



WGV Summary
 γ from B to charm decays

*Robert Fleischer
and Stefania Ricciardi
on behalf of the speakers of WGV*

12 Talks

Mainly experimental discussions: time-dependent and time-integrated measurements of γ

Introduction and conclusions by theorists

*Jure Zupan, **The case for measuring gamma precisely***

*RUBIN, Ada, **BaBar time-dependent gamma measurements***

*ONUKE, Yoshiyuki, **Belle time-dependent gamma measurements***

*GLIGOROV, Vladimir, **LHCb time-dependent gamma measurements***

*RICCIARDI, Stefania, **Charm inputs to gamma measurements from CLEO***

*HORII, Yasuyuki, **Belle time-integrated gamma measurements***

*MARCHIORI, Giovanni, **BaBar time-integrated gamma measurements***

*SQUILLACIOTI, Paola **Tevatron time-integrated gamma measurements and prospects***

*WILLIAMS, J Michael, **LHCb time-integrated gamma measurements and prospects***

*SPRADLIN, Patrick, **Charm inputs for the next decade***

*POLUEKTOV, Anton, **Ultimate sensitivity on gamma/phi3 from B to DK***

*FLEISCHER, Robert, **Extracting gamma from Bs to J/psi Ks***

WGV - γ from B to charm decays: what have we learnt?

1. The case for a very precise measurement of γ
2. New results from well-established methods
3. New methods (since CKM2008)
4. Future prospects (LHCb and beyond)

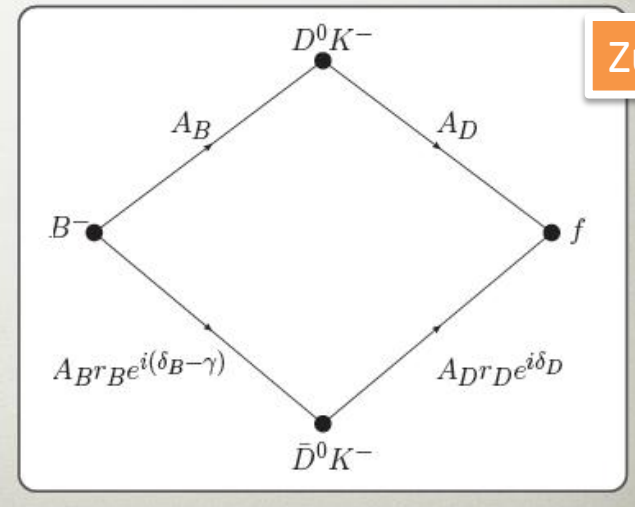
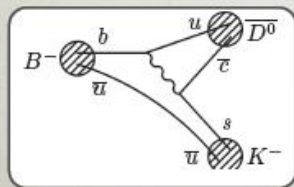
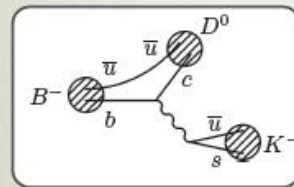
Measuring γ with B to charm decays: definitions

- γ is extracted from the interference between $b \rightarrow c$ and $b \rightarrow u$ transitions in decays of the B->DK family
 - tree-level amplitudes only
 - no penguin pollution, only one weak phase
 - Other B and D hadronic parameters in game, including B and D strong phases

r_B = relative magnitude of suppressed B-decay amplitude over favoured one

δ_B = B-decay strong phase difference

r_D and δ_D similarly defined



Several clean methods to extract all unknowns from data
(use combinations of several D modes or input from charm studies)

How clean is γ from B to charm decays?

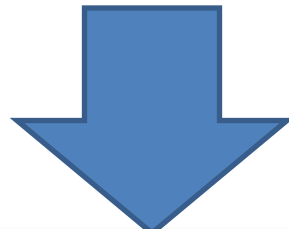
Beyond the usual mantra:
Only tree-level amplitudes,
No theoretical uncertainties,
No NP contributions,
SM standard candle

Theory errors: D-mixing

[Grossman, Soffer, JZ, 2005]

[Bondar, Poluektov, Vorobiev, arXiv 1004.2350]

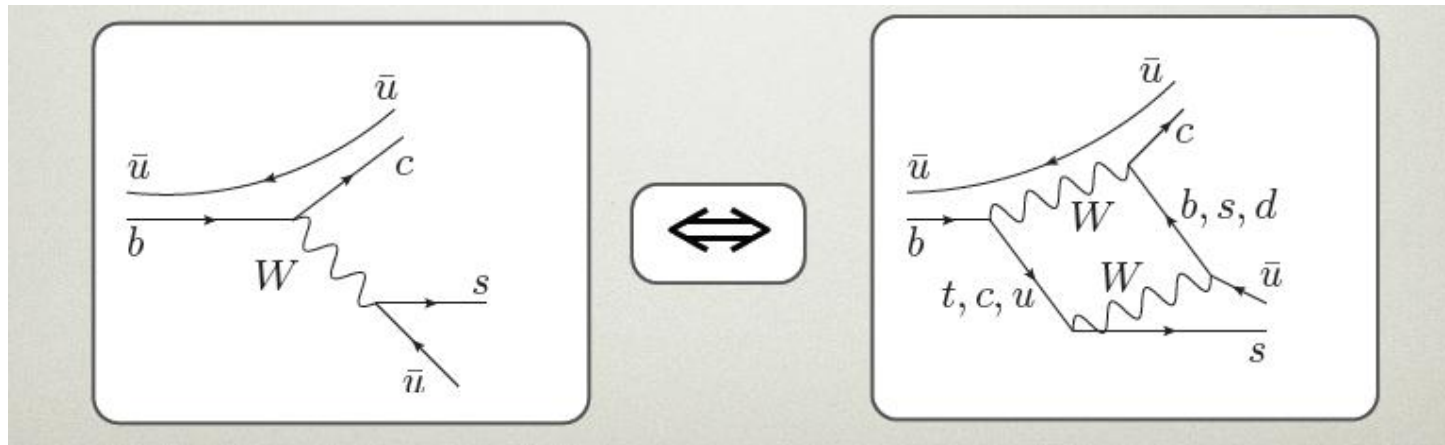
- Assuming SM:
 - D-mixing is CP conserving in SM, hence error on γ is small
 - if D-mixing neglected \rightarrow error $< 1^\circ$
 - Most importantly: D-mixing effects can be included exactly if x_D and y_D precisely measured



NO irreducible uncertainty

Theory errors: electroweak corrections

- Only contribution which can change CKM structure is from box diagrams



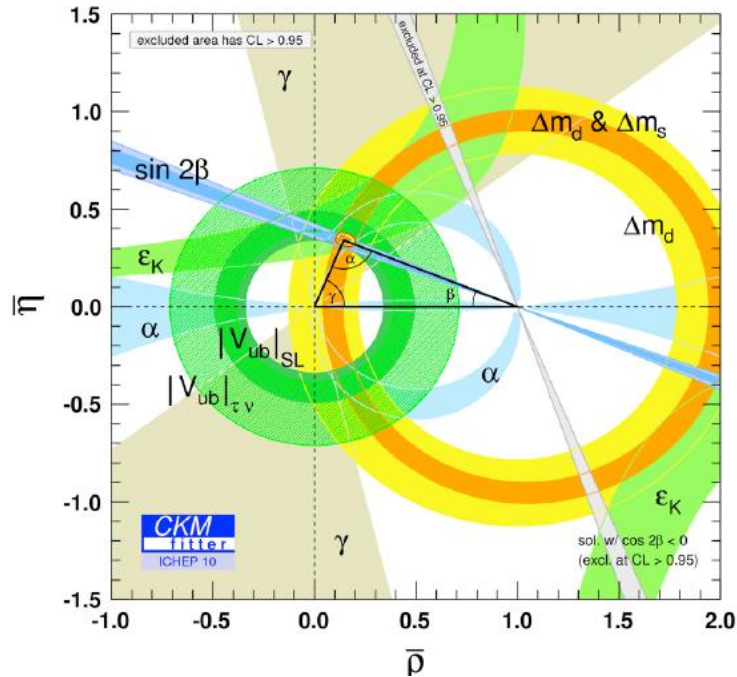
Shift in γ if different weak phase than leading order.

Largest shift:
$$\sim \frac{g^2}{16\pi^2} V_{cb} V_{cs}^* V_{cs}^* V_{us} \frac{m_c^2}{m_W^2} [A_B / (V_{cb} V_{us}^*)] \sim \frac{g^2}{16\pi^2} \frac{m_c^2}{m_W^2} A_B$$

irreducible theory error on γ is

$$\delta\gamma/\gamma \sim O(10^{-6})$$

Current experimental precision



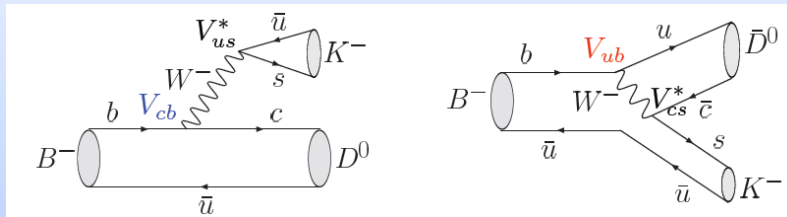
- Error still very large
- Individual measurements more precise than CKM Fitter average
 - An issue here?
 - Not discussed at this workshop
 - Consensus: larger data sample will reduce disagreement between different statistical treatments
- Achieved precision much beyond B-factory design, thanks (mainly) to
 - B-factories excellent performance
 - GGSZ method (new on the scene at CKM2003)

$$\gamma_{\text{CKMFITTER}} = (71^{+21}_{-25})^\circ$$

$$\gamma_{\text{UTFIT}} \sim 11-12^\circ \quad [\text{see A. Stocchi, Joint Session}]$$

Smallest theoretical uncertainty but largest experimental error among all UT constraints!

Results from well-established methods



1. Time-integrated methods



2. Time-dependent methods

GLW : D to CP eigenstates

Gronau & London, PLB 253, 483 (1991);

Gronau & Wyler, PLB 265, 172 (1991)

ADS: D to pseudo-flavour specific states

Atwood, Dunietz, & Soni, PRL 78, 3257 (1997),

Atwood, Dunietz, & Soni, PRD 63, 036005 (2001)

GGSZ: D to 3-body decays

Giri, Grossman, Soffer, & Zupan, PRD 68, 054018 (2003)

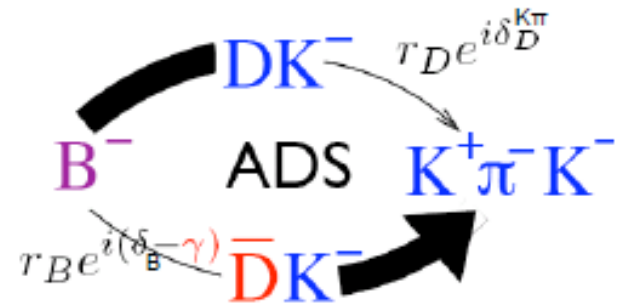
Bondar, PRD 70, 072003 (2004)

Several new results from B-factories and Tevatron
 NO signs of “dusk” yet! On the contrary...

$B^\pm \rightarrow D^0(K\pi)K^\pm$ with the ADS method

Atwood-Dunietz-Soni (ADS) method uses Doubly Cabibbo suppressed decays to enhance γ/ϕ_3 -sensitive interference terms

$$r_D^{K\pi} \approx 0.06 \text{ similar magnitude to } r_B \approx 0.1$$



$$\Gamma(B^- \rightarrow (K^+ \pi^-)_D K^-) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} - \gamma)$$

$$\Gamma(B^+ \rightarrow (K^+ \pi^-)_D K^+) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} + \gamma)$$

Coefficients of interference terms similar order to rest of expression

Method can be extended to multibody decays, e.g., $K\pi\pi\pi$:

$\delta_D^{K3\pi}$ is the average strong phase difference over Dalitz space

$$\Gamma(B^- \rightarrow (K^+ \pi^- \pi^- \pi^+)_D K^-) \propto r_B^2 + (r_D^{K3\pi})^2 + 2r_B r_D^{K3\pi} R_{K3\pi} \cos(\delta_B + \delta_D^{K3\pi} - \gamma)$$

Coherence factor $R_{K3\pi}$ value between 0 (incoherent) and 1 (2 body single amplitude limit)

FIRST evidence of suppressed ADS modes $B^- \rightarrow D(K^+\pi^-)K^-$ and $B^+ \rightarrow D(K^-\pi^+)K^+$ from Belle

PRELIMINARY

Simultaneous Fit for $B^- \rightarrow [K^+\pi^-]_D h^-$ 772 M BB

- ▶ Projections for $h=K$ in signal regions are shown.

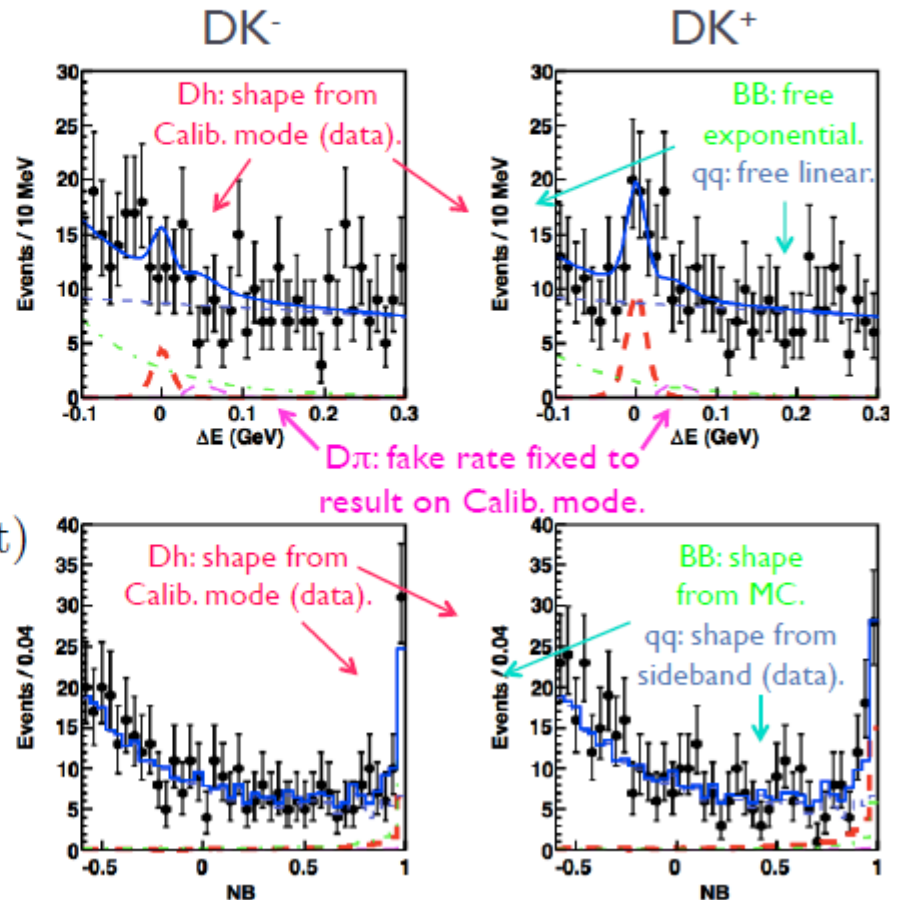
- ▶ $NB > 0.5$
- ▶ $|\Delta E| < 0.04$ GeV

- ▶ The results (R_{DK} in 10^{-2}) are

$$\mathcal{R}_{DK} = 1.62 \pm 0.42(\text{stat})_{-0.19}^{+0.16}(\text{syst})$$

$$\mathcal{A}_{DK} = -0.39 \pm 0.26(\text{stat})_{-0.04}^{+0.06}(\text{syst})$$

- ▶ First evidence is obtained with a significance 3.8σ (including syst).



ADS results from CDF (5 fb^{-1})

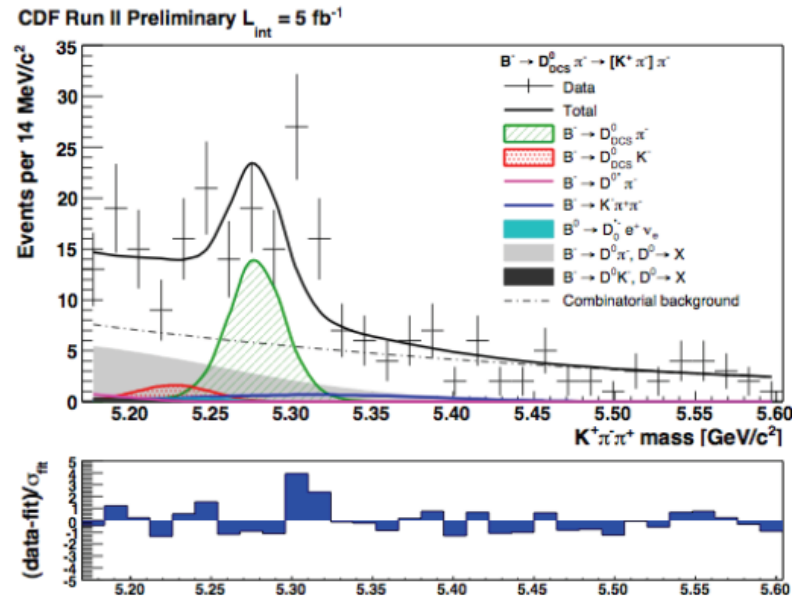
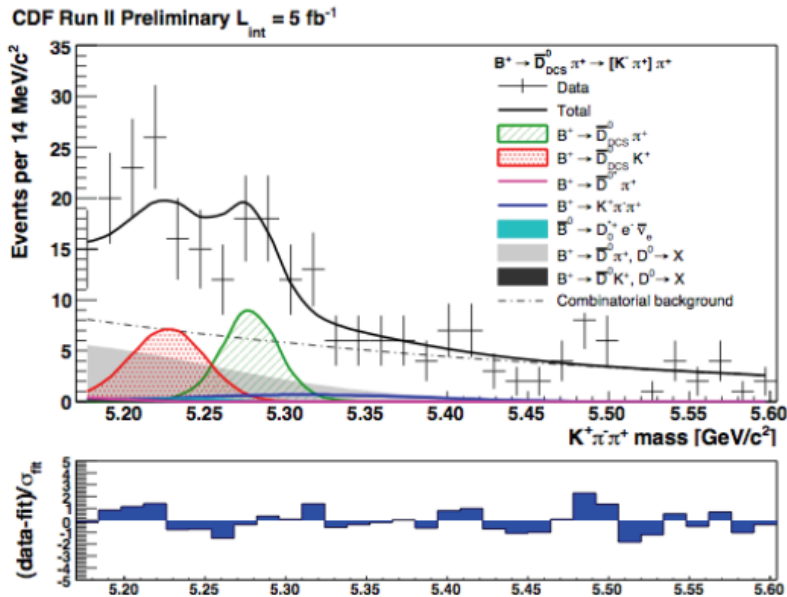
- This supplements recently published first *GLW* analysis in hadron collisions within a CDF global program to measure angle gamma from trees.

$$\begin{aligned} \text{Yield } (B \rightarrow D_{\text{DCS}} K) &= 34 \pm 14 \text{ (} 5 \text{ fb}^{-1}\text{)} \\ \text{Yield } (B \rightarrow D_{\text{DCS}} \pi) &= 73 \pm 16 \text{ (} 5 \text{ fb}^{-1}\text{)} \end{aligned}$$

Significance for all DCS
signal ($D_{\text{DCS}}\pi + D_{\text{DCS}}K$) $> 5 \sigma$

$$B^+ \rightarrow \bar{D}^0_{\text{DCS}} \pi^+ \rightarrow [K^- \pi^+] \pi^+$$

$$B^- \rightarrow D^0_{\text{DCS}} \pi^- \rightarrow [K^+ \pi^-] \pi^-$$





Results

$$R_{ADS}(\pi) = 0.0041 \pm 0.0008(stat) \pm 0.0004(syst)$$

$$A_{ADS}(\pi) = 0.22 \pm 0.18(stat) \pm 0.06(syst)$$

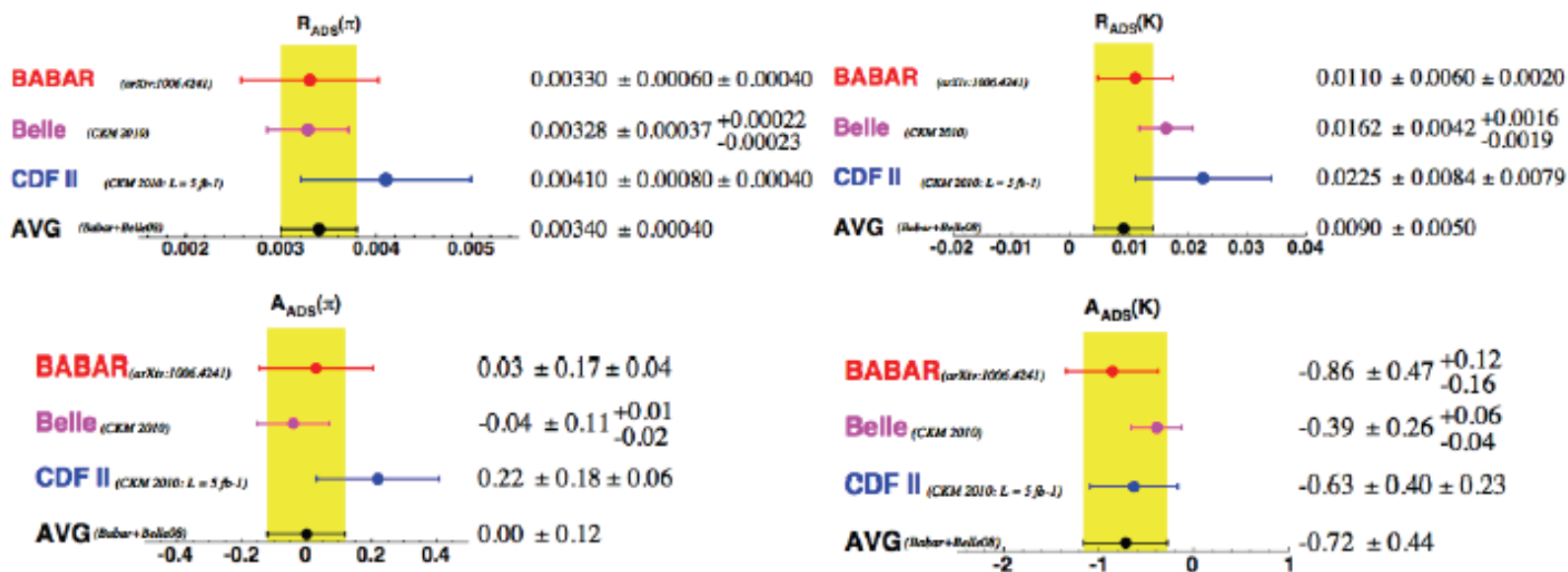
$$R_{ADS}(K) = 0.0225 \pm 0.0084(stat) \pm 0.0079(syst)$$

$$A_{ADS}(K) = -0.63 \pm 0.40(stat) \pm 0.23(syst)$$

$$R_{ADS}(K) = \frac{N(B^- \rightarrow D_{DCS}^0 K^-) + N(B^+ \rightarrow D_{DCS}^0 K^+)}{N(B^- \rightarrow D_{CF}^0 K^-) + N(B^+ \rightarrow D_{CF}^0 K^+)}$$

$$A_{ADS}(K) = \frac{N(B^- \rightarrow D_{DCS}^0 K^-) - N(B^+ \rightarrow D_{DCS}^0 K^+)}{N(B^- \rightarrow D_{DCS}^0 K^-) + N(B^+ \rightarrow D_{DCS}^0 K^+)}$$

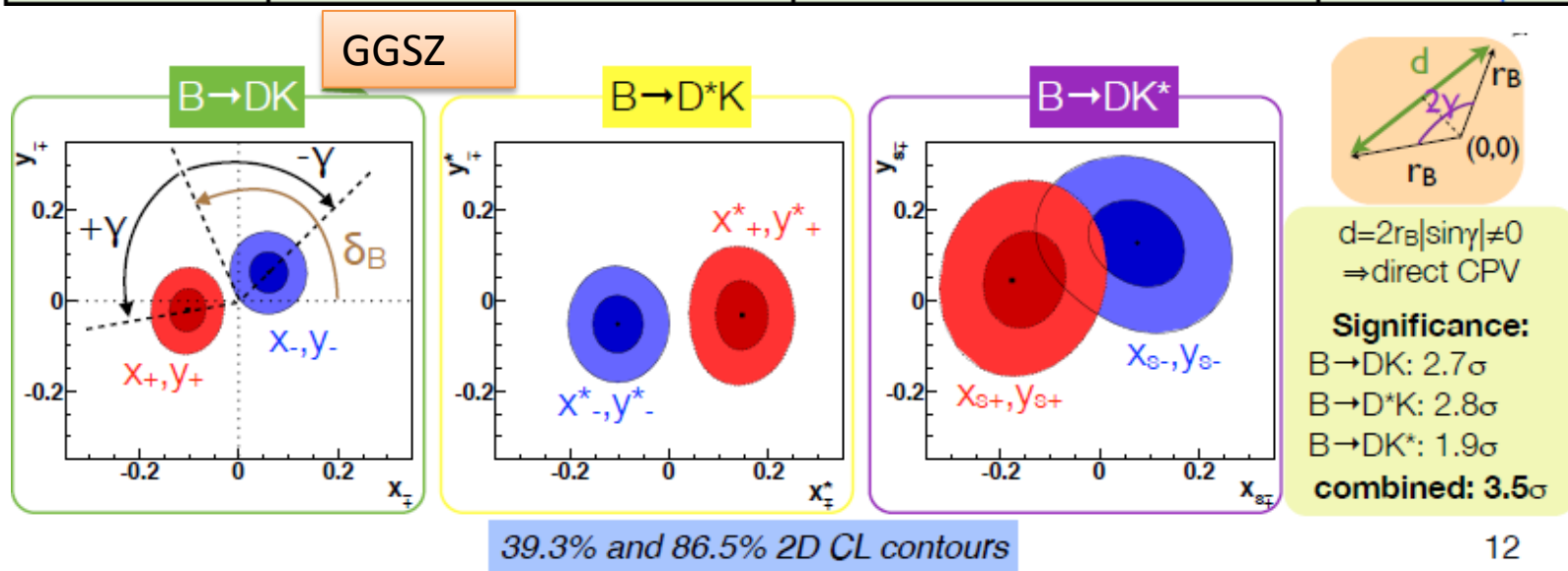
- First measurement of A_{ADS} and R_{ADS} at a hadron collider.
- Agrees with previous measurements from other experiments.



Time-integrated γ at BaBar

GLW, ADS, and GGSZ measurements updated recently using full Y(4S) data set (468M BB pairs)

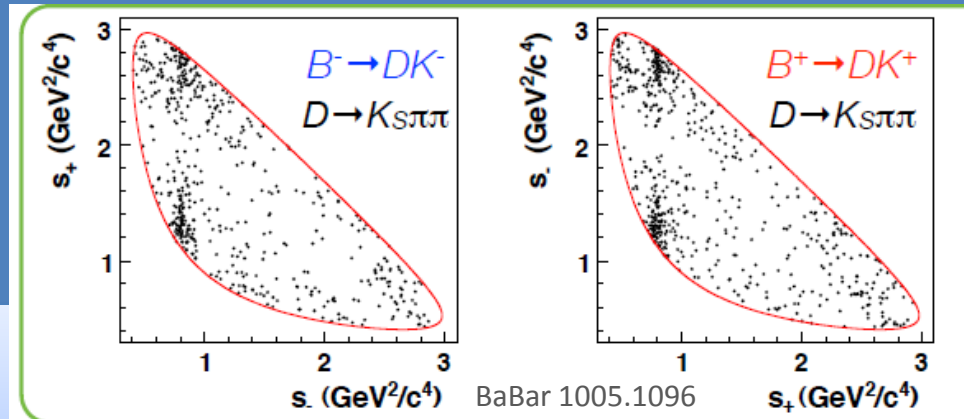
Measurement	CKM 2008		CKM 2010		changes
	N(B \bar{B})	pub. status	N(B \bar{B})	pub. status	
GGSZ D $^{(*)0}$ K $^{(*)}$	383M	PRD 78, 034023 (2008)	468M	arXiv:1005.1096 accepted by PRL	updated Dalitz model, added DK * (D \rightarrow KsKK)
GLW D 0 K	382M	PRD 77, 111102 (2008)	467M	arXiv:1007.0504 accepted by PRD	improved fit technique, added CL scan of γ
ADS D $^{(*)0}$ K	232M	PRD 72, 032004 (2005)	467M	arXiv:1006.4241 submitted to PRD	improved fit technique, better statistical analysis, CL scan of γ



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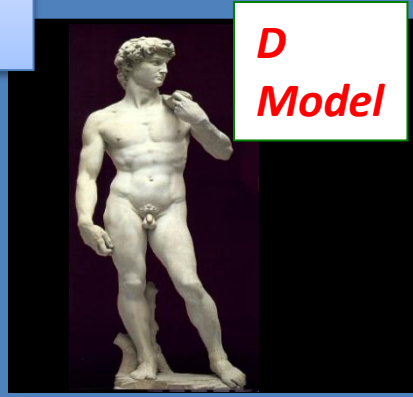
Reminder: GGSZ or “Dalitz” method

- Exploits different interference pattern in the two D to $K_S\pi\pi$ Dalitz plot (from B^+ and B^-)
- CLASSIC APPROACH* : amplitude fit to the B event densities in the D Dalitz plots



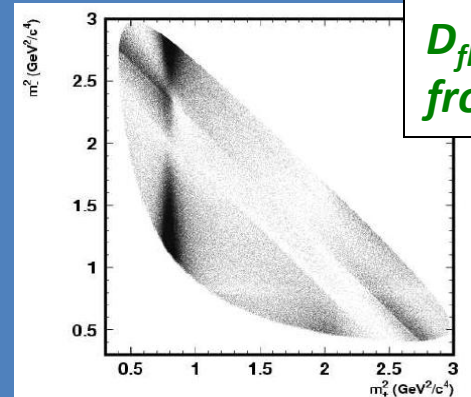
$D \rightarrow K_S \pi \pi$ DP
for B^+ and B^-

Analysis main ingredients



D
Model

+



$D_{flav} \rightarrow K_S \pi \pi$
from $D^* \rightarrow D \pi$

$$A(B^\pm \rightarrow D(K_S \pi \pi) K^\pm) \propto f(m_+, m_\pm) + r_B e^{i(\delta_B \pm \gamma)} f(m_+, m_\pm)$$

- D-decay amplitude determined from a flavour-tagged sample from $D^{*+} \rightarrow D^0 \pi^+$ using model assumptions

GGSZ results from Belle and BaBar on full data set

$$\phi_3 = 78.4^\circ \begin{matrix} +10.8^\circ \\ -11.6^\circ \end{matrix} \pm 3.6^\circ (\text{syst}) \pm 8.9^\circ (\text{model})$$

A. Poluektov et al., PRD 81, 112002 (2010)

Belle

657M BB
D(K_sππ)K

$$\gamma(\text{mod}180^\circ) = (68 \pm 14 \pm 4 \pm 3)^\circ$$

stat syst model

Babar

468M BB
D(K_sππ)K
D(K_sKK)K

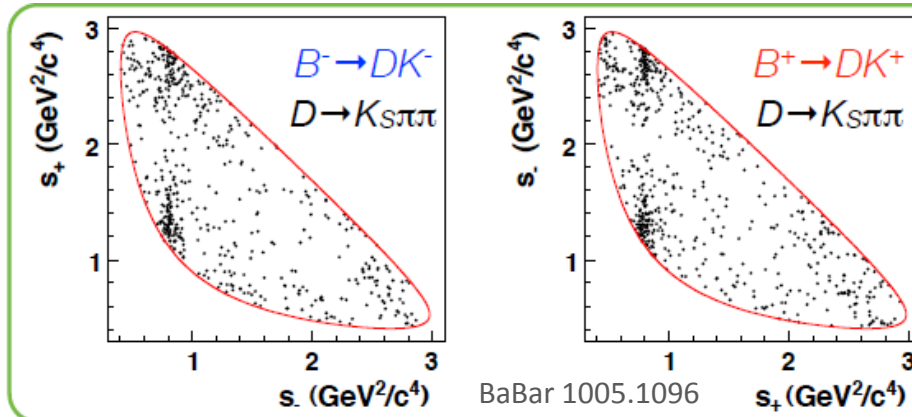
Still dominated by statistical error.

Improved model and much reduced model error from BaBar: 3 degrees.

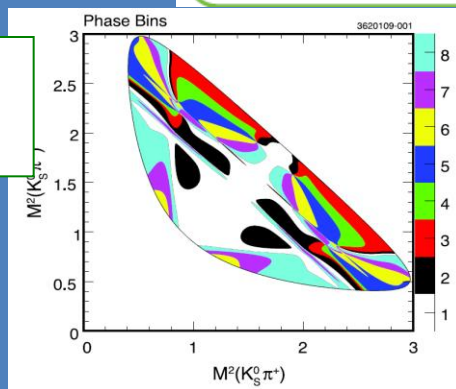
Still model error hard to quantify .Will limit the precision of future high-statistics measurements using this method

From “classic” to “modern” art: model independent methods

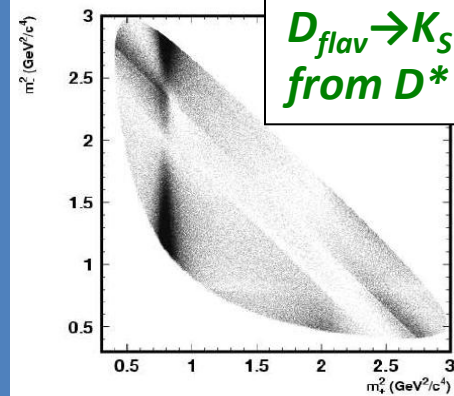
[GGSZ, PRD 68(2003)054018,
Bondar&Poluektov, EPJ C 47(2006)
347, EPJ C55 (2008) 51]



CLEO-c
Binned δ_D



+



$D_{flav} \rightarrow K_S \pi \pi$
from $D^* \rightarrow D \pi$

Binned fit, no model assumptions: uses instead external binned information on δ_D from CLEO-c

CLEO-c results on δ_D

First successes: $K_S\pi\pi$ and $K_S KK$

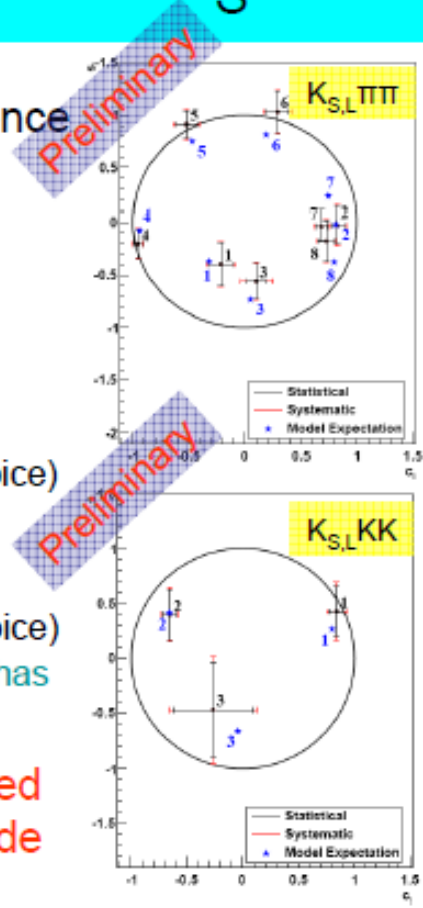
CLEO-c has measured the strong phase difference of D^0 decays to $K_{S,L}\pi\pi$ and $K_{S,L}KK$ in bins of expected strong phase

Toy studies estimate uncertainty on potential measurement of γ/ϕ_3 at LHCb from CLEO-c precision:

$K_{S,L}\pi\pi$: 1.7-3.9° systematic (varies with bin choice)
 Estimated LHCb statistical uncertainties:
 ~15.0° with 2 fb⁻¹, ~7° with 10 fb⁻¹

$K_{S,L}KK$: 3.1-4.5° systematic (varies with bin choice)
 BaBar arXiv:1005.1096 [hep-ex] indicates that $K_S KK$ has the same per-event sensitivity as $K_S\pi\pi$

Current precision sufficient for LHCb, but improved BESIII precision needed for Belle II/LHCb Upgrade
 Belle II predicts 2° with 50 ab⁻¹ of $K_S\pi\pi$



CLEO-c: See talk by Stefania Ricciardi

Results from well-established methods – Part II

I. Time-integrated methods

II. Time-dependent methods

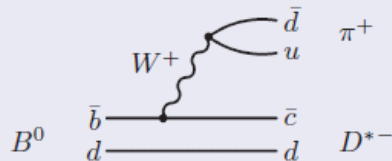
Sensitive to $\sin(2\beta_{(s)} + \gamma)$ via interference in decay w and w/o mixing.

More results from B-factories...

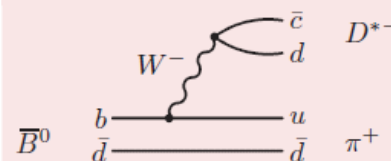
Time-dependent at BaBar

- Comprehensive review
- One on-going analysis $B^0 \rightarrow D^{0(*)} K_s$
- Several published measurements (to be updated to full data sample)
 - 1) Partial Reconstruction of B to $D^{*+} \pi^-$ (BaBar, PRD, 2005)
 - 2) Full Reconstruction of B to $D^{(*)+} \pi^-$ and $D^+ \rho^-$ (BaBar, PRD, 2006)
 - 3) Dalitz plot analysis of $B^0 \rightarrow D^+ K^0 \pi^-$ (BaBar, PRD, 2008)

Favored: $V_{cb} \approx 0.04$



Suppressed: $V_{ub} \approx 0.004$



Extraction of $\sin(2\beta+\gamma)$ from 2) and 3) requires external constraint on r = ratio of suppressed over favoured amplitude (very small)

$$r = \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{*+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+)}} \frac{f_{D_s^*}}{f_{D^{*-}}} \tan(\theta_C) \Rightarrow 0.015_{-0.006}^{+0.004} + 30\%$$

- 30% systematic to account from SU(3) breaking and factorization

Time-dependent: Belle

- Two recent results for $R_{D^*\pi}$
 - Using isospin relations (Belle, PRL 2008)

$$R_{D^*\pi} = \sqrt{\frac{\tau_{B^0} 2\mathcal{B}(B^+ \rightarrow D^{*+} \pi^0)}{\tau_{B^+} \mathcal{B}(B^0 \rightarrow D^{*-} \pi^+)}}$$

$$R_{D^*\pi} < 0.051 (90\% \text{ C.L.})$$

Dominated by statistical error on $\mathcal{B}(B \rightarrow D^*\pi^0)$ (UL)

- Using SU(3) flavour symmetry assumptions

$$R_{D^*\pi} = \tan\theta_c \left(\frac{f_{D^*}}{f_{D_s^*}} \right) \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{*+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+)}}$$

$$R_{D^*\pi} = 1.58 \pm 0.15 \pm 0.10 \pm 0.03\%$$

stat. syst. th. error

PRD81(2010)031101

$$R_{D\pi} = 1.71 \pm 0.11 \pm 0.09 \pm 0.02\%$$

stat. syst. th. error

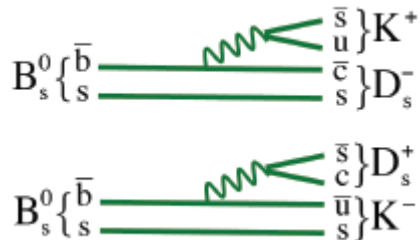
arXiv:1007.34619

NEW

Most precise determinations but possible non-factorizable SU(3) breaking effects not completely accounted for in theory errors

Time-dependent: $B_s \rightarrow D_s K$ at LHCb

The golden mode is $B_s \rightarrow D_s K$ because of the much larger interference than in the B_d modes

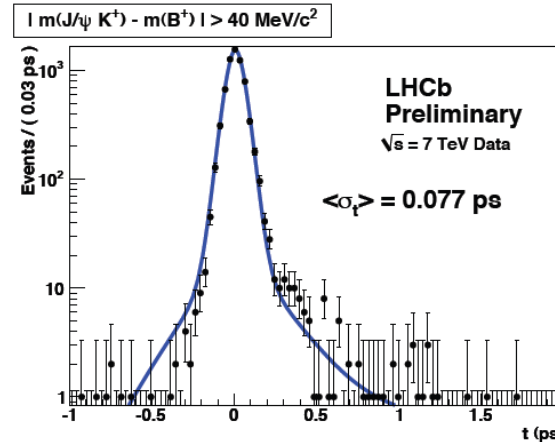


$B_s \rightarrow D_s \pi$ @LHCb²⁰¹¹ ~ 67 k

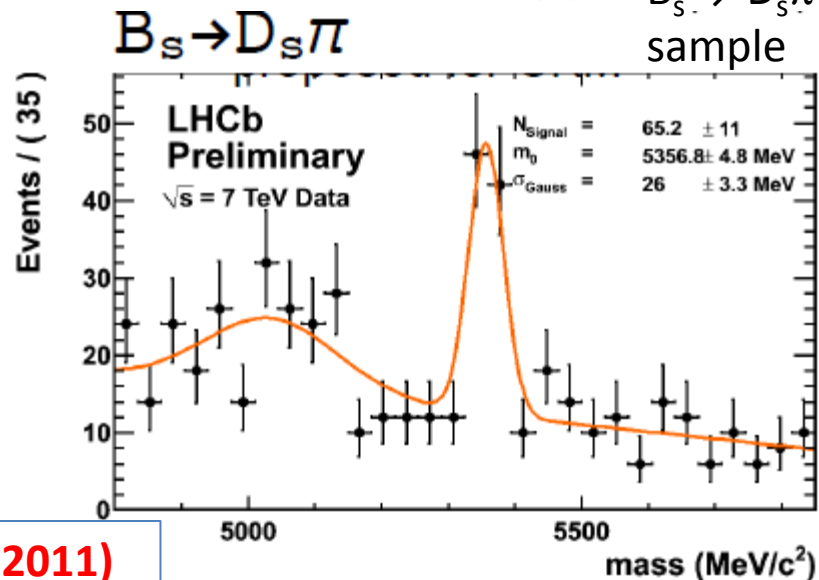
$B_s \rightarrow D_s K$ @LHCb²⁰¹¹ ~ 5.6 k

From MC sensitivity to γ is 10° with 6k $B_s \rightarrow D_s K$: we should not be far off this!

Expect $\sigma_{\text{stat}}(\gamma) \sim 10^\circ$ with 1/fb at LHCb(2011)



Time-dependent
Fast B_s oscillations
Important:
- proper time resolution
- Tagging
Simultaneous fit to $B_s \rightarrow D_s \pi$ control sample



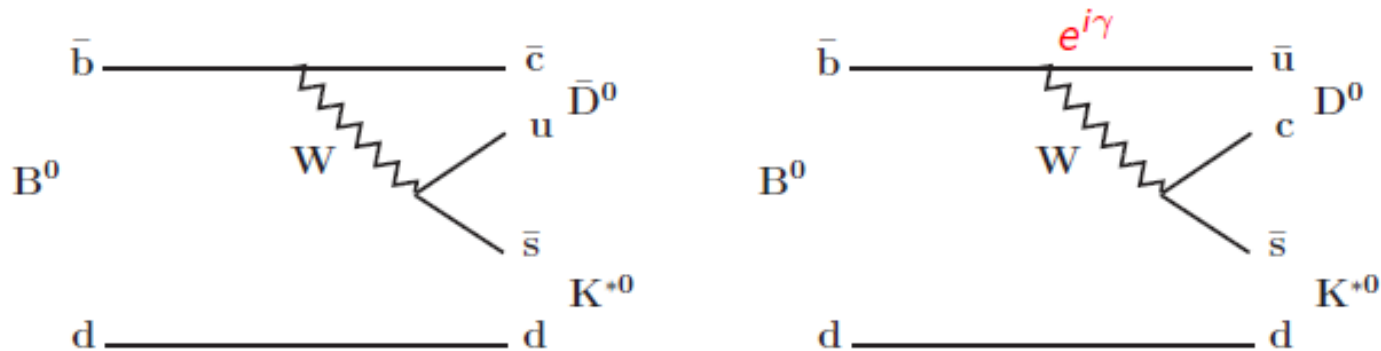
New methods for the measurement of γ

1. $B^0 \rightarrow DK^+\pi^-$
2. $B_s \rightarrow D\phi$
3. $B_s \rightarrow J/\psi\phi$

Reminder: γ from $B^0 \rightarrow D^0 K^{*0}$

Neutral GLW/ADS

The neutral analog of $B^\pm \rightarrow D(hh)K^\pm$, the decays $B^0 \rightarrow D(hh)K^{*0}$, can also be used to determine γ due to the interference b/t amplitudes where the D/\bar{D} decay to the same final state.



- Good: both diagrams are color suppressed ($r_{B^0} \approx 3 \times r_{B^\pm}$); increased interference increases the sensitivity on γ .
- Bad: the K^* interferes w/ the $B \rightarrow DK\pi$ background; effective hadronic parameters must be introduced (reduces sensitivity).

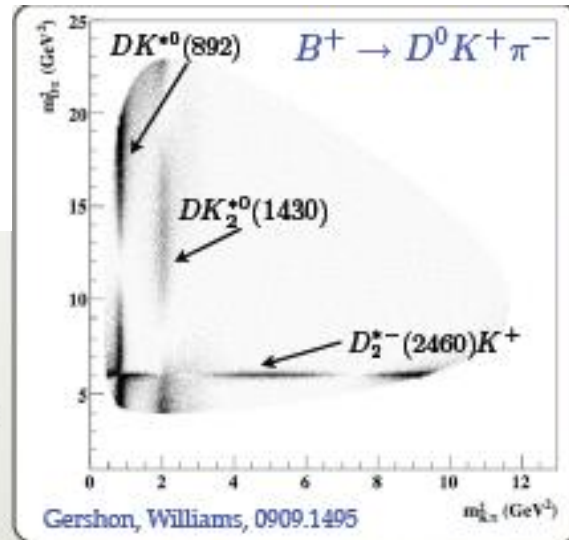
Another powerful Dalitz plot analysis

$B^0 \rightarrow DK^+\pi^-$ and prospects at LHCb

Exploits resonance structure in the Dalitz plot from the self-tagged B^0 multibody decay

- contains flavor specific $D_2^{*-}(2460) \rightarrow \bar{D}^0 \pi^-$
- interf. with other resonances (e.g. $B^0 \rightarrow DK^{*0}$) gives γ
- many choices for $D \rightarrow f$ still
- equivalent of GLW does not need CP-odd $D \rightarrow K_S \pi^0$ decays (that is difficult for LHCb)

J. Zupan The case for measuring gamma... 5



Gershon,2008

Gershon and Williams, 2009

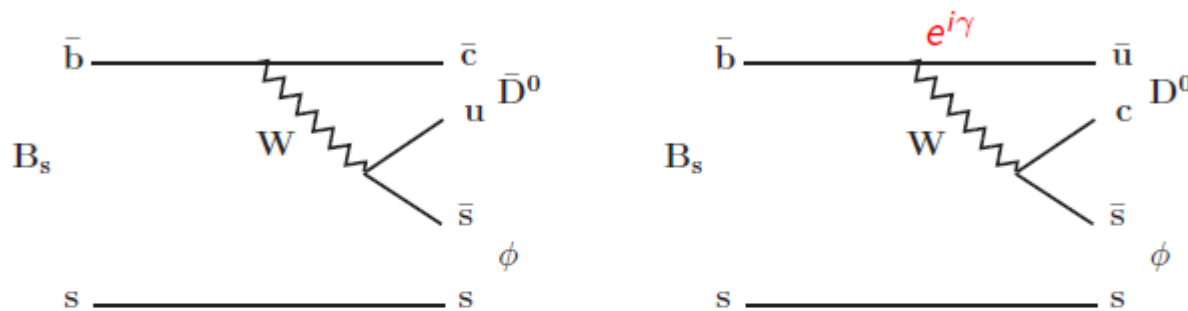
Gershon and Poluektov,2009

Expect $\sigma_{\text{stat}}(\gamma) \sim 11^\circ$ with 1/fb at LHCb(2011)

Estimated with assumptions on the DP model to be assessed on early LHCb data [measure branching ratios of main resonance components]

Exploiting B_s production at LHCb: γ from $B_s \rightarrow D\phi$ (untagged)

The strange analog of $B^0 \rightarrow DK^{*0}$, the decays $B_s \rightarrow D\phi$, can also be used to determine γ using the GLW/ADS method.



Large CP asymmetry, very small background

Expected yields in 1 fb^{-1} @ 7 TeV (2011 running)

$B_s + \bar{B}_s \rightarrow D_{\text{fav}}\phi$	$B_s + \bar{B}_s \rightarrow D(K3\pi)\phi$	$B_s + \bar{B}_s \rightarrow D_{CP+}\phi$
~ 200	~ 200	~ 25

Expect $\sigma_\gamma \sim 17^\circ$ (see CERN-LHCB-PUB-2010-005)

Including $\Delta\Gamma_s$ corrections (from Zupan)

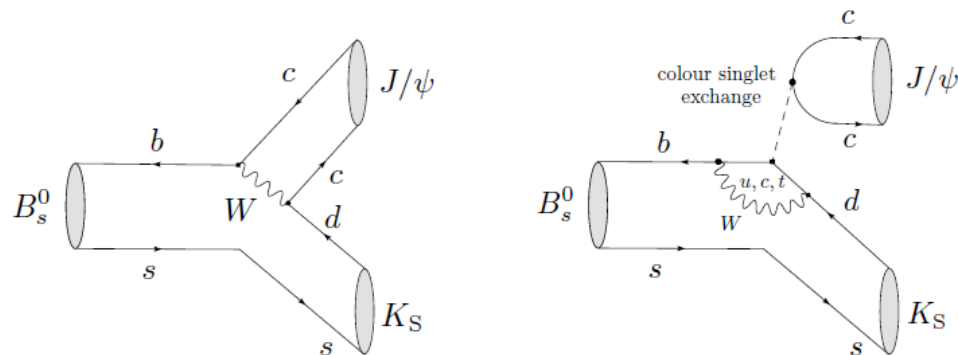
Another decay with a promising physics potential: $B_s \rightarrow J/\psi K_S$ (time-dependent)

[R.F., Eur. Phys. J. C 10 (1999) 299 [arXiv:hep-ph/9903455]]

U-spin partner of the “golden”
 $B_d \rightarrow J/\psi K_S$

Sensitivity to γ from interference
 between tree and penguin
 (suppressed for B_d but not for B_s)

With assumption on U-spin
 flavour symmetry
 γ and penguin decay parameters
 (a, θ) can be extracted



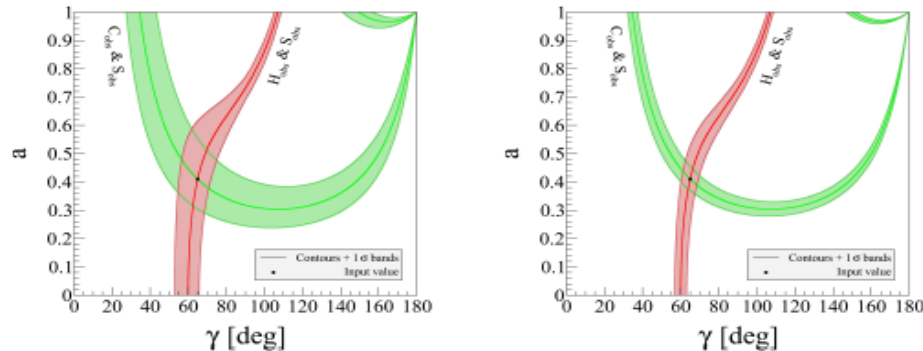
$$A(B_s^0 \rightarrow J/\psi K_S) = -\lambda \mathcal{A} [1 - a e^{i\theta} e^{i\gamma}]$$

$$\mathcal{A} \equiv \lambda^2 A [A_T^{(c)} + A_P^{(c)} - A_P^{(t)}], \quad a e^{i\theta} \equiv R_b \left[\frac{A_P^{(u)} - A_P^{(t)}}{A_T^{(c)} + A_P^{(c)} - A_P^{(t)}} \right]$$

$$A \equiv |V_{cb}|/\lambda^2, \quad R_b \equiv \left(1 - \frac{\lambda^2}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right|$$

$B_s \rightarrow J/\psi K_S$: feasibility studies at LHCb

Contours in the γ - a plane: [6 fb^{-1} and 50 fb^{-1}]



R.Fleischer in collaboration
with P.Koppenburg
and K. De Bruyn

Numerical results: [only statistical sensitivity]

$$6 \text{ fb}^{-1} : \quad \gamma = (65.0 \pm 7.4)^\circ, \quad a = 0.410 \pm 0.060, \quad \theta = (194 \pm 13)^\circ,$$

$$50 \text{ fb}^{-1} : \quad \gamma = (65.0 \pm 3.3)^\circ, \quad a = 0.410 \pm 0.024, \quad \theta = (194.0 \pm 4.3)^\circ.$$

Our LHCb feasibility study shows:

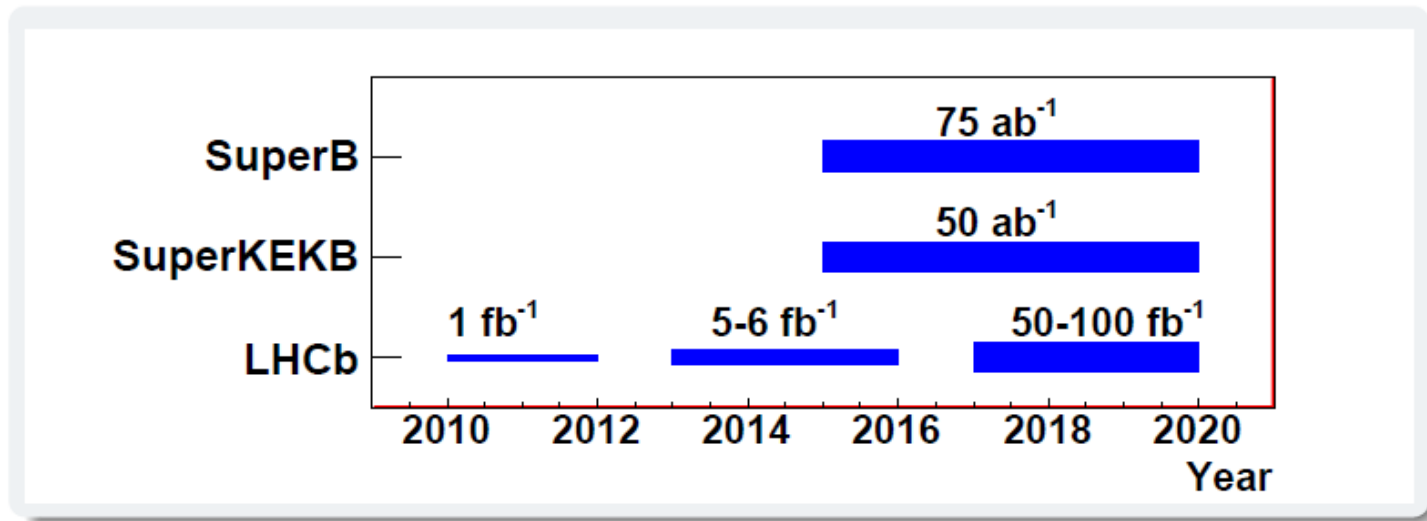
- The $B_{s,d} \rightarrow J/\psi K_S$ strategy offers another extraction of γ .
- The major application will be the control of the penguin effects in $(\sin 2\beta)_{J/\psi K_S}$, which will allow us to match the experimental precision:

→ may eventually allow us to resolve NP in $B_d^0 - \bar{B}_d^0$ mixing.



Visions for the next decade and beyond

Comparison on experimental reach



LHCb:

20×10^{12} produced $B\bar{B}$ pairs
 detection efficiency $< 1\%$.
 B/S typically $O(1)$

SuperB:

50×10^9 produced $B\bar{B}$ pairs
 detection efficiency $O(100\%)$
 clean signals

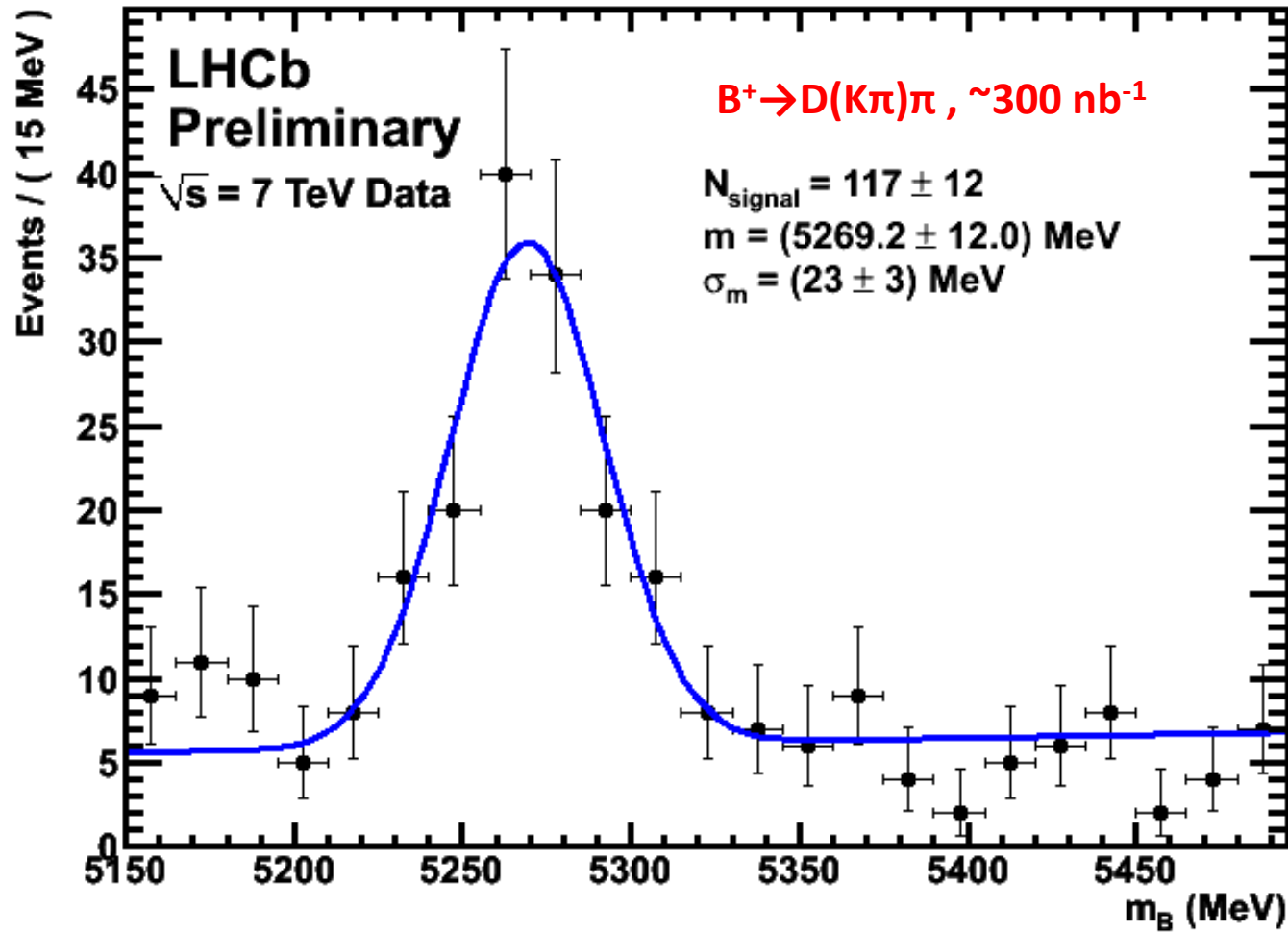
'Super- γ ' (~ 2020 AD)

- Various independent methods should allow for $\sim 1 - 3^\circ$ measurement with SuperB and upgraded LHCb:
 - ADS + GLW modes
 - $B \rightarrow D(K_S \pi \pi)K$ Dalitz analysis
 - Self-tagging $B^0 \rightarrow DK\pi$ modes
 - $B_s \rightarrow D_s K$ (LHCb only)
- Overall, LHCb sensitivity with 50 fb^{-1} potentially looks better than that of SuperB, but higher backgrounds can reduce it. SuperB is more stable against "unlucky" parameter combinations when the sensitivity can be significantly reduced.
- Having a large ($\sim 10\text{-}20 \text{ fb}^{-1}$) sample at charm threshold is desirable for an efficient use of B data:
 - Significant fraction of BES-III sample.
 - Dedicated charm-tau factory.
 - SuperB operated at low energy.

Back to near future: 2010-2012

By 2012 (next CKM?) expect to hear new exciting results on γ from B to charm decays from experiments at *hadron colliders*:

- CDF has demonstrated capability of hadron colliders with B to charm decays
- New ADS/GLW results (5/fb) results competitive with B-factories
- Exploration continues, double data-set by 2011 (Expect 10-12/fb)
- LHCb expects $\sigma(\gamma) < 10^0$ degrees by end 2011, several promising measurements ($\sim 1/\text{fb}$ at 7TeV)
- Excellent tracking, PID and trigger performance for these multi-hadron decay modes demonstrated with $< 1/\text{pb}$ of data collected and analysed this summer



Similar significance expected for the “suppressed” ADS mode ($B \rightarrow DK$) at LHCb with 3 order of magnitude larger data sample by the end of 2011

Acknowledgements

Many other new results presented in these sessions. Apologies, could not show them all!

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