrightarrow 2$ transitions
 - ▶ Potentially large contributions to $2 \leftrightarrow 3$ transitions
- In abelian models, sfermions of different generations need not be degenerate
 - ▶ A single $U(1)$ & $O(1)$ 1-2 mass splitting lead to $(\delta_{d,u}^{LL})_{12} \sim \mathcal{O}(\lambda)$
 - ▶ $U(1) \times U(1)$ allows *alignement* in the down sector $(\delta_d^{LL})_{12} \approx 0 \Rightarrow (\delta_u^{LL})_{12} \sim \mathcal{O}(\lambda)$
 - ▶ Large effects in D^0 - \bar{D}^0 mixing

Chirality structure of flavour violating terms

- Different flavour symmetries lead to different patterns of flavour violation
- Mass insertions: $M_{\tilde{d}}^2 = \text{diag}(\tilde{m}^2) + \tilde{m}^2 \begin{pmatrix} \delta_d^{LL} & \delta_d^{LR} \\ \delta_d^{RL} & \delta_d^{RR} \end{pmatrix}$
- $\delta^{LL}, \delta^{RR}, \delta^{LR}$ fixed by the flavour symmetry up to $O(1)$ factors

Representative flavour models

Representative (non-) abelian flavour models (not just 4 examples...!)

AC model $U(1)$
[Agashe, Carone]

Large, $O(1)$ RR
mass insertions

AKM model $SU(3)$
[Antusch, King, Malinsky]

Only CKM-like RR
mass insertions

RVV model $SU(3)$
[Ross, Velasco-S., Vives]

CKM-like LL & RR
mass insertions

δ LL model $(S_3)^3$
[e.g. Hall, Murayama]

Only CKM-like LL
mass insertions

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & \lambda^2 \\ 0 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix}$$

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^5 & \lambda^3 \\ \lambda^5 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix}$$

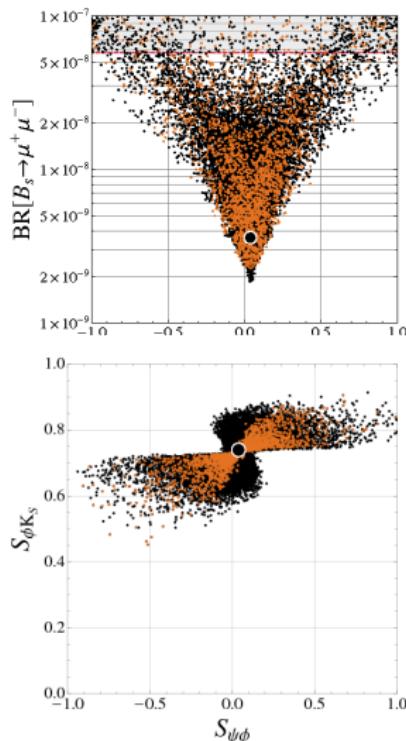
$$\delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 1 \\ 0 & 1 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^3 \\ \lambda^3 & \cdot & \lambda^2 \\ \lambda^3 & \lambda^2 & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & \lambda^3 & \lambda^2 \\ \lambda^3 & \cdot & \lambda \\ \lambda^2 & \lambda & \cdot \end{pmatrix} \quad \delta_d^{RR} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & 0 \\ 0 & 0 & \cdot \end{pmatrix}$$

Hp: CP is spontaneously broken in the flavor sector [Nir & Rattazzi '96]

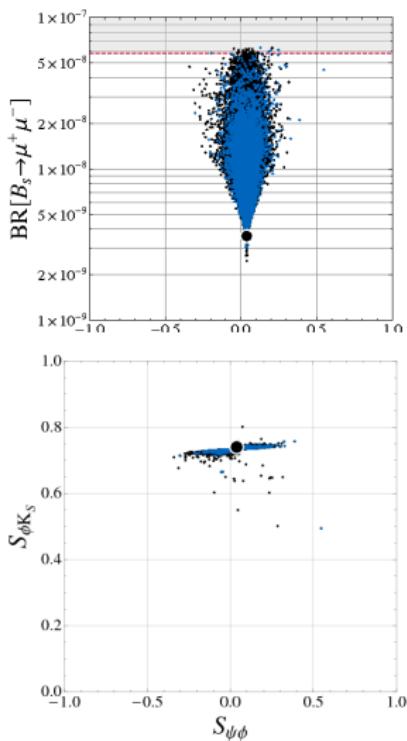
$b \rightarrow s$ transitions & SUSY flavor models

[Altmannshofer et al., '09]

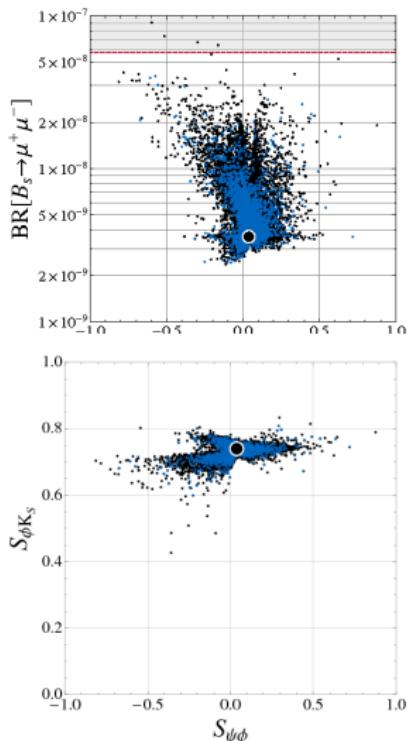
AC



AKM



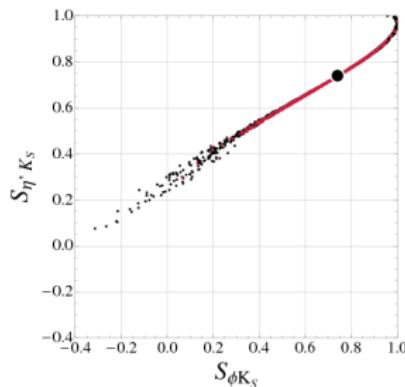
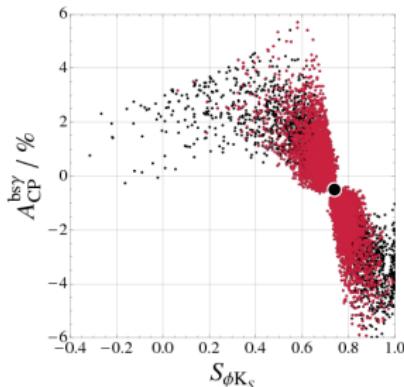
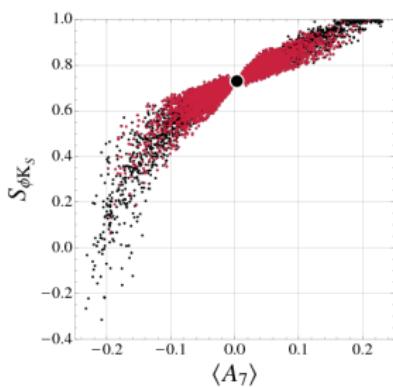
RVV



- Orange (Blue) points: UT tension solved through contribution to $\Delta M_d / \Delta M_s$ (ϵ_K)
- Scan ranges: $m_0 < 2 \text{ TeV}$, $M_{1/2} < 1 \text{ TeV}$, $|A_0| < 3m_0$, $5 < \tan \beta < 55$

Pattern of NP effects in the δLL model:

- No large effects in $S_{\psi\phi}$
- Large, correlated effects in $S_{\phi K_S}$, $S_{\eta' K_S}$, $A_{\text{CP}}(b \rightarrow s\gamma)$, $\langle A_{7,8} \rangle$ and EDMs
- $\langle A_{7,8} \rangle$: T-odd CP asymmetries in $B \rightarrow K^* \ell^+ \ell^-$

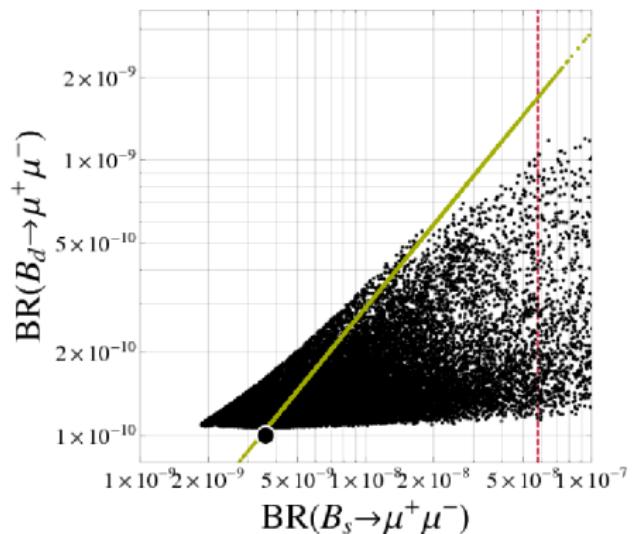


- Scan ranges: $m_0 < 2$ TeV, $M_{1/2} < 1$ TeV, $|A_0| < 3m_0$, $5 < \tan \beta < 55$,

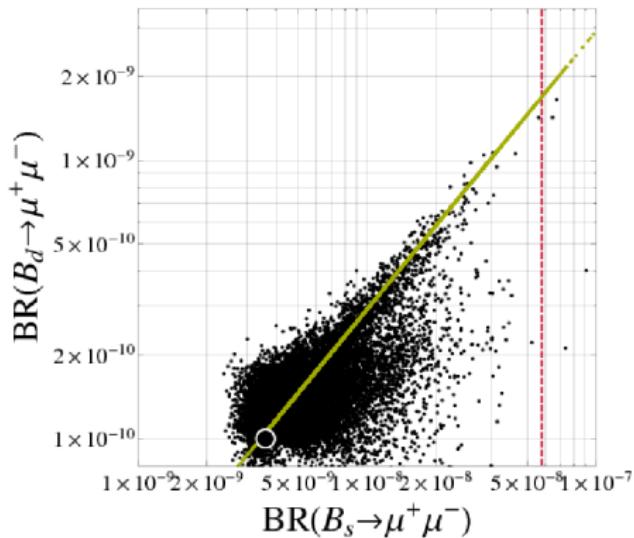
[Altmannshofer et al., '09]

$Br(B_s \rightarrow \mu^+ \mu^-)$ vs. $Br(B_d \rightarrow \mu^+ \mu^-)$

Abelian (AC)



Non abelian (RVV)



[Altmannshofer et al., '09]

$$Br(B_s \rightarrow \mu^+ \mu^-) / Br(B_d \rightarrow \mu^+ \mu^-) = |V_{ts}/V_{td}|^2 \text{ in MFV models}$$

[Hurth, Isidori, Kamenik & Mescia, '08]

CPV in D-physics

CPV in $D^0 - \bar{D}^0$ $\sim ((V_{cb} V_{ub}) / (V_{cs} V_{us})) \sim 10^{-3}$ in the SM

- $\langle D^0 | \mathcal{H}_{\text{eff}} | \bar{D}^0 \rangle = M_{12} - \frac{i}{2} \Gamma_{12}, \quad |D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$
 - $\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{i}{2} \Gamma_{12}^*}{M_{12} + \frac{i}{2} \Gamma_{12}}}, \quad \phi = \text{Arg}(q/p)$
 - $x = \frac{\Delta M_D}{\Gamma} = 2\tau \text{Re} \left[\frac{q}{p} (M_{12} - \frac{i}{2} \Gamma_{12}) \right]$
 - $y = \frac{\Delta \Gamma}{2\Gamma} = -2\tau \text{Im} \left[\frac{q}{p} (M_{12} - \frac{i}{2} \Gamma_{12}) \right]$
 $\mathbf{S}_f = 2\Delta Y_f = \frac{1}{\Gamma_D} (\hat{\Gamma}_{\bar{D}^0 \rightarrow f} - \hat{\Gamma}_{D^0 \rightarrow f})$
 $\eta_f^{\text{CP}} S_f = x \left(\left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) \sin \phi - y \left(\left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) \cos \phi$
- $$\mathbf{a}_{\text{SL}} = \frac{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) - \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)}{\Gamma(D^0 \rightarrow K^+ \ell^- \nu) + \Gamma(\bar{D}^0 \rightarrow K^- \ell^+ \nu)} = \frac{|q|^4 - |p|^4}{|q|^4 + |p|^4}$$

[Nir et al., Kagan et al., Petrov et al., Bigi et al., Buras et al., ...]

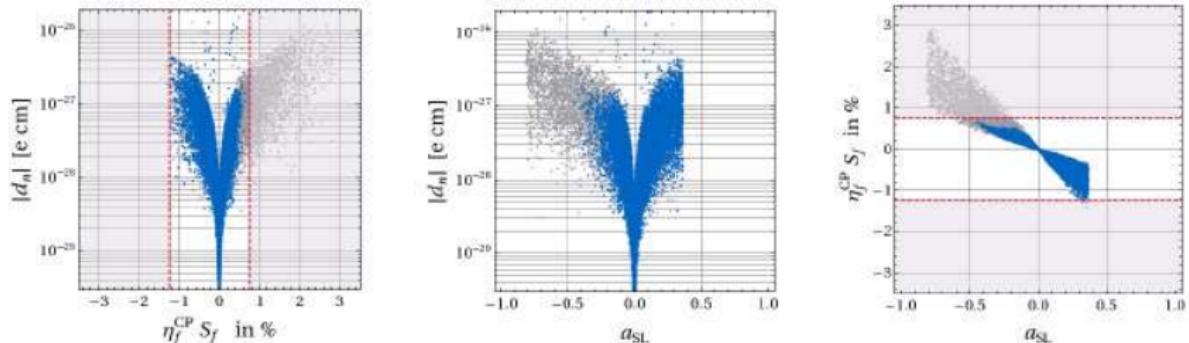


FIG. 3: Correlations between d_n and S_f (left), d_n and a_{SL} (middle) and a_{SL} and S_f (right) in SUSY alignment models. Gray points satisfy the constraints (8)-(10) while blue points further satisfy the constraint (11) from ϕ . Dashed lines stand for the allowed range (18) for S_f .

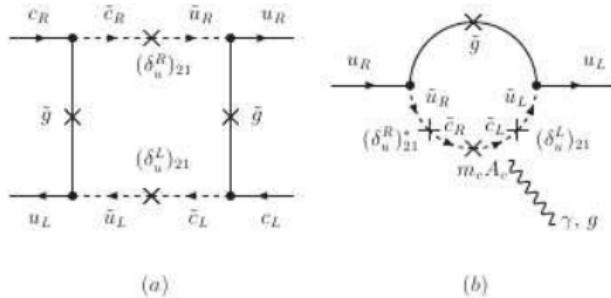
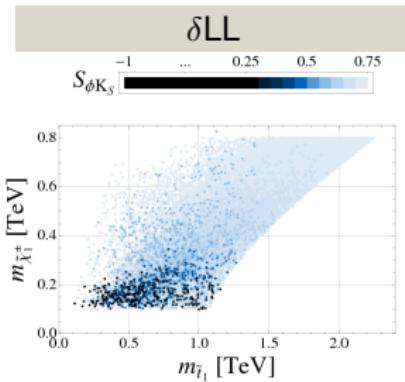
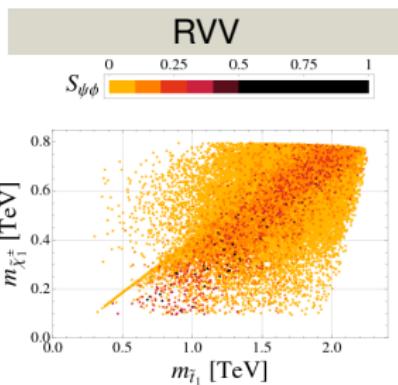
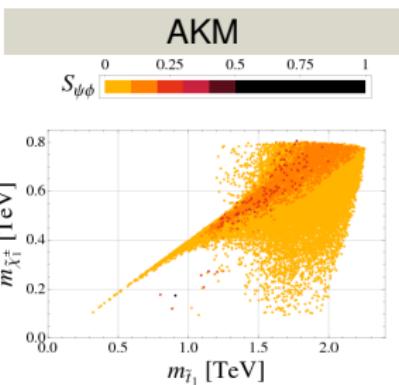
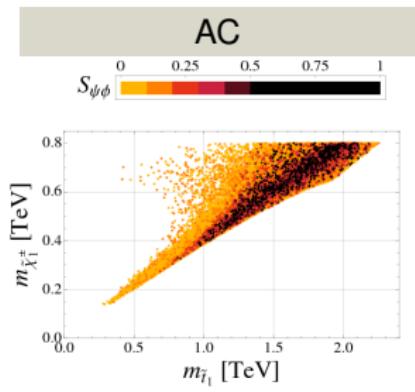


FIG. 2: Examples of relevant Feynman diagrams contributing (a) to $D^0 - \bar{D}^0$ mixing and (b) to the up quark (C)EDM in SUSY alignment models.

LHC vs. flavour



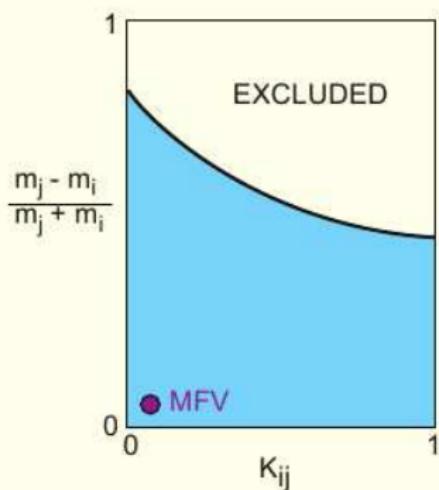
- Large effects in $S_{\psi\phi}$ even possible for spectra beyond the LHC reach in the models with RH currents
- Large effects in $S_{\phi K_S}$ not possible for spectra beyond the LHC reach in the δLL model

“DNA-Flavour Test”

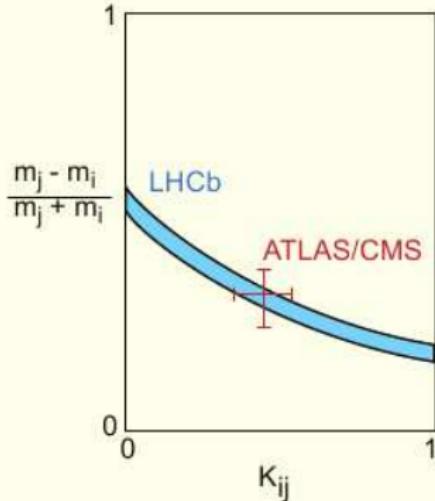
	GMSSM	AC	RVV2	AKM	δLL	FBMSSM	
$S_{\phi K_S}$	★★★	★★★	●●	■	★★★	★★★	
$A_{CP}(B \rightarrow X_s \gamma)$	★★★	■	■	■	★★★	★★★	
$B \rightarrow K^{(*)} \nu \bar{\nu}$	●●	■	■	■	■	■	
$\tau \rightarrow \mu \gamma$	★★★	★★★	★★★	■	★★★	★★★	
$D^0 - \bar{D}^0$	★★★	★★★	■	■	■	■	
$A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$	★★★	■	■	■	★★★	★★★	vs.
$A_9(B \rightarrow K^* \mu^+ \mu^-)$	★★★	■	■	■	■	■	 
$S_{\psi \phi}$	★★★	★★★	★★★	★★★	■	■	
$B_s \rightarrow \mu^+ \mu^-$	★★★	★★★	★★★	★★★	★★★	★★★	
ϵ_K	★★★	■	★★★	★★★	■	■	
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	★★★	■	■	■	■	■	
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	★★★	■	■	■	■	■	
$\mu \rightarrow e \gamma$	★★★	★★★	★★★	★★★	★★★	★★★	
$\mu + N \rightarrow e + N$	★★★	★★★	★★★	★★★	★★★	★★★	
d_n	★★★	★★★	★★★	★★★	●●	★★★	
d_e	★★★	★★★	★★★	●●	■	★★★	
$(g-2)_\mu$	★★★	★★★	★★★	●●	★★★	★★★	

[Altmannshofer et al., '09]

The SUSY flavor plane



Flavor Factories
MFV



FF+ATLAS/CMS
Non-MFV

[Nir @ Planck '09]

► Flavour physics in the LHC era

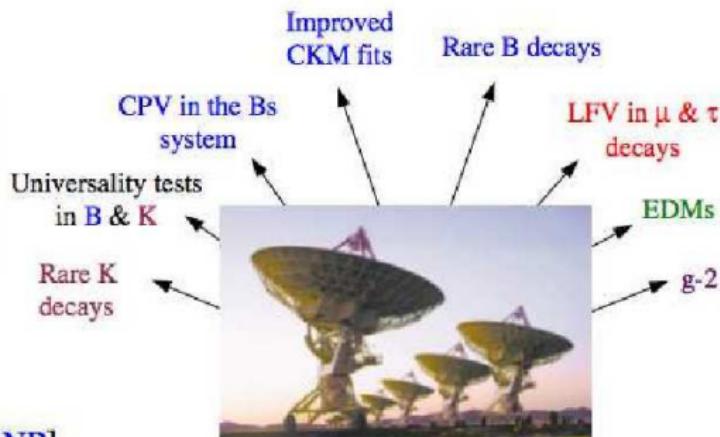
LHC [high p_T]

A *unique* effort toward the high-energy frontier



[to determine the energy scale of NP]

Flavour physics



A *collective* effort toward the high-intensity frontier

[to determine the flavour structure of NP]