

**What can $e^+e^- \rightarrow M_1M_2$ tell us
about power corrections in
 $B \rightarrow M_1M_2$ decays?**

Alex Kagan

University of Cincinnati

-based on work done with Murugesh Duraisamy, arXiv:0812.3162, and to appear

Outline

- Motivation
- Leading power vs. power corrections
- Power corrections in $e^+e^- \rightarrow M_1M_2$ vs. $B \rightarrow M_1M_2$
- PP final states
 - $e^+e^- \rightarrow \pi^+\pi^-, K^+K^-$ at CLEO-c
 - $B \rightarrow K\pi, \pi\pi$ and the $K\pi$ puzzle
- VP final states
 - $e^+e^- \rightarrow VP$ at CLEO-c and at the $\Upsilon(4S)$
 - power corrections in $B \rightarrow K^*\pi$
- VV final states
 - $e^+e^- \rightarrow \rho^+\rho^-$ at the $\Upsilon(4S)$
 - the longitudinal polarizations in penguin dominated $B \rightarrow \phi K^*, \rho K^*$
- Conclusion

Motivation

Many "puzzles" in charmless $B \rightarrow M_1 M_2$ at **leading power** in the $1/m_b$ expansion:

● in $B \rightarrow PP$:

● $\text{Br}(K^0\pi^0), \text{Br}(\pi^0\pi^0)$ **too small**

● $A_{CP}(\pi^+\pi^-)$ too small; $A_{CP}(K^+\pi^-)$ has **wrong sign** and magnitude **too small**

● $A_{CP}(K^+\pi^-) \approx A_{CP}(K^+\pi^0)$ **contrary** to observation

● in $B \rightarrow VP$:

● $B \rightarrow \phi K$ and $B \rightarrow K^*\pi$ rates **too small**

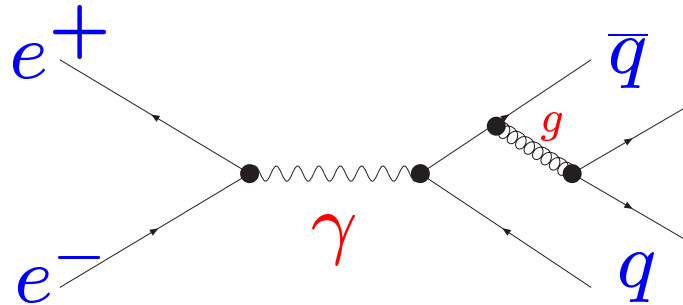
● in $B \rightarrow VV$

● $B \rightarrow \phi K^*, B \rightarrow K^*\rho$ longitudinal polarization fractions (≈ 1) **much larger** than observed ($\approx 50\%$)

Focus on possibility that

- certain power corrections (PC's) in $1/m_b$ are enhanced due to long-distance effects, e.g.,
 - in an outgoing meson, one valence quark is hard, the other soft
 - large "soft-overlap" between the fast and soft valence quarks is required
- can not estimate power correction magnitudes via comparison to leading power!!!
- CLEO-c and the B factories measure $e^+e^- \rightarrow M_1M_2$ cross sections at different \sqrt{s} . They are either PC dominated, or pure PC's in $1/\sqrt{s}$.
 - ideal for isolating PC's and checking for large soft-overlaps
- $\sqrt{s} \sim m_B \Rightarrow$ learn about the importance of soft-overlaps in $B \rightarrow M_1M_2$. Could they be $O(1)$?

Leading power vs. power corrections: $e^+e^- \rightarrow M_1M_2$



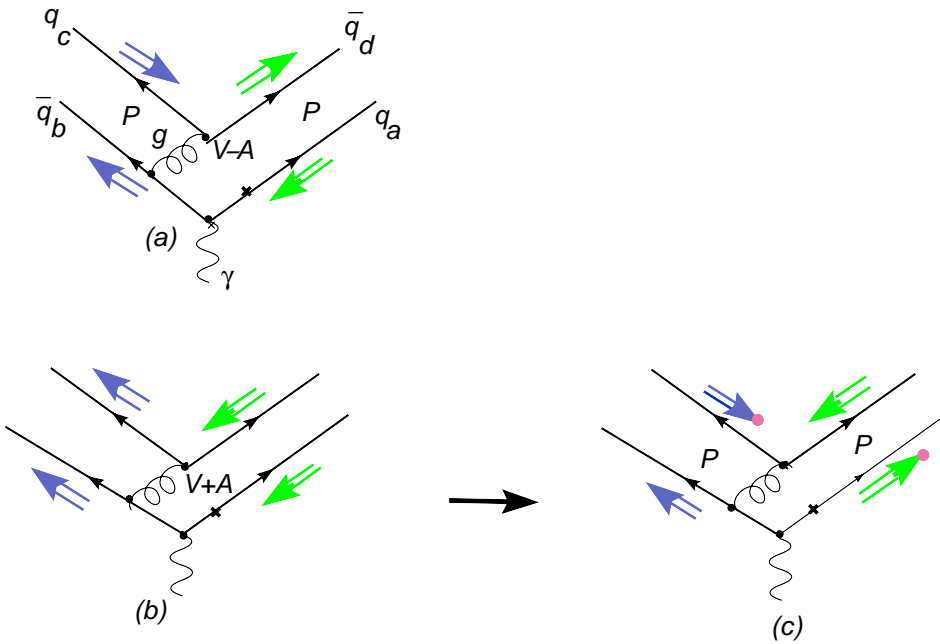
$$\propto \langle M_1 M_2 | \bar{q} \gamma_\mu q | 0 \rangle$$

parametrized in terms of dimensionless timelike form factors

- Each quark helicity flip requires transverse momentum, k_\perp

$\Rightarrow O(\Lambda_{QCD}/\sqrt{s})$ form factor suppression, for meson with energy $\sqrt{s}/2$

● $e^+e^- \rightarrow \pi^+\pi^-, K^+K^-: \langle P_1 P_2 | J_{\text{em}}^\mu | 0 \rangle = F_P(s)(p_1 - p_2)^\mu$



(a) leading power: **no helicity flip**

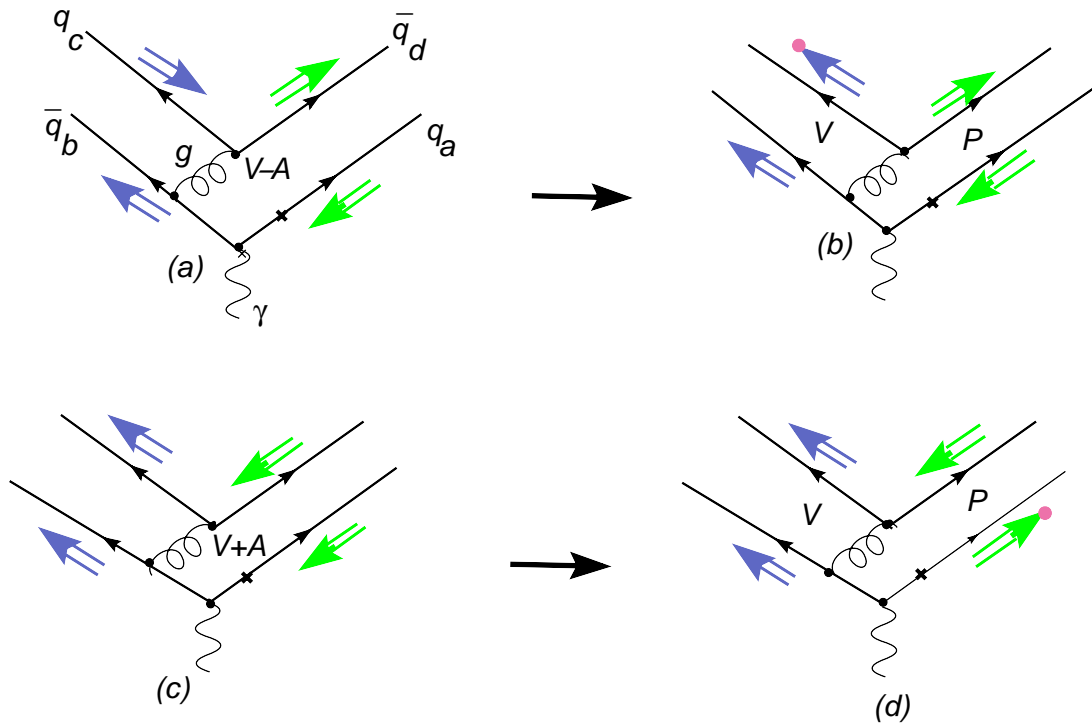
$$F_\pi^{\text{LP}} \propto \frac{1}{s}, \quad \text{calculable in QCD Factorization}$$

(b), (c) power correction: **two helicity flips**

$$\delta F_\pi \propto \frac{1}{s^2}, \quad \text{infrared divergent, not calculable}$$

● $e^+e^- \rightarrow VP: \quad \langle VP|J_{\text{em}}^\mu|0\rangle = \frac{1}{m_P+m_V} 2i V_{VP}(s) \epsilon_{\mu\nu\rho\sigma} \epsilon^\nu p_V^\sigma p_P^\rho$

Parity + angular momentum conservation \Rightarrow V is transverse



always need one helicity flip $\Rightarrow V_{VP}$ is a pure power correction

$$V_{VP} \propto \frac{1}{s^2}, \text{ infrared divergent, not calculable}$$

● $e^+e^- \rightarrow V_1V_2$:

Three form factors: for LL , TL , and TT polarizations

$T \equiv$ transverse, $L \equiv$ longitudinal

$$\langle V_1V_2 | J_{em}^\mu | 0 \rangle = \left[\frac{m_{V_1}(\epsilon_1^* \cdot p_2)}{2E^2} \right] \left[\frac{m_{V_2}(\epsilon_2^* \cdot p_1)}{2E^2} \right] (p_1 - p_2)^\mu V_{LL}(s) + \left(\epsilon_{1\perp}^{*\mu} \left[\frac{m_{V_2}(\epsilon_2^* \cdot p_1)}{2E^2} \right] - \epsilon_{2\perp}^{*\mu} \left[\frac{m_{V_1}(\epsilon_1^* \cdot p_2)}{2E^2} \right] \right) V_{LT}(s) + (\epsilon_{1\perp}^* \cdot \epsilon_{2\perp}^*) (p_1 - p_2)^\mu V_{TT}(s)$$

● LL: no helicity flips \Rightarrow leading power, $V_{LL}^{LP} \propto 1/s$

two helicity flips \Rightarrow power correction, $\delta V_{LL} \propto 1/s^2$

● LT: one helicity flip \Rightarrow pure power correction, $V_{LT} \propto 1/s$

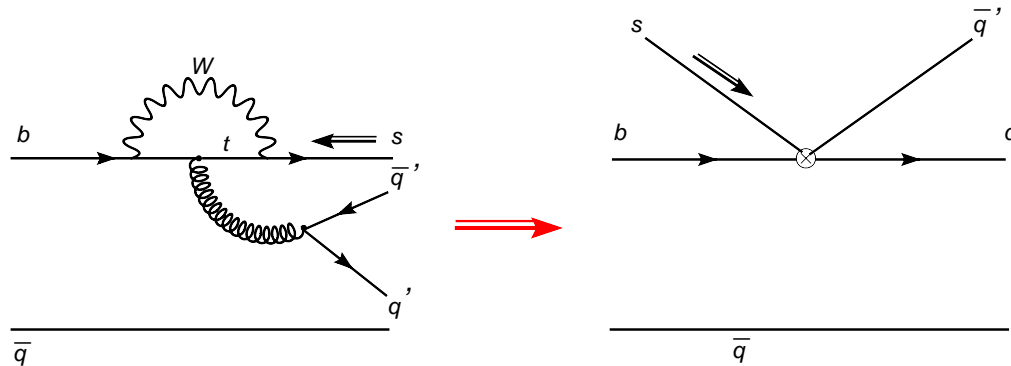
● TT: two helicity flips \Rightarrow pure power correction, $O(\Lambda_{QCD}^2/s)$ suppression

The power corrections are infrared divergent, not calculable

Leading power vs. power corrections: $B \rightarrow M_1 M_2$

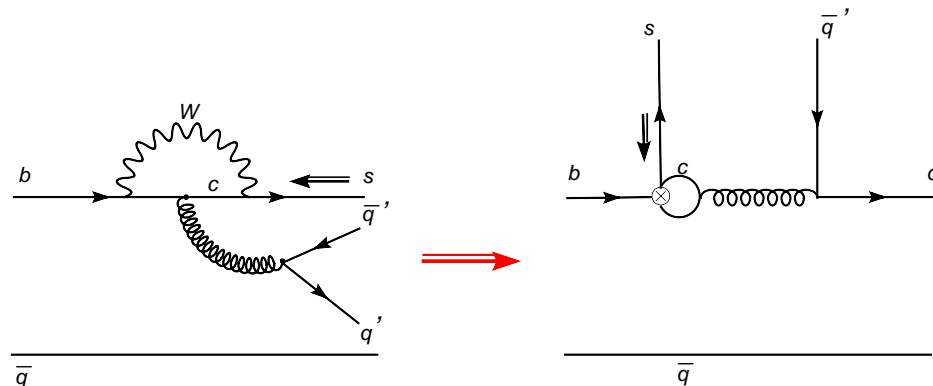
QCD penguin amplitude (P) at leading power:

- leading order in α_s (naive factorization), e.g.,



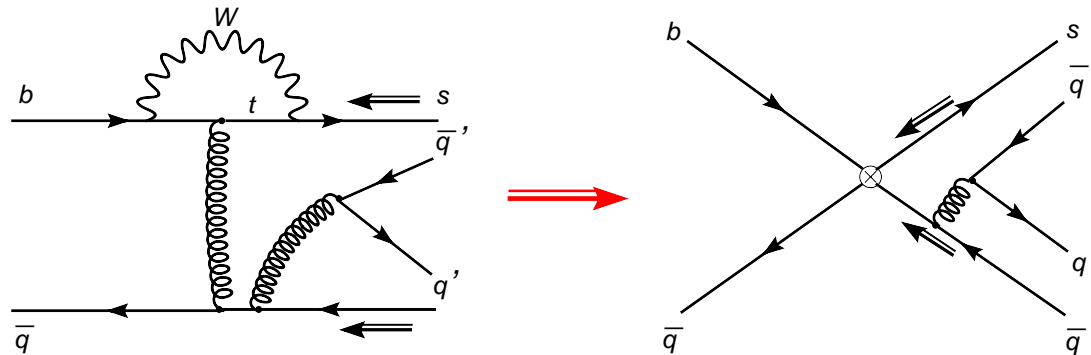
$$\begin{aligned} \mathcal{A} &\propto \langle M_2 | \bar{s} \gamma^\mu (1 \mp \gamma_5) q' | 0 \rangle \langle M_1 | \bar{q}' \gamma_\mu (1 - \gamma_5) b | \bar{B} \rangle \\ &\propto \text{decay constant} \times \text{form factor, scales like } m_B^{1/2} \end{aligned}$$

- leading power but higher order in α_s , e.g., **charm loops**:



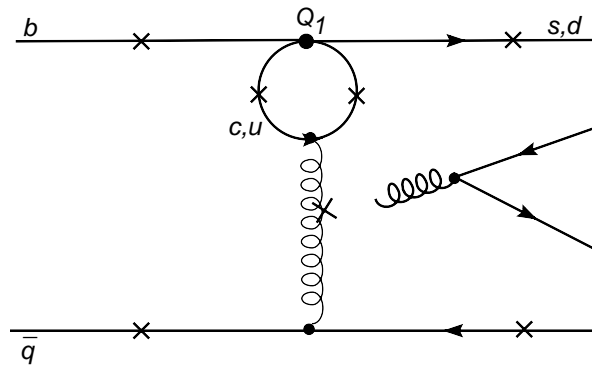
QCD penguin power corrections

- “Weak annihilation”, e.g., (perturbative limit)



- annihilation topology $\Rightarrow 1/m_b$ suppression ($\mathcal{A} \propto f_{M_1} f_{M_2} f_B$)
- quark helicity flip in PP , VP , or VV final states $\Rightarrow 1/m_b$ suppression

- Charm loop power corrections, e.g., (perturbative limit)



- charm loop PC's cancel weak annihilation (and hard spectator) leading $\log \mu_b$ renormalization scale dependence

Power correction amplitudes

- At subleading powers in $1/m_b$:

short / long distance factorization breaks down

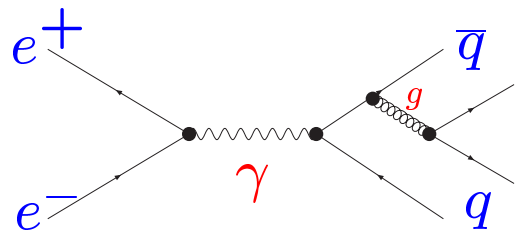
⇒ amplitudes could be soft dominated
- Signaled by infrared log divergences in the convolution integrals

⇒ mesons produced in asymmetric configurations, e.g.,

fast valence antiquark, soft valence quark
- the light mesons would be produced via soft-overlaps, necessarily non-perturbative ⇒ large strong phases are possible

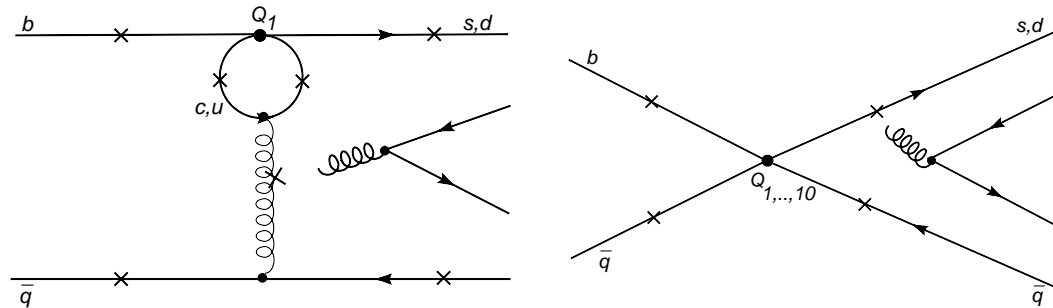
Power corrections in $e^+e^- \rightarrow M_1 M_2$ vs. QCD penguins

Compare timelike form factor PC's



$$F_{M_1 M_2} \propto \langle M_1 M_2 | \bar{q} \gamma_\mu q | 0 \rangle$$

to penguin PC's, e.g.,



in both cases

1

- have hard outgoing quark and antiquark, $E \sim \sqrt{s}/2$ or $m_B/2$
- each hadronizes with soft quark or antiquark, i.e., both light mesons produced in asymmetric configurations via soft overlaps
- PC's for C (color suppressed amplitude): only one light meson produced via soft-overlap

Analysis Procedure

- Perturbative calculations of PC's on the light-cone contain infrared log-divergent terms

$$\sim \alpha_s(\mu_h) \left(\frac{1}{\sqrt{s}} \right)^n \left(\log \frac{\sqrt{s} \text{ or } m_B}{\Lambda} \right)^m,$$

$\Lambda \sim \Lambda_{QCD}$ represents a physical IR cutoff

- Separate PC's into "perturbative" parts, and "non-perturbative" parts, e.g., for the pion form factor

$$\delta F_\pi = \delta F_\pi^{\text{pert.}} + \delta F_\pi^{\text{non-pert.}}$$

- **perturbative parts** correspond to $\Lambda \gtrsim \sqrt{1} \text{ GeV}$, $1 \text{ GeV} \lesssim \mu_h \lesssim \sqrt{s} \text{ or } m_B$

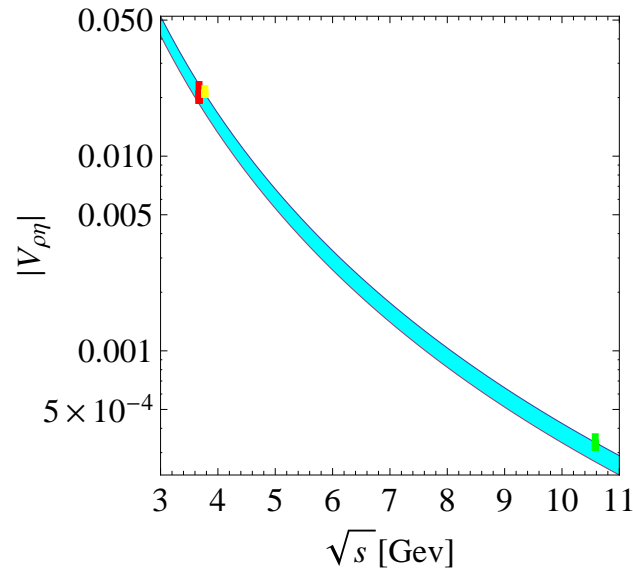
- comparison with $e^+e^- \rightarrow M_1 M_2$ data yields **non-perturbative** parts, e.g., $\delta F_\pi^{\text{non-pert.}} / \delta F_\pi^{\text{pert.}}$

- Assume B decay "puzzles" due to PC's. Fit **non-perturbative** PC's to data.

- Compare ratios of non-perturbative to perturbative PC's in $e^+e^- \rightarrow M_1 M_2$ and $B \rightarrow M_1 M_2$.

Two ways to test power counting rules

- check \sqrt{s} dependence of $e^+e^- \rightarrow M_1 M_2$ form factors, e.g.,
 $V_{\rho\eta} \propto 1/s^2$ (CLEO-c, BELLE):



- compare power corrections in $e^+e^- \rightarrow PP$ ($\delta F_\pi, \delta F_K$) and in the QCD penguin amplitudes ($\delta P_{\pi\pi}, \delta P_{K\pi}$), and similarly for VP and VV final states
 - The “perturbative parts” of the power corrections are consistent with power counting rules \Rightarrow ratios of non-perturbative to perturbative parts of PC’s with similar kinematics should be consistent (order of magnitude), e.g.,

$$\delta F_\pi^{\text{non-pert.}} / \delta F_\pi^{\text{pert.}} \sim \delta P_{\pi\pi}^{\text{non-pert.}} / \delta P_{\pi\pi}^{\text{pert.}}$$

and similarly for VP, VV final states

CLEO-c continuum $e^+e^- \rightarrow \pi^+\pi^-, K^+K^-$ at $\sqrt{s} = 3.67$ GeV

- CLEO-c measures $\langle P^+P^- | J_{\text{em}}^\mu | 0 \rangle = F_P(s) (p^+ - p^-)^\mu$

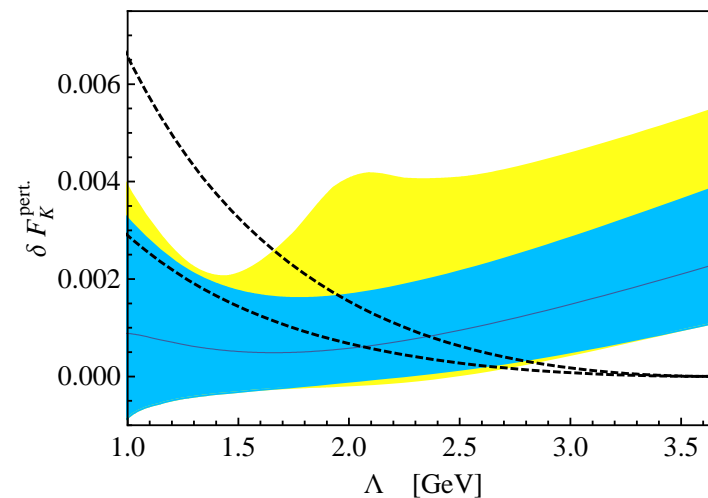
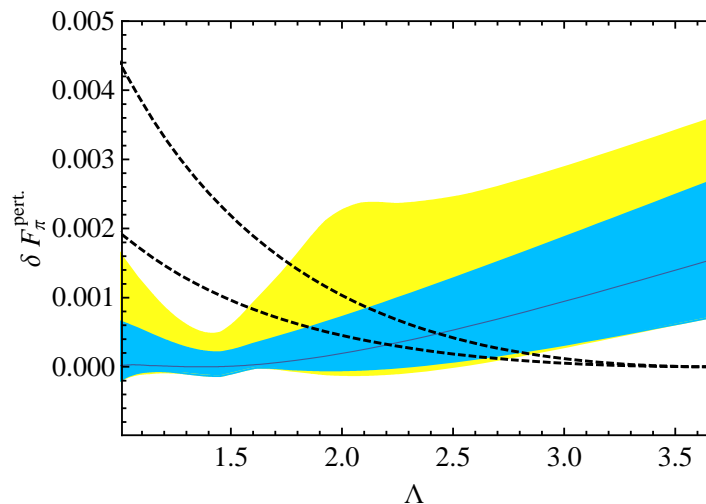
$$|F_\pi| = 0.075 \pm 0.009, \quad |F_K| = 0.063 \pm 0.004$$

- calculable leading power contributions,

$$F_\pi^{\text{LP}} = -0.01_{-0.004}^{+0.002}, \quad F_K^{\text{LP}} = -0.014_{-0.006}^{+0.002}$$

$\Rightarrow F_\pi, F_K$ dominated by PC's entering at $O(1/s)$!

- perturbative PC's. blue bands: variation of inputs ($\mu_h = \Lambda$); yellow bands: add variation of μ_h ; dashed lines: asymptotic light-cone distribution amplitudes



- CLEO-c data implies

$$\frac{\delta F_{\pi}^{\text{non-pert.}}}{\delta F_{\pi}^{\text{pert.}}} = O(10), \quad \frac{\delta F_K^{\text{non-pert.}}}{\delta F_K^{\text{pert.}}} = O(10)$$

⇒ very large soft-overlaps !

- similar soft enhancement would account for $F_{\pi}(m_{J/\Psi}) \approx 0.10$, obtained from J/Ψ decays

- Leading power form factors obey canonical $SU(3)_F$ flavor symmetry breaking

$$(F_{\pi}/F_K)_{\text{LP}} \approx f_{\pi}^2/f_K^2 = 0.67$$

- $|F_{\pi}/F_K|_{\text{exp.}} = 1.20 \pm 0.17 \Rightarrow$ PC's satisfy $|\delta F_{\pi}/\delta F_K| > 1$

- apparently, soft-overlap larger for pions than kaons
- source for large $SU(3)_F$ breaking

$B \rightarrow K\pi, \pi\pi$ power correction fit procedure

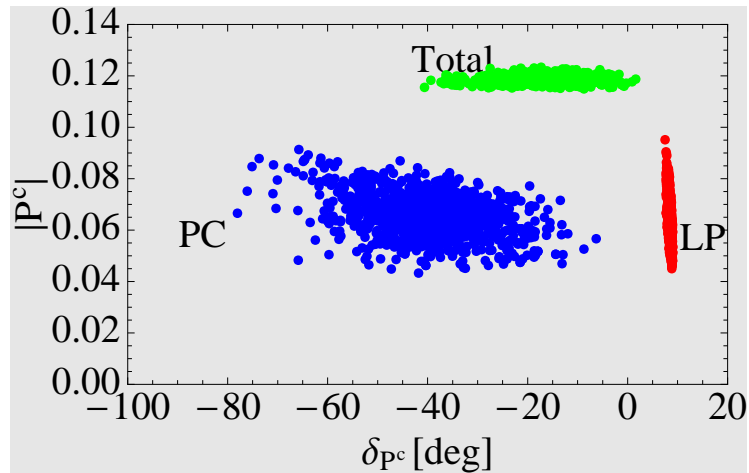
scan procedure:

- vary input parameters uniformly within errors, ($\gamma \in [50^\circ, 80^\circ], \dots$)
- require all Br's, direct CP asymmetries $A_{K^+\pi^-}, A_{K^0\pi^+}, A_{K^+\pi^0}, A_{\pi^+\pi^-}$, time-dep. CP asymmetry $S_{\pi^+\pi^-}$ lie within 1σ errors
- obtain predictions for $C_{K_S\pi^0} = -A_{K_S\pi^0}, S_{K_S\pi^0}$
- Goodness of $B \rightarrow K\pi$ fit:
 $\chi_{\min}^2/d.o.f. \approx 3.5/2$ or only $\approx 1.4\sigma$ from Standard Model
- but are the power correction magnitudes in the fit natural?

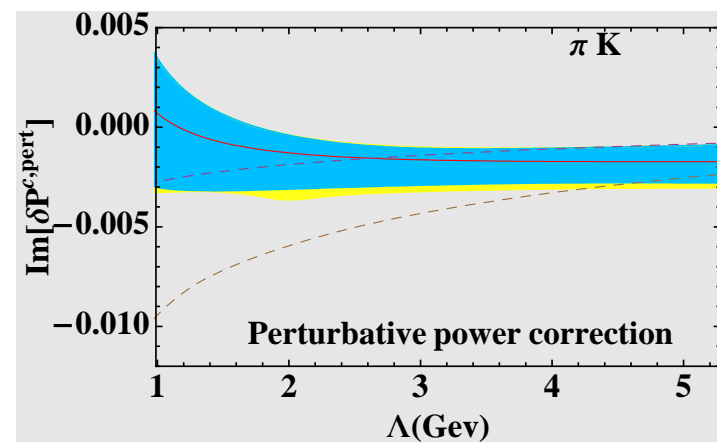
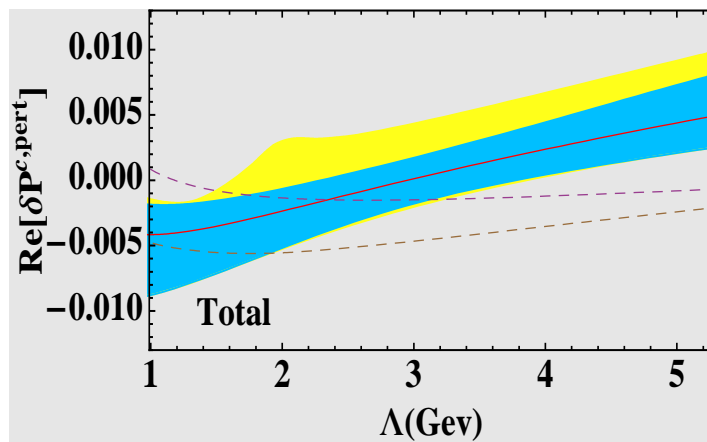
$B \rightarrow K\pi, \pi\pi$ penguin power corrections

$K\pi$ scatter plot for $|\delta P^c|$ vs. δ_{P^c} (strong phase relative to naive factorization):

$A_{CP}(K^+\pi^-)$ favors $\delta P^c \approx P_{LP}^c$ with significant strong phase



Compare to $\delta P^{c, \text{pert.}}$ for $K\pi$

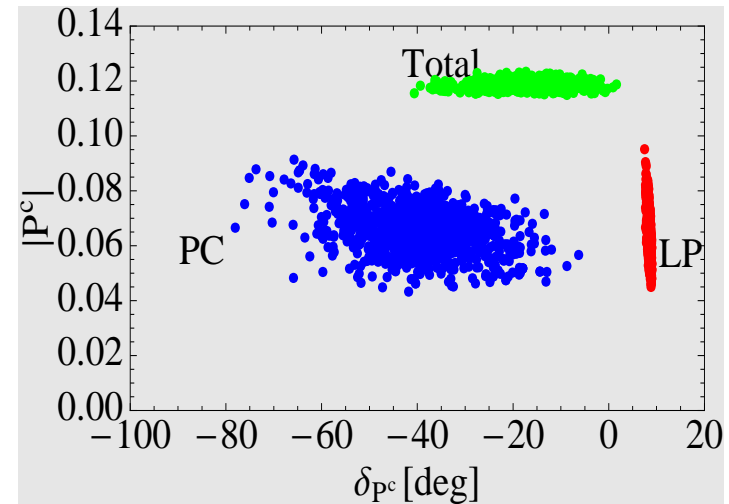
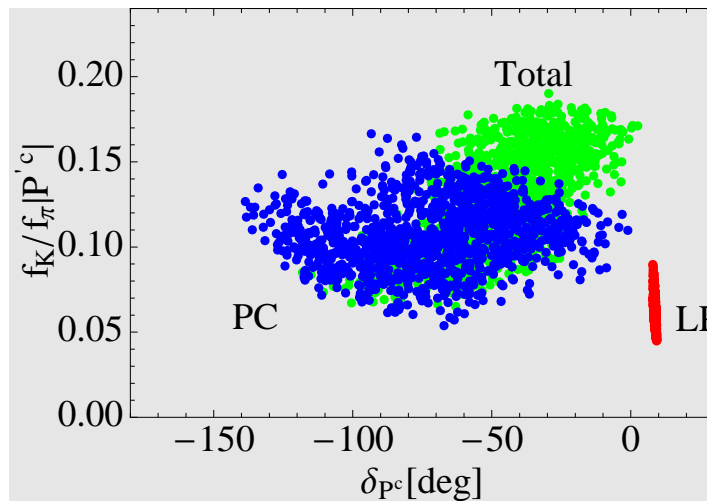


● Fits give:

$$K\pi : \left| \frac{\delta P^{c, \text{non-pert.}}}{\delta P^{c, \text{pert.}}} \right| = O(10), \quad \pi\pi : \left| \frac{\delta P'^{c, \text{non-pert.}}}{\delta P'^{c, \text{pert.}}} \right| = O(10)$$

similar to continuum $\delta F_{\pi, K} \Rightarrow$ gives us confidence the fit is natural

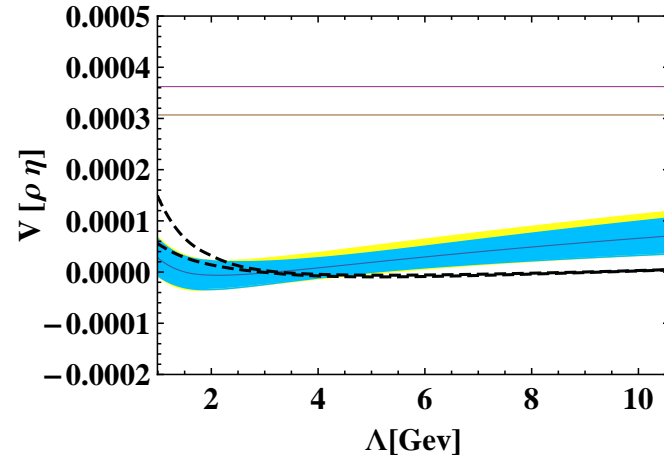
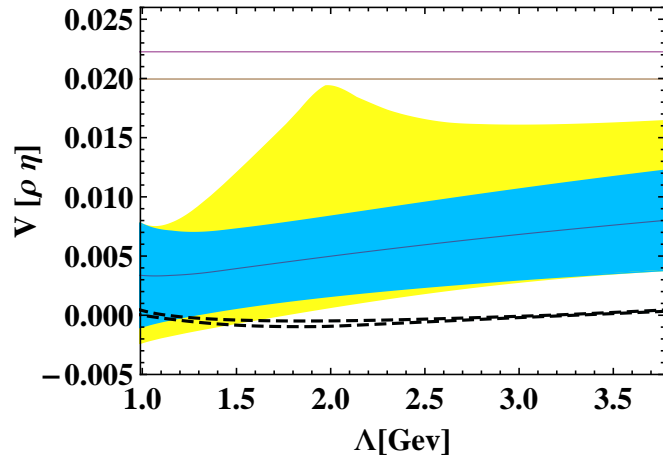
● LP penguins obey canonical $SU(3)_F$ breaking: $(f_K/f_\pi)P'_{LP}{}^c(\pi\pi) \approx P_{LP}^c(K\pi)$.
Compare



● appears $\delta P'^{c, \text{non-pert.}}(\pi\pi) > \delta P^{c, \text{non-pert.}}(K\pi)$, as in continuum $\delta F_\pi > \delta F_K$, i.e., again appears larger soft-overlap larger for pions than kaons!

$e^+e^- \rightarrow VP$ at $\sqrt{s} \approx 3.7$ GeV, 10.58 GeV

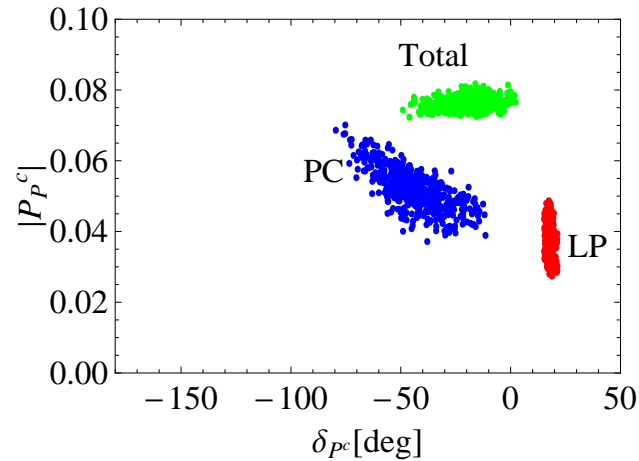
$V_{\rho\eta}$ at $\sqrt{s} = 3.77$ GeV (CLEO-c), and at the $\Upsilon(4S)$ (BELLE)



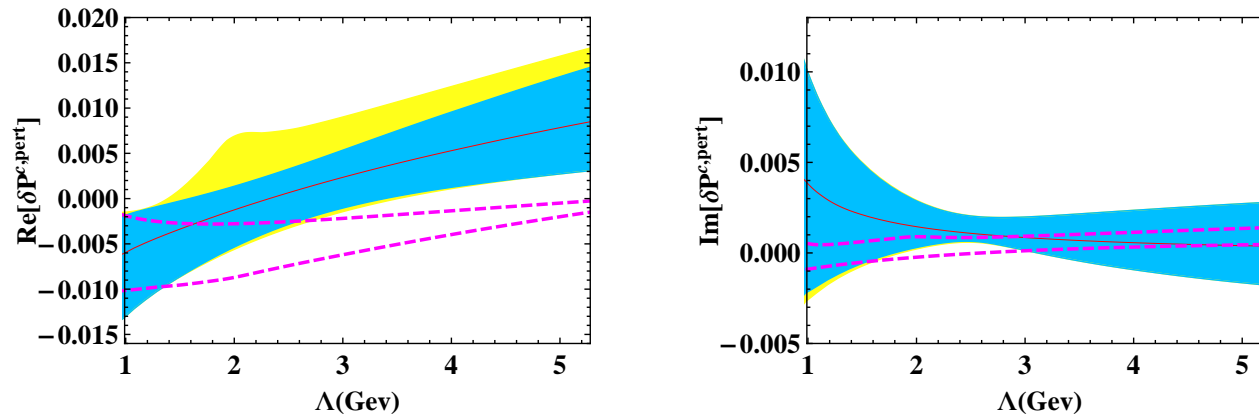
$$\frac{V_{VP}^{\text{non-pert.}}}{V_{VP}^{\text{pert.}}} \geq O(\text{few}), \text{ and appears } \frac{V_{VP}^{\text{non-pert.}}}{V_{VP}^{\text{pert.}}} < \frac{F_{\pi}^{\text{non-pert.}}}{F_{\pi}^{\text{pert.}}}$$

$B \rightarrow VP$ penguin power corrections

$B \rightarrow K^* \pi$ PC fits: varied four Br's, four A_{CP} 's within 1σ errors



$B \rightarrow K^* \pi$ “perturbative” QCD penguin PC’s:



For $B \rightarrow VP$, find $|\delta P_P^{c,\text{non-pert.}} / \delta P_P^{c,\text{pert.}}| \geq O(\text{few})$, consistent with $e^+e^- \rightarrow VP$

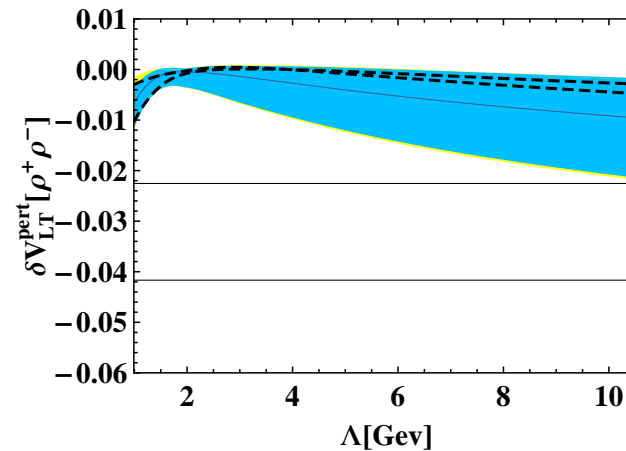
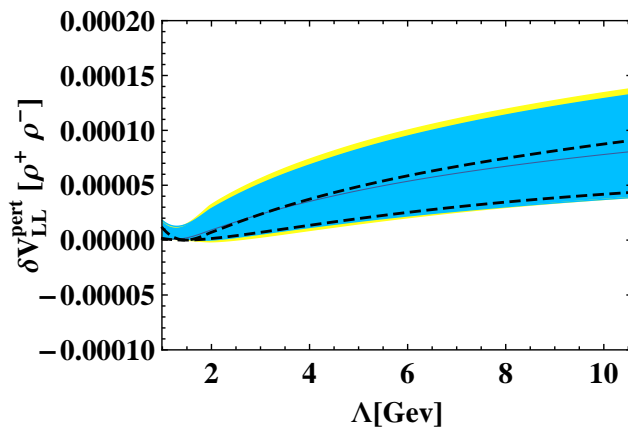
$e^+e^- \rightarrow \rho^+\rho^-$ at the $\Upsilon(4S)$ (BABAR)

$$\sigma(e^+e^- \rightarrow \rho^+\rho^-) = 19.6 \pm 1.6 \pm 3.2 \text{ fb} + \text{angular analysis}$$

$$\Rightarrow |V_{LL}| = 0.0069 \pm 0.0017, \quad |V_{LT}| = 0.032 \pm 0.01$$

Angular analysis has large uncertainties, but contains useful information:

- V_{LL} has LP and PC contributions, V_{LT} is a pure PC
- Leading power contribution to V_{LL} is calculable in QCDF $\Rightarrow V_{LL}^{LP} = -0.002 \pm 0.0005$
- perturbative power corrections

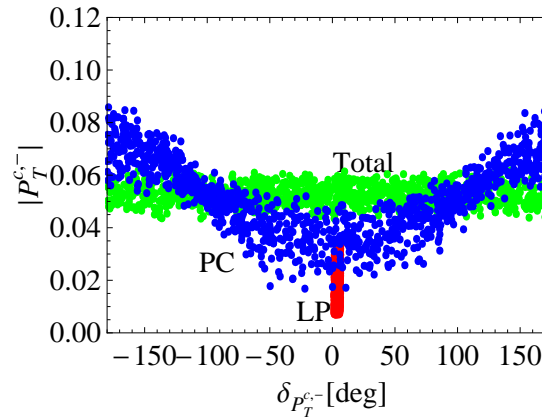
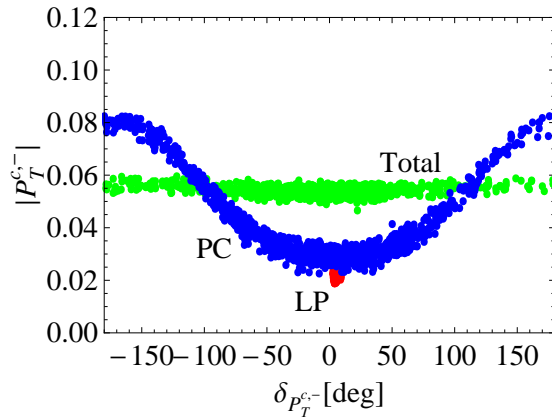


- V_{LL} should be dominated by the LP contribution
- $|\delta V_{LT}^{\text{non-pert.}} / \delta V_{LT}^{\text{pert.}}| = O(1 - \text{few})$, within large errors

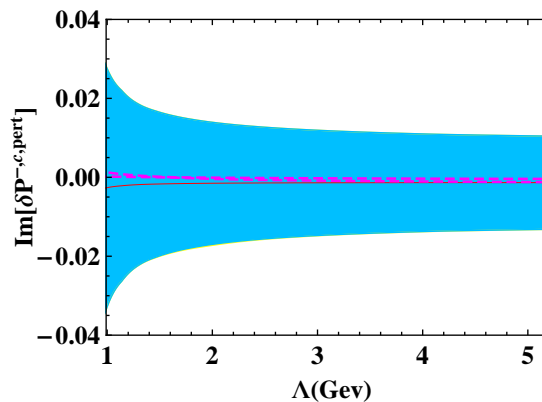
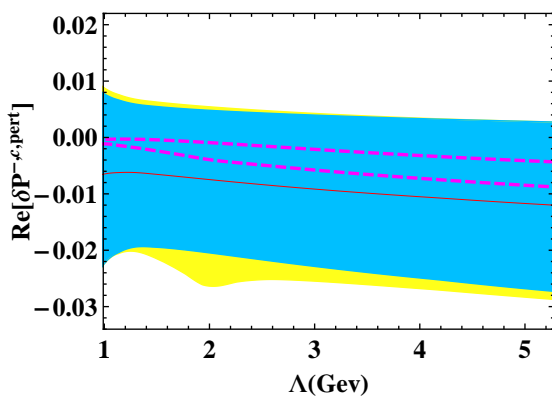
QCD penguin PC's in $B \rightarrow \phi K^*$, $K^* \rho$

- PC fits: varied all available Br, CP asymmetry, transversity angular analysis measurements within 1σ errors

- The negative helicity $\bar{B} \rightarrow \phi K^{*0}$ and $B^- \rightarrow K^{*0} \rho^-$ QCD penguins



- $B \rightarrow \phi K^{*0}$ “perturbative” QCD penguin PC's:



Consistent with $|\delta P^{c-, \text{non-pert.}} / \delta P^{c-, \text{pert.}}| = O(1 - \text{few})$, within large errors, and with $e^+ e^- \rightarrow \rho^+ \rho^-$

Conclusions

- puzzles in charmless $B \rightarrow M_1 M_2$ could be accounted for via power corrections if they have large soft-overlaps
 - PP, VP, VV penguin power corrections would be **same order** as leading power penguins
 - PP : $O(10)$ enhancement of PC's due to soft-overlaps
 VP, VV : consistent with more moderate $O(1)$ to $O(\text{few})$ enhancement of PC's
- $e^+e^- \rightarrow PP, VP, VV$ provides a direct probe of non-perturbative power corrections
 - continuum CLEO-c and $\Upsilon(4S)$ data yields a similar pattern to what would be required in B decays:
 - $O(10)$ non-perturbative enhancement of power corrections in PP , and consistent with more moderate $O(1)$ to $O(\text{few})$ enhancement in VP, VV
- Therefore, the e^+e^- data is telling us that the power correction orders of magnitude required in B decays are natural and not at all surprising

More measurements that would be helpful:

- **strong phase difference** between (LL) and (LT) helicity amplitudes in $e^+e^- \rightarrow \rho^+\rho^-$ at the $\Upsilon(4S)$, improve the precision of the $\rho^+\rho^-$ analysis
- BELLE should also do the $\rho^+\rho^-$ analysis
- we do not have a continuum $e^+e^- \rightarrow VV$ analysis at CLEO-c energies
- $V_{\omega\pi}$ at the $\Upsilon(4S)$. Can be combined with precise and clean CLEO-c measurement at 3.77 GeV, to further test power counting
- BABAR should also measure $V_{\rho\eta}$
- $V_{K^*0K^0}$ at the $\Upsilon(4S)$
- High luminosity flavor factories: use initial state radiation to measure F_π at $\sqrt{s} > 3.67$ GeV. Expect $\sigma(e^+e^- \rightarrow \pi^+\pi^-) \sim 0.5 \text{ pb}$ at $\sqrt{s} \approx m_B$