

Lifetimes, mixings and widths of neutral b and c hadrons

Review of the results on

- D^0 mixing

-Neutral B meson widths

-B hadron lifetimes

See other talks in this session and Tuesday for CPV in mixing

Sneha Malde
University of Oxford

D^0 mixing

Meson Mixings and Width differences

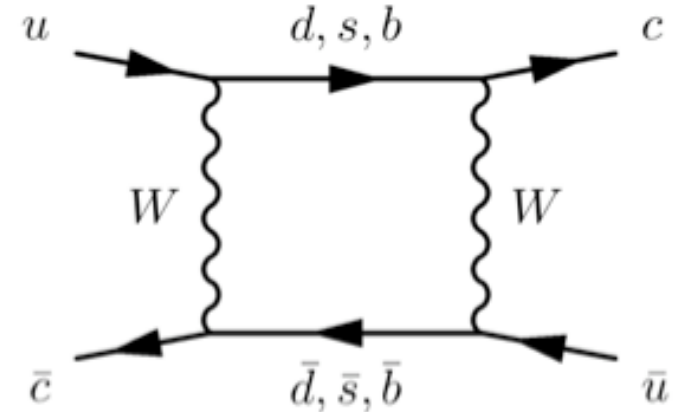
Taking the D^0 meson as an example:

Flavor	Mass
$ D^0(c\bar{u})\rangle$	$ D^1(M_1, \Gamma_1)\rangle$
$ \bar{D}^0(\bar{c}u)\rangle$	$ D^2(M_2, \Gamma_2)\rangle$

$$|D^1\rangle = p|D^0\rangle + q|\bar{D}^0\rangle$$

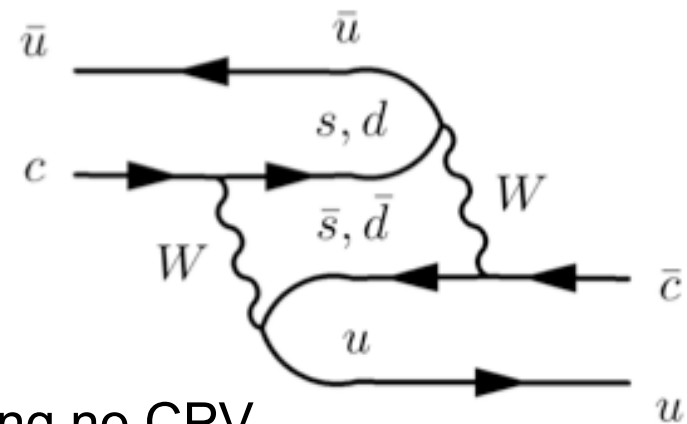
$$|D^2\rangle = p|D^0\rangle - q|\bar{D}^0\rangle$$

$$|p|^2 + |q|^2 = 1, p = q = 1/\sqrt{2} \text{ assuming no CPV}$$



Short range

Long range



Meson Mixings and Width differences

Useful to define these mixing parameters

$$x = \frac{M_1 - M_2}{\Gamma}$$
$$y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}$$

	x	y
K^0 (1957)	0.95	0.99
B^0 (1987)	0.78	~0
B_s (2006)	26	0.15
D^0 (2007)	0.0098	0.0083

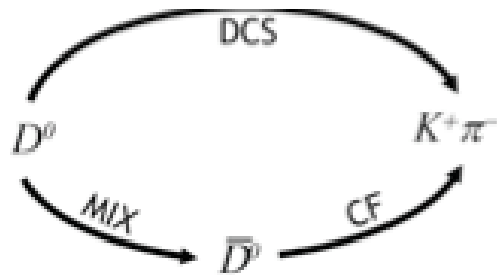
D system also mixes the least

D meson - fraction of one oscillation has occurs in ~10 lifetimes

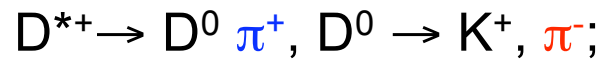
D⁰ mixing - “Wrong Sign” Decays

Tag flavor of the D⁰ by using decay D^{*+} → D⁰ π⁺

Right sign: D^{*+} → D⁰ π⁺, D⁰ → K⁻ π⁺ Cabibbo favored decay (CF)



Doubly Cabibbo suppressed decay (DCS)



Mixing then Cabibbo favored decay



$$\frac{dN_{WS}}{dt}(t) \propto e^{-\Gamma t} \left[\underbrace{R_D}_{\text{DCS}} + \underbrace{y'(\Gamma t)\sqrt{R_D}}_{\text{Interference}} + \underbrace{\frac{x'^2 + y'^2}{4}(\Gamma t)^2}_{\text{Mixing}} \right]$$

Can only measure x'² and y'

non-0 value is signature of mixing

$$x' = x \cos \delta + y \sin \delta$$

$$y' = y \cos \delta - x \sin \delta$$

δ is the strong phase

Experimental ingredients

Time dependent measurements

Accurate measurement of production and decay vertex

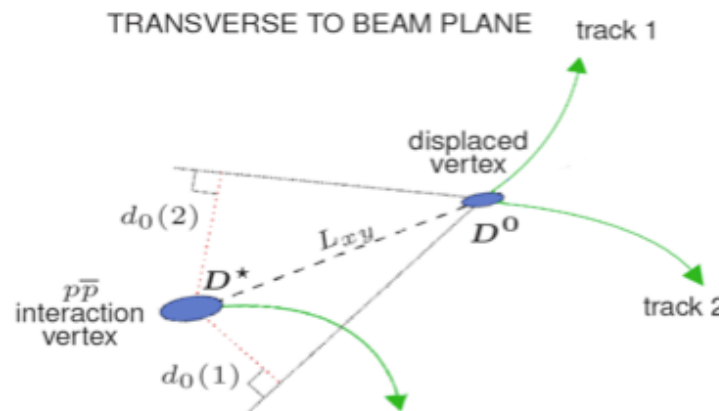
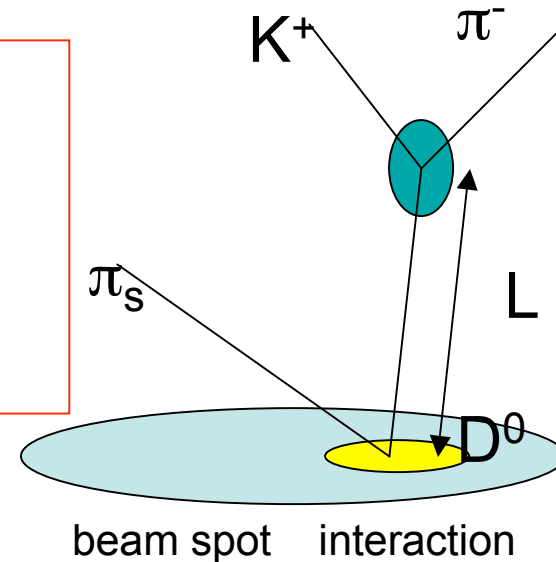
Silicon vertex detectors

BaBar

3-D flight path

$L \sim 200 \mu\text{m}$

$\sigma_L \sim 100 \mu\text{m}$



CDF

Measurement in transverse plane

Trigger requires displaced vertex

$L_{xy} > 200 \mu\text{m}$

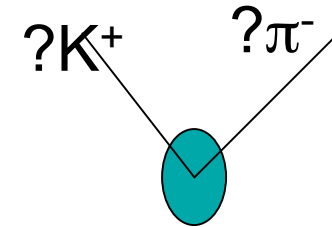
Analysis requires $L_{xy} / \sigma_{L_{xy}} > 4$

Experimental ingredients (2)

Identification of pion from kaon

Excellent at BaBar and Belle [purpose built detector components]

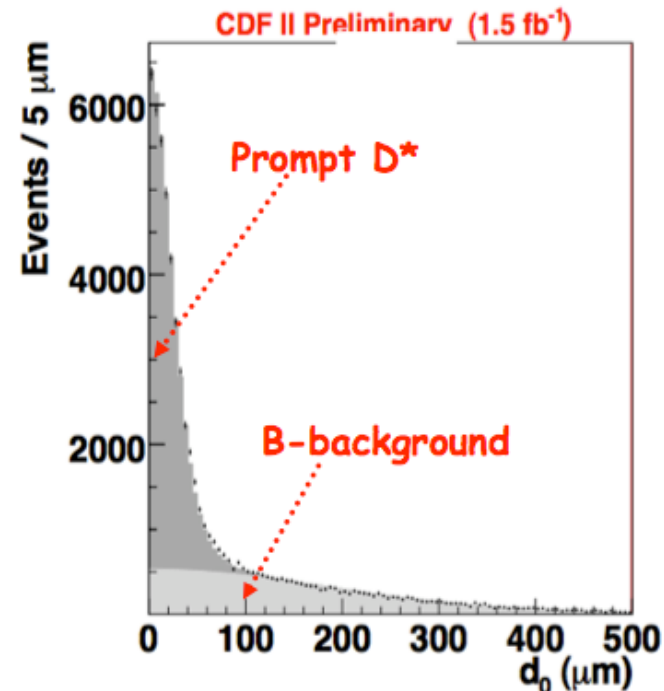
Statistical separation at CDF. Add cut: WS events require a RS mass cut to reduce doubly misidentified tracks



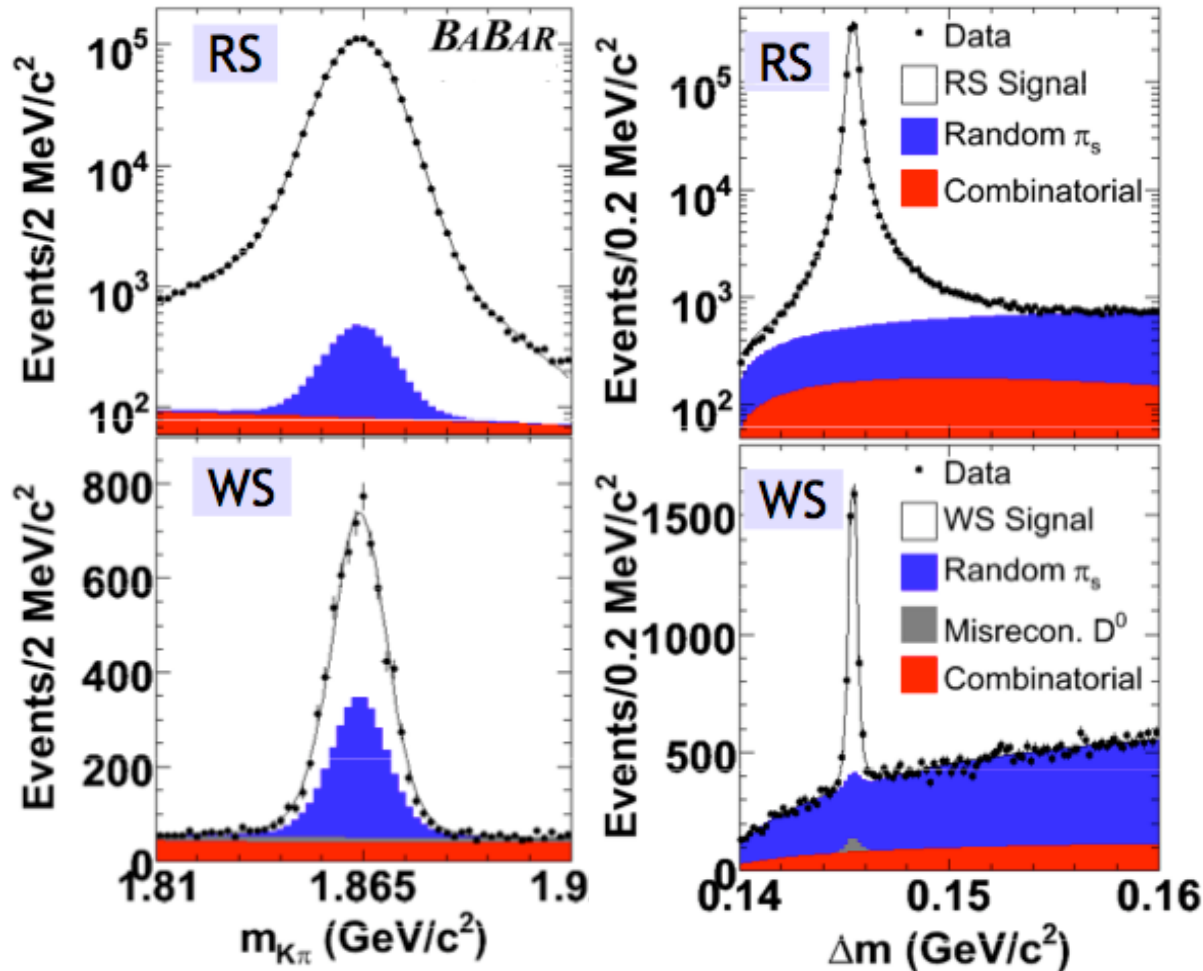
Removal of D^* from B bkg

B factories: Minimum momentum requirements in the CM frame.

CDF: Analysis of the IP distribution to determine secondary production contribution



Analysis strategy

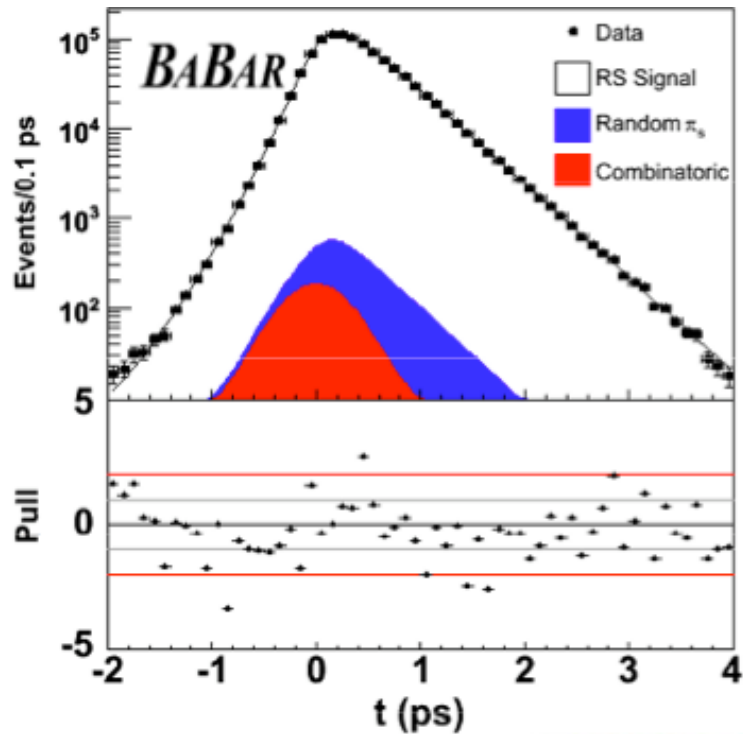


Sample composition determined from fit to $m_{K\pi}$ and Δm ($m(D^*) - m(D^0)$)

384 fb^{-1}

RS: 1141500 ± 1200 WS: 4030 ± 90

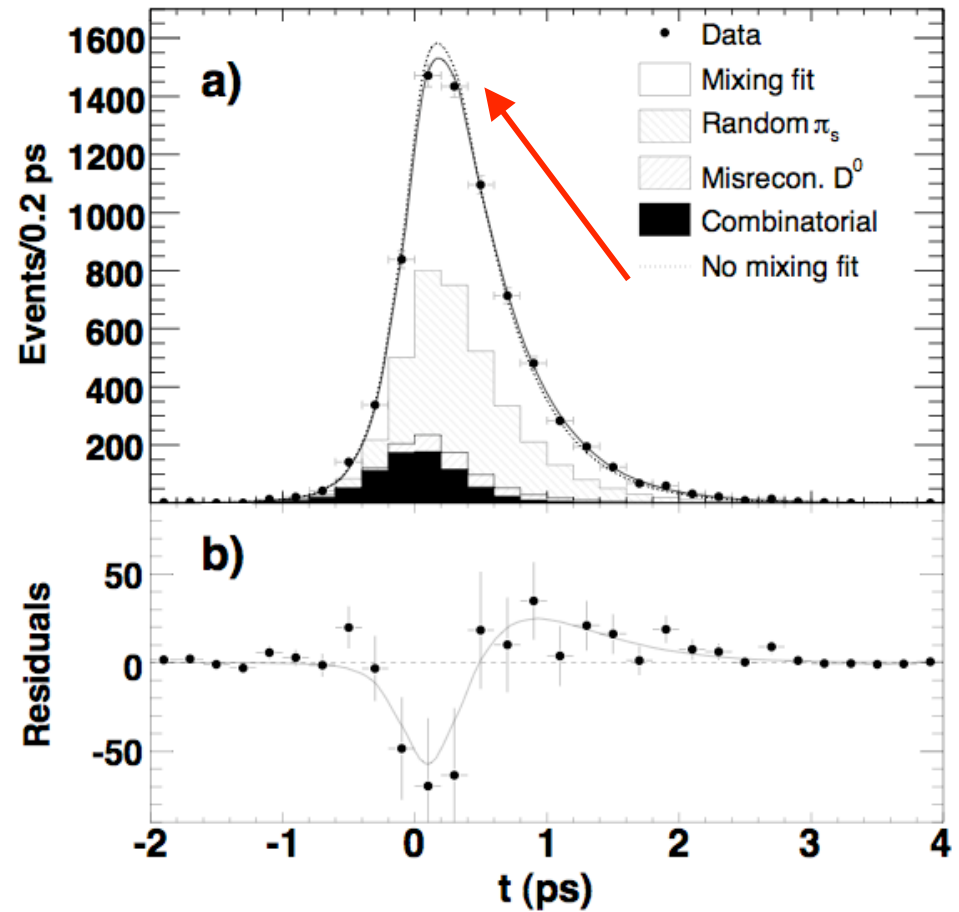
Time fit including mixing



Lifetime (exponential) and resolution fitted in the RS sample.

$\tau(D^0)$ consistent with PDG

In WS fit resolution fixed from RS fit

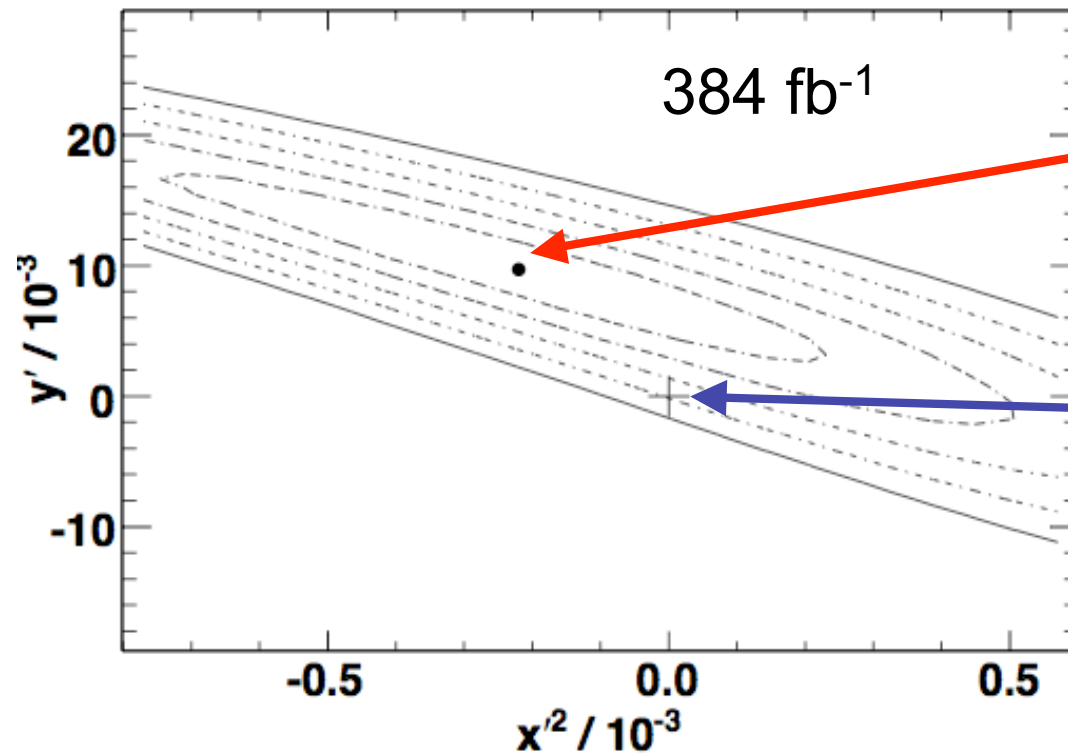


WS fit with mixing parameters provides better fit to data

Allowed x'^2 y' contours



Current status using the WS decays:



Best fit point

Inconsistent with
mixing at 3.9σ

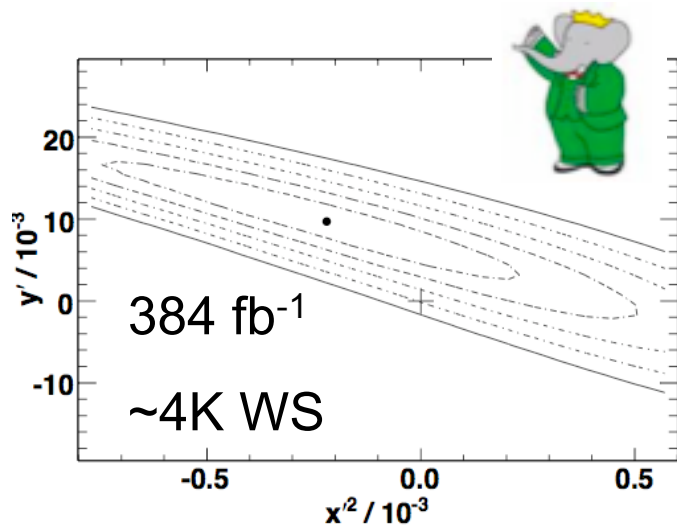
No mixing point

$$R_D: (3.03 \pm 0.16 \pm 0.10) \times 10^{-3}$$

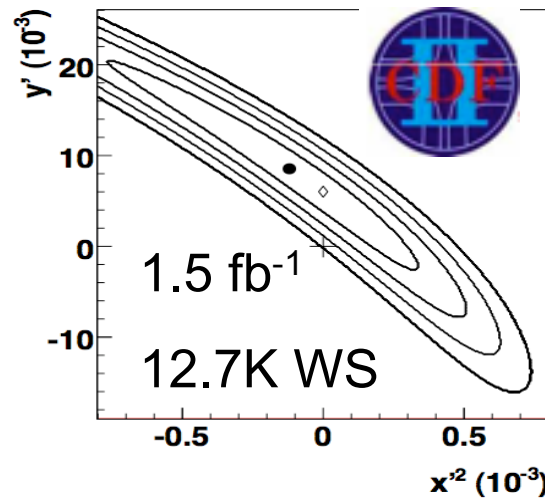
$$x'^2: (-0.22 \pm 0.30 \pm 0.21) \times 10^{-3}$$

$$y': (9.7 \pm 4.4 \pm 3.1) \times 10^{-3}$$

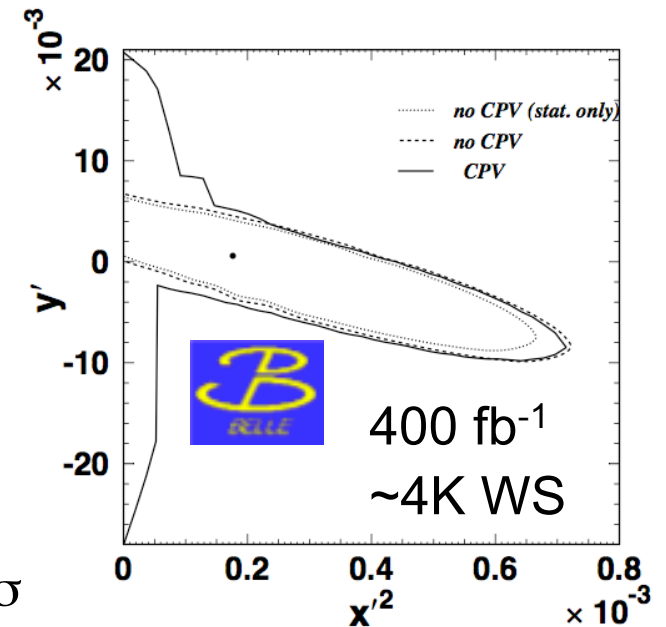
WS analysis at other experiments



Evidence of mixing at 3.9σ



Evidence of mixing at 3.8σ



No mixing point at 2.0σ

Agreement between the 3 experiments

Different production methods

Different analysis methods

Time-dependent amplitude analysis of $D^0 \rightarrow K_s hh$

Allows direct measurement of x and y

D^* used to tag whether $D^0/\overline{D^0}$

Dalitz plot $s^+ = M(K_s h^+)$ $s^- = M(K_s h^-)$

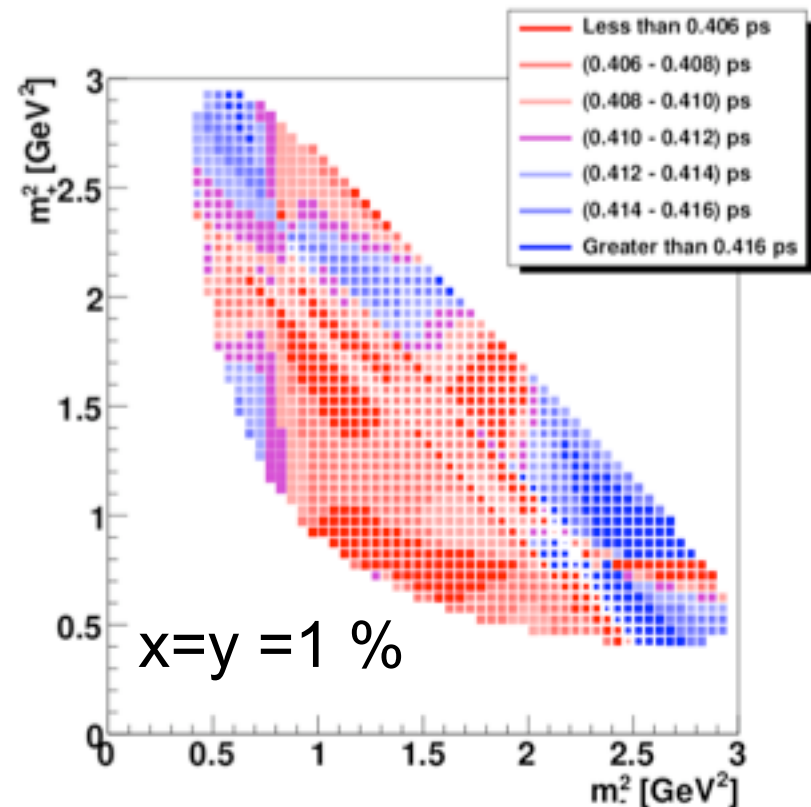
In the absence of CPV:

$$A(s^+, s^-) = \overline{A}(s^-, s^+)$$

Distribution of events across Dalitz space vs. $t(D^0)$

Variation \rightarrow signature of mixing.

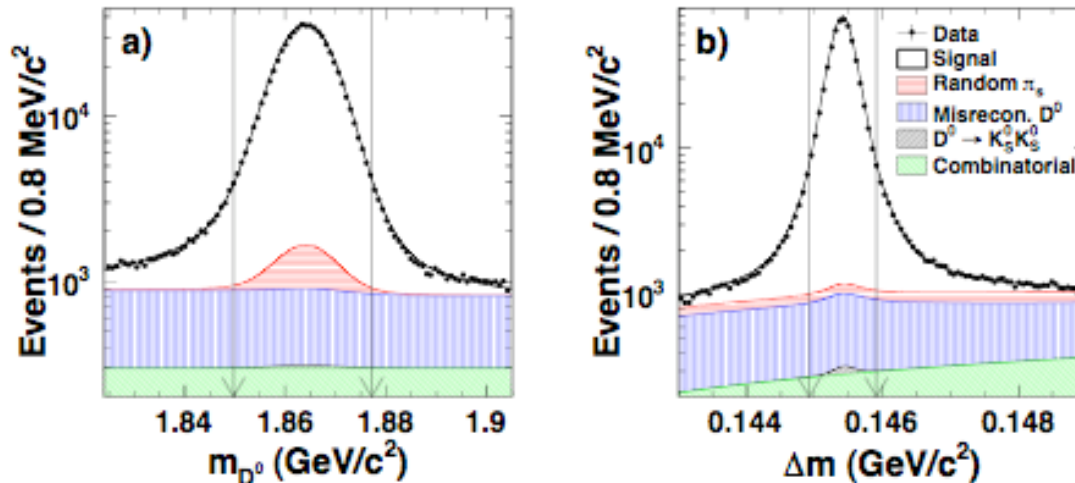
Sensitivity to x and y comes mainly from regions with interference of CF and DCS, or CP eigenstates



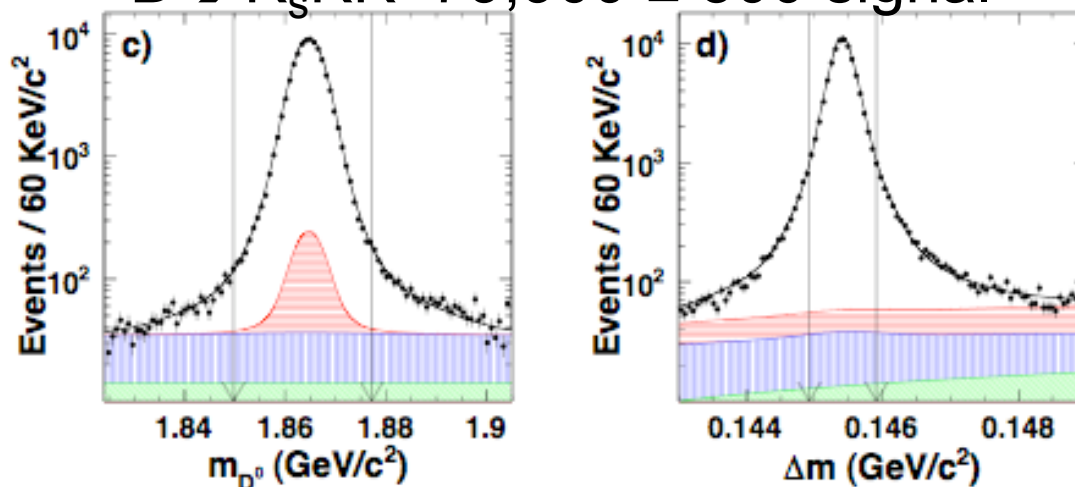
Yields and Purities



$D \rightarrow K_s \pi \pi$ $540,800 \pm 800$ signal



$D \rightarrow K_s K K$ $79,900 \pm 300$ signal



First stage

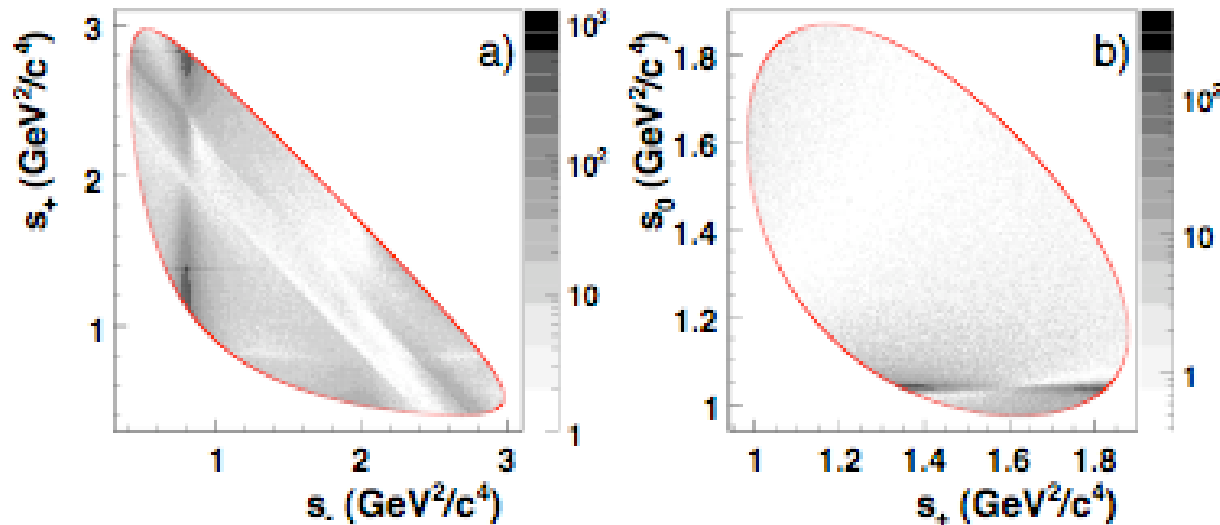
Fit the signal and the background shapes using the m and Δm

Fix the bkg component types and define the signal regions

Purity 98.5 % ($K_s \pi \pi$)

99.2 % ($K_s K K$)

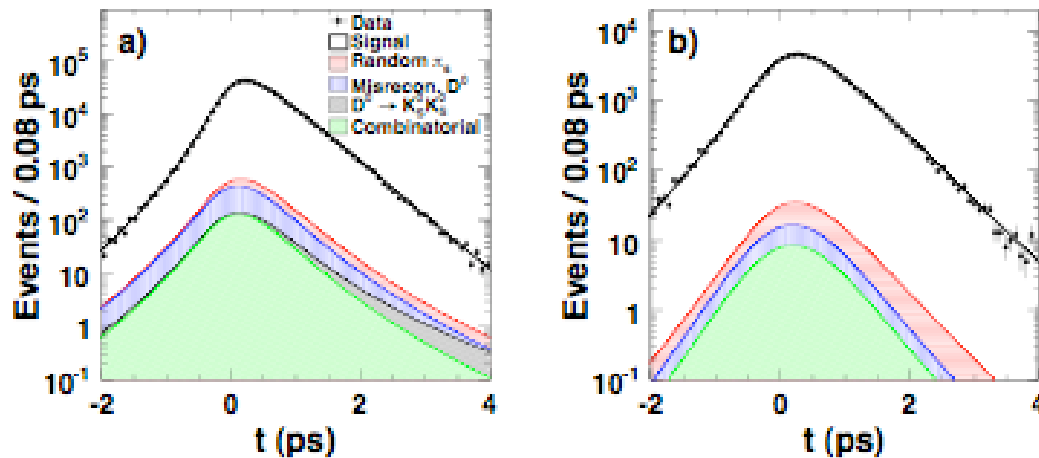
Time dependent amplitude fit



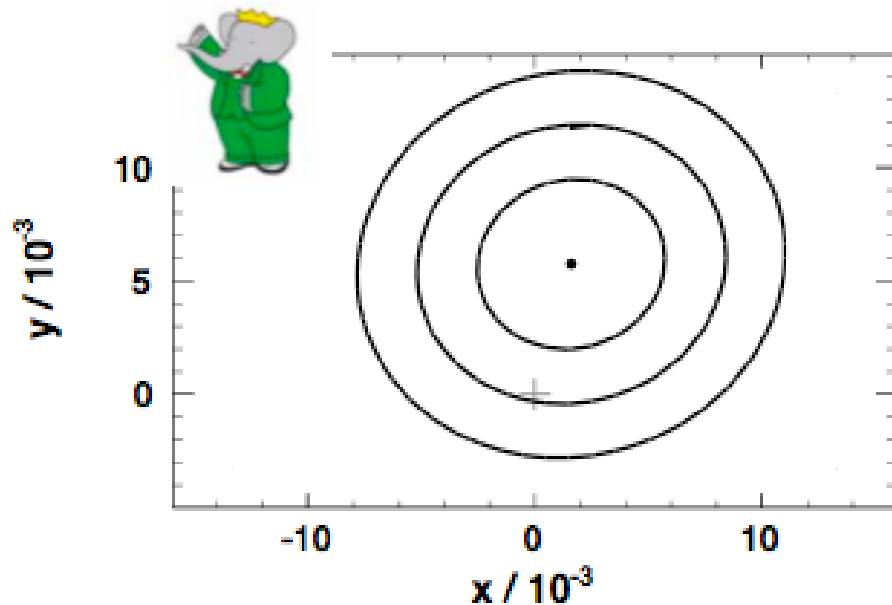
Amplitude model is defined by coherent sum of quasi-two body amplitudes.

x and y determined from a likelihood fit.

PDF based on $A(s^+, s^-)$ and the decay time.



x , y values



Dis-favours no mixing hypothesis at 1.9σ

$$x = (0.16 \pm 0.23 \pm 0.12 \pm 0.08)\%$$

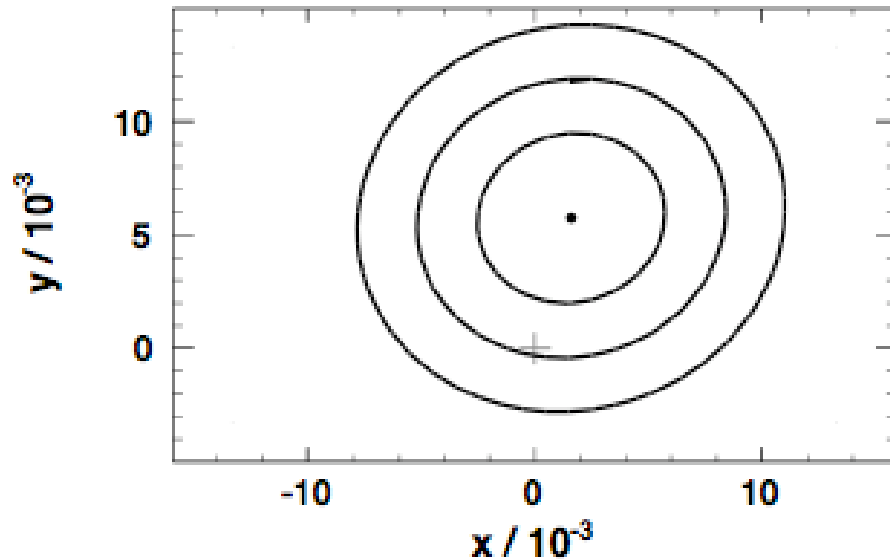
$$y = (0.57 \pm 0.20 \pm 0.13 \pm 0.07)\%$$

Most precise single measurement of x

Consistent between the two decay channels

$$468.5 \text{ fb}^{-1}$$

x , y values



$$x = (0.16 \pm 0.23 \pm 0.12 \pm 0.08)\%$$

$$y = (0.57 \pm 0.20 \pm 0.13 \pm 0.07)\%$$

Most precise single measurement of x



Consistent between the two decay channels

Belle $K_s \pi \pi$ analysis 540 fb^{-1}

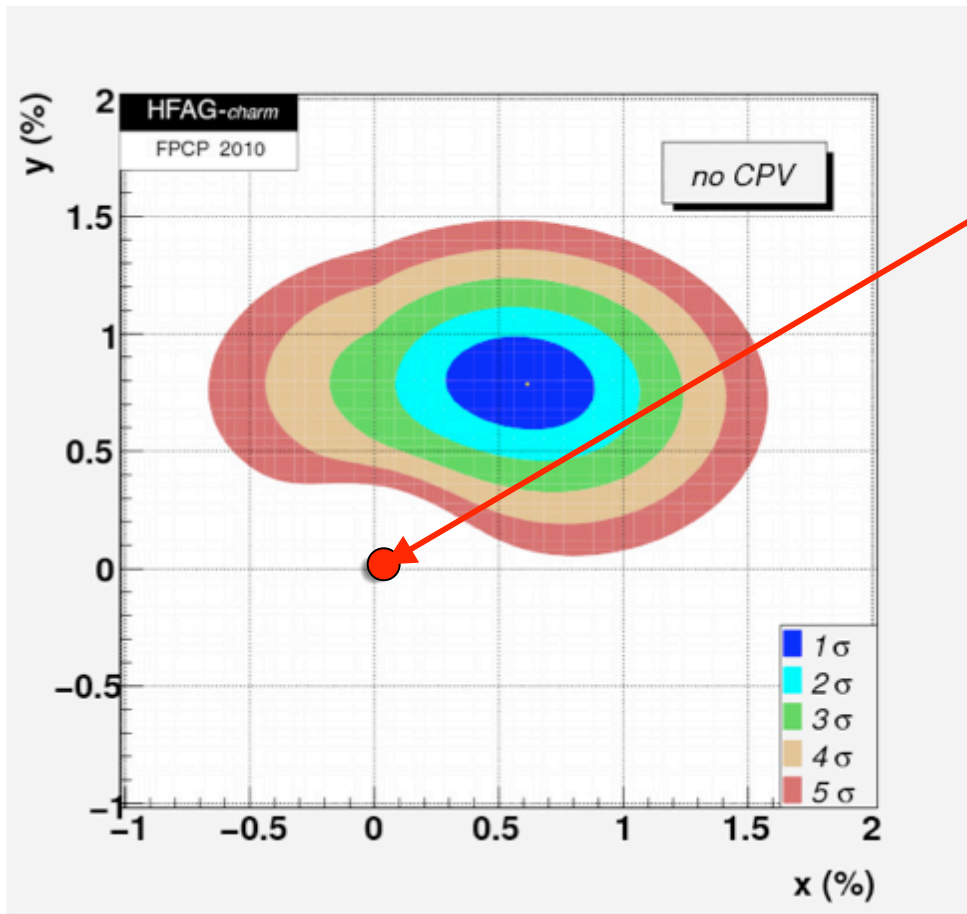
$$x = 0.80 \pm 0.29^{+0.09}_{-0.07} \text{ }^{+0.10}_{-0.14} \%$$

$$y = 0.33 \pm 0.24 \text{ }^{+0.08}_{-0.12} \text{ }^{+0.06}_{-0.08} \%$$



Status today

While no one measurement has observed mixing at 5σ the combined evidence is clear:



No mixing point excluded at 10σ level

Prospects:

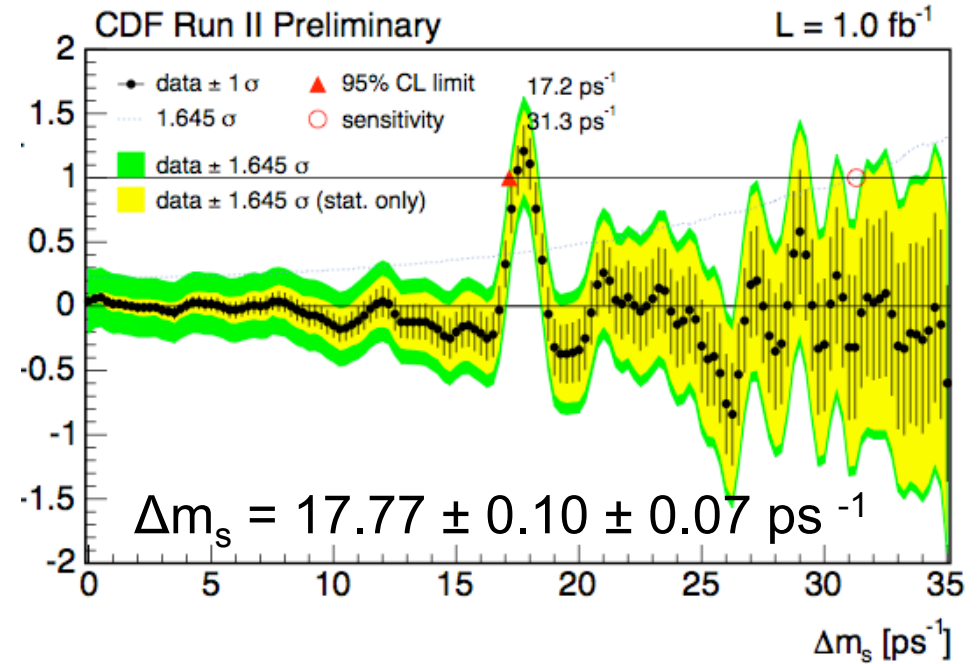
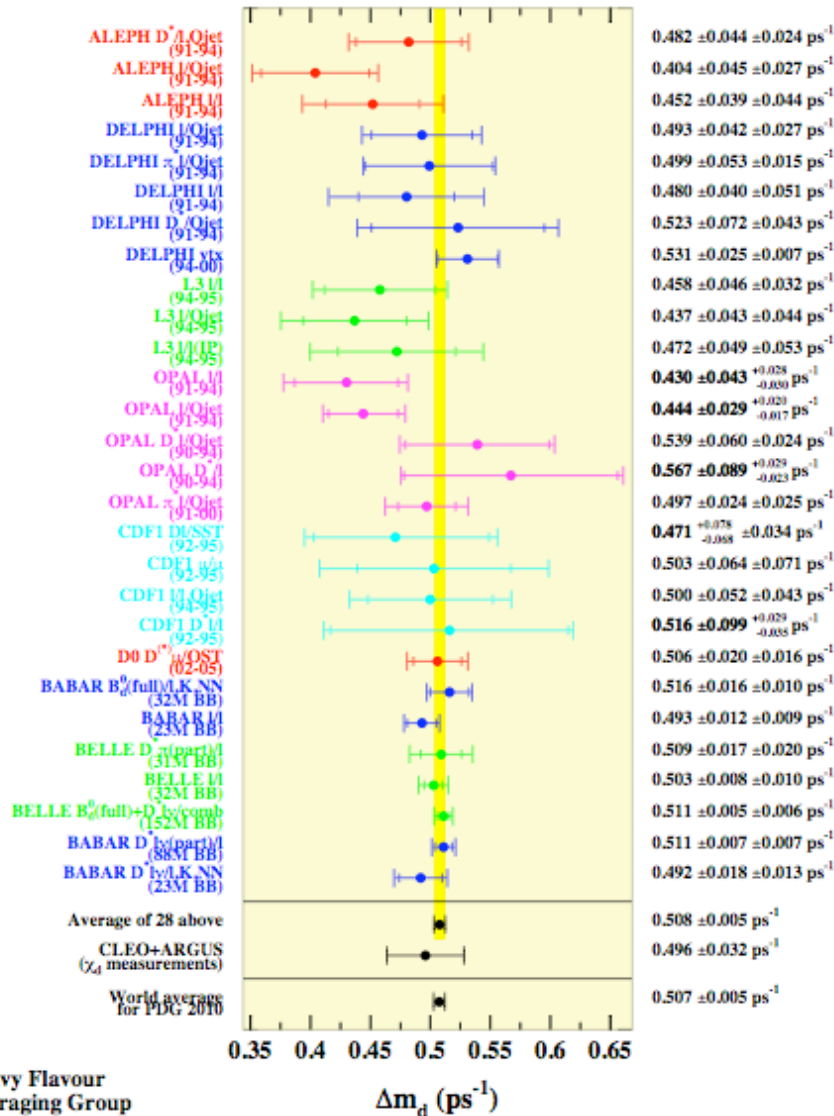
CDF has much more data to analyse

Results from LHCb soon

M. Gersabeck

B meson width difference

Neutral B meson mixing



B^0 mixing first seen in 1987

$$\Delta m_d = 0.507 \pm 0.005 \text{ ps}^{-1}$$

Confirmed by many experiments

B_s mixing so far only at the Tevatron

B_q Width Difference

Width difference provides extra test of the standard model

$$\frac{\Delta\Gamma_d}{\Gamma_d} = 41_{-10}^{+9} \cdot 10^{-4}$$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = 0.13 \pm 0.04$$

BaBar measured

$$\text{sign Re}(\lambda_{cp})\Delta\Gamma/\Gamma = 0.009 \pm 0.037$$

Uses B decay in a CP eigenstate

Smaller difference for B_d

Width differences caused by existence of final states to which both the B^0 and \overline{B}^0 can decay.

Involves $b \rightarrow c\overline{c}q$, Cabibbo suppressed if $q=d$

see Tuesday's talk U. Nierste

B_q Width Difference

Width difference provides extra test of the standard model

$$\frac{\Delta\Gamma_d}{\Gamma_d} = 41_{-10}^{+9} \cdot 10^{-4}$$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = 0.13 \pm 0.04$$

Additionally can be used as a test of NP

$$\Delta\Gamma_s = \Delta\Gamma_s^{SM} \cos(2\beta_s)$$

Assuming no CPV B_s^L is CP even, B_s^H is CP odd

Measure lifetimes in CP specific modes ($\Delta\Gamma^{CP}$)

Measure $\Delta\Gamma$ directly $B_s \rightarrow J/\psi\phi$

Use branching ratios $B_s \rightarrow D_s D_s$

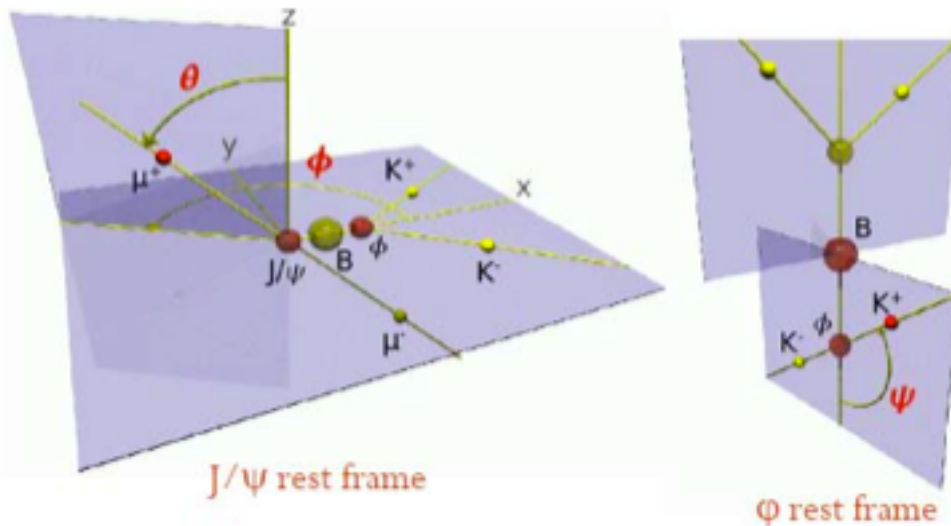
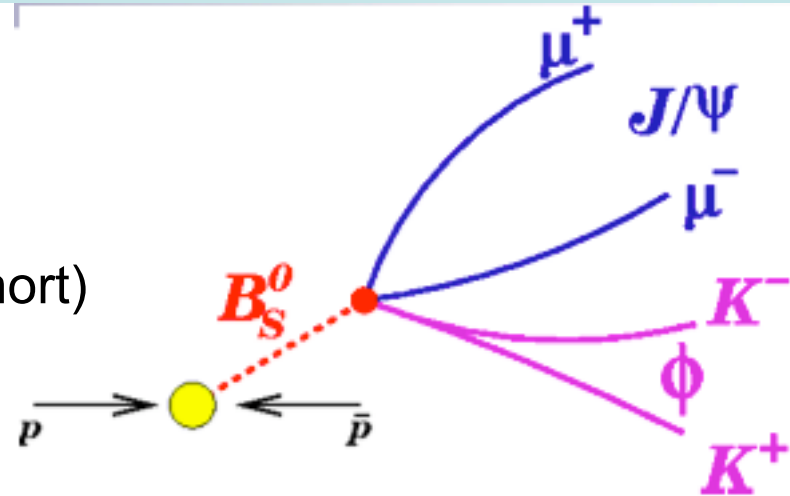
$B_s \rightarrow J/\psi \phi$

$B_s(\text{spin-0}) \rightarrow J/\psi(\text{spin-1}) \phi(\text{spin-1})$

3 angular momentum states

$L=0$ (s-wave), 2 (d-wave) CP even (short)

$L=1$ (p-wave), CP odd (long)

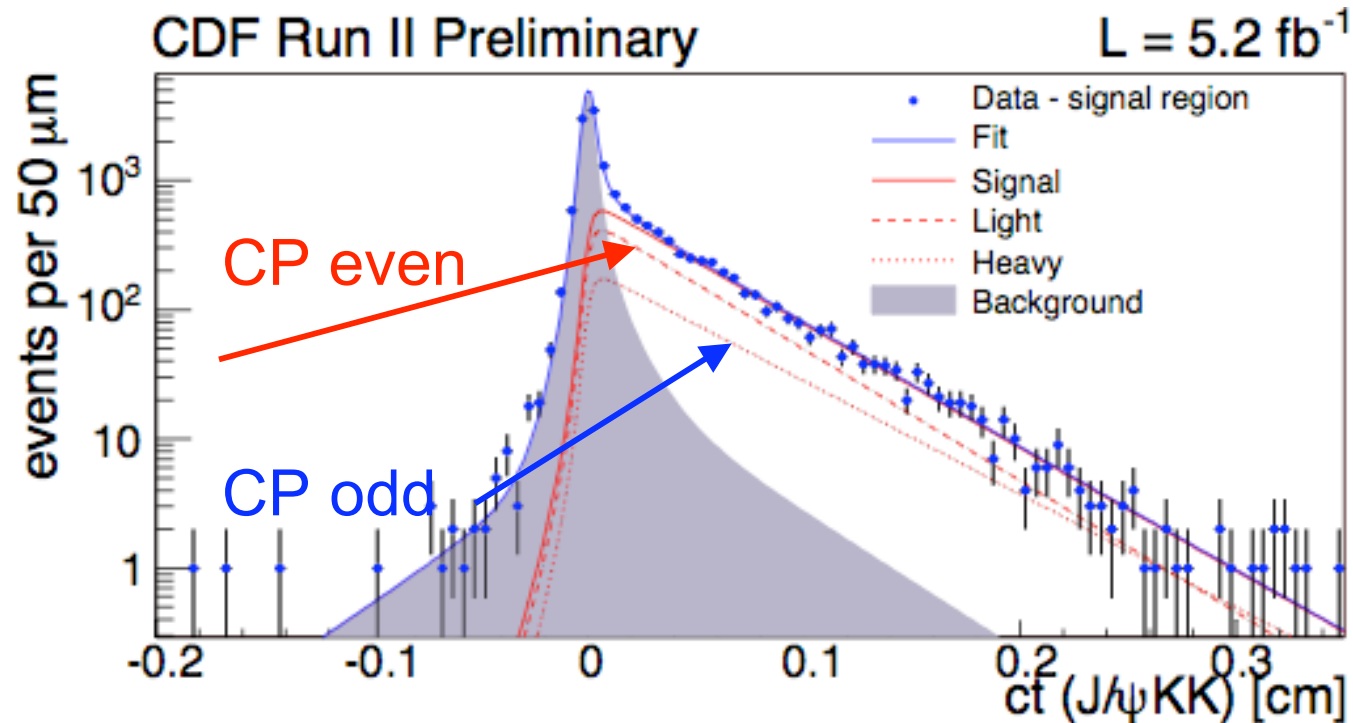


Three decay angles

$\rho(\theta, \phi, \psi)$

Describe the angular direction of the decay products

Measurement of width difference



Simultaneous fit to the mass, lifetime, and angular distributions

-provides separation of CP odd and even

Allows measurement of the mean lifetime and width difference

$$\tau_s = 1.53 \pm 0.025 \text{ (stat.)} \pm 0.012 \text{ (syst.) ps}$$

$$\Delta\Gamma = 0.075 \pm 0.035 \text{ (stat.)} \pm 0.01 \text{ (syst.) ps}^{-1}$$

$$\bar{\tau}_s = 1.45 \pm 0.04 \pm 0.01 \text{ ps}$$

$$\Delta\Gamma_s = 0.15 \pm 0.06 \pm 0.01 \text{ ps}^{-1}$$



5.2 fb⁻¹



6.2 fb⁻¹

Using Branching Fractions

Decay $B_s \rightarrow D_s^+ D_s^-$ CP Even ; $B_s \rightarrow D_s^{*+} D_s^{*-}$ CP Even to within 5 %

Under various theoretical assumptions $2 \times Br(B_s \rightarrow D_s^{(*)+} D_s^{(*)-}) \sim \frac{\Delta\Gamma}{\Gamma}$

see Tuesday's talk U. Nierste

“under various theoretical assumptions”

- i.e don't draw too many conclusions from a Branching fraction measurement

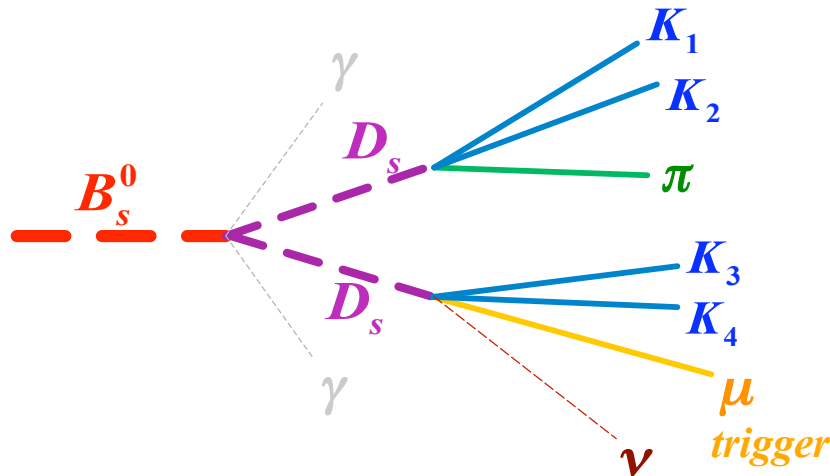
Nonetheless, $\tau(B_s \rightarrow D_s^+ D_s^-)$ is interesting

Using Branching Fractions



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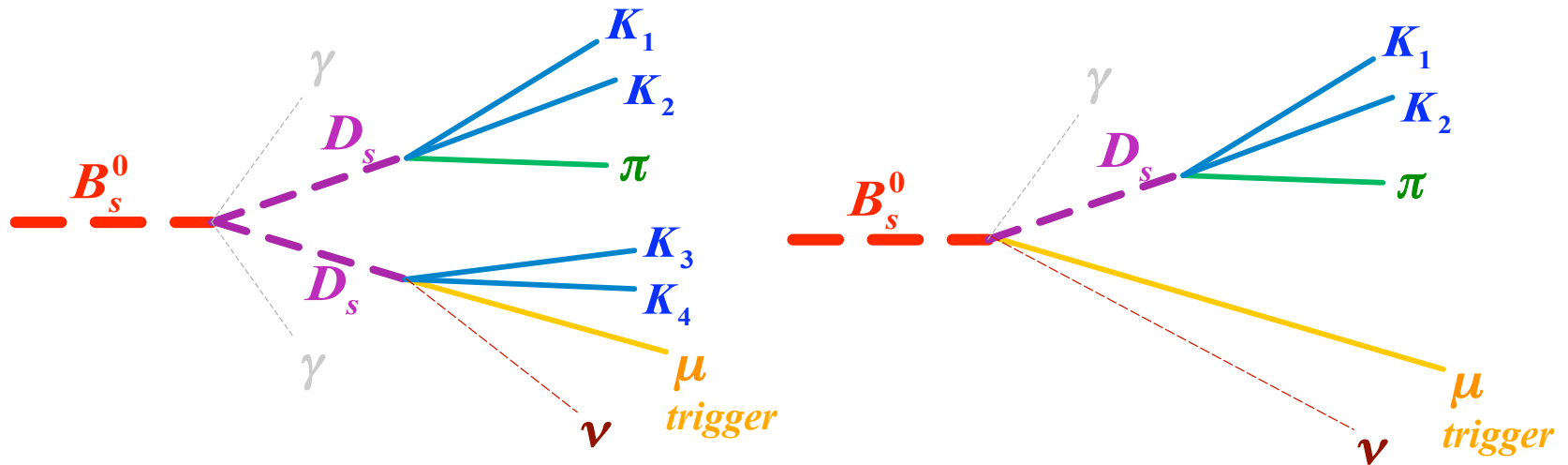


Using Branching Fractions



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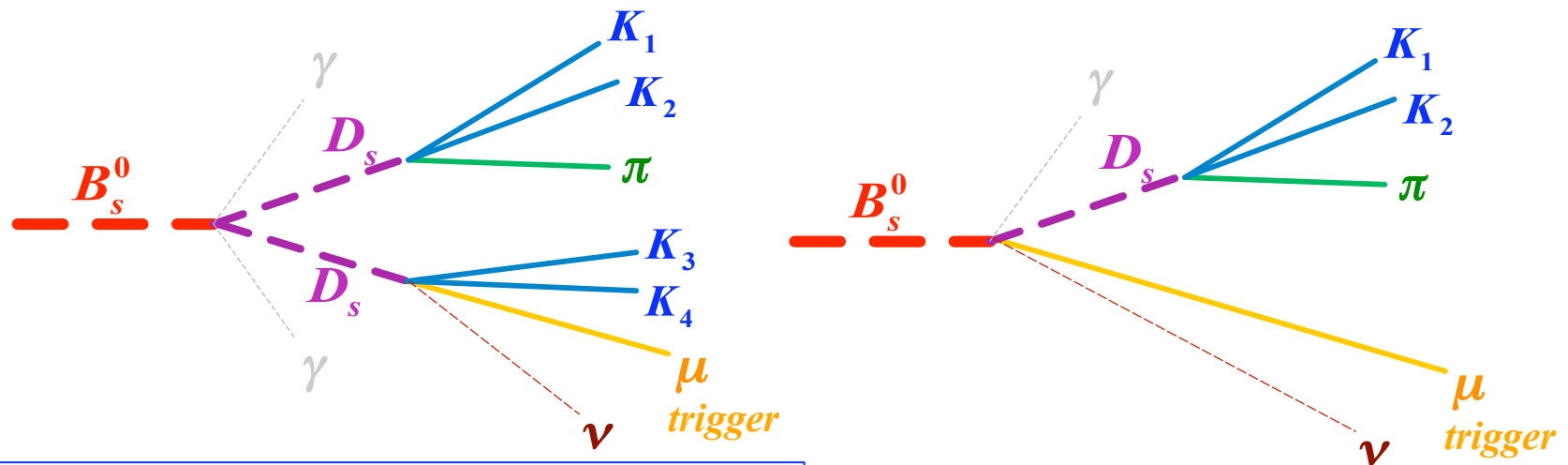


Using Branching Fractions



Decay $B_s \rightarrow D_s^+ D_s^-$ CP Even ; $B_s \rightarrow D_s^{*+} D_s^{*-}$ CP Even to within 5 %

Under various theoretical assumptions $2 \times Br(B_s \rightarrow D_s^{(*)+} D_s^{(*)-}) \sim \frac{\Delta\Gamma}{\Gamma}$



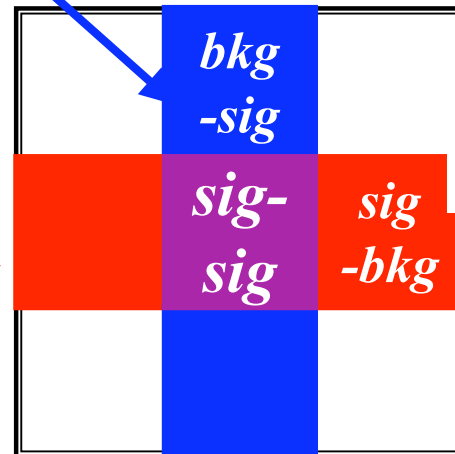
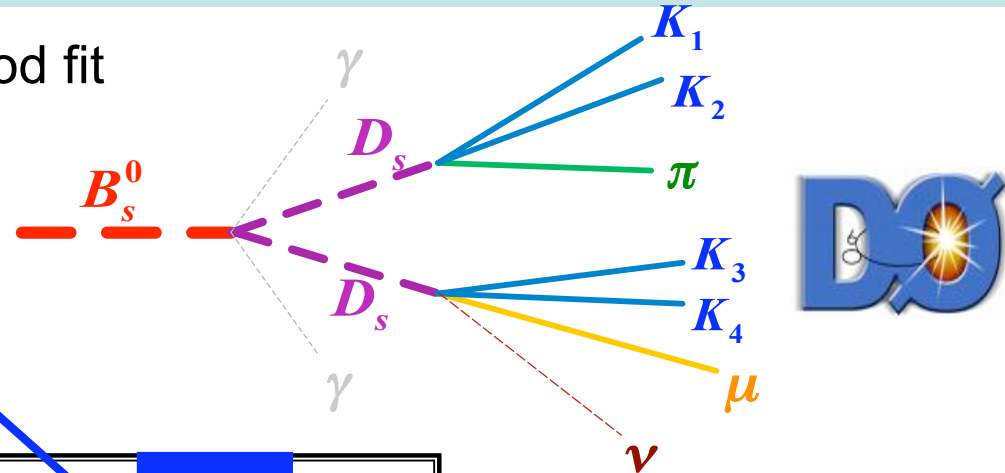
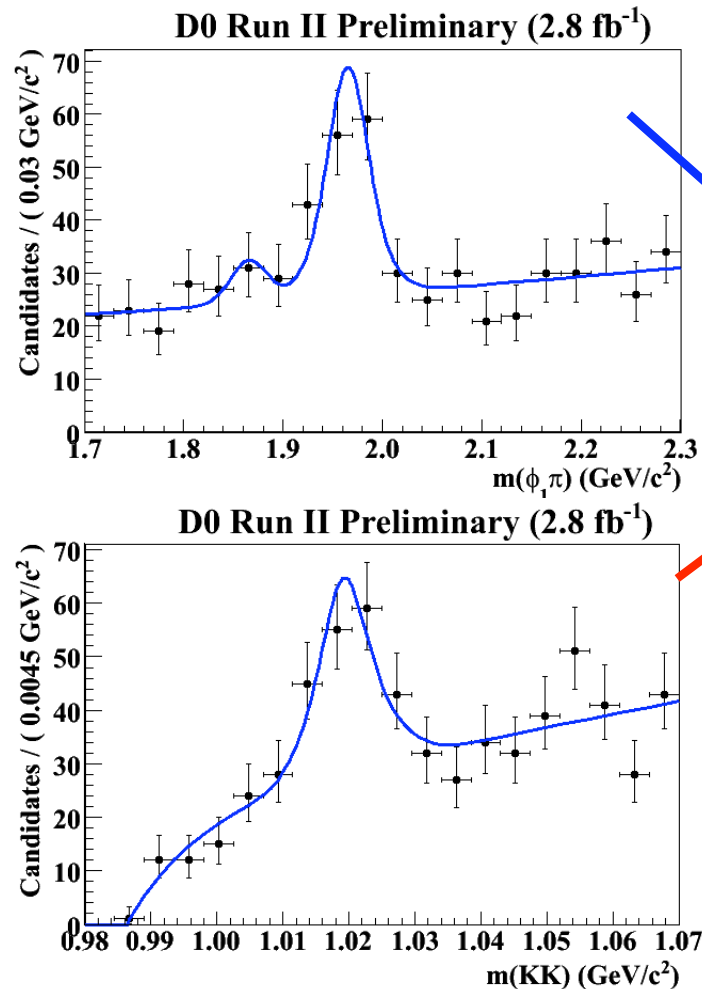
$$\frac{N(B_s \rightarrow D_s^{(*)+} D_s^{(*)-})}{N(B_s \rightarrow D_s^{(*)+} \mu \nu)} = 2R \cdot \frac{\epsilon(B_s \rightarrow D_s^{(*)+} D_s^{(*)-})}{\epsilon(B_s \rightarrow D_s^{(*)+} \mu \nu)}$$

$$R \equiv \frac{Br(B_s \rightarrow D_s^{(*)+} D_s^{(*)-}) \cdot Br(D_s \rightarrow \varphi \mu \nu) \cdot Br(\varphi \rightarrow K^+ K^-)}{Br(B_s \rightarrow D_s^{(*)+} \mu \nu)}$$

Many detector related systematics cancel

Branching fraction measurement

2-D likelihood maximum likelihood fit



$$N_{\text{sig}} = 26.6 \pm 8.4 \text{ events}$$

$$\mathcal{B}(B_s^0 \rightarrow D_s^{(*)+} D_s^{(*)-}) = 0.035 \pm 0.015.$$

$$\frac{\Delta\Gamma_s}{\Gamma_s} = 0.072 \pm 0.030.$$

“Width difference” without a lifetime fit

CDF also working towards update

$B_s B_d \Lambda_b$
Lifetimes

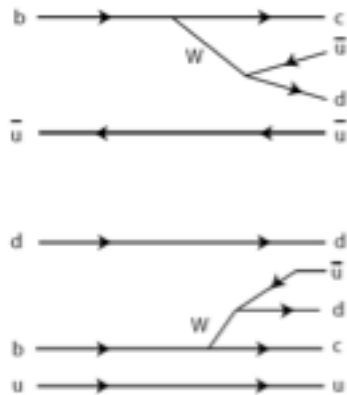
Lifetimes

Spectator model: all B hadrons have the same lifetime

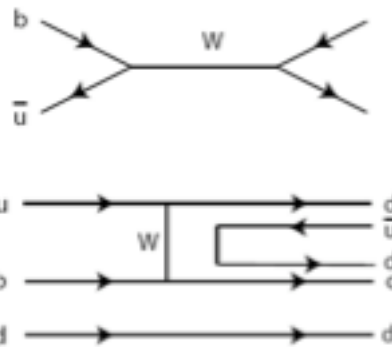
Difference from light quark interactions

In general $\tau(B_u) > \tau(B_d) \sim \tau(B_s) > \tau(\Lambda_b)$

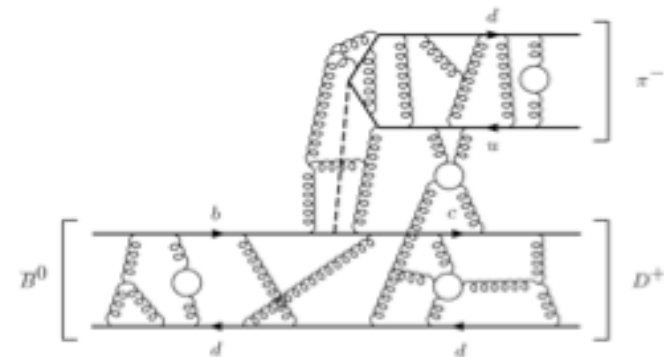
Understand these differences qualitatively



Pauli interference:
prolongs lifetimes
+3% Λ_b , +5% B_u
cf B_d



Weak scattering:
reduces lifetimes
-7% Λ_b , cf. B_d



Lifetimes important for understanding the interactions of quarks inside hadrons. Ratios predicted by HQE

HQE is used to calculate Γ_{12} and semileptonic asymmetry

Recent B_s lifetime results

Theoretical prediction:

$$\tau(B_s) = (1.00 \pm 0.01) \tau(B_d) \text{ (theory)}$$

End of 2006 small experimental tension

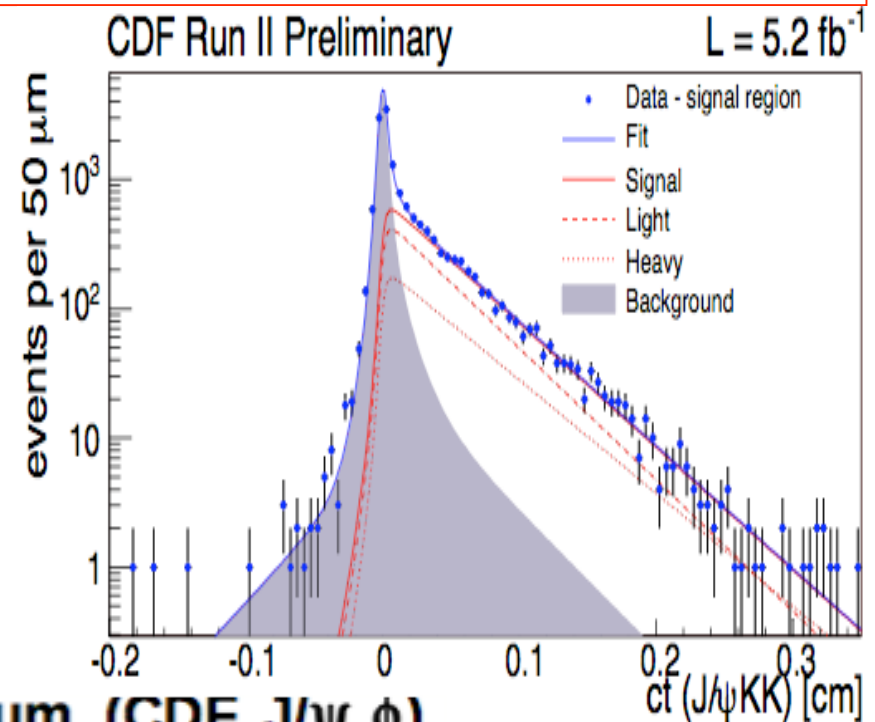
$$\tau(B_s) = (0.950 \pm 0.019) \tau(B_d) \text{ (exp)}$$

Recent $B_s \rightarrow J/\psi \phi$ results give most accurate $\tau(B_s)$

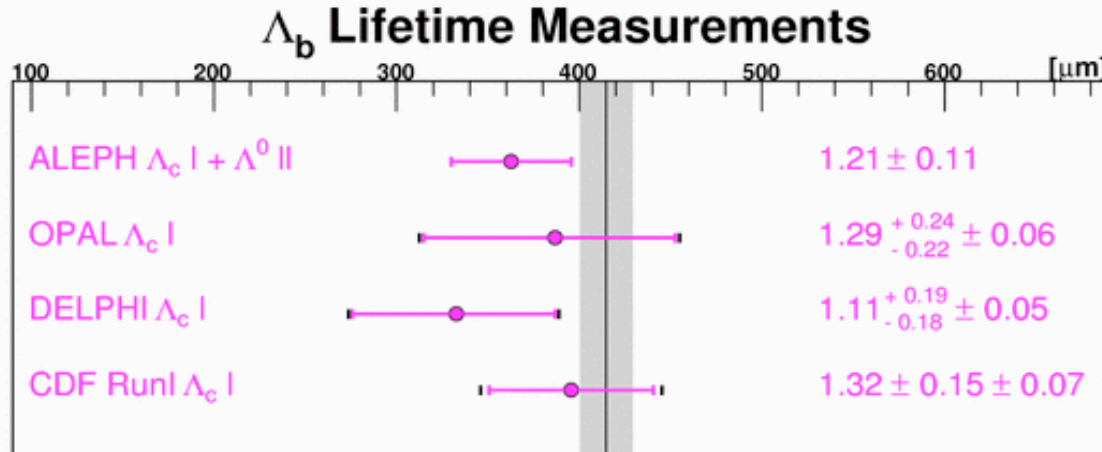
$$c\tau_s = 458.7 \pm 7.5(\text{stat.}) \pm 3.6(\text{syst.}) \mu\text{m} \text{ (CDF, } J/\psi \phi \text{)}$$

$$c\tau_d = 459 \pm 2.7 \mu\text{m} \text{ PDG world average}$$

Similarity of s,d quark, hard to introduce differences



Λ_b “puzzle” - historical overview



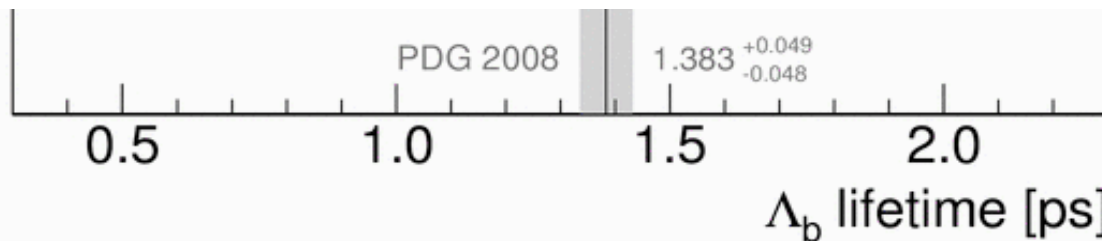
Early measurements were “low” cf to theory predictions

1996:

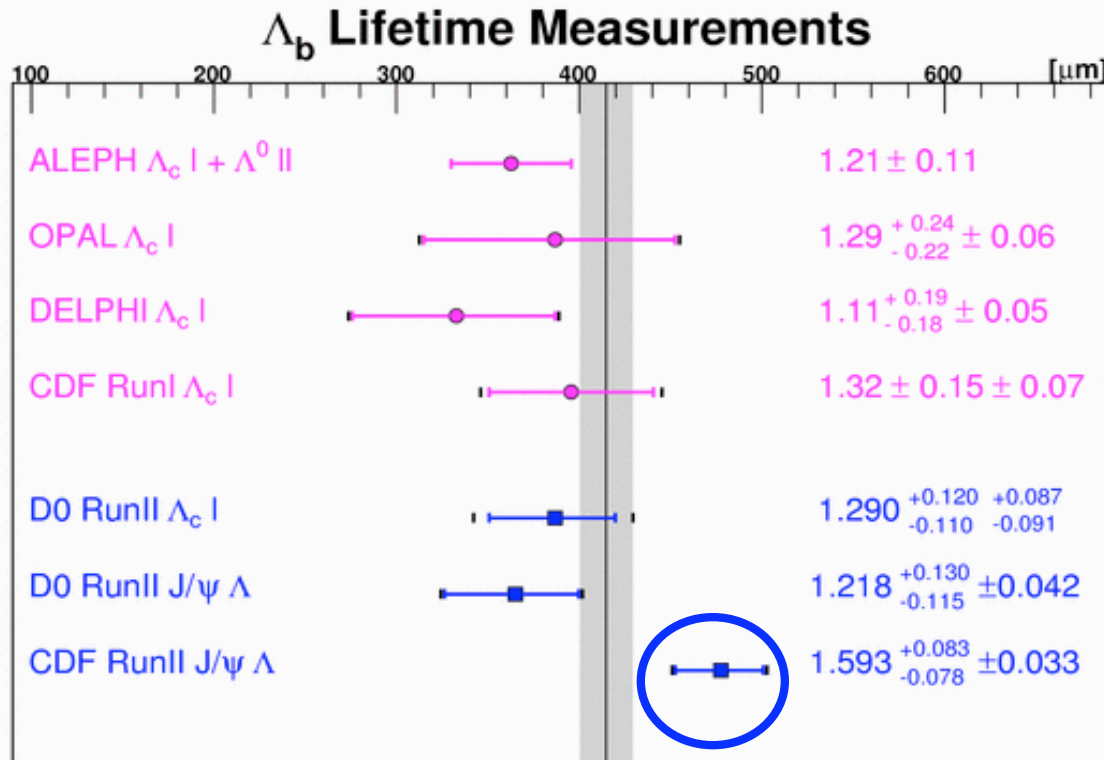
- ➔ World average: 0.78 ± 0.05
- ➔ LO + spect. effect: $0.90-0.95$
(Bigi et al.)

2004:

- ➔ World average: 0.804 ± 0.049
- ➔ NLO+ $O(1/m_b^4)$: 0.86 ± 0.05
Gabbiani et al.,
PRD70 094031

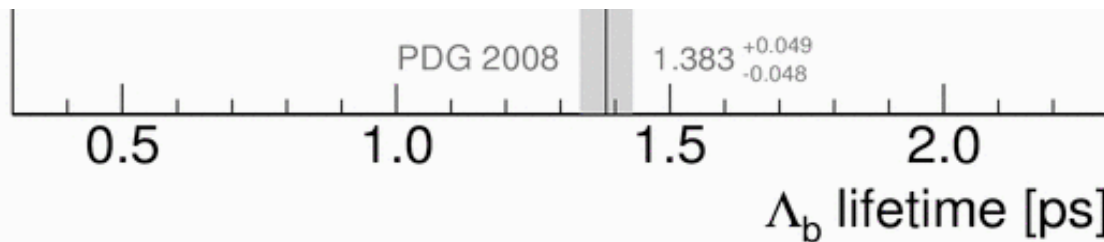


Λ_b “puzzle” - new measurement

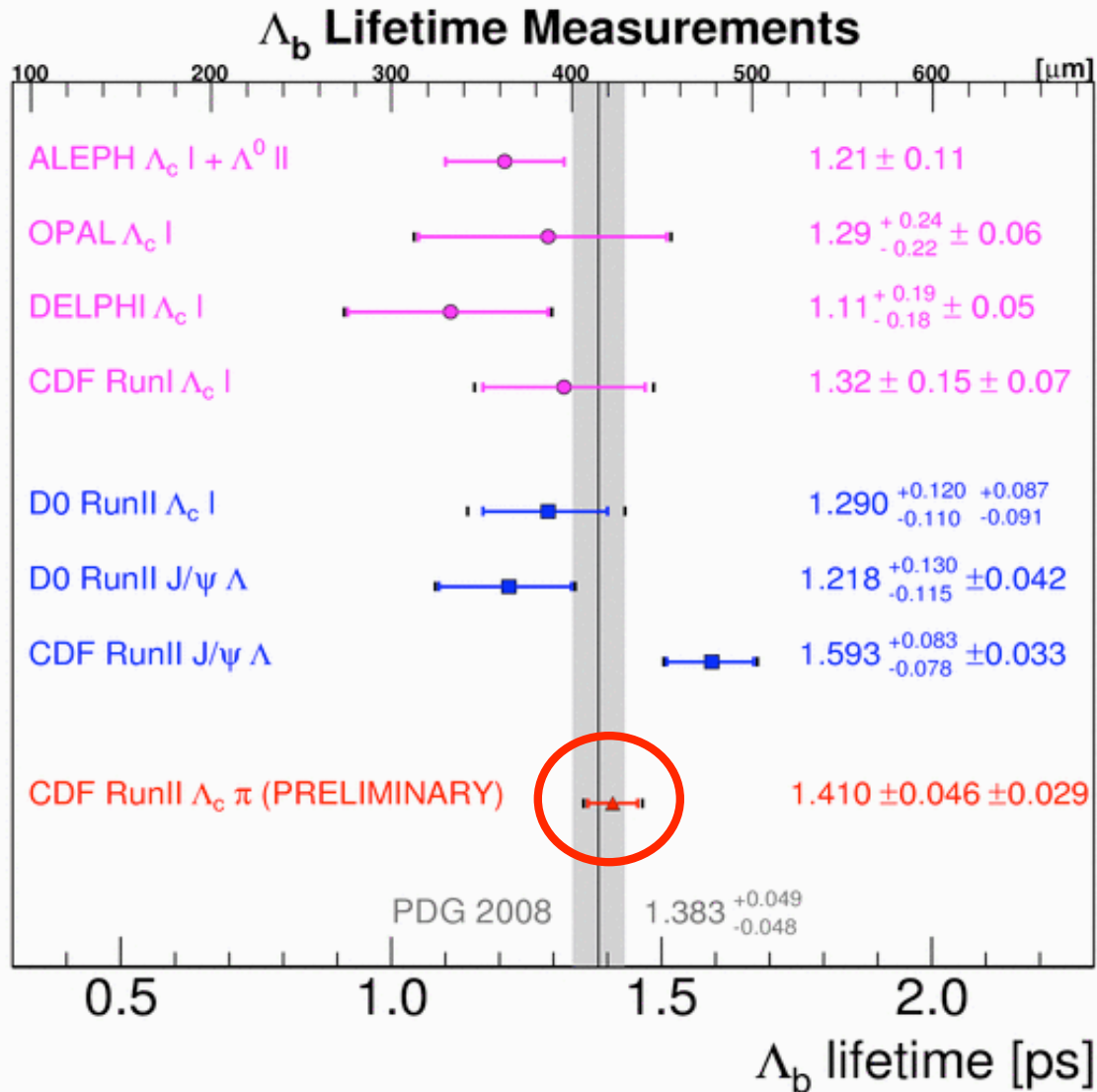


Early measurements were “low” cf to theory predictions

2007 CDF Fully reconstructed measurement considerably higher [$J/\psi \Lambda$]



Λ_b “puzzle” 2008 measurement



Early measurements were “low” cf to theory predictions

2007 Fully reconstructed measurement considerably higher [$J/\psi \Lambda$]

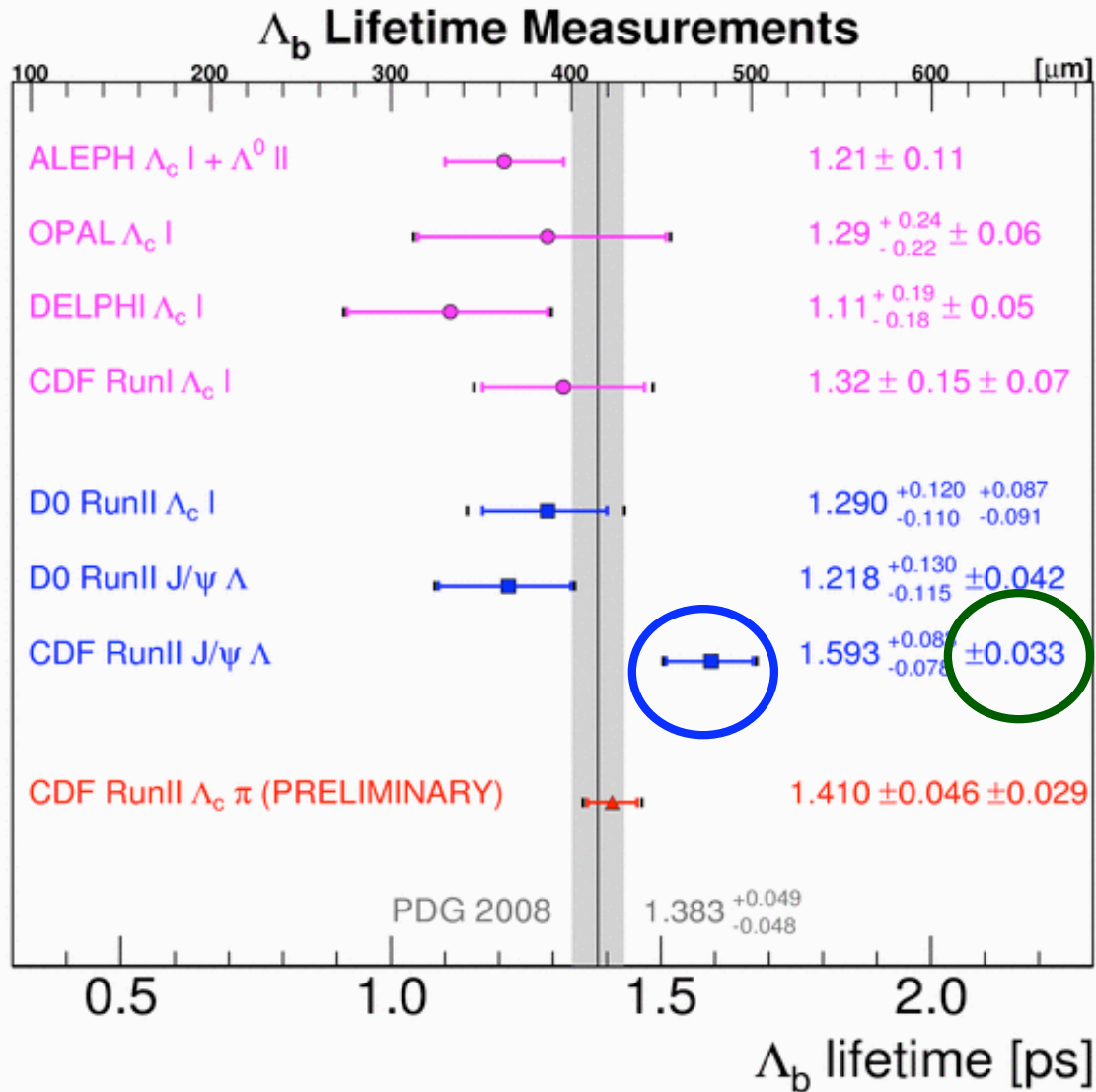
2008 measurement fell in the middle [$\Lambda_c \pi$]

-Different decay channel

-Collected through different trigger

-Systematics between two measurements uncorrelated

Λ_b “puzzle” 2010 update



Early measurements were “low” cf to theory predictions

2007 Fully reconstructed measurement considerably higher [$J/\psi \Lambda$]

2007 measurement updated with $\sim x4$ data

Improved analysis techniques to reduce systematic uncertainties (resolution was leading)

$\Lambda_b \rightarrow J/\psi \Lambda$

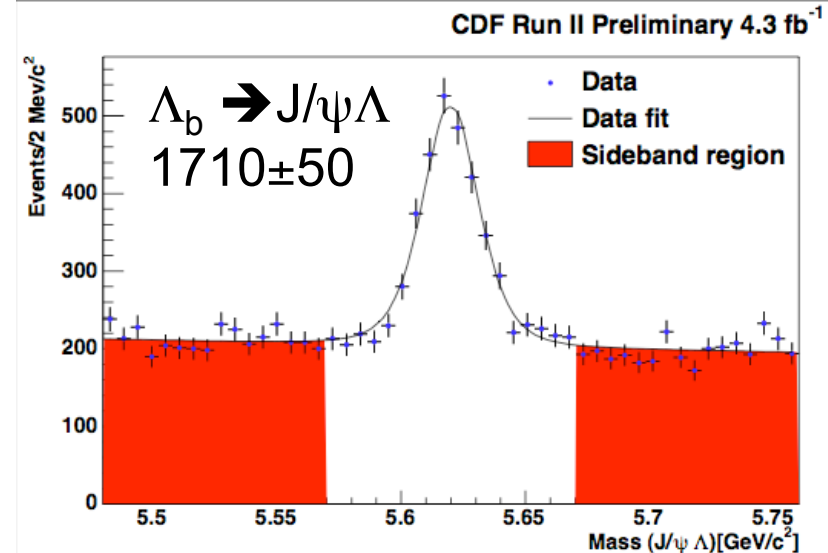
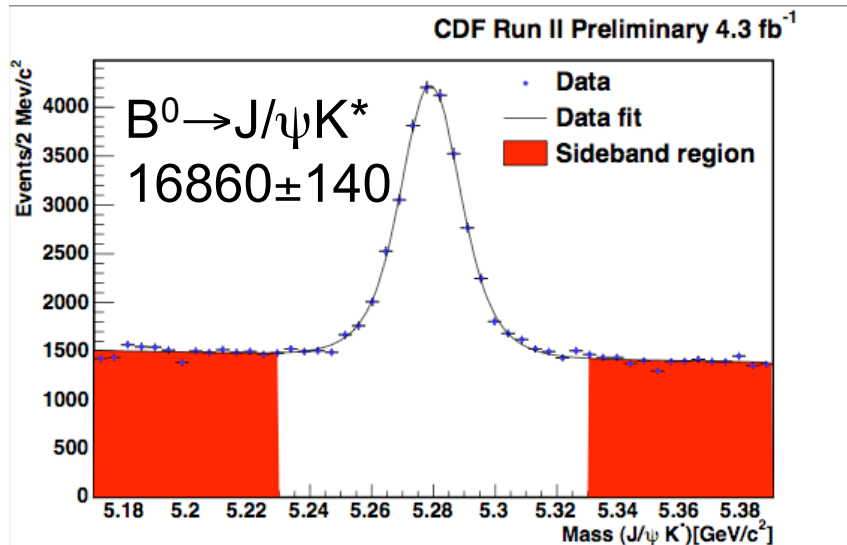
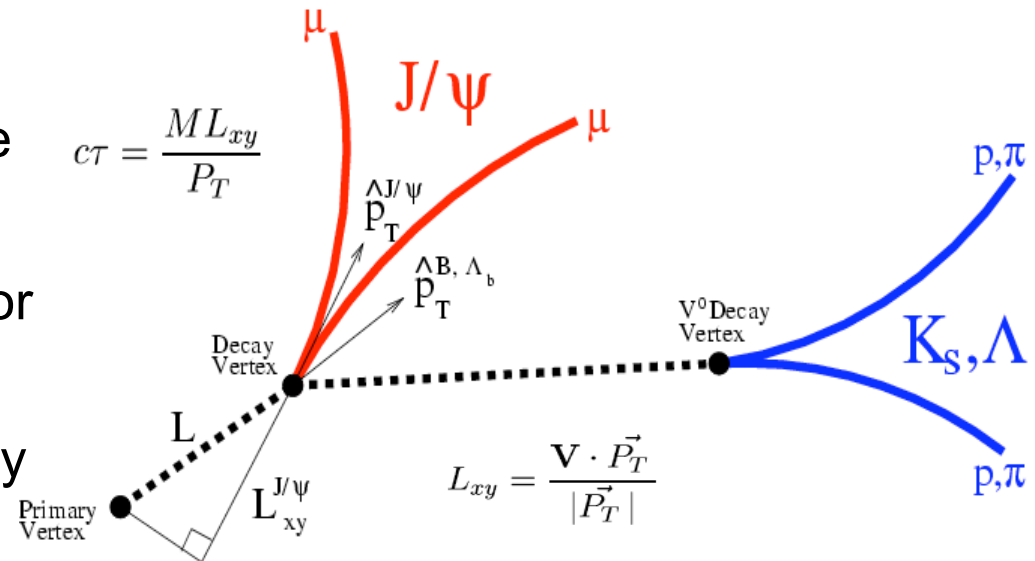


$B^+ \rightarrow J/\psi K^+$ $B^0 \rightarrow J/\psi K^*$, $B^0 \rightarrow J/\psi K_S$
used as control modes.

Use the J/ψ vertex to determine the
Decay Vertex for all modes

Makes detector resolution similar for
all channels

Use the J/ψ sample for further study



Determining the resolution



σ_{ct} measured for each candidate

Detector resolution described
Gaussian with width σ_{ct} x scale
factor

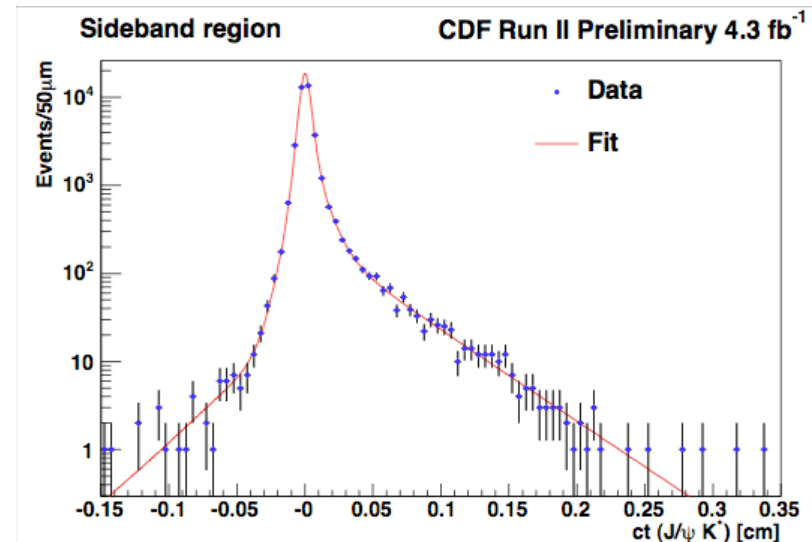
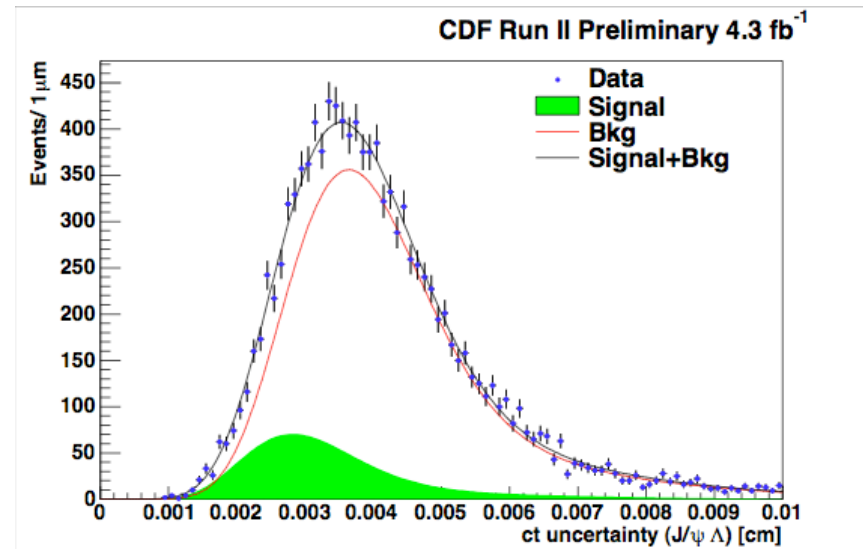
scale factor not reproduced by MC

Background is mainly prompt.
(80-90)%

Carefully model the mass
sideband data → extract the
parameters that determine the
detector resolution.

Overall systematic reduction
for analysis

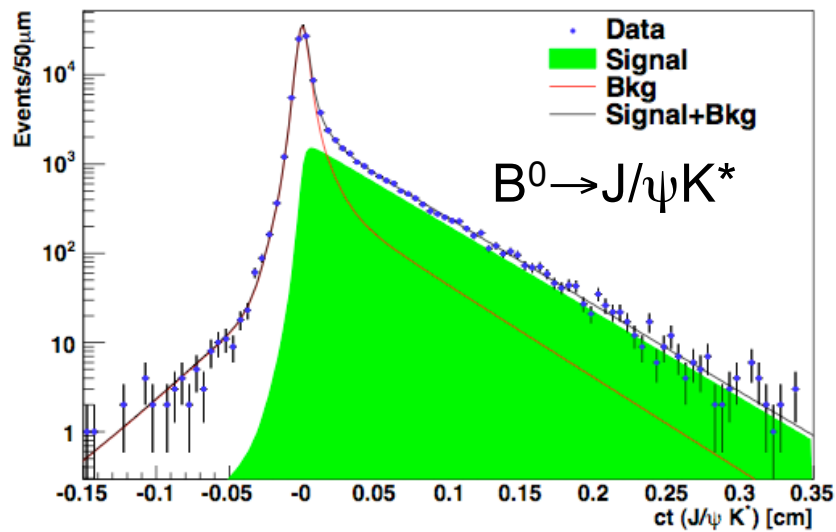
0.016 ps → 0.008 ps (B^0)



B^0 & Λ_b Lifetime fit projection

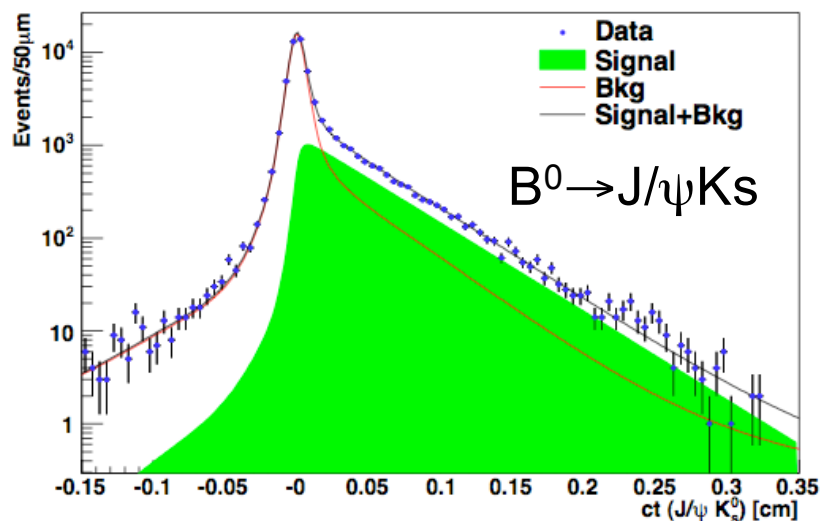


CDF Run II Preliminary 4.3 fb⁻¹

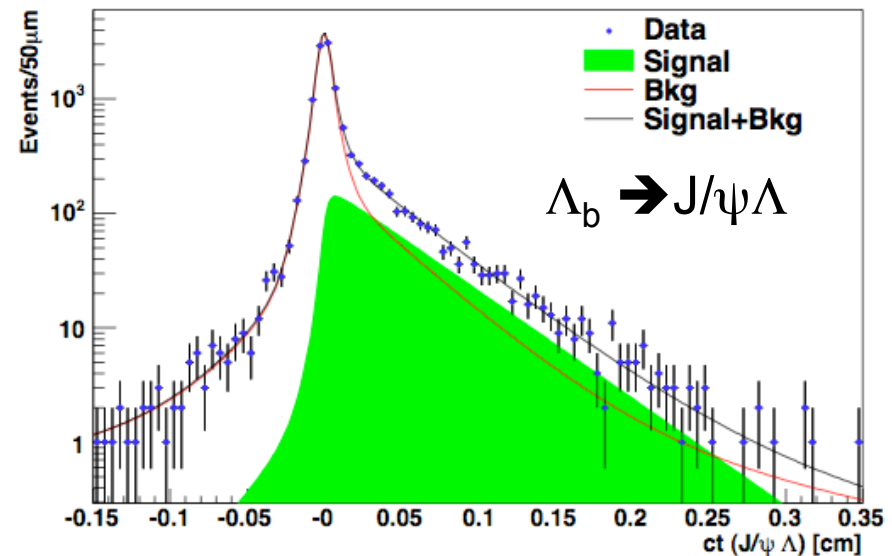


Lifetime extracted from an
un-binned likelihood fit,
simultaneous in
Mass
Decay time
Decay time error

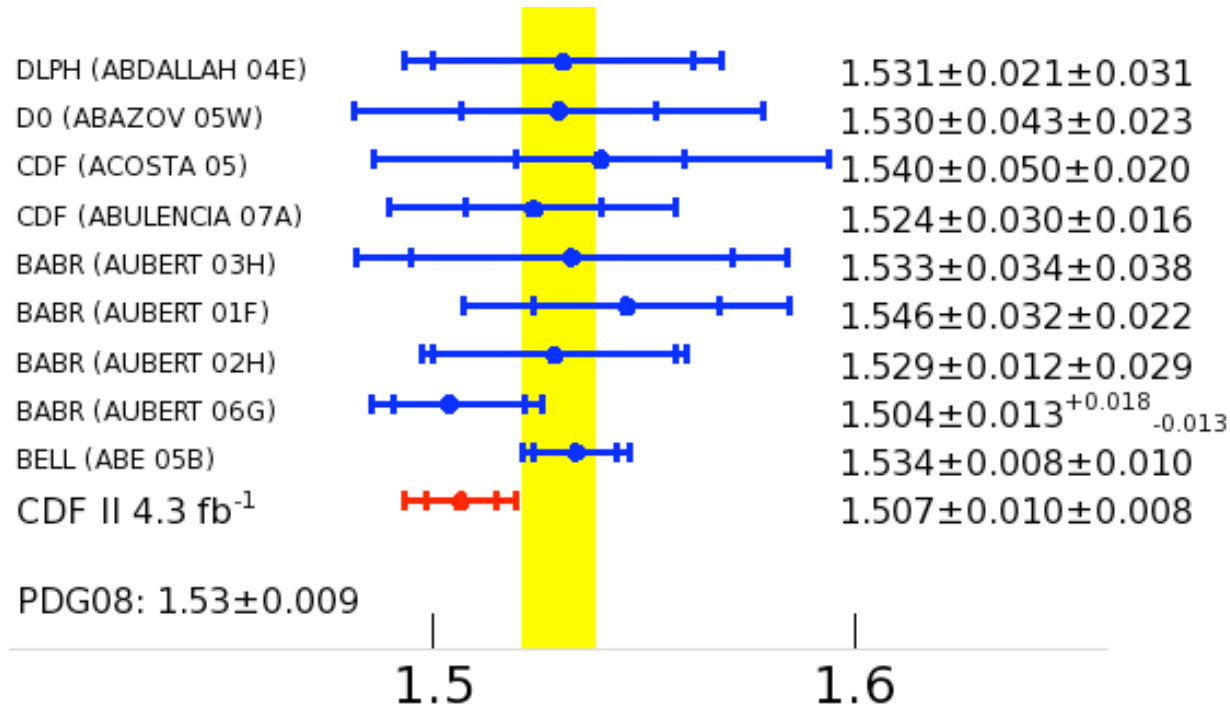
CDF Run II Preliminary 4.3 fb⁻¹



CDF Run II Preliminary 4.3 fb⁻¹



B⁰ Lifetime



Result slightly lower than WA

Competitive with the B factories

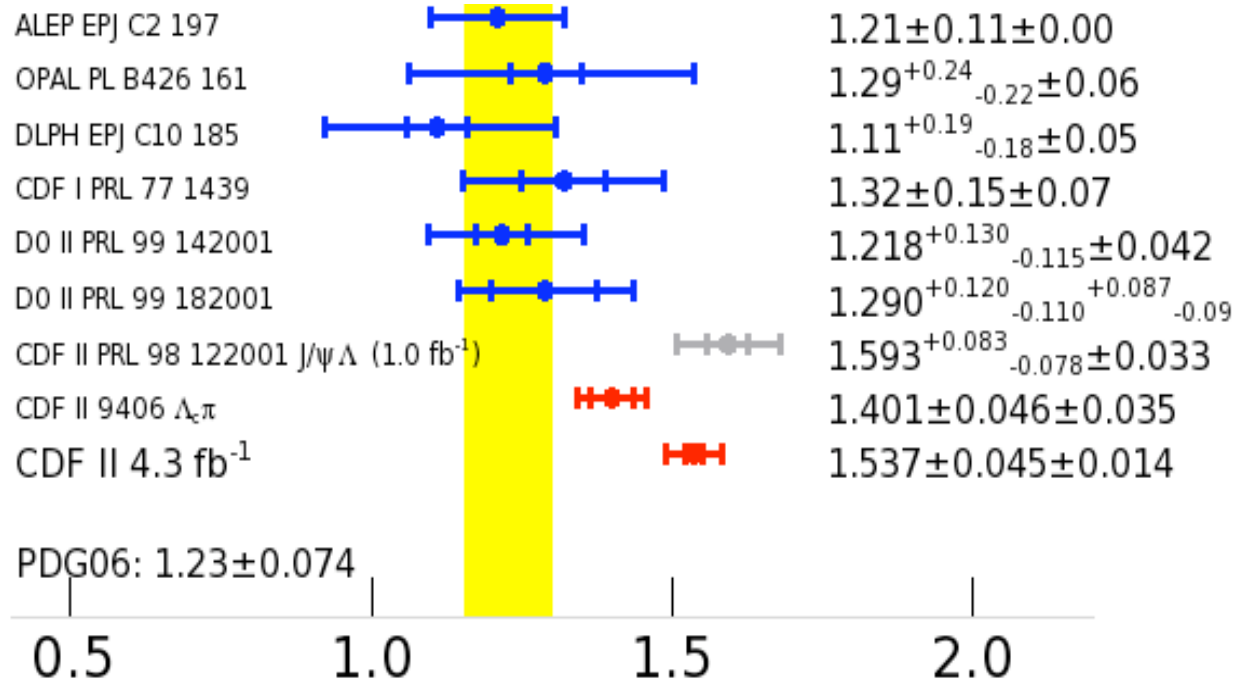
Most precise measurement of the B⁺/B⁰ ratio

In agreement with theoretical prediction:

$$\tau(B^+) = (1.063 \pm 0.027) \tau(B_d) \text{ (theory)}$$

$$\tau(B^+) = (1.088 \pm 0.009 \pm 0.004) \tau(B_d) \text{ (exp)}$$

Λ_b Lifetime



Lifetime remains high
Systematic uncertainties reduced

$$\tau(\Lambda_B)/\tau(B^0) = 1.020 \pm 0.030 \pm 0.008$$

Theoretical predictions 0.83 -0.95

Look forward to further inputs both experimental and theoretical

Summary & Prospects

Lifetimes : v. large samples at LHCb

e.g $B_s \rightarrow D_s \pi$ @ LHCb²⁰¹¹ ~67K

see V. Gligorov WG V

Expect progress on the lifetimes front: B_s Λ_B particularly interesting.
Other B Baryons too.

Mixings and widths:

Results shown today only from past 3-4 years.

B_s oscillation and D^0 mixing established.

Next 3-4 years?

Lifetime difference measurements

Assuming no CPV, mass eigenstates = CP eigenstates

Lifetime ratio can determine y

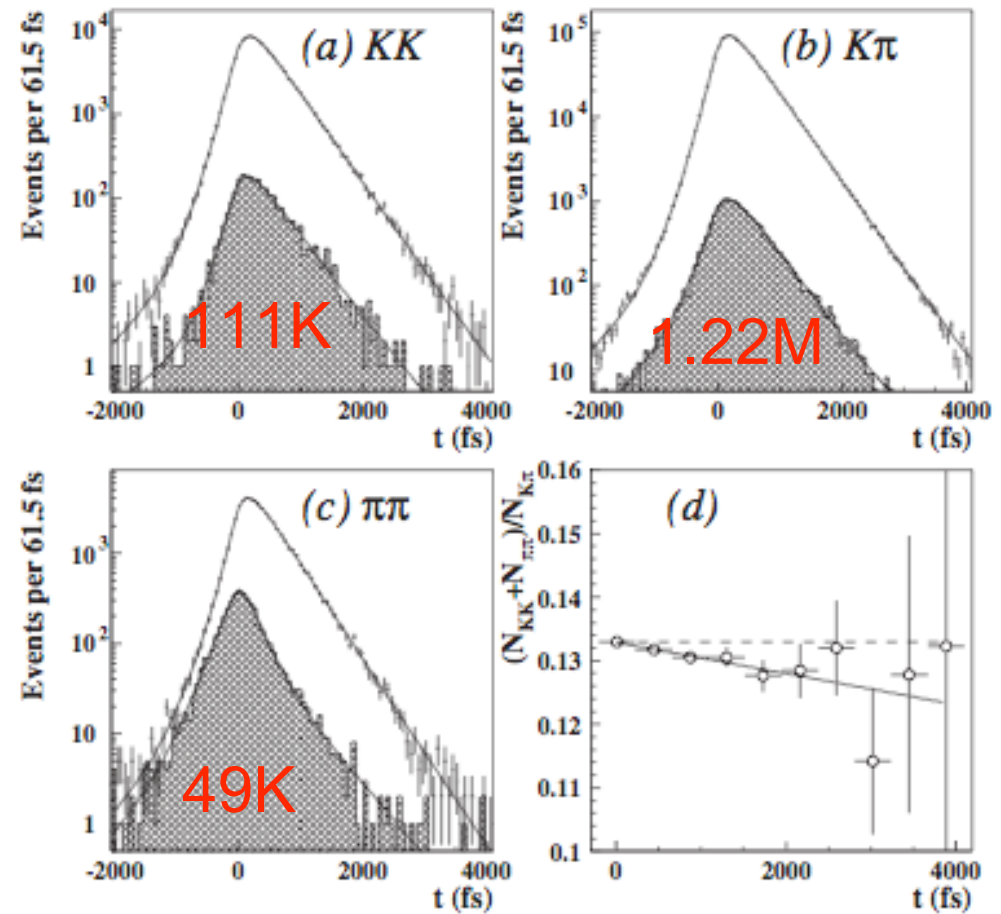
$$y_{cp} \approx y = \frac{\tau(D \rightarrow K\pi)}{\tau(D \rightarrow hh)} - 1$$

$hh = KK, \pi\pi$

CP eigenstate

Not CP eigenstate

540 fb⁻¹ 



Lifetime difference measurements

Assuming no CPV, mass eigenstates = CP eigenstates

Lifetime ratio can determine y

$$y_{cp} \approx y = \frac{\tau(D \rightarrow K\pi)}{\tau(D \rightarrow hh)} - 1$$

$hh = KK, \pi\pi$

Belle result:

$$y_{cp} = (1.31 \pm 0.32 \pm 0.25) \%$$

3.2 σ evidence

Babar:

$$y_{cp} = (1.24 \pm 0.39 \pm 0.13) \%$$

3.0 σ evidence

Further update using untagged see next talk

