

Belle time-integrated $\gamma(\phi_3)$ measurements

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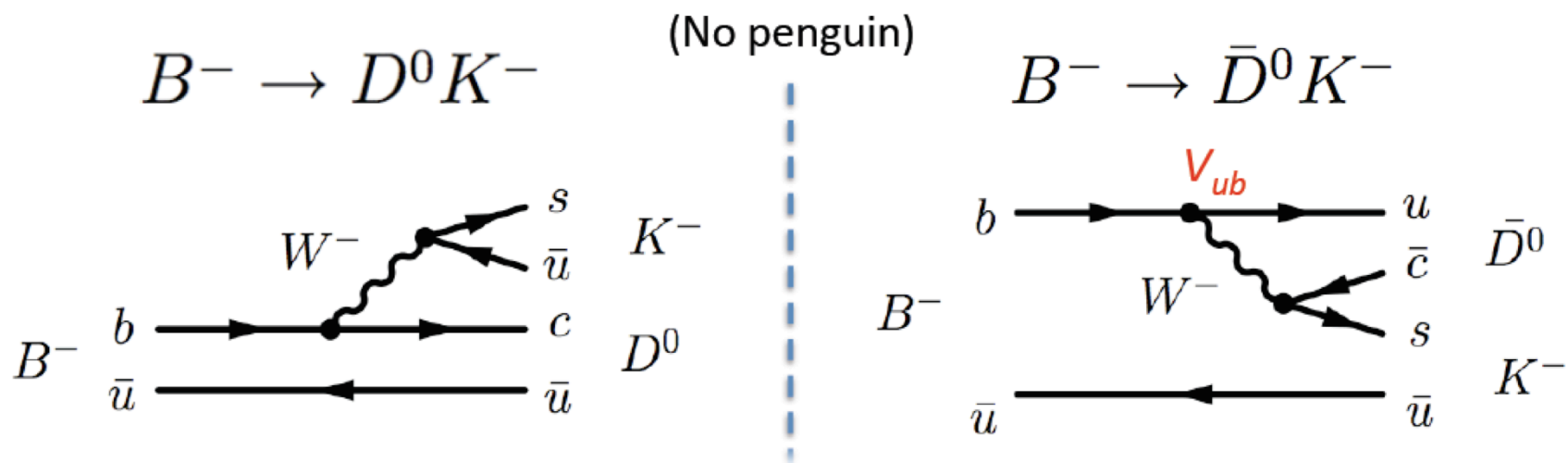
CKM2010

Introduction

- ▶ The phase ϕ_3 is included in the transition $b \rightarrow u$.

$$\phi_3 \equiv \arg \left(\frac{V_{ud}V_{ub}^*}{-V_{cd}V_{cb}^*} \right) \sim -\arg(V_{ub})$$

- ▶ Most popular methods use the decay $B^- \rightarrow DK^-$ (and the conjugate).



- ▶ Value of ϕ_3 is extracted through the **interference** of two paths, which occurs when D^0 and \bar{D}^0 decay to the same final state.

Introduction

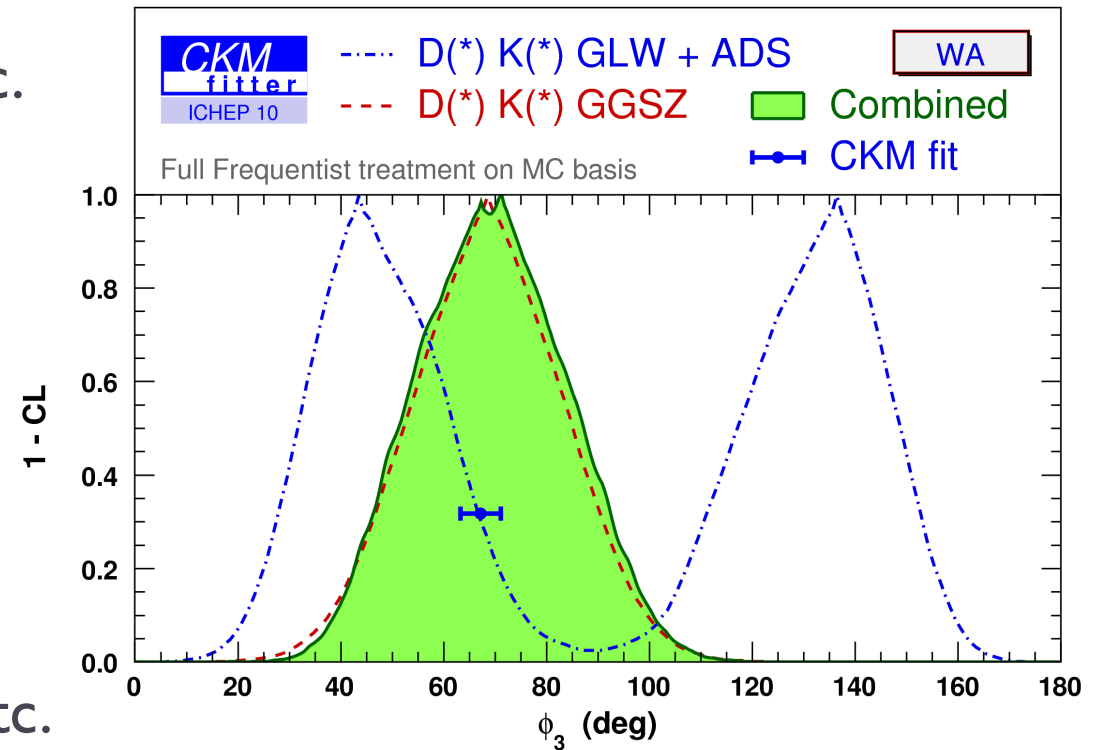
▶ Dalitz (GGSZ)

- ▶ GGSZ, PRD 68, 054018 (2003).
- ▶ Dalitz analysis on $D \rightarrow K_S \pi^+ \pi^-$, etc.
- ▶ Most sensitive.

▶ GLW+ADS

- ▶ GW, PLB 265, 172 (1991).
ADS, PRL 78, 3257 (1997).
- ▶ Fit using the observables from $D \rightarrow CP$ eigenstates, $K^+ \pi^-$, etc.

- ▶ In each case, enough information is obtained to extract the ratio of magnitudes of amplitudes (r) and the strong phase (δ).



Topics for Today

▶ $B^- \rightarrow D^{(*)} K^-$, $D \rightarrow K_S \pi^+ \pi^-$ Dalitz

▶ A. Poluektov et al.,
PRD 81, 112002 (2010).

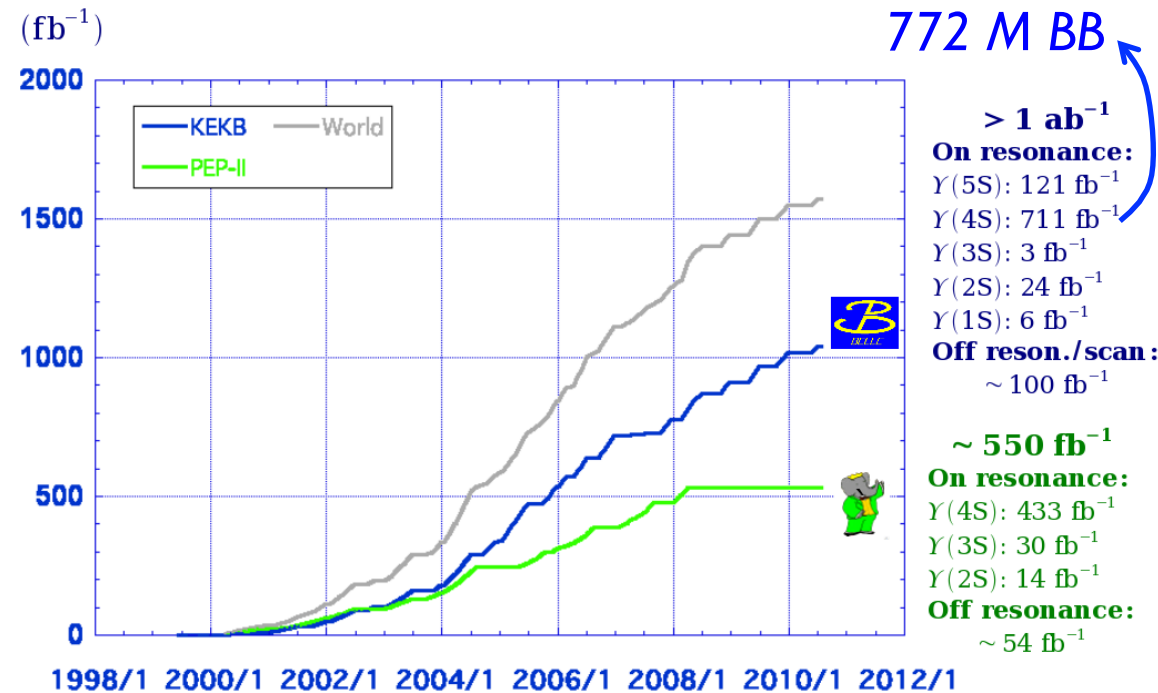
▶ 657 M BB.

▶ $B^- \rightarrow DK^-$, $D \rightarrow K^+ \pi^-$ ADS

▶ **New result (preliminary)
shown for the first time.**

▶ 772 M BB:
full $Y(4S)$ data for Belle.

Luminosity at B factories



B Meson Reconstruction

▶ Primary particles

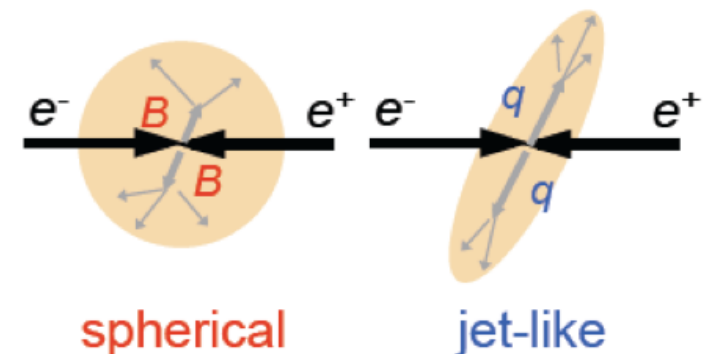
- ▶ **K/ π identification: efficiency $\sim 85\%$, fake rate $\sim 10\%$.**
- ▶ K_S : reconstructed from $\pi^+\pi^-$ using $M_{\pi\pi}$ and vertex information.
- ▶ π^0 : reconstructed from $\gamma\gamma$ using $M_{\gamma\gamma}$ and E_γ .

▶ Two kinematic variables

- ▶ **Energy difference** $\Delta E \equiv E_B - E_{\text{beam}}$
- ▶ **Beam-energy constrained mass** $M_{\text{bc}} \equiv \sqrt{E_{\text{beam}}^2 - |p_B|^2}$

▶ Continuum suppression by

- ▶ Fisher discriminant of SFW moments or
- ▶ **Neural Network including more variables.**



$B^- \rightarrow D^{(*)} K^-$, $D \rightarrow K_S \pi^+ \pi^-$ Dalitz

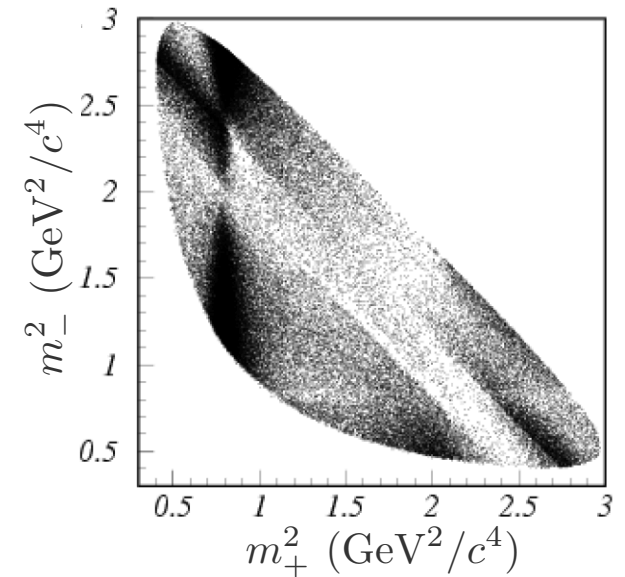
- ▶ Amplitude of $B^\pm \rightarrow DK^\pm$ process can be expressed as

$$M_\pm = \underline{f(m_\pm^2, m_\mp^2)} + \underline{r} e^{\pm i\phi_3 + i\delta} \underline{f(m_\mp^2, m_\pm^2)}$$

$$m_\pm^2 = m_{K_S \pi^\pm}^2$$

Ratio of magnitudes
of interfering amplitudes.

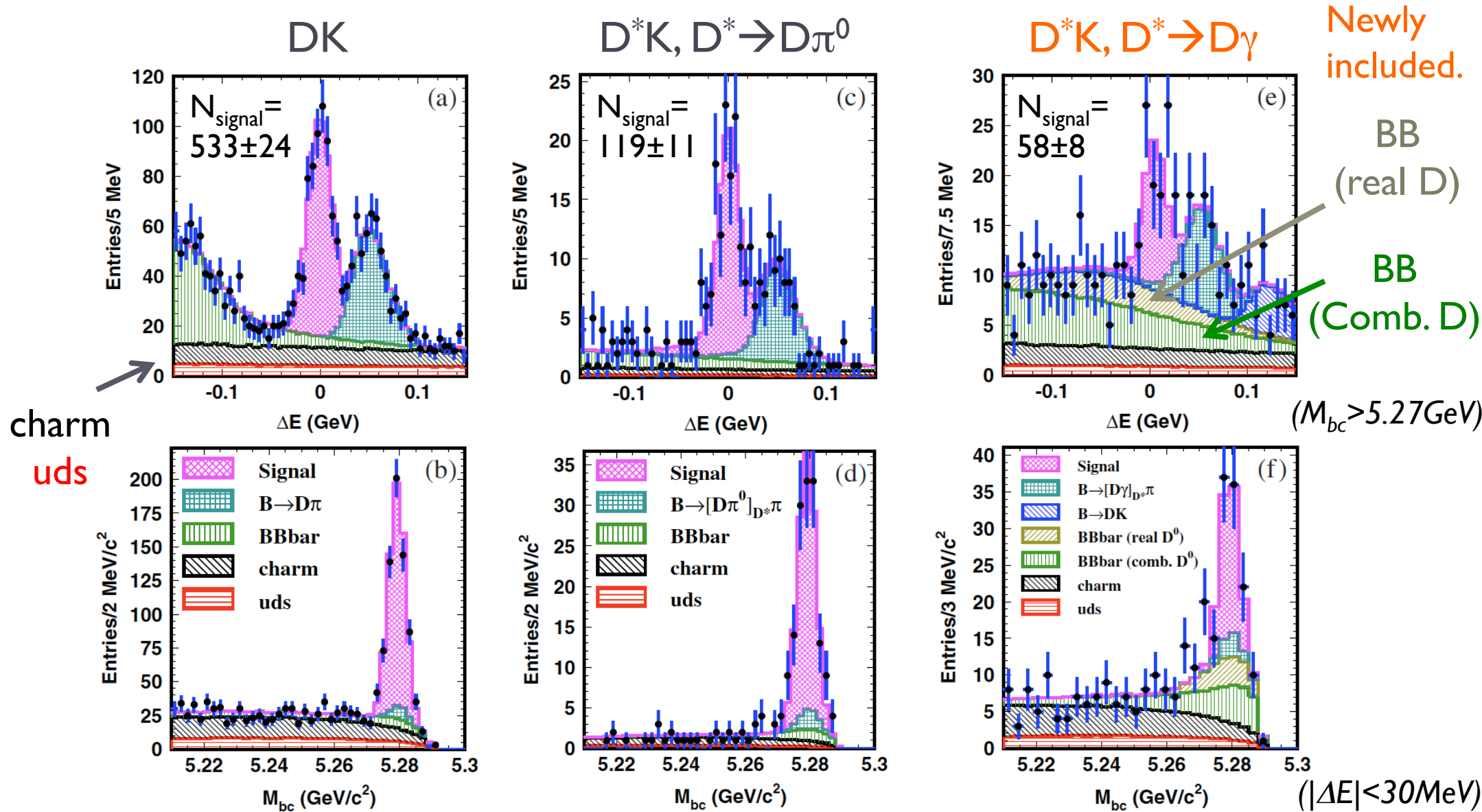
Amplitude of $D \rightarrow K_S \pi^+ \pi^-$ decay
determined from Dalitz plot of large continuum data
(Flavor is tagged by soft-pion charge in $D^{*\pm} \rightarrow D \pi_{\text{soft}}^\pm$).
Isobar-model assumption with BW for resonances.



- ▶ Procedure of analysis:

1. Background fractions are determined by 2-D UML fit for ΔE and M_{bc} .
2. Fit is performed to m_\pm (Dalitz plane).

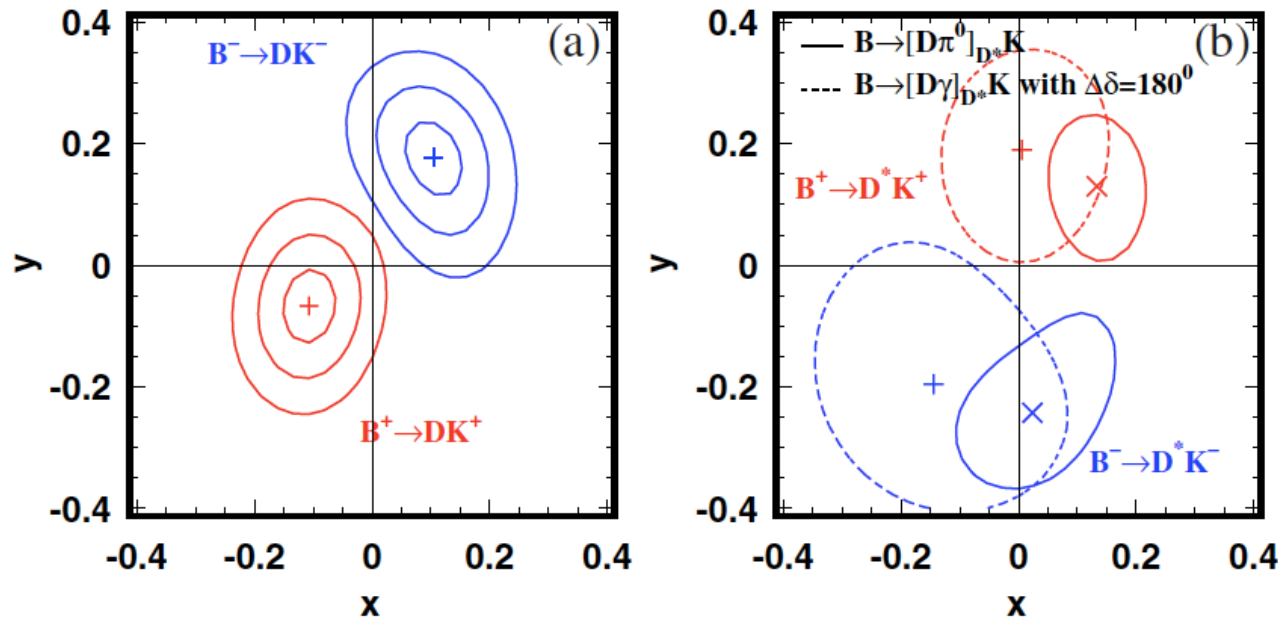
$B^- \rightarrow D^{(*)} K^-$ Dalitz, ΔE and M_{bc} Projections



$B^- \rightarrow D^{(*)} K^-$ Dalitz, Result

657 M BB

- Using the background fractions, Dalitz plane is fitted with the parameters $x_{\pm} = r_{\pm} \cos(\pm\phi_3 + \delta)$ and $y_{\pm} = r_{\pm} \sin(\pm\phi_3 + \delta)$.



- Combining the results for $B \rightarrow D^{(*)} K$, we obtain Model-independent analysis will be applied for 772M BB.

$$\phi_3 = 78.4^\circ \begin{matrix} +10.8^\circ \\ -11.6^\circ \end{matrix} \pm 3.6^\circ (\text{syst}) \pm 8.9^\circ (\text{model})$$

$$\left(\begin{array}{l} r_{DK} = 0.160^{+0.040}_{-0.038} \pm 0.011^{+0.050}_{-0.010}, \quad \delta_{DK} = 136.7^\circ \begin{matrix} +13.0^\circ \\ -15.8^\circ \end{matrix} \pm 4.0^\circ \pm 22.9^\circ \\ r_{D^*K} = 0.196^{+0.072}_{-0.069} \pm 0.012^{+0.062}_{-0.012}, \quad \delta_{D^*K} = 341.9^\circ \begin{matrix} +18.0^\circ \\ -19.6^\circ \end{matrix} \pm 3.0^\circ \pm 22.9^\circ \end{array} \right)$$

$B^- \rightarrow DK^-, D \rightarrow K^+\pi^-$ ADS

- ▶ Large effect of ϕ_3 appears in the branching fraction due to similar magnitudes of interfering amplitudes.
- ▶ We also analyze $B \rightarrow D\pi$ as a reference.

▶ We measure

▶ Partial rate

$$\begin{aligned} \mathcal{R}_{Dh} &\equiv \frac{\mathcal{B}(B^- \rightarrow [K^+\pi^-]_D h^-) + \mathcal{B}(B^+ \rightarrow [K^-\pi^+]_D h^+)}{\mathcal{B}(B^- \rightarrow [K^-\pi^+]_D h^-) + \mathcal{B}(B^+ \rightarrow [K^+\pi^-]_D h^+)} \\ &= r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \phi_3, \end{aligned}$$

Calibration Mode

▶ Asymmetry

$$\begin{aligned} \mathcal{A}_{Dh} &\equiv \frac{\mathcal{B}(B^- \rightarrow [K^+\pi^-]_D h^-) - \mathcal{B}(B^+ \rightarrow [K^-\pi^+]_D h^+)}{\mathcal{B}(B^- \rightarrow [K^+\pi^-]_D h^-) + \mathcal{B}(B^+ \rightarrow [K^-\pi^+]_D h^+)} \\ &= 2r_B r_D \sin(\delta_B + \delta_D) \sin \phi_3 / \mathcal{R}_{Dh}, \end{aligned}$$

$h = K \text{ or } \pi$

$r_{B(D)}$: ratio of magnitudes of amplitudes for B (D) decays.

$\delta_{B(D)}$: strong-interaction phase for B (D) decays.

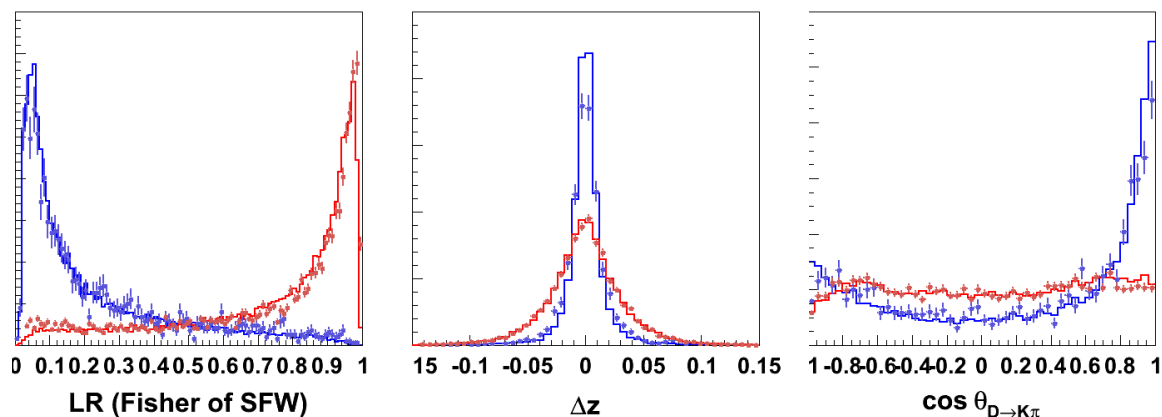
HFAG and CLEO-c inputs for r_D and δ_D .

Continuum Suppression

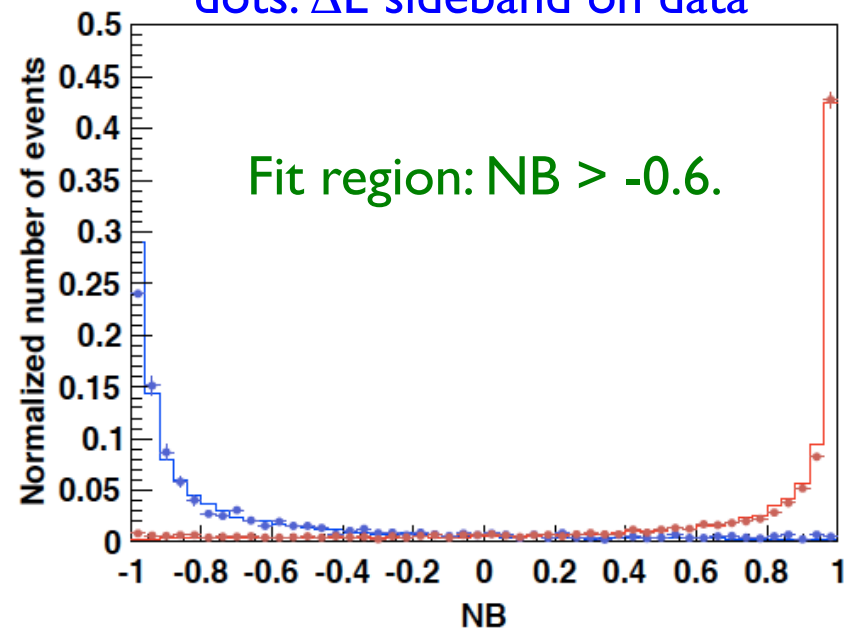
- ▶ Main background is $e^+e^- \rightarrow q\bar{q}$ ($q=u, d, s, c$) continuum process.
- ▶ To discriminate this background, new technique employs NeuroBayes (NB) neural network.

NB inputs (10 in total):

- LR for Fisher of SFV moments
- Vertex separation between reconstructed B and the other B (Δz)
- Decay angle for $D \rightarrow K\pi$
- ...



histogram: signal on MC
dots: Calib. mode ($D\pi$) on data
histogram: qq on MC
dots: ΔE sideband on data

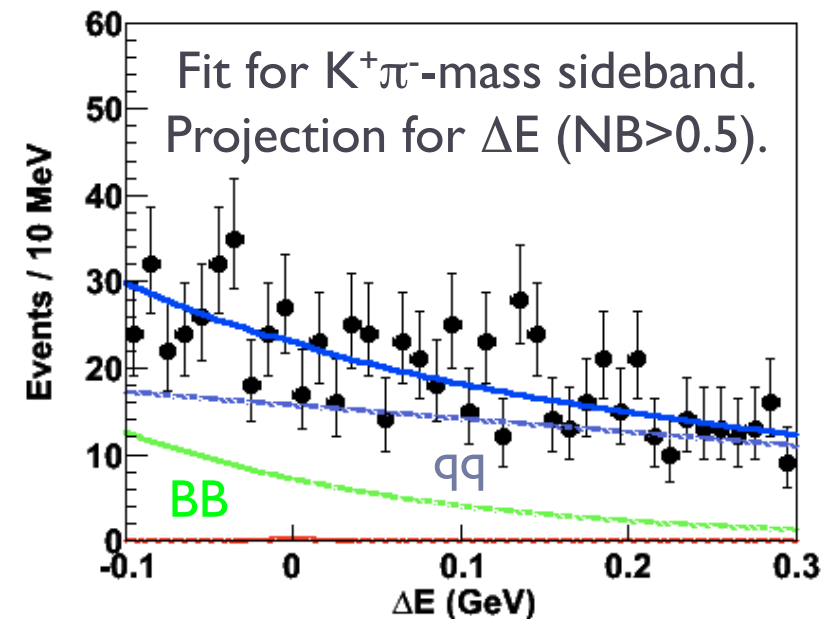


Peaking Background

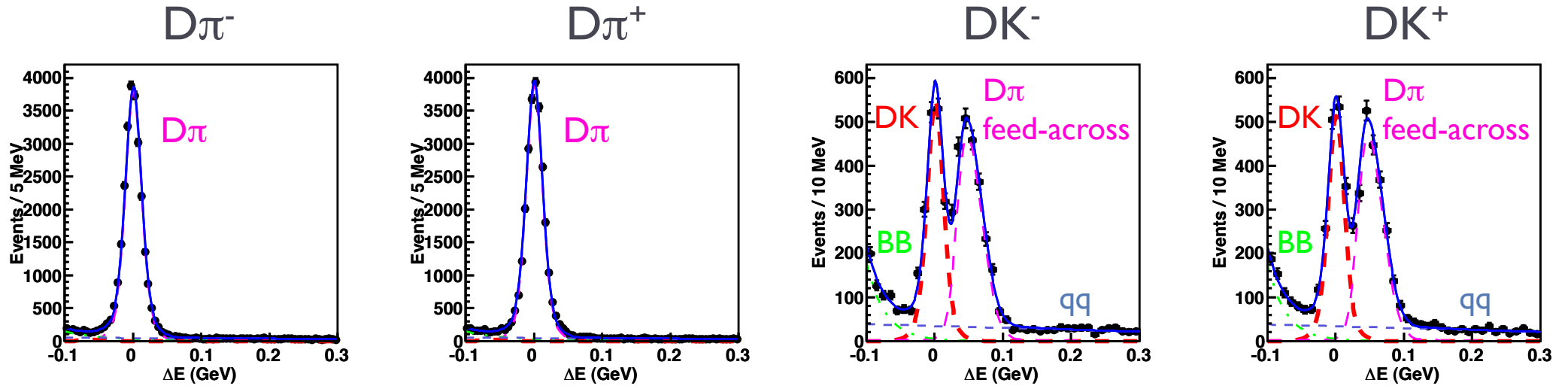
- ▶ $B^- \rightarrow D\pi^-, D \rightarrow K^+K^-$ (same final state)
 - ▶ Veto on K^+K^- mass.
- ▶ $B^- \rightarrow Dh^-, D \rightarrow K^-\pi^+$ (double mis-ID)
 - ▶ Veto on $K^-\pi^+$ mass, where ID is exchanged.
- ▶ Charmless $B^- \rightarrow K^+K^-\pi^-$ (same final state)

} ~Flat $K^+\pi^-$ -mass distribution.

- ▶ We estimate the total contribution using $K^+\pi^-$ -mass sideband of data.
 - ▶ $0.020 < |M_{K\pi} - 1.865| < 0.050$ (in GeV).
 - ▶ Estimated number = 0.4 ± 5.5 .



Simultaneous Fit for $B^- \rightarrow [K^- \pi^+]_D h^-$ (Calib. Modes)



(Projections for all fitted regions are shown.)

ΔE : Dh: 2 Gaussians (the same free shape for π/K).
 $D\pi$ feed-across: 2 Asym. Gaussians ($\mu, \sigma_{l, \text{right}}$ free).
 BB: free exponential. qq: free linear.

NB: Dh: Hist. from $|\Delta E| < 10$ MeV. \leftarrow Subtract qq.
 $D\pi$ feed-across: Hist. from $|\Delta E - 50 \text{ MeV}| < 10$ MeV.
 BB: Hist. from MC. qq: Hist. from M_{bc} sideband.

Simultaneous Fit for $B^- \rightarrow [K^+\pi^-]_D h^-$

772 M BB

- ▶ Projections for $h=\pi$ in signal regions are shown.

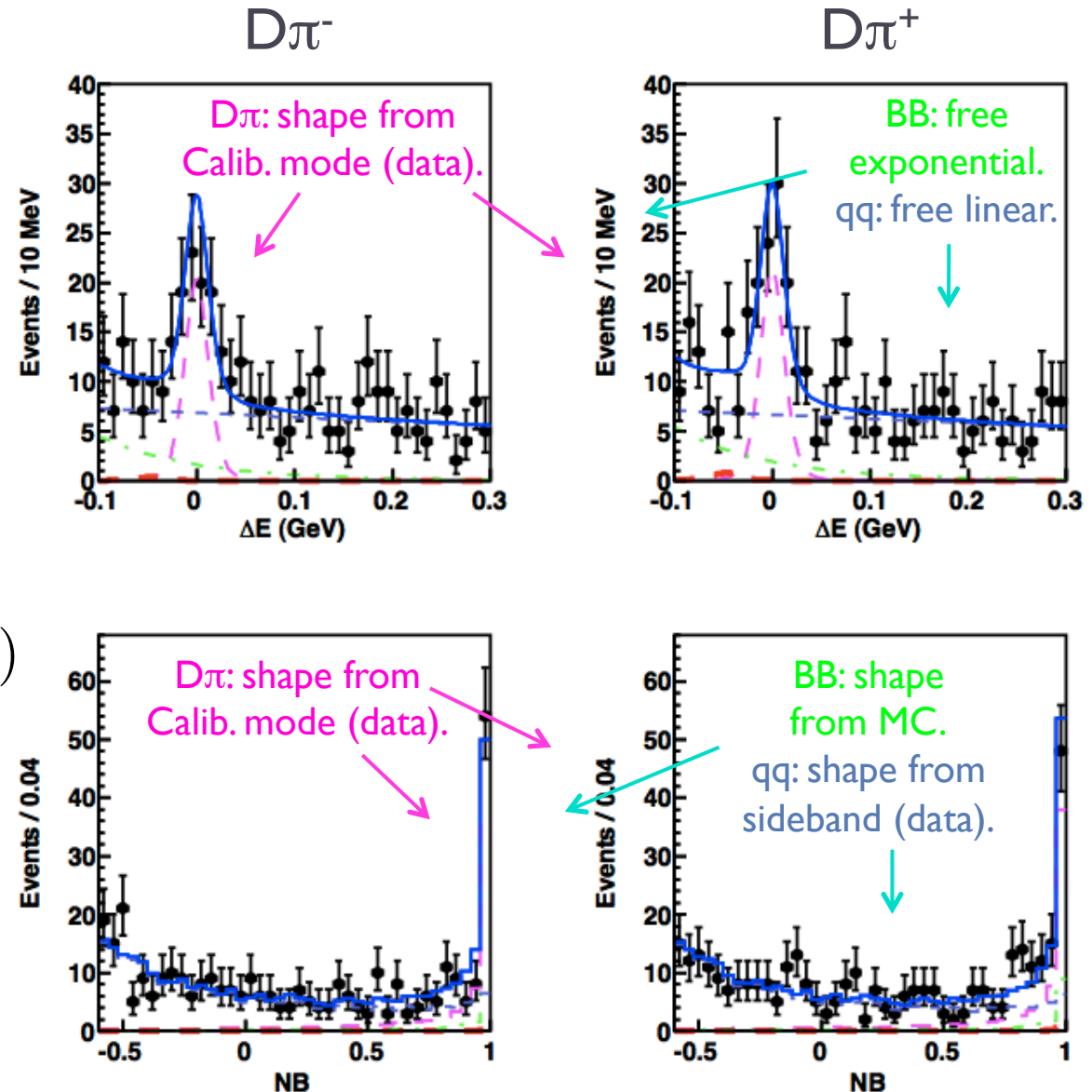
- ▶ $NB > 0.5$
- ▶ $|\Delta E| < 0.04$ GeV

- ▶ The results ($R_{D\pi}$ in 10^{-3}) are

$$\mathcal{R}_{D\pi} = 3.28 \pm 0.37(\text{stat})_{-0.23}^{+0.22}(\text{syst})$$

$$\mathcal{A}_{D\pi} = -0.04 \pm 0.11(\text{stat})_{-0.02}^{+0.01}(\text{syst})$$

- ▶ Most precise measurements to date with a significance 8.4σ (including syst).



Simultaneous Fit for $B^- \rightarrow [K^+\pi^-]_D h^-$

772 M BB

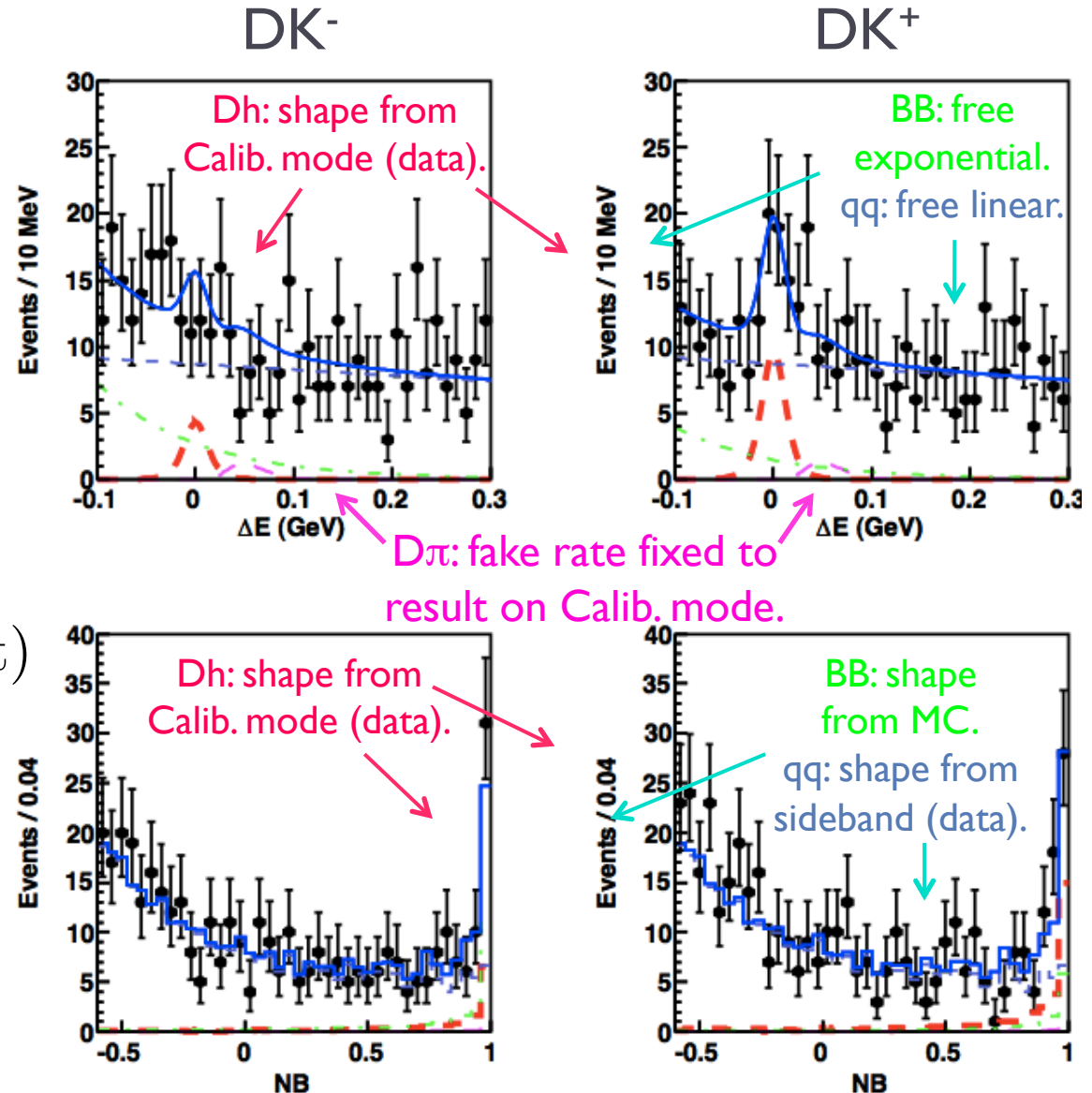
- ▶ Projections for $h=K$ in signal regions are shown.
 - ▶ $NB > 0.5$
 - ▶ $|\Delta E| < 0.04$ GeV

- ▶ The results (R_{DK} in 10^{-2}) are

$$\mathcal{R}_{DK} = 1.62 \pm 0.42(\text{stat})_{-0.19}^{+0.16}(\text{syst})$$

$$A_{DK} = -0.39 \pm 0.26(\text{stat})_{-0.04}^{+0.06}(\text{syst})$$

- ▶ First evidence is obtained with a significance 3.8σ (including syst).



Systematic Uncertainties

| Source | \mathcal{R}_{DK} | $\mathcal{R}_{D\pi}$ | \mathcal{A}_{DK} | $\mathcal{A}_{D\pi}$ |
|-----------------------|--------------------|----------------------|--------------------|----------------------|
| Fit | +9.7% -6.3% | +6.5% -5.3% | +0.05 -0.04 | +0.009 -0.018 |
| (ΔE -PDF | +4.4% -3.6% | +2.4% -2.3% | ± 0.02 | ± 0.003) |
| (\mathcal{NB} -PDF | +4.2% -1.6% | +4.0% -2.8% | +0.02 -0.01 | +0.001 -0.010) |
| (Yield and asymmetry | $\pm 1.1\%$ | $\pm 0.1\%$ | ± 0.01 | ± 0.005) |
| Peaking backgrounds | +0.7% -9.9% | +0.0% -4.1% | +0.03 -0.00 | +0.002 -0.000 |
| Efficiency | $\pm 1.7\%$ | $\pm 1.5\%$ | ... | ... |
| Detector asymmetry | ... | ... | ± 0.02 | ± 0.005 |

- ▶ The uncertainties due to the fit are dominant components.
 - ▶ Conservatively take a linear sum of all uncertainties in the fit.
- ▶ Detector asymmetry is obtained by the calibration mode.
- ▶ The total systematic error is the sum in quadrature.

Summary

▶ $B^- \rightarrow D^{(*)} K^-, D \rightarrow K_S \pi^+ \pi^-$ Dalitz

▶ 657 M BB.

▶ Mode $D^* \rightarrow D\gamma$ is included.

▶ Most precise measurement of ϕ_3 is obtained.

$$\phi_3 = 78.4^\circ \begin{matrix} +10.8^\circ \\ -11.6^\circ \end{matrix} \pm 3.6^\circ (\text{syst}) \pm 8.9^\circ (\text{model})$$

▶ $B^- \rightarrow DK^-, D \rightarrow K^+ \pi^-$ ADS (PRELIMINARY)

▶ 772 M BB: full Y(4S) data.

▶ New approach on continuum suppression is employed.

▶ First evidence of signal is obtained with a significance 3.8σ .

Backup

A Check for NeuroBayes Performance

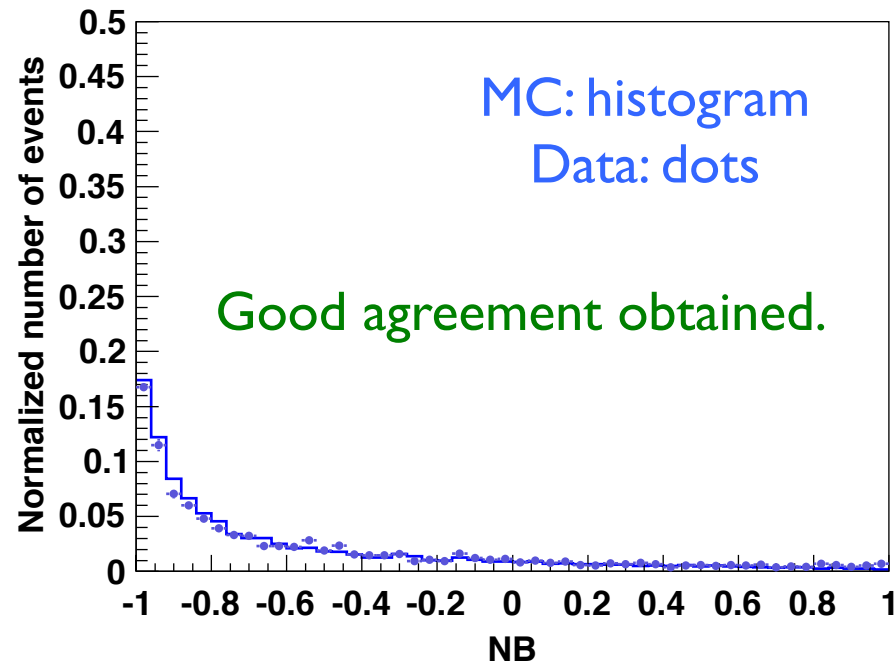
NB training is performed with 7 variables (removing Δz , $\cos\theta_{D\rightarrow K\pi}$, and distance_{Dh}).

By using the result of this training, we obtain the NB-output distributions for

qq MC shown with a histogram and

data ($\Delta E > 150$ MeV: qq-dominated region) shown with dots.

some data/MC differences



Note: we obtain the PDF used for the fit from M_{bc} sideband ($5.20 \text{ GeV} < M_{bc} < 5.26 \text{ GeV}$) of data; the result will not be effected by a discrepancy between data and MC.

Comparison between Different Results

| | This Analysis | Previous Result by Belle | Latest Result by BaBar |
|---------------------------------------|-------------------------------------|--|-------------------------------------|
| $\mathcal{R}_{DK} [\times 10^{-2}]$ | 1.62 ± 0.42 $^{+0.16}_{-0.19}$ | 0.78 $^{+0.62}_{-0.57}$ $^{+0.20}_{-0.28}$ | $1.1 \pm 0.6 \pm 0.2$ |
| $\mathcal{R}_{D\pi} [\times 10^{-3}]$ | 3.28 ± 0.37 $^{+0.22}_{-0.23}$ | 3.40 $^{+0.55}_{-0.53}$ $^{+0.15}_{-0.22}$ | $3.3 \pm 0.6 \pm 0.4$ |
| \mathcal{A}_{DK} | -0.39 ± 0.26 $^{+0.06}_{-0.04}$ | -0.1 $^{+0.8}_{-1.0} \pm 0.4$ | -0.86 ± 0.47 $^{+0.12}_{-0.16}$ |
| $\mathcal{A}_{D\pi}$ | -0.04 ± 0.11 $^{+0.01}_{-0.02}$ | -0.02 $^{+0.15}_{-0.16} \pm 0.04$ | $0.03 \pm 0.17 \pm 0.04$ |
| N(BB) = | 772 M | 657 M | 467 M |

- ▶ The consistencies for $D\pi$ results strongly encourage us to be confident with our new method.
- ▶ The value of \mathcal{R}_{DK} is $\sim 1\sigma$ higher than the previous value by Belle, for which the reason can be statistical since more than 60 % events are independent of the ones in the previous analysis.
(In the previous analysis, tight cut was applied for qq suppression.)

Significance

- ▶ The significance is estimated by convoluting the likelihood in the fit and an asymmetric Gaussian whose widths are the systematic errors.

