



# $B \rightarrow X_{s/d} \gamma$ & $B \rightarrow X_{s/d} l^+l^-$

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(on behalf of the BaBar Collaboration)



**Outlook:**

- $B \rightarrow X_{s/d} \gamma$  :

**Motivations**

$X_s \gamma$  (Belle), Acp ( $X_{s+d} \gamma$ ) (BaBar),  $|V_{td}/V_{ts}|$  (BaBar)

**Spectral Moments**

- $B \rightarrow X_{s/d} l^+l^-$  :

**Motivations**

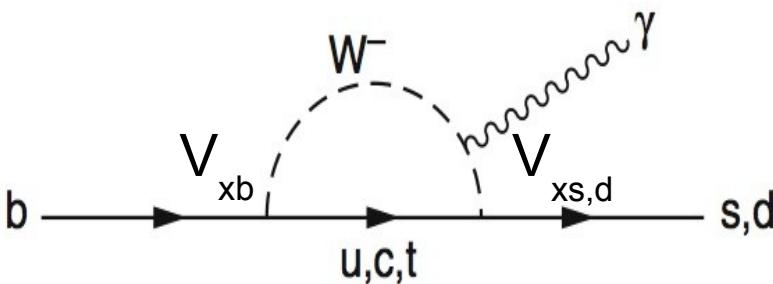
$K^{(*)} l^+l^-$  (Belle),  $K^{(*)} \mu^+\mu^-$  (CDF),  $K^+ \tau^+\tau^-$  (BaBar)

$\pi l^+l^-$

- **Conclusions**



# $B \rightarrow X_{s/d} \gamma$ : Motivations



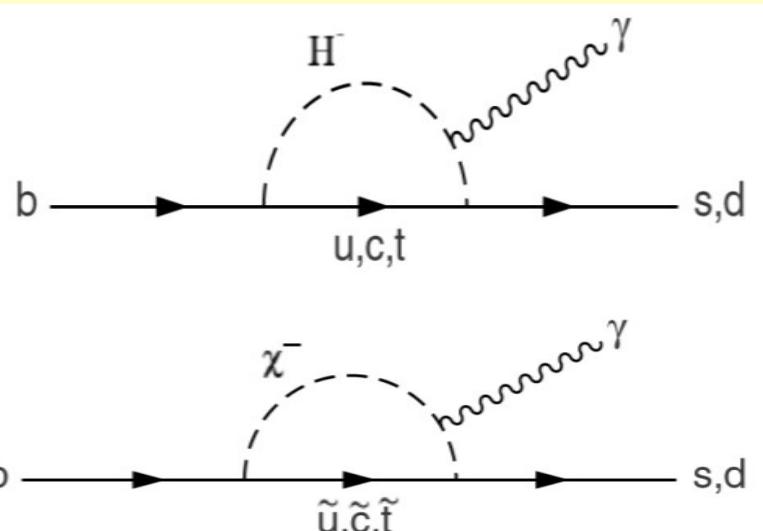
FCNC process forbidden at tree level:  
Probe the SM!

NNLL order  $\text{BR}(b \rightarrow s\gamma)_{(E^*\gamma > 1.6 \text{ GeV})} = (3.15 \pm 0.23) * 10^{-4}$   
(Misiak et al. PRL 98 022002)

## Search for New Physics

New heavy particles in the loop  
could:

- Modify BR wrt SM prediction
- Modify Direct  $A_{CP}$



**Radiative  
Penguins are  
an Excellent  
Laboratory to**

Study the dynamics  
of b-quark inside B  
mesons

- Provide inputs to Global Fits in the Kinetic scheme to  $V_{cb}$ ,  $V_{ub}$  & Heavy Quark Expansion parameters.

Measure  $|V_{td}/V_{ts}|$  from

- $\text{BR}(b \rightarrow d\gamma)/\text{BR}(b \rightarrow s\gamma)$
- NP could affect in different way  $X_s \gamma$  vs  $X_d \gamma$  final states

# $B \rightarrow X_{s/d} \gamma$ Measurements

## Exclusive Measurements

- Experimentally easier, reconstruct resonances ( $K^*\gamma$ ,  $\rho(\omega)\gamma$ ) with low Background
- Need Form Factors, modeling  $X_s$  fragmentation
- Affected by large theoretical uncertainties ( $\delta|V_{td}/V_{ts}| \sim 7\%$ )

VS

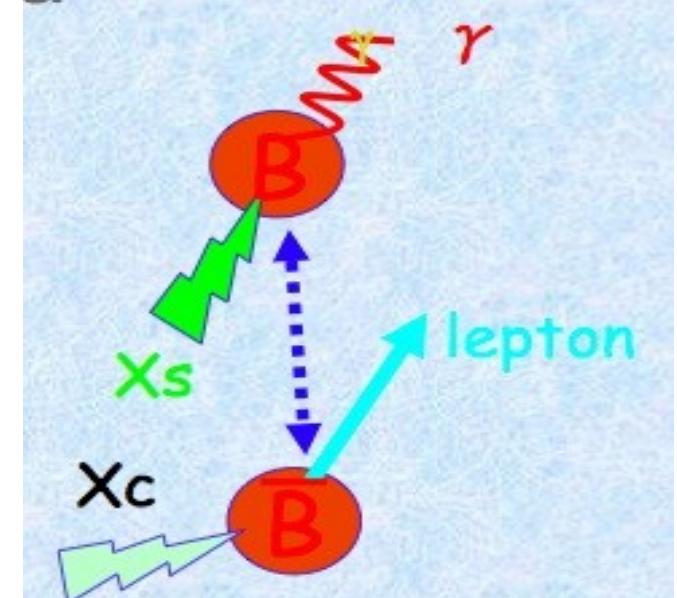
## Inclusive Measurements

- Smaller theoretical error exploiting quark-hadron duality (small hadronization effects)
- Experimentally harder, large background

## Recent Analyses Strategies:

Make the measurement **as inclusive as possible**, suppressing backgrounds via:

- Cut on  $E_\gamma > [1.7-2.0] \text{ GeV}$
- Use recoil of reconstructed B or Lepton Tag  
**OR**
- Combined cut on  $E_\gamma, M(X_{s/d}) < [1.8-2.0] \text{ GeV}$
- Sum over many exclusive modes



# Belle Inclusive $B \rightarrow X_s \gamma$ (605 fb<sup>-1</sup>)

PRL 103, 241801

## •B-Meson Not Reconstructed: Not distinguish $X_s$ & $X_d$ !

- Select High Energy Isolated  $\gamma$   
 $E_\gamma(B_{CM}) > 1.7$  GeV

Lowest threshold up to now, covered  
97% of  $X_s$  spectrum, smallest model  
uncertainty

- $\pi^0/\eta$  suppressed exploiting  $m_{\gamma\gamma}$ ,  
shower profile,  $E_\gamma$ ,  $\theta_\gamma$
- Bhabha events overlapped with B  
decays removed using timing  
information

- Dominant Background from Continuum suppressed by means of two  
different analysis streams (largely statistically uncorrelated) based on:

- Lepton Tag:  
(1.26 GeV <  $P_{lept}^*$  < 2.20 GeV)

- Two Fisher discriminants exploiting  
Energy Flow & Event Shape

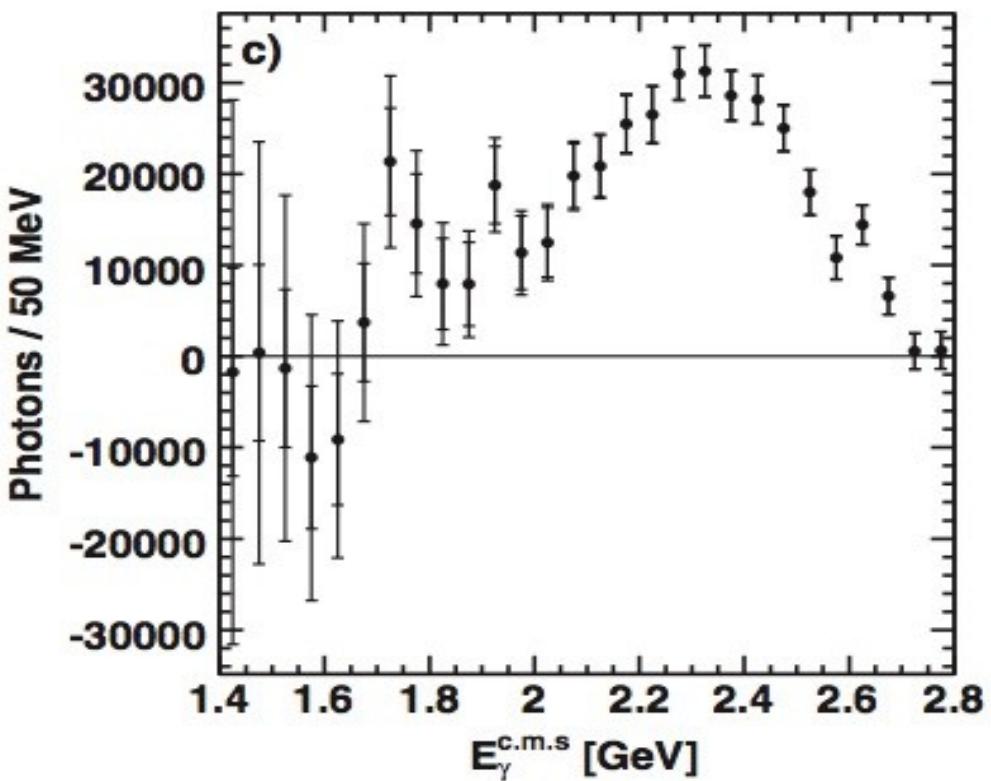
- Residual amount subtracted using off-resonance Data (corrected for Energy  
effects)

- $B\bar{B}$  Background from  $\pi^0/\eta$  decays estimated using Data-Corrected MC  
samples and subtracted

- BKG Subtraction checked in control regions  $E_\gamma(Y_{CM}) < 1.7$  GeV (> 2.8 GeV)  
for  $B\bar{B}$  (Continuum): No bias found

# Belle Inclusive $B \rightarrow X_s \gamma$ (605 fb $^{-1}$ )

PRL 103, 241801



$E_\gamma$ Cut (GeV)	$\text{BR}(B \rightarrow X_s \gamma) (10^{-4})$
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1.7	$3.45 \pm 0.15 \pm 0.40$
-----	--------------------------

2.0	$3.02 \pm 0.10 \pm 0.11$
-----	--------------------------

- True Spectrum obtained by means of efficiency correction & unfolding procedure
- $X_d$  contribution subtracted assuming  $\text{BR}(X_d)/\text{BR}(X_s) = 4.5\%$   
[Hurth et al., Nucl. Phys. B704 56, Charles et al., Eur. Phys. C41 1]

To date:

- Lowest  $E_\gamma$  threshold, lowest theory error**
- Most Precise Result lowest systematic error**

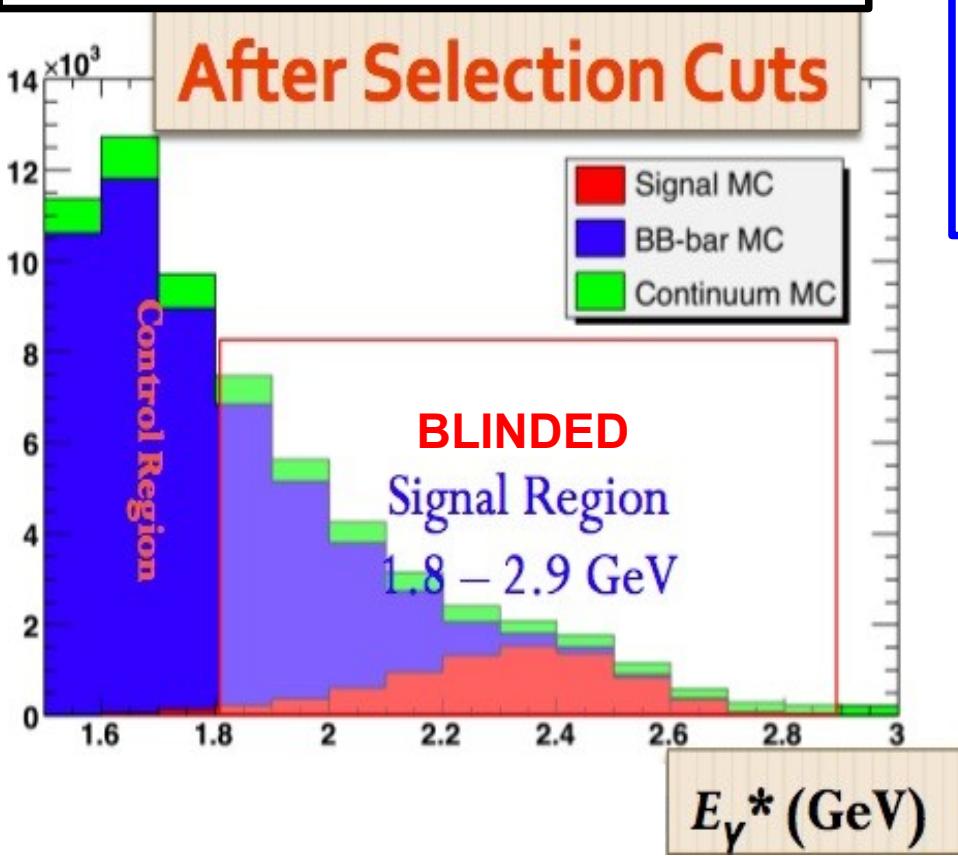
- Systematics dominated by Continuum &  $\bar{B}B$  BKG subtraction

# BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag ( $347 \text{ fb}^{-1}$ )

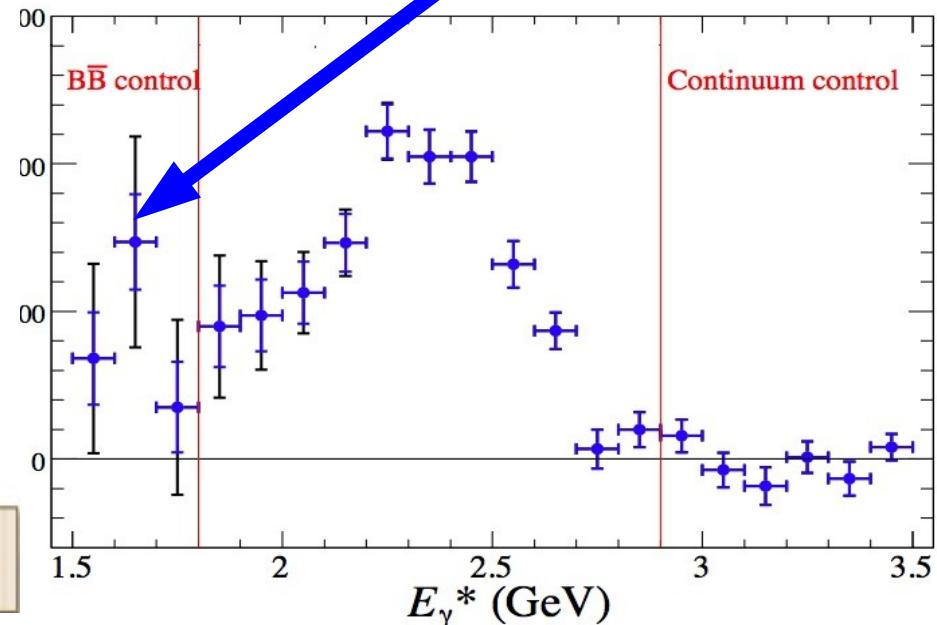
PRELIMINARY

## Similar to Lepton-Tag Belle Analysis:

- Continuum suppressed using Lepton-Tag & Neural Network (Event Shape,  $P^*$ <sub>lept</sub>,  $\theta_{\gamma\text{-lept}}$ )



- $\bar{B}\bar{B}$  Background Estimated on MC & corrected on DATA control samples (97% of BKG yield:  $\pi^0/\eta$ ,  $\omega$ ,  $e, \dots$ )
- Background subtraction test:  $1.4\sigma$  bias found in the  $\bar{B}\bar{B}$  control region, partly due to a tail of 100-400 signal events (depending on model)



# BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag ( $347 \text{ fb}^{-1}$ )

$$A_{CP}(B \rightarrow X_q \gamma) = \frac{\Gamma(\bar{B} \rightarrow X_q \gamma) - \Gamma(B \rightarrow X_{\bar{q}} \gamma)}{\Gamma(\bar{B} \rightarrow X_q \gamma) + \Gamma(B \rightarrow X_{\bar{q}} \gamma)}$$

Experimentally:

$$A_{CP}(B \rightarrow X_{s+d} \gamma) = \frac{1}{1 - 2\omega} \cdot \frac{N^+ - N^-}{N^+ + N^-}$$

Lepton Charge gives B flavor

- Dilution due to mixing, cascade decays, fakes,  $\omega \sim 13\%$

- Most of the systematics common for +/- leptons cancel in  $A_{CP}$

Possible Bias from:

- $B\bar{B}$  Background asymmetry: checked in control region ( $-0.004 \pm 0.006$  effect)
- Lepton tag asymmetry =  $0.011 \pm 0.011$  measured in DATA control samples ( $e^+e^-$ ,  $\mu^+\mu^-\gamma$ ,  $K^*J/\Psi(l^+l^-)$ )
- Estimated error  $\pm 0.013$  (Main systematic uncertainty)

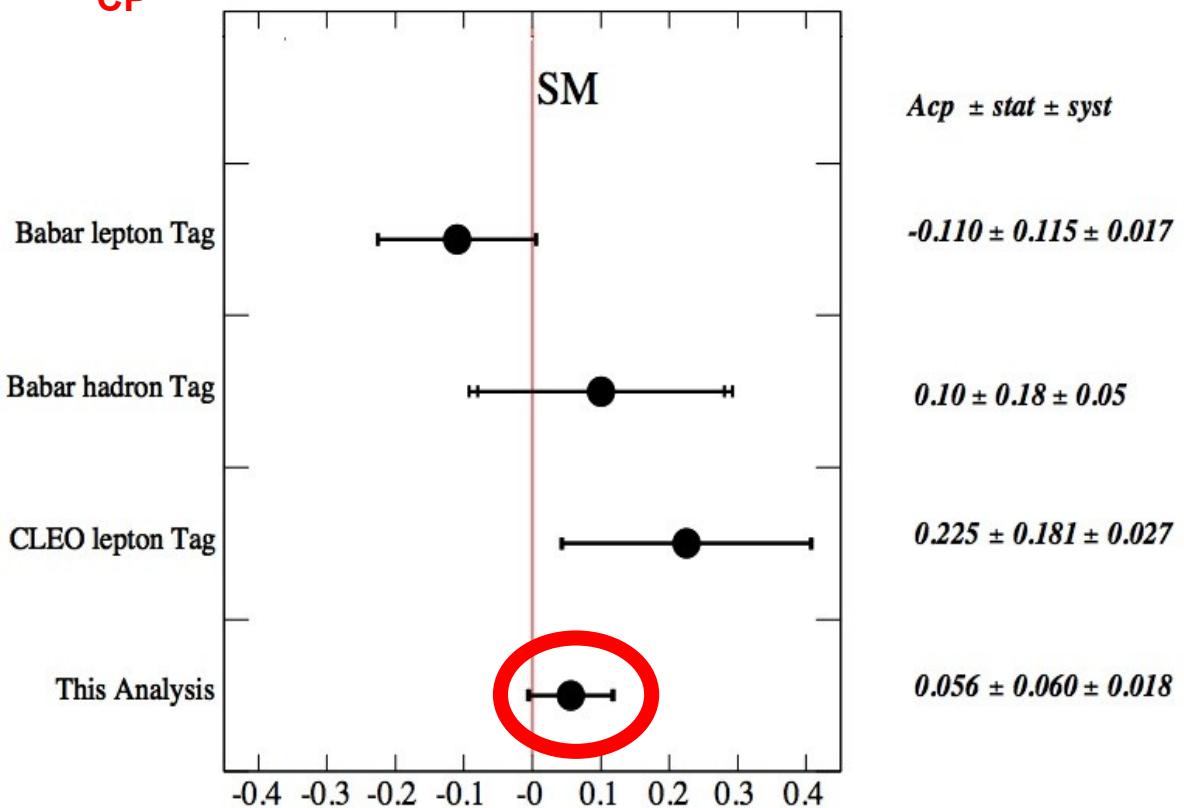
# BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag ( $347 \text{ fb}^{-1}$ )

## Preliminary Result

$$N(l^+) = 2623 \pm 158$$

$$N(l^-) = 2397 \pm 151$$

$$A_{CP} = 0.056 \pm 0.060(\text{stat}) \pm 0.018(\text{syst})$$



- $A_{CP}$  total error minimized with  $2.1 \text{ GeV} < E_\gamma (\text{Y}_{CM}) < 2.8 \text{ GeV}$

- Statistical error dominated by continuum subtraction

- Most precise measurement to date
- Consistent with SM expectation

Same analysis will soon provide BR and spectral moments.

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

[PRD-RC 82, 051101]

- Ratio of Exclusive modes  $B \rightarrow (\rho, \omega)\gamma$ ,  $K^*\gamma$  provides a  $|V_{td}/V_{ts}|$  measurement complementary to the more precise result from  $\Delta m_d/\Delta m_s$

- New Physics could affect  $b \rightarrow s\gamma/d\gamma$  in different way

**Inclusive Measurements reduce theory error from 7% to ~1%**

## Experimentally:

- Inclusive rates extrapolated from a sum of 7 exclusive modes:

$B \rightarrow X_d\gamma$	$B \rightarrow X_s\gamma$
$B^0 \rightarrow \pi^+ \pi^- \gamma$	$B^0 \rightarrow K^+ \pi^- \gamma$
$B^+ \rightarrow \pi^+ \pi^0 \gamma$	$B^+ \rightarrow K^+ \pi^0 \gamma$
$B^+ \rightarrow \pi^+ \pi^- \pi^+ \gamma$	$B^+ \rightarrow K^+ \pi^+ \pi^- \gamma$
$B^0 \rightarrow \pi^+ \pi^- \pi^0 \gamma$	$B^0 \rightarrow K^+ \pi^- \pi^0 \gamma$
$B^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^- \gamma$	$B^0 \rightarrow K^+ \pi^- \pi^+ \pi^- \gamma$
$B^+ \rightarrow \pi^+ \pi^- \pi^+ \pi^0 \gamma$	$B^+ \rightarrow K^+ \pi^- \pi^+ \pi^0 \gamma$
$B^+ \rightarrow \pi^+ \eta \gamma$	$B^+ \rightarrow K^+ \eta \gamma$

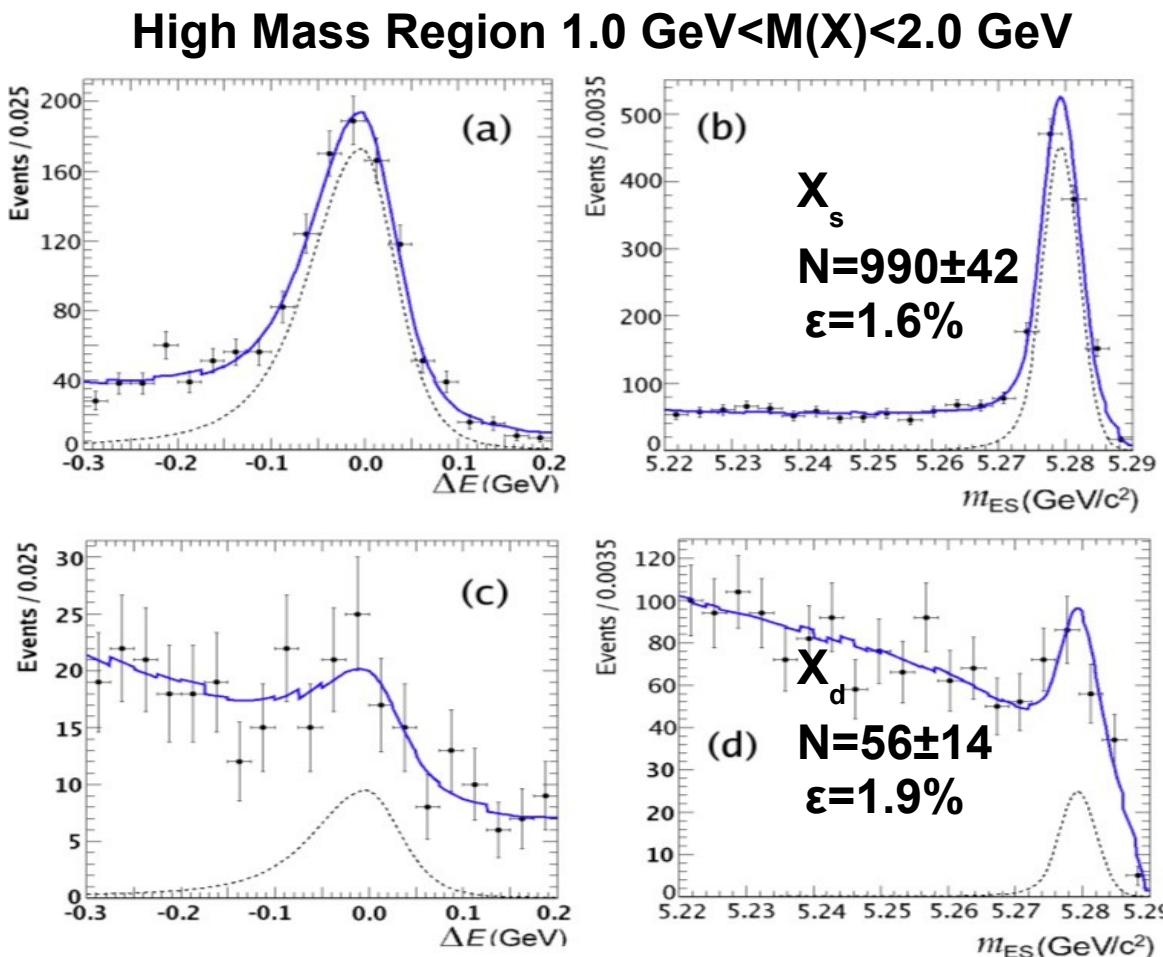
Add estimated missing states using Jetset  $X_{s/d}$  fragmentation models corrected for measured exclusive  $X_s$  BRs [PRD 72, 052005]

## Use two hadronic mass bins:

- $0.5\text{GeV} < M(X) < 1.0\text{GeV}$  (contains the previously measured  $K^*$ ,  $\rho, \omega$  states)
- $1.0\text{GeV} < M(X) < 2.0\text{GeV}$

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

- Select High Energy Isolated  $\gamma$
- $\pi^0/\eta$  suppression by  $m_{\gamma\gamma}$  cut
- Same cuts to  $s\gamma/d\gamma$  final states reduce systematics in the BR ratio
- Continuum suppressed using Neural Network (event shape)



- Yields from Simultaneous Fit to

$$\Delta E = E_B^* - E_{\text{beam}}$$

$$m_{\text{ES}} = \sqrt{E_{\text{beam}}^{*2} - \vec{p}_B^{*2}}$$

**$0.5 \text{ GeV} < M_{\text{HAD}} < 2.0 \text{ GeV}$**

**BR( $b \rightarrow s\gamma$ ) =  $230 \pm 8 \pm 30 \times 10^{-6}$**

**BR( $b \rightarrow d\gamma$ ) =  $9.2 \pm 2.0 \pm 2.3 \times 10^{-6}$**

**First high  $M_{\text{HAD}}$  measurement**

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

- Extract  $|V_{td}/V_{ts}|$  from:

$$\frac{\Gamma(b \rightarrow d\gamma)}{\Gamma(b \rightarrow s\gamma)} = \xi^2 \left| \frac{V_{td}}{V_{ts}} \right|^2 (1 + \Delta R)$$

[Ali et al. Phys. Lett. B 429, 87]

- Unmeasured  $M(X) > 2.0$  GeV extrapolated using Kagan-Neubert spectral shape

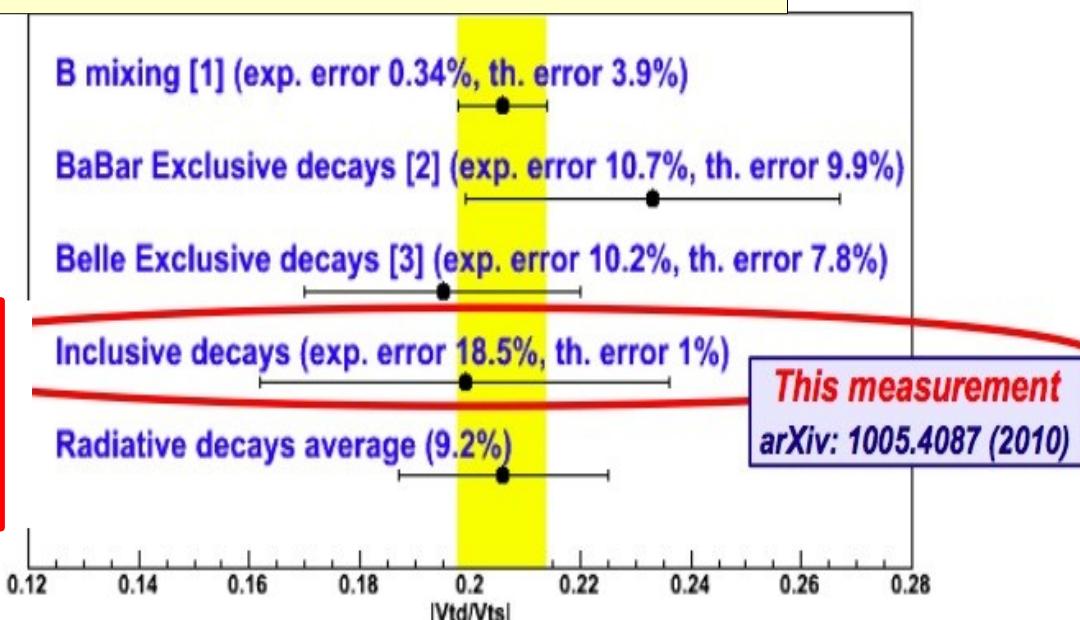
[PRD 58, 094012]

$$|V_{td}/V_{ts}| = 0.199 \pm 0.022(\text{stat}) \pm 0.024(\text{syst}) \pm 0.002(\text{th})$$

- Systematics dominated by Extrapolation to Inclusive Rates (alternative fragmentation models)

- Compatible & Competitive with Previous exclusive decay results (with lower theory error) !

- $\xi$ (SU(3) Breaking),  $\Delta R$ (annihilation correction) computed in terms of Wolfenstein parameters ( $\rho, \eta$ )
- ( $\rho, \eta$ ) re-expressed in terms of angle  $\beta$  to avoid circularity from previous  $|V_{td}/V_{ts}|$  measurements



# $\text{BR}(\text{B} \rightarrow \text{X}_s \gamma)$ : Summary

- Experiments cut on minimum  $E_\gamma$
- BR extrapolated to  $E_{\min} = 1.6 \text{ GeV}$  using Shape Functions (correlated error)
- Error dominated by Systematics

**HFAG 2010 Inclusive  $\text{BR}(\text{b} \rightarrow \text{s}\gamma) \times 10^{-6}$ :**

Mode	$\mathcal{B}$	$E_{\min}$	$\mathcal{B}(E_\gamma > E_{\min})$	$\mathcal{B}^{\text{env}}(E_\gamma > 1.6)$
CLEO Inc. [3]	$321 \pm 43 \pm 27^{+18}_{-10}$	2.0	$306 \pm 41 \pm 26$	$327 \pm 44 \pm 28 \pm 6$
Belle Semi.[4]	$336 \pm 53 \pm 42^{+50}_{-54}$	2.24	—	$369 \pm 58 \pm 46^{+56}_{-60}$
BABAR Semi.[6]	$335 \pm 19^{+56+4}_{-41-9}$	1.9	$327 \pm 18^{+55+4}_{-40-9}$	$349 \pm 20^{+59+4}_{-46-3}$
BABAR Inc. [7]	—	1.9	$367 \pm 29 \pm 34 \pm 29$	$390 \pm 31 \pm 47 \pm 4$
BABAR Full [8]	$391 \pm 91 \pm 64$	1.9	$366 \pm 85 \pm 60$	$389 \pm 91 \pm 64 \pm 4$
Belle Inc.[5]	—	1.7	$345 \pm 15 \pm 40$	$347 \pm 15 \pm 40 \pm 1$
Average				$355 \pm 24 \pm 9$

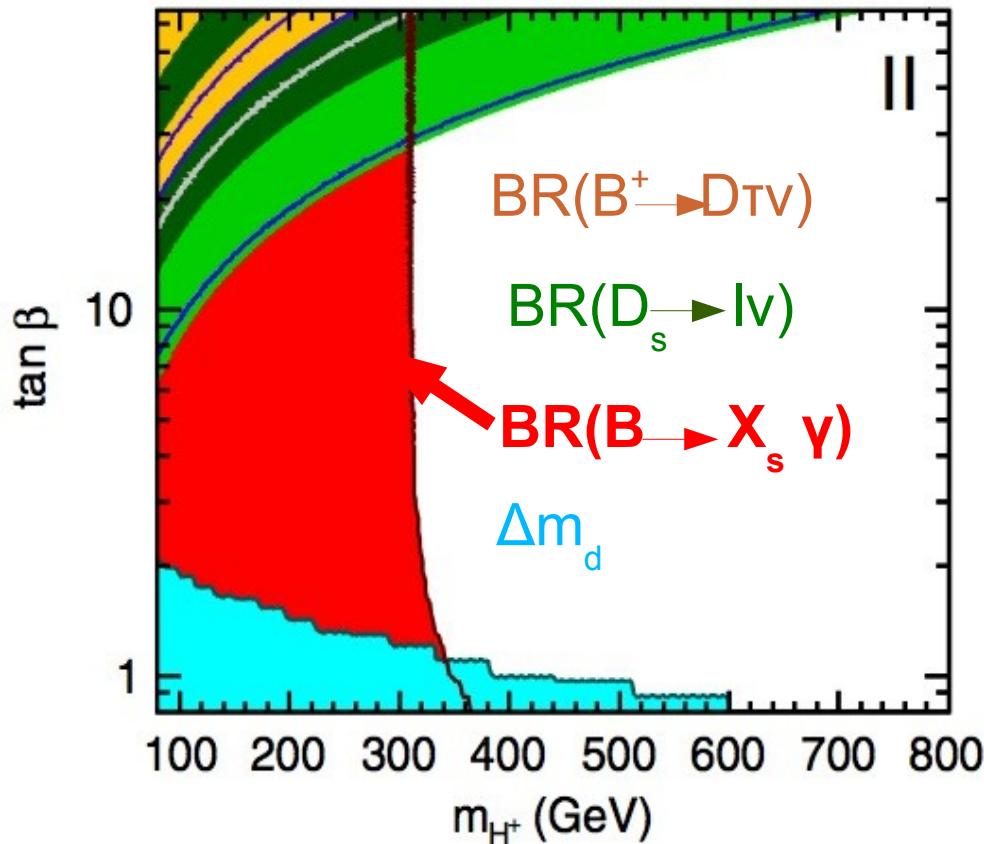
SM:  $\text{BR}(\text{b} \rightarrow \text{s}\gamma)_{(E^*\gamma > 1.6 \text{ GeV})} = (315 \pm 23) \times 10^{-6}$

Misiak et al. PRL 98 022002 (2007)

5% non-perturbative error

**Good Agreement ( $1.2 \sigma$ ) with NNLL prediction**

# $\text{BR}(\text{B} \rightarrow X_s \gamma)$ : Summary



- Recent Calculations in the 2Higgs-Doublet-Model framework provide Constraints on the coupling of the 2<sup>nd</sup> & 3<sup>rd</sup> generation fermions to  $H^+$  obtained from flavor physics experimental results:
- $\text{BR}(\text{B} \rightarrow X_s \gamma)$ ,  $\Delta m_d$ ,  $\text{BR}(\text{B}^+ \rightarrow (\text{D}) \bar{\nu} \nu)$ ,  $\text{BR}(\text{D}_s \rightarrow \ell \bar{\nu})$

• Best Limit on  
 $M_{H^+} > 300 \text{ GeV @ 95% CL}$

[Mahmoudi, Stal, PRD81 035016]

$\tan \beta$ -independent

# $B \rightarrow s\gamma$ Spectral Moments

## $V_{cb}$ & $V_{ub}$ from Inclusive Semileptonic Decays

- $V_{cb}$  from inclusive  $B \rightarrow X_c l\nu$  using HQET & OPE requires non perturbative parameters
- $V_{ub}$  from inclusive  $B \rightarrow X_u l\nu$  requires Shape functions to extrapolate the Inclusive BR from Partial Rates & compute kinematic acceptances

## Universal motion of b-quark inside B meson:

- Global Fits to the moments of inclusive distributions in  $B \rightarrow X_c l\nu$  &  $B \rightarrow X_s \gamma$  in the kinetic mass scheme provide  $V_{cb}$  together with non-perturbative parameters ( $m_b$ , kinetic expectation value  $\mu_\pi^2$ )

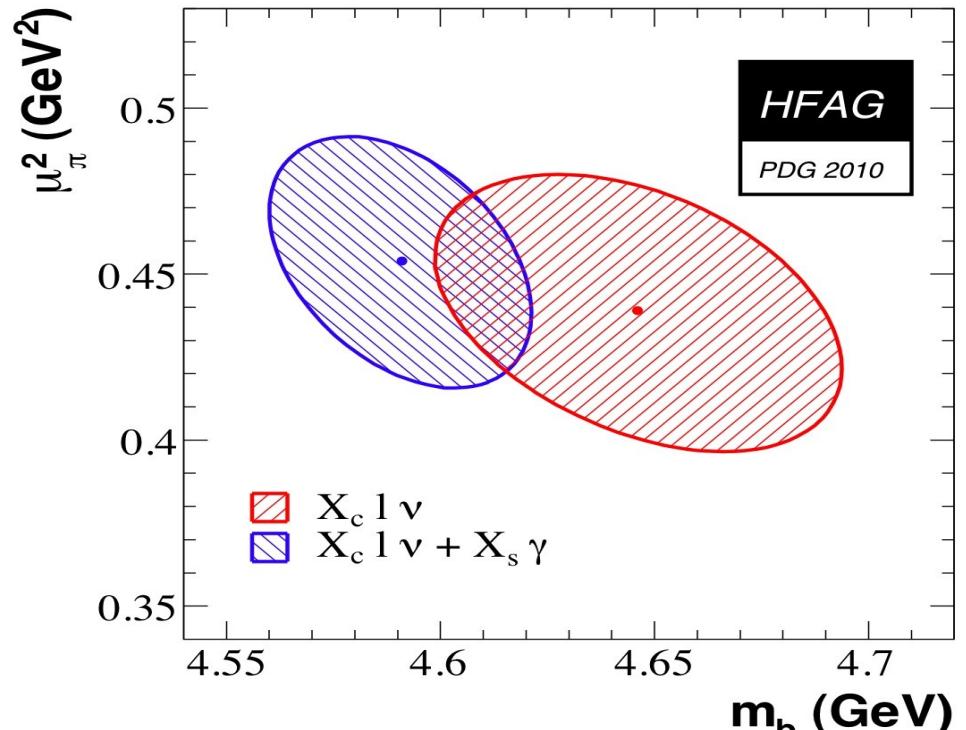
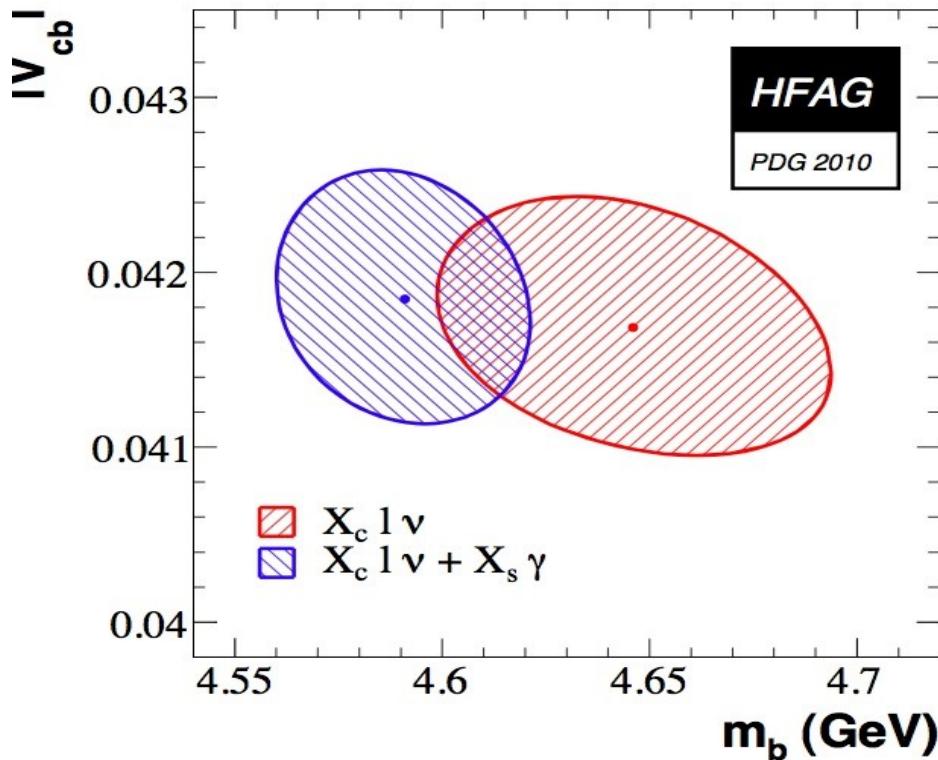
[Gambino et al., Eur. Phys. C34 181-189;  
Benson et al., Nucl Phys. B710, 371-401]

- Uncertainties on shape functions limited by comparing the inclusive  $B \rightarrow X_u l\nu$  rate & inclusive  $B \rightarrow X_s \gamma$  photon spectrum

[Neubert et al., PRD 49 4623-4633 ; Leibovich et al., PRD 61 053006; Lange et al., JHEP 10 084]

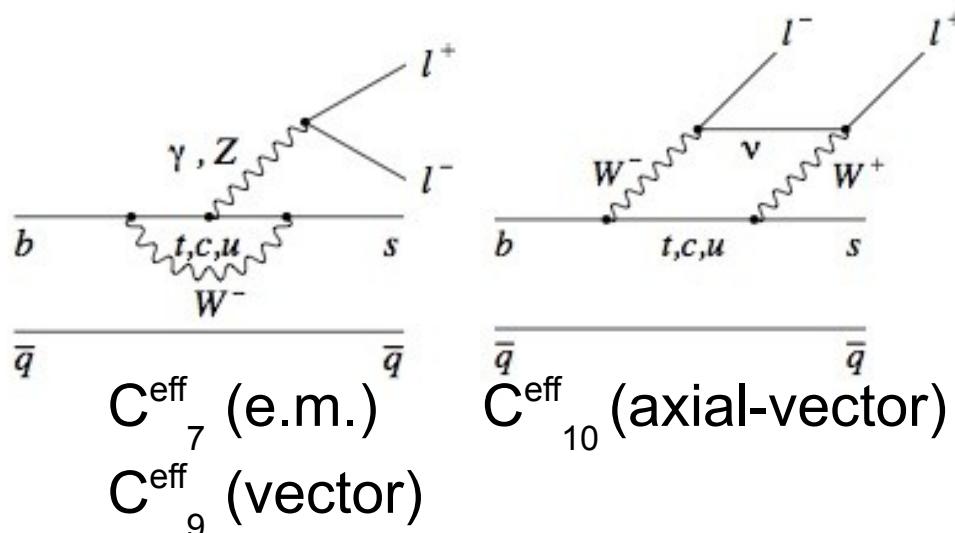
# B $\rightarrow$ s $\gamma$ Spectral Moments

HFAG Fit in Kinetic Mass Scheme (2010)



Data	$\chi^2/\text{dof}$	$ V_{cb}  (10^{-3})$	$m_b^{\text{kin}} (\text{GeV})$	$\mu_\pi^2 (\text{GeV}^2)$
All moments ( $X_c \ell \nu_\ell$ and $X_s \gamma$ )	$29.7/(66 - 7)$	$41.85 \pm 0.73$	$4.591 \pm 0.031$	$0.454 \pm 0.038$
$X_c \ell \nu_\ell$ only	$24.2/(55 - 7)$	$41.68 \pm 0.74$	$4.646 \pm 0.047$	$0.439 \pm 0.042$

# $B \rightarrow X_{s/d} l^+ l^-$ : Motivations



FCNC process forbidden at tree level,  $\text{BR} \sim 10^{-6}$ : Probe the SM!  
 Amplitudes expressed using OPE in terms of:

- Hadronic FF (accuracy  $\sim 20\%$ )  
 [Bharucha et al. Hep-ph 1004.3249]
- Wilson coefficients  $C_{\text{eff}}^{\text{e.m.}}_7, C_{\text{eff}}^{\text{vector}}_9, C_{\text{eff}}^{\text{axial-vector}}_{10}$   
 [Ali et al. PRD 61 074024, Z. Phys. C 67 417]

## New Particles in the loop could:

- Modify SM Wilson Coefficients
- Introduce additional ones

## Observables Include:

- Inclusive BR,  $d\text{BR}/dq^2$
- $A_{\text{CP}}$ ,  $A_{\text{ISOSPIN}}$ ,  $\text{RK}^{(*)}$  (theory error suppressed in the ratios!)
- Angular observables (defined below)

SM predicts ( $q^2 = m_{l^+ l^-}^2$ ):

$$A_{\text{CP}}^{K^{(*)}} \equiv \frac{\mathcal{B}(\overline{B} \rightarrow \overline{K}^{(*)} \ell^+ \ell^-) - \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)}{\mathcal{B}(\overline{B} \rightarrow \overline{K}^{(*)} \ell^+ \ell^-) + \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)} \quad \sim 10^{-3}$$

$$A_I \equiv \frac{(\tau_{B^+}/\tau_{B^0}) \mathcal{B}(K^{(*)0} \ell^+ \ell^-) - \mathcal{B}(K^{(*)\pm} \ell^+ \ell^-)}{(\tau_{B^+}/\tau_{B^0}) \mathcal{B}(K^{(*)0} \ell^+ \ell^-) + \mathcal{B}(K^{(*)\pm} \ell^+ \ell^-)} \quad < 10\% \quad \text{All } q^2$$

$$R_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)} \quad \begin{array}{l} \text{RK=1} \\ \text{RK*}=0.75 \\ (q^2 \rightarrow 0 \text{ } \gamma\text{-pole}) \end{array}$$

# Belle $B \rightarrow K^{(*)} l^+ l^-$ (605 fb $^{-1}$ )

PRL 103, 171801

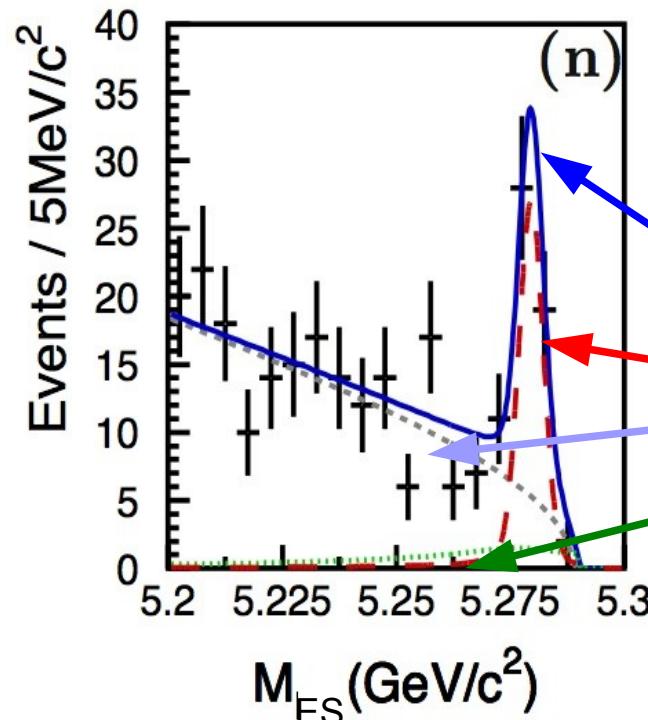
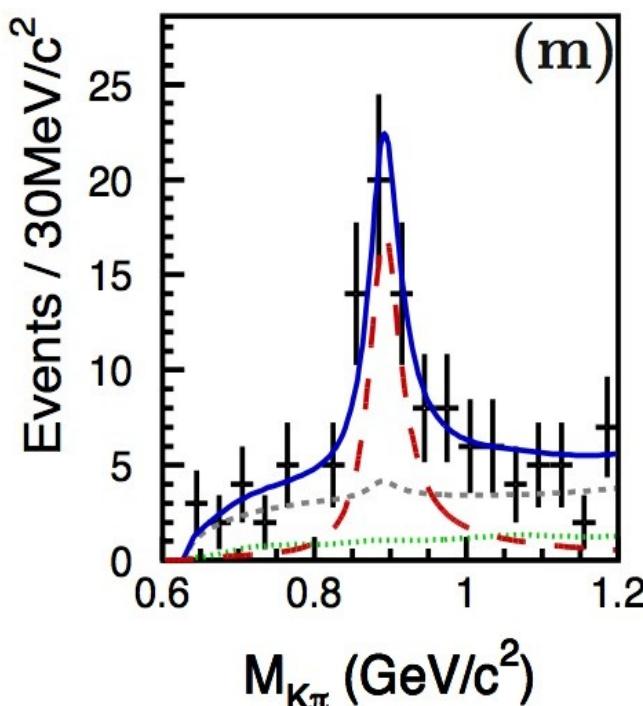
$B \rightarrow K^{(*)} l^+ l^-$  fully reconstructed in 10 final states:  $(K^+ \pi^-, K_s^0 \pi^+, K^+ \pi^0, K^+, K_s^0) + l^+ l^-$

- Peaking  $B \rightarrow J/\Psi(\Psi') X$  rejected by  $m_{l^+ l^-}^2$  cut

- Continuum Suppressed exploiting Event Shape Variables

- B Semileptonic Decays Suppressed using Event Shape, Missing Mass, Lepton distance of closest approach along beam axis

**K\* Fit** (single bin:  $10.09 < q^2 < 12.86 \text{ GeV}^2$ )



- $K^{(*)}$  Signal Yields determined by unbinned fit to  $m_{ES}$ ,  $(m_{K\pi})$  in 6  $q^2$  bins

Full Fit  
Signal  
Combinatorial  
 $J/\Psi(\Psi') X$

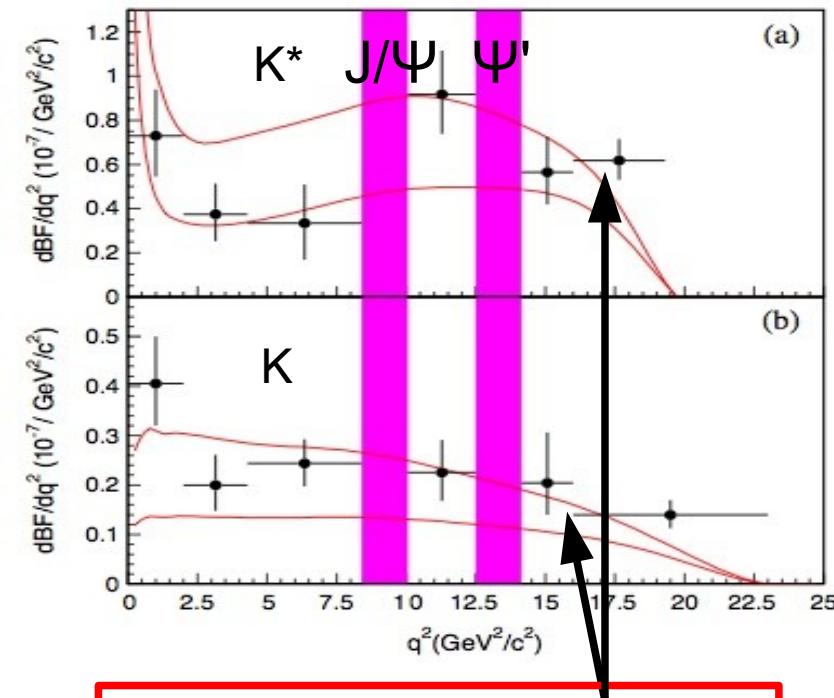
Full  $q^2 = m_{l^+ l^-}^2$  range:

$N(K l^+ l^-) = 162 \pm 22$   
 $N(K^* l^+ l^-) = 246 \pm 15$

# Belle $B \rightarrow K^{(*)} \ell^+ \ell^-$ (605 fb $^{-1}$ )

$d\text{BR}/dq^2$  from Signal Yields corrected for  $\epsilon(q^2)$

PRL 103, 171801



SM prediction with different FF assumptions  
 [Ali et al. PRD61 074024, PRD66 034002]

Inclusive BR,  $A_{CP}$ ,  $A_I$  & e/ $\mu$  ratio agree with SM:

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (10.7^{+1.1}_{-1.0} \pm 0.9) \times 10^{-7},$$

$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = (4.8^{+0.5}_{-0.4} \pm 0.3) \times 10^{-7},$$

$$A_{CP}(K^* \ell^+ \ell^-) = -0.10 \pm 0.10 \pm 0.01;$$

$$A_{CP}(K^+ \ell^+ \ell^-) = 0.04 \pm 0.10 \pm 0.02.$$

$$A_I(B \rightarrow K^* \ell^+ \ell^-) = -0.29^{+0.16}_{-0.16} \pm 0.09$$

$$A_I(B \rightarrow K \ell^+ \ell^-) = -0.31^{+0.17}_{-0.14} \pm 0.08$$

$$R_{K^*} = 0.83 \pm 0.17 \pm 0.08,$$

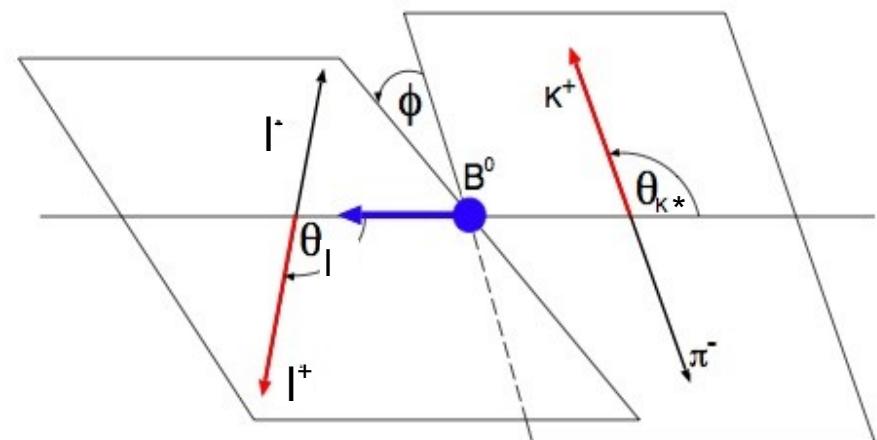
$$R_K = 1.03 \pm 0.19 \pm 0.06.$$

- Systematics dominated by tracking, PID, lepton selection & MC Decay Models

# Belle $B \rightarrow K^{(*)} l^+ l^-$ (605 fb $^{-1}$ )

PRL 103, 171801

- Event Angular Distribution depends on three angles
- $K^*$  longitudinal polarization fraction  $F_L$  & lepton  $A_{FB}$  obtained from fits to  $\theta_{K^*}$  &  $\theta_l$  in  $q^2$  bins



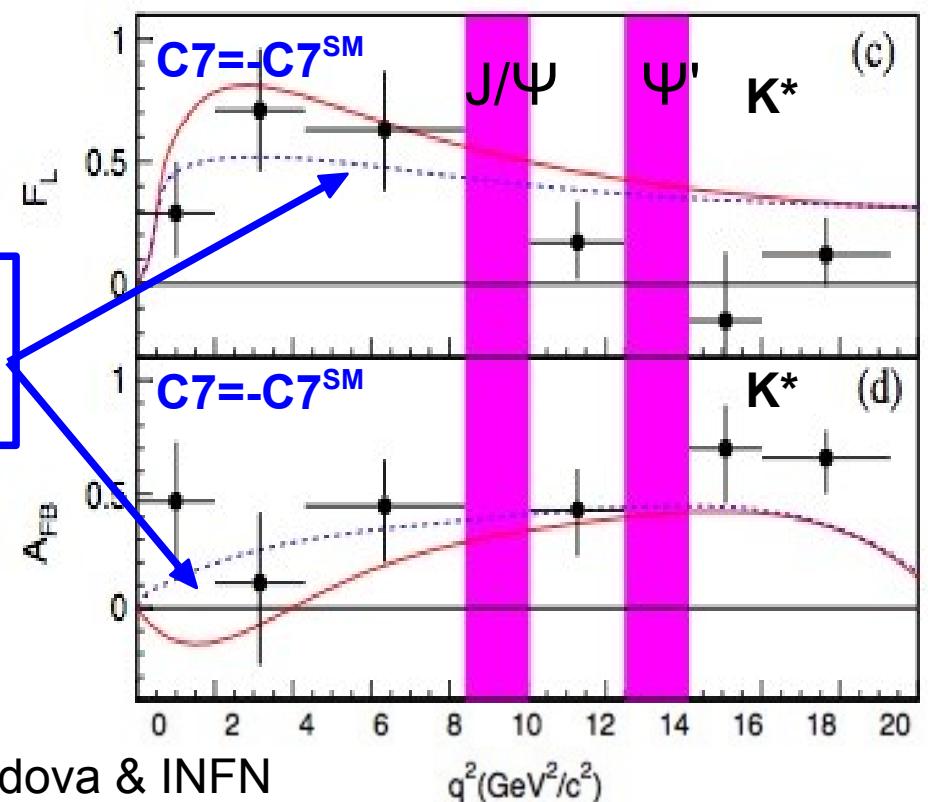
$$W(\cos \theta_K) = \frac{3}{2} \mathcal{F}_L \cos^2 \theta_K + \frac{3}{4} (1 - \mathcal{F}_L) \sin^2 \theta_K$$

$$W(\cos \theta_\ell) = \frac{3}{4} \mathcal{F}_L \sin^2 \theta_\ell + \frac{3}{8} (1 - \mathcal{F}_L) (1 + \cos^2 \theta_\ell)$$

$$+ A_{FB} \cos \theta_\ell$$

$A_{FB}, F_L (q^2=m_{l^+l^-}^2 < m^2(J/\Psi))$   
sensitive to  $C_7$  sign-flip

- Dominant Systematics from fixed normalization & fixed  $F_L$  in  $A_{FB}$  fit



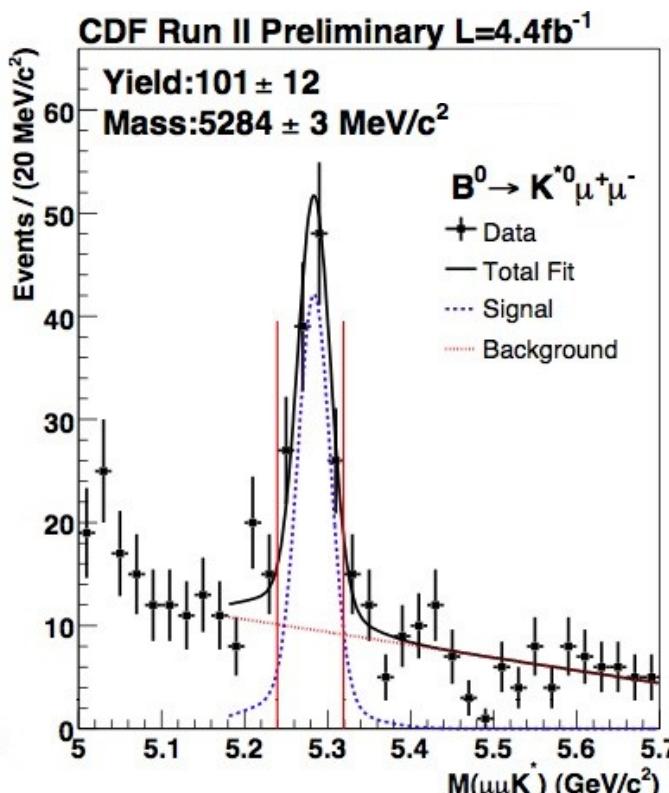
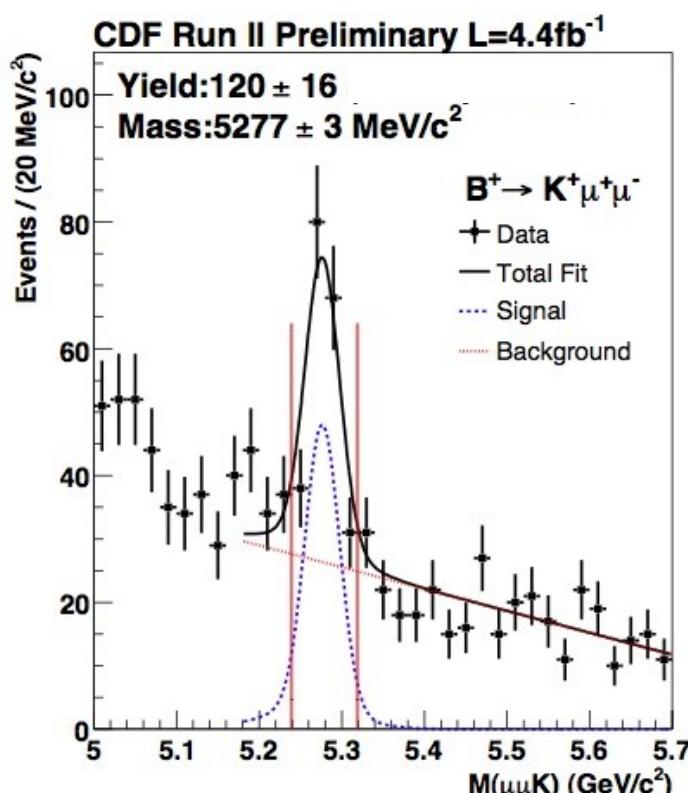
# CDF $B \rightarrow K\mu^+\mu^-$ (4.4 $\text{fb}^{-1}$ )

$B \rightarrow K^{(*)}\mu^+\mu^-$  fully reconstructed ( $K^* \rightarrow K^+\pi^-$ )

**PRELIMINARY**  
CDF Note 10047

- Dimuon level-3 trigger applied ( $P_T$ , VTX( $\mu^+\mu^-$ ) information)
- Vetoes applied to reject peaking  $B \rightarrow J/\Psi (\Psi')$ ,  $D\pi$  (fake  $\mu^+\mu^-$ )

- Signal selected using a Neural Network (vertexes, event shape, lepton separation)



- Signal yield from unbinned likelihood fit to  $m(B)$
- N(KI<sup>+</sup>I<sup>-</sup>) = 120±16**  
**N(K\*I<sup>+</sup>I<sup>-</sup>) = 101±12**

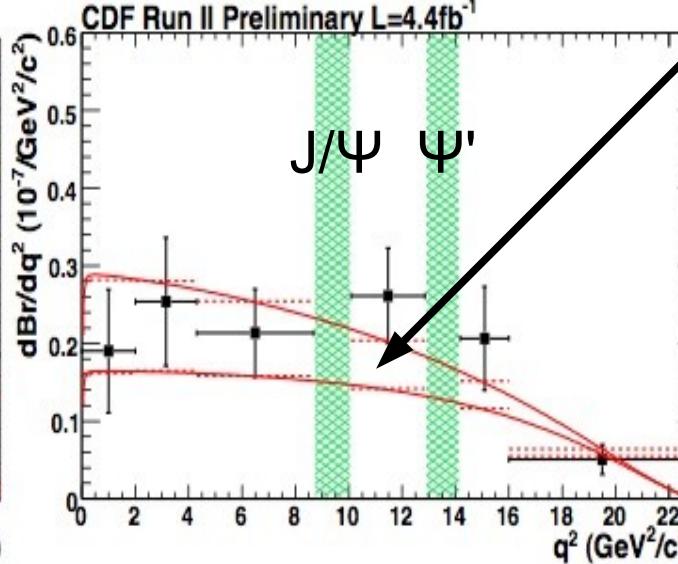
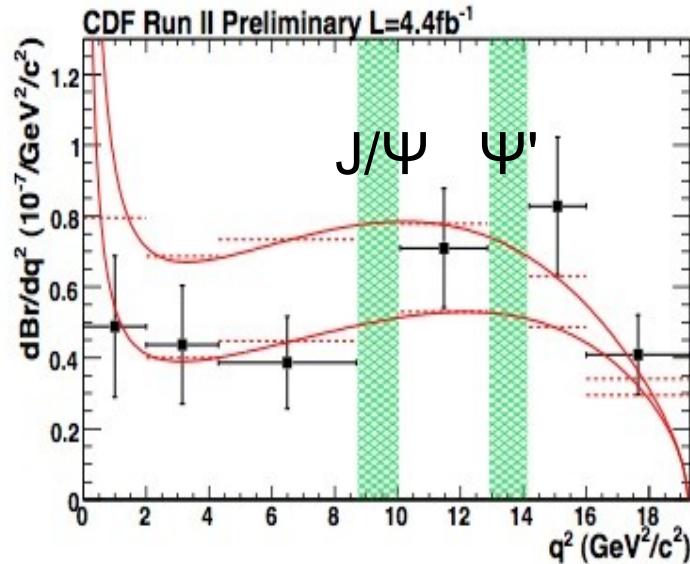
- BR computed relative to  $\text{BR}(B \rightarrow J/\Psi K^{(*)})$  (identical final states) to reduce efficiency systematics in the ratio

# CDF $B \rightarrow K\mu^+\mu^-$ (4.4 $\text{fb}^{-1}$ )

$$\mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-) = [0.38 \pm 0.05(\text{stat}) \pm 0.03(\text{syst})] \times 10^{-6}$$

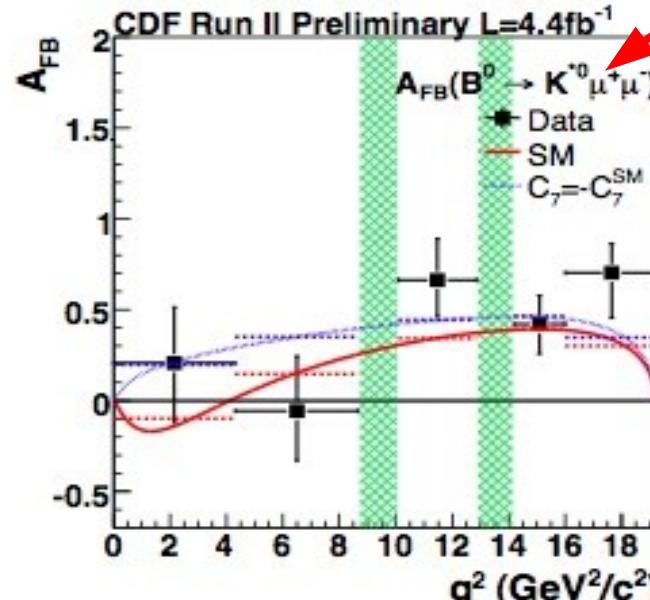
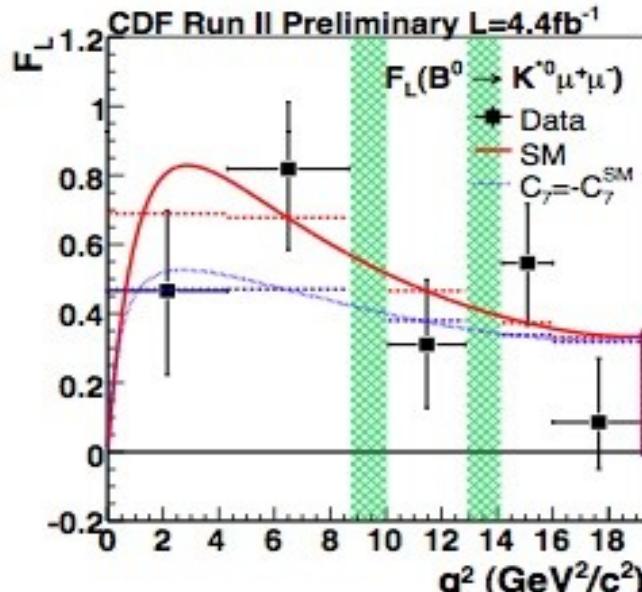
$$\mathcal{B}(B^0 \rightarrow K^{*0}\mu^+\mu^-) = [1.06 \pm 0.14(\text{stat}) \pm 0.09(\text{syst})] \times 10^{-6}$$

Results consistent with SM



BR Systematics from:

- Background m(B) PDF
- $\mathcal{B}(B \rightarrow J/\Psi K^{(*)})$



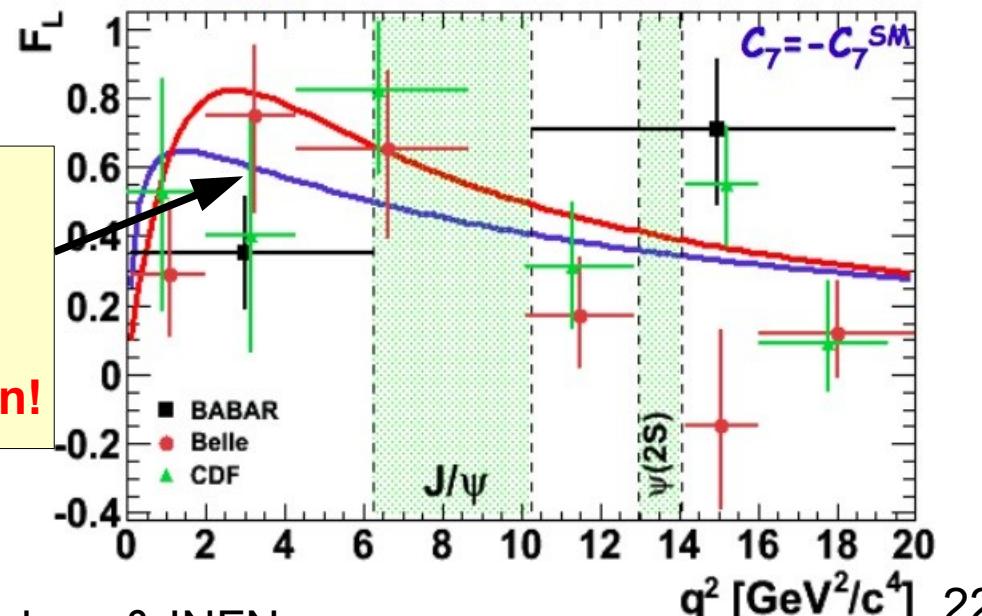
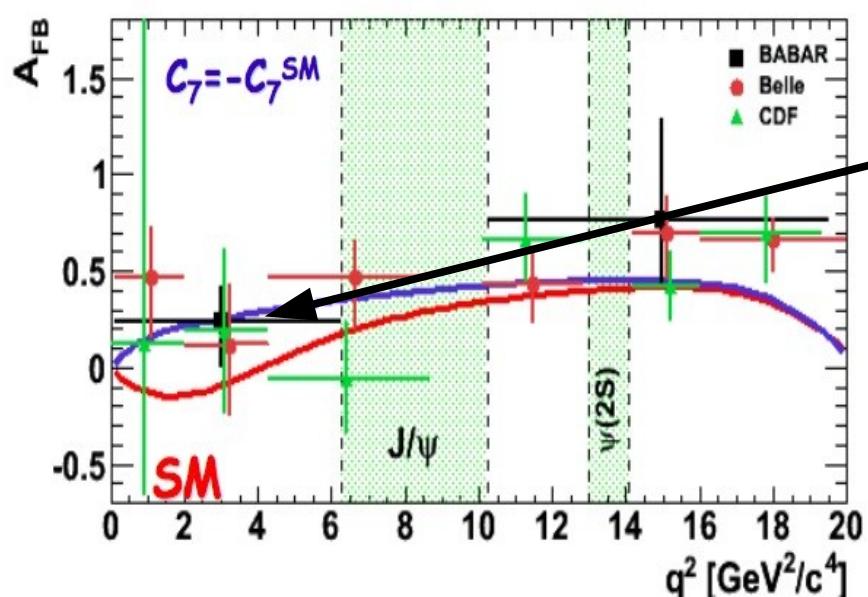
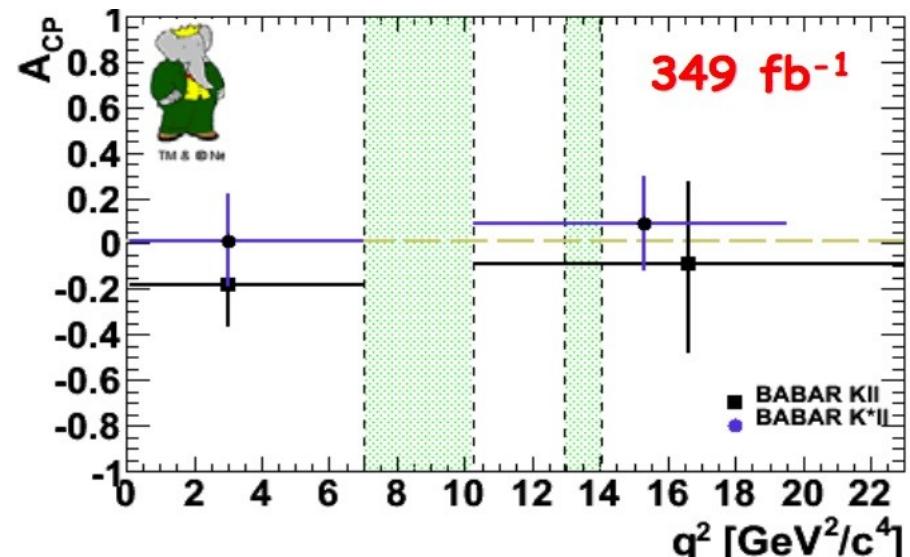
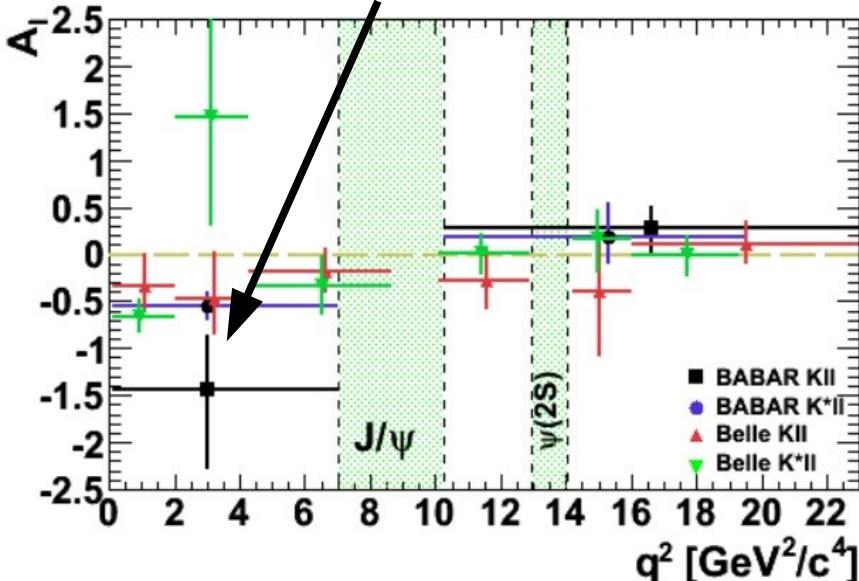
$A_{FB}$  : first measurement from hadron collider !

Angular Analysis Systematics from:

- Fraction of  $K-\pi$  swapped  $K^*$  (~7%)
- Combinatorial PDF from B-mass Side Band

# $B \rightarrow X_s^- l^+ l^-$ : Summary

- BaBar finds a hint of  $A_{\text{ISOSPIN}}$  deviation in the low  $q^2$  region [PRL 102 091803]
- Belle results in agreement both with SM & BaBar [PRL 103 171801]



# BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$ )

- $\text{BR}(B \rightarrow X_s l^+ l^-)$  expected to show weak dependence on lepton flavor in the high  $q^2$  region
- $B^+ \rightarrow K^+ \tau^+ \tau^- \sim 50\%$  of total  $X_s \tau^+ \tau^-$  inclusive rate  
[Hewett, PRD53 4964-4969]

$$\text{BR}(B \rightarrow X_s l^+ l^-) \quad 0.6 < (q/m_b)^2 < 1$$

Electron	$8.5 \times 10^{-7}$
Muon	$8.5 \times 10^{-7}$
Tau	$4.3 \times 10^{-7}$

- In NMSSM New Physics could couple with strength  $\sim m_{\text{LEPTON}}^2$
- [Hiller, PRD70 034018]

→ **Important Channel!**

**Experimentally:**

Exclusive reconstruction not possible due 2-4 neutrinos in the final state

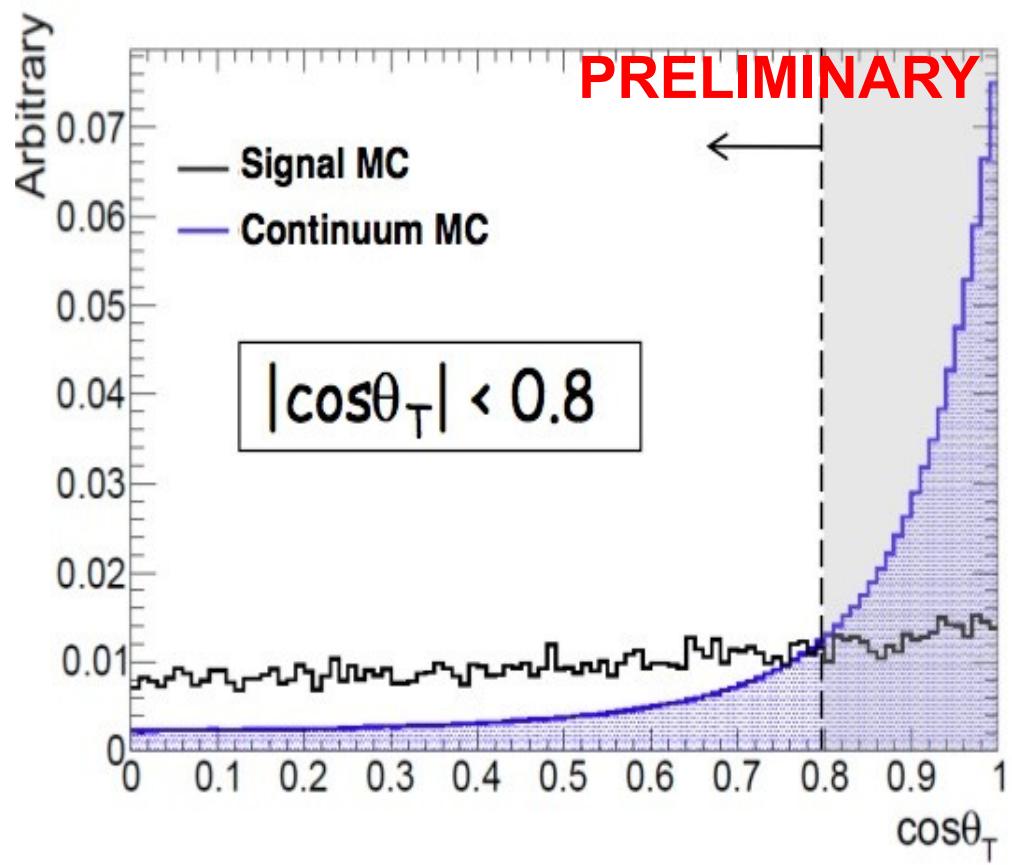
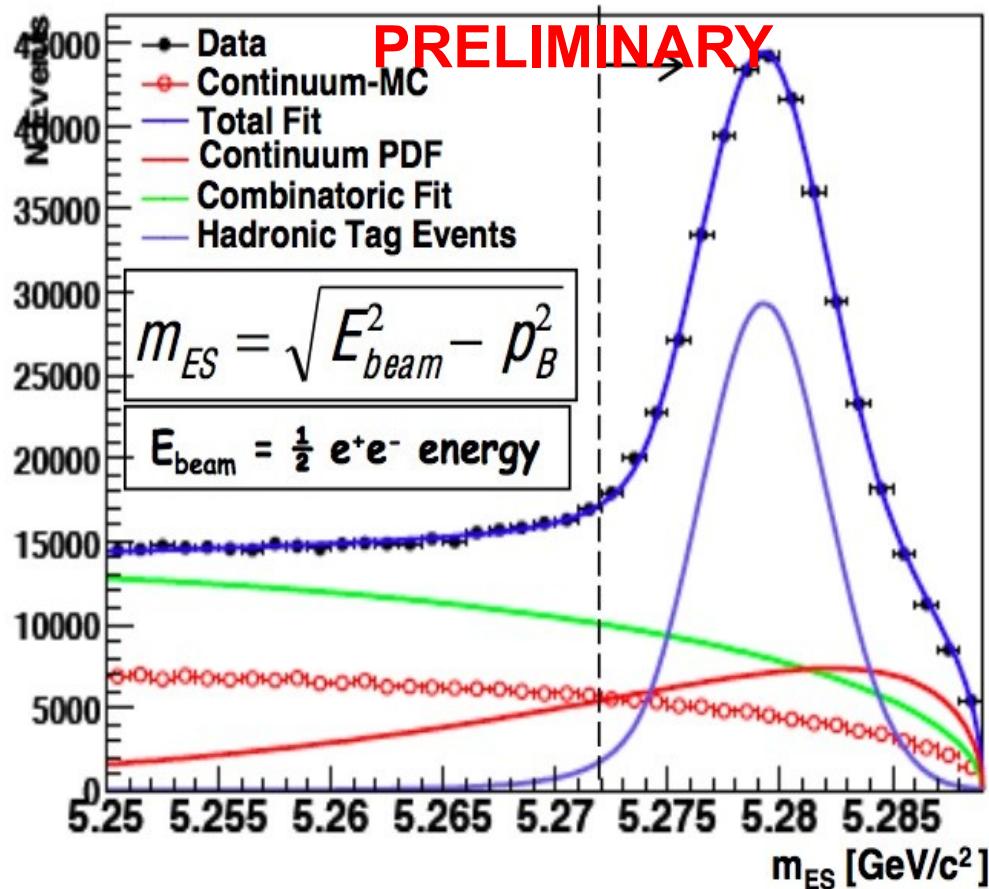
**BaBar performed the first search for  $B^+ \rightarrow K^+ \tau^+ \tau^-$ !**

# BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$ )

**PRELIMINARY**

- $K^+\tau^+\tau^-$  Decays searched on the recoil of fully reconstructed  $B \rightarrow D^{(*)}X$
- $\varepsilon_{tag} = 0.13\%$

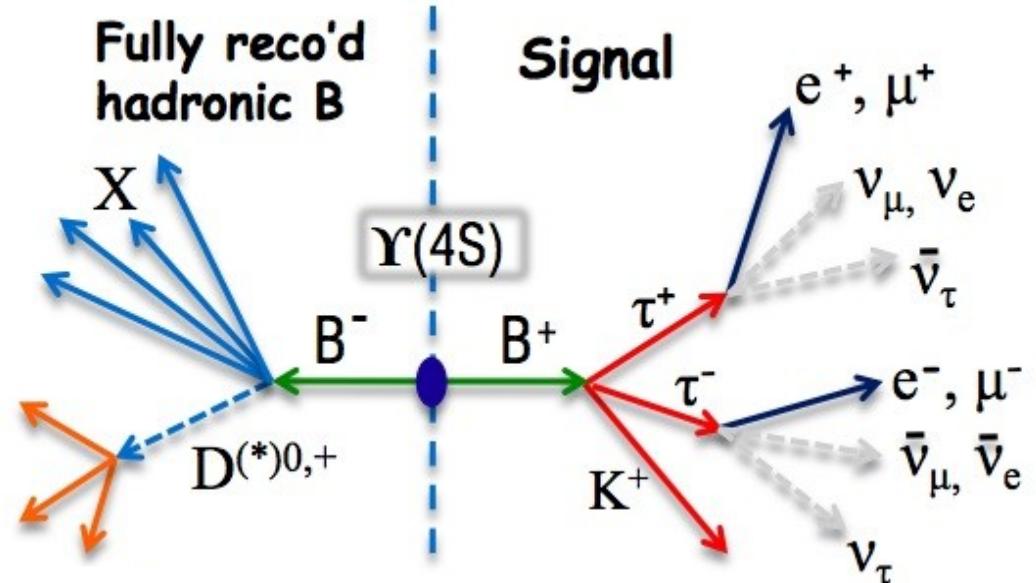
- Continuum Background suppressed exploiting the opening angle between the tag B thrust and the rest-of-event thrust:



# BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$ )

PRELIMINARY

- One-prong  $\tau$  decays reconstructed:  
 $\tau \rightarrow e(\mu)vv, \pi v$
- Di-tau candidates selected with 3 charged tracks only  
( $K^+$  & neutral pair of  $e, \mu, \pi$ )
- Signal searched exploiting:  
Missing Energy,  
Extra neutral energy,  
 $q^2 = (p_{Y(4S)} - p_{TAG} - p_K)^2$



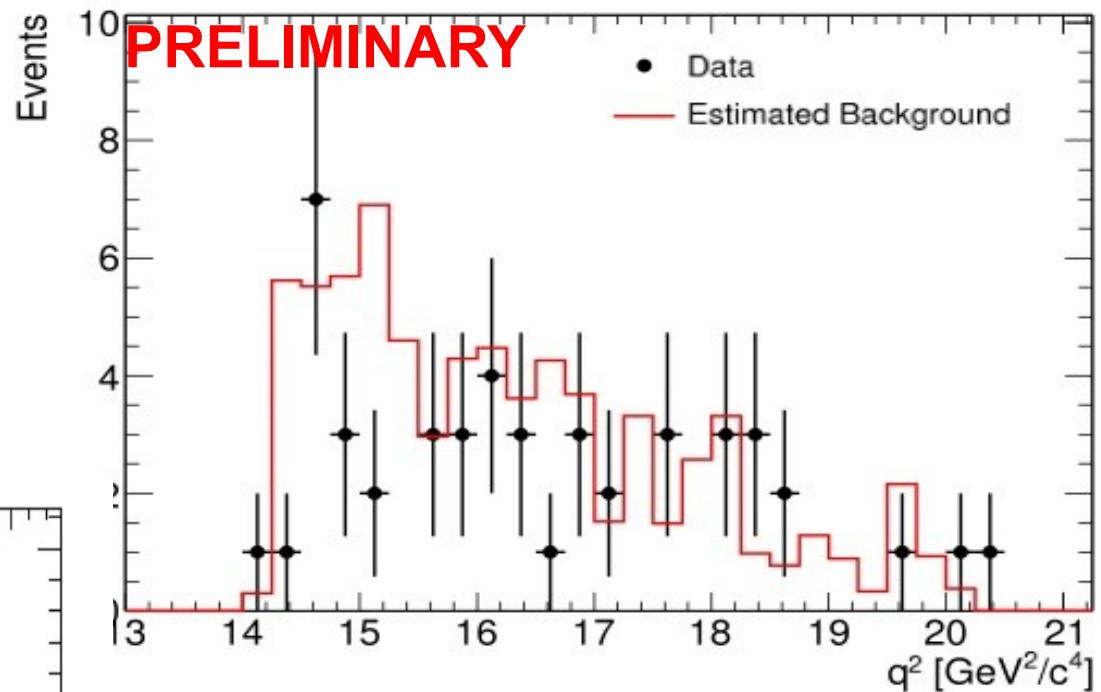
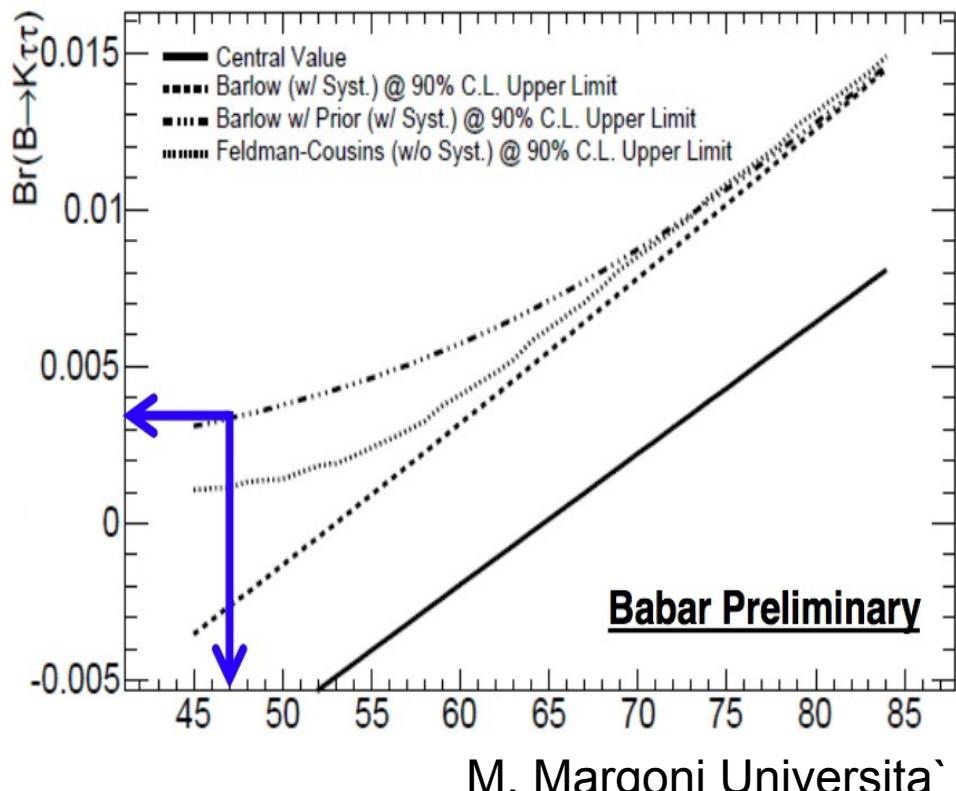
Peaking Background:

- $B$  semileptonic Decays Suppressed by  $P_{\text{Lepton}} \text{ cut} < 1.59 \text{ GeV}$
- $B \rightarrow DX$  Reduced by combining the signal  $K^+$  with the signal  $\tau$  daughter of opposite charge assigned a  $\pi$  mass hypothesis and requiring the resulting invariant mass to be  $m(K\pi) > 1.96 \text{ GeV}$

# BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$ )

- Systematics from  $\varepsilon_{\text{SIGNAL}}$  (tracking, PID),  
Background  $m_{\text{ES}}$  shape & yield

**47 events observed  
(65 expected from BKG)**



- Upper Limit obtained using Barlow method [Comput. Phys. Commun. 149, 97] with Bayesian prior
- Conservative Approach!

**BR( $B^+ \rightarrow K^+ \tau^+ \tau^-$ ) <  $3.3 \times 10^{-3}$  @ 90% CL  
PRELIMINARY**

$$B \rightarrow \pi^- l^+ l^-$$

No Inclusive Analyses performed. Experiments Fully reconstruct  $B \rightarrow \pi^- l^+ l^-$

### Main Backgrounds:

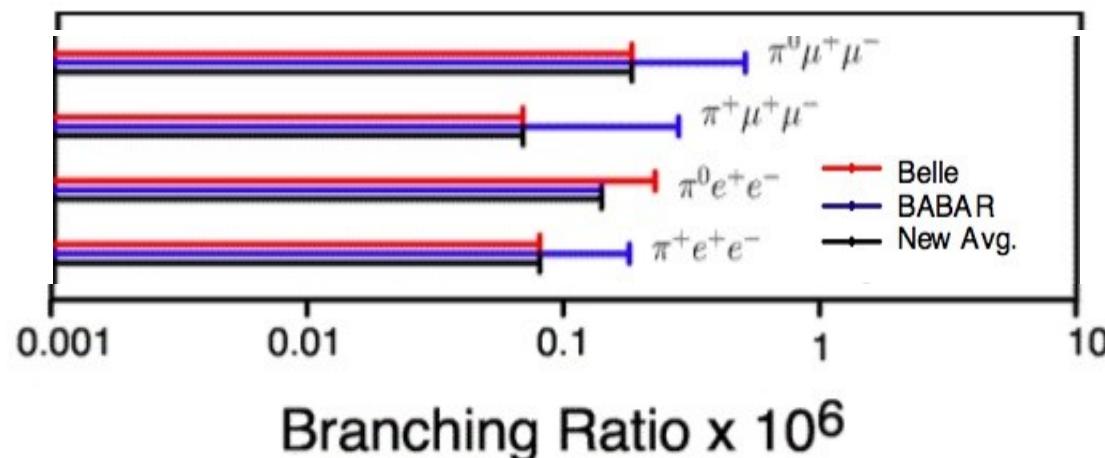
- Continuum reduced exploiting event shape variables & B-flavor tagging

Belle (605 fb<sup>-1</sup>) [PRD 78 011101R]

$$\text{BR}(B \rightarrow \pi^- l^+ l^-) < 6.2 \times 10^{-8}$$

BaBar (209 fb<sup>-1</sup>) [PRL 99 051801]

$$\text{BR}(B \rightarrow \pi^- l^+ l^-) < 9.1 \times 10^{-8}$$



- J/ψ(Ψ'), γ conversion vetoes applied

- B & D Semileptonic Decays suppressed by means of missing energy, vertex fit information

HFAG 2010:

$$\text{BR}(B \rightarrow \pi^- l^+ l^-) < 6.2 \times 10^{-8}$$

SM:

$$\text{BR}(B \rightarrow \pi^- l^+ l^-) = 3.3 \times 10^{-8}$$

[Aliev, Savic, PRD60 014005]

# Conclusions

Radiative penguin decays are an excellent laboratory for the search for physics beyond the SM & the study of b-quark dynamics

**Almost all results in agreement with expectations**

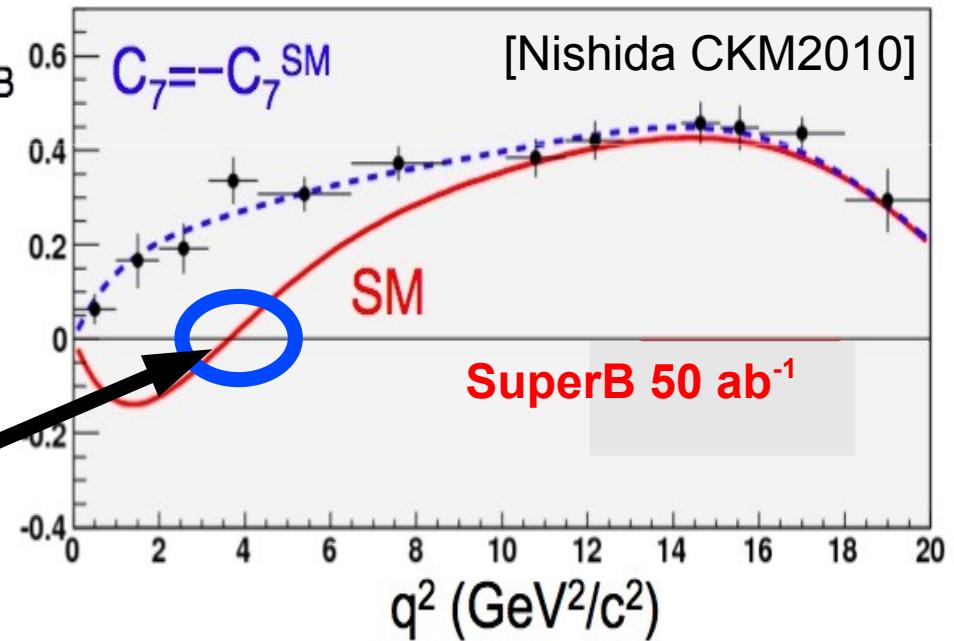
In the Future they will offer Opportunity to:

- Improve Experimental Techniques by using new angular observables with reduced dependence on Form Factors (e.g. Transversity Amplitudes)

[Bobeth et al., arXiv:1006.5013]

$A_{FB}(q^2_0)=0$   
SuperBelle( $50\text{ab}^{-1}$ )  $\delta q^2_0 \sim 5\%$   
LHCb( $2\text{fb}^{-1}$ ):  $\delta q^2_0 \sim 13\%$   
LHCb( $100\text{fb}^{-1}$ ):  $\delta q^2_0 \sim 2\%$

- Provide very stringent SM tests:



- Hopefully discover/understand New Physics

# Backup

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

- Fragmentation of hadronic system in MC not the same in data – need to correct what we can.
- $B \rightarrow X_s \gamma$  has high signal yield – can measure fragmentation of hadronic system here and correct the MC.
- We measure 7 modes, also take advantage of data/MC differences found in previous sum-of-inclusive  $b \rightarrow s \gamma$  analysis.

Decay mode	Efficiency-corrected	Efficiency-corrected	Ratio data/MC	Ratio data/MC in previous analysis
	fraction in MC	fraction in data		
$B \rightarrow K^+ \pi^- \gamma$	0.193	0.098	$0.51 \pm 0.04$	$0.65 \pm 0.04$
$B \rightarrow K^+ \pi^0 \gamma$	0.118	0.033	$0.28 \pm 0.05$	$0.36 \pm 0.06$
$B \rightarrow K^+ \pi^+ \pi^- \gamma$	0.206	0.230	$1.21 \pm 0.08$	$1.34 \pm 0.11$
$B \rightarrow K^+ \pi^+ \pi^0 \gamma$	0.250	0.370	$1.48 \pm 0.08$	$1.35 \pm 0.11$
$B \rightarrow K^+ \pi^+ \pi^+ \pi^- \gamma$	0.058	0.079	$1.36 \pm 0.30$	$0.75 \pm 0.27$
$B \rightarrow K^+ \pi^+ \pi^+ \pi^0 \gamma$	0.158	0.182	$1.15 \pm 0.25$	$1.00 \pm 0.23$
$B \rightarrow K^+ \eta \gamma$	0.017	0.009	$0.50 \pm 0.25$	$1.05 \pm 0.41$

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

- Low mass regions easy – correct for unreconstructed  $K^*/\omega$  decays.
- High mass regions – how much width do our 7 decay modes cover?
  - Use weighted MC for  $b \rightarrow s\gamma$ , unweighted MC for  $b \rightarrow d\gamma$ .
- For systematic error, vary each category of missing modes (high and low multiplicity) by some amount, then renormalise to retain total BF in mass region, and see how proportion of our reconstructed modes changes.
  - Known  $b \rightarrow s\gamma$  data/MC corrections are varied within their errors.
  - What about unknown missing fractions? Consider alternative fragmentation models e.g. applying  $b \rightarrow s\gamma$  corrections to  $b \rightarrow d\gamma$ , “hybrid” mix of resonances + non-res MC.

Proportion in $b \rightarrow s\gamma$ 1.0-2.0 GeV/ $c^2$	Default model	Hybrid model
7 reconstructed modes	35.6%	40.0%
“known” 2/3/4 body modes	35.8%	40.2%
unreconstructed 2/3/4 body modes	12.6%	11.5%
unreconstructed 5+ body modes	16.1%	8.3%

Proportion in $b \rightarrow d\gamma$ 1.0-2.0 GeV/ $c^2$	Default model	$b \rightarrow s\gamma$ weights applied	Hybrid model
7 reconstructed modes	42.3%	39.5%	46.9%
unreconstructed 2/3/4 body modes	27.0%	34.5%	34.9%
unreconstructed 5+ body modes	30.7%	26.0%	18.3%

# BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$ )

Extract  $X=|V_{td}/V_{ts}|$  from Ratio of Inclusive BFs

- Use NLO calculation [Ali et al., Phys. Lett. B429 87]

$$R = \lambda^2[1 + \lambda^2(1 - 2\bar{\rho})] \left[ (1 - \bar{\rho})^2 + \bar{\eta}^2 + \frac{D_u}{D_t}(\bar{\rho}^2 + \bar{\eta}^2) + \frac{D_r}{D_t}(\bar{\rho}(1 - \bar{\rho}) - \bar{\eta}^2) \right]$$

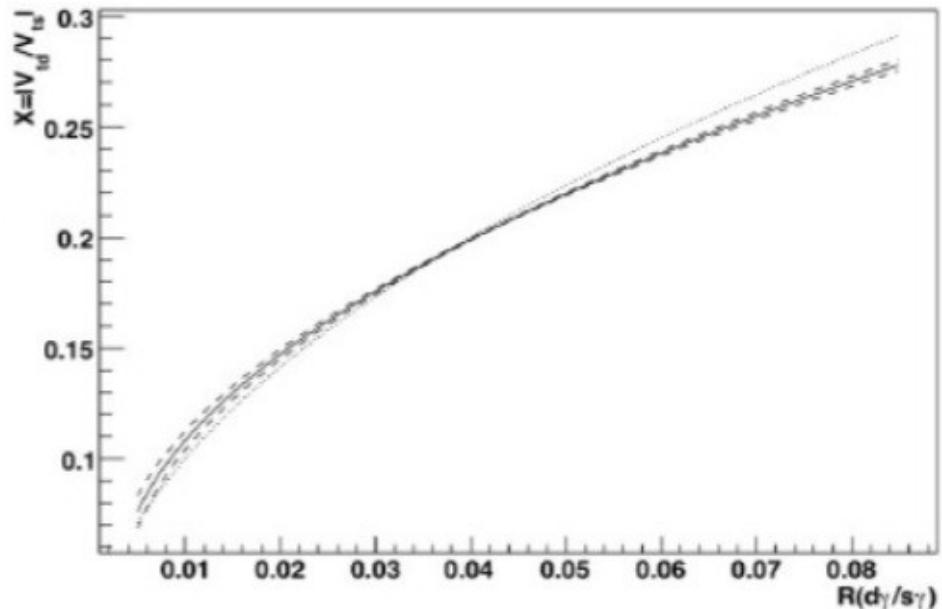
- Rewrite in terms of  $X$  and UT angle  $\beta$

$$R = \kappa_1 X^2 + \kappa_2 X + \kappa_3,$$

$$\kappa_1 = 1 + \frac{D_u}{D_t} (1 - 2\lambda^2 \cos^2 \beta) - \frac{D_r}{D_t} (\lambda^2 \cos^2 \beta + 1),$$

$$\kappa_2 = \lambda \cos \beta \left[ \frac{D_u}{D_t} (3\lambda^2 - 2) + \frac{D_r}{D_t} \left( 1 + \frac{\lambda^2}{2} \right) \right],$$

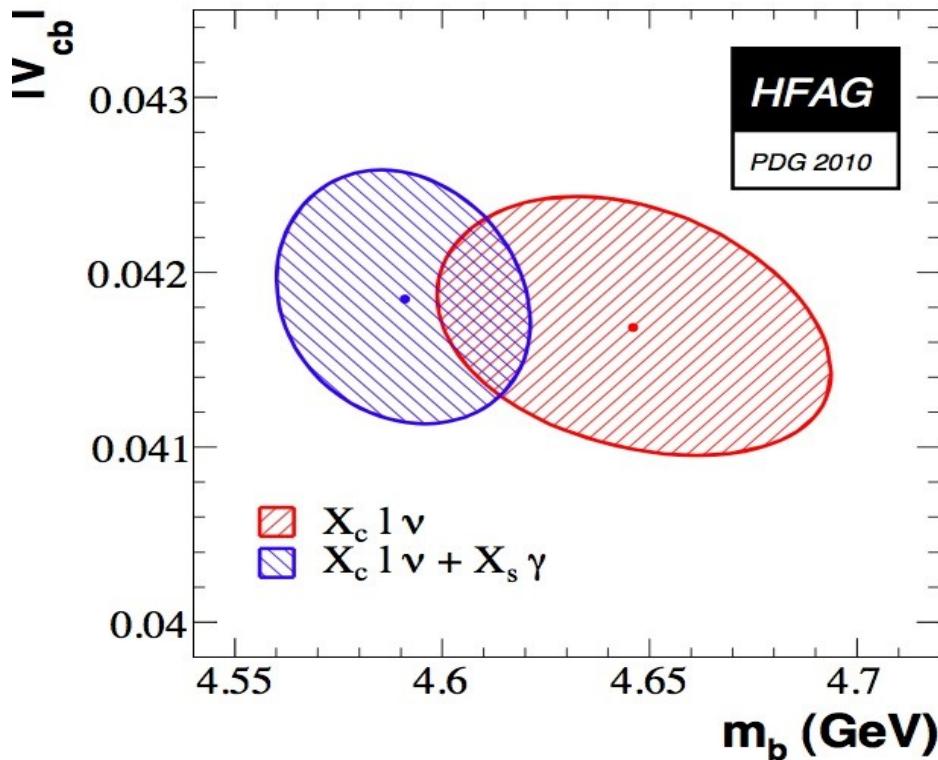
$$\kappa_3 = \lambda^2 \frac{D_u}{D_t} (1 - \lambda^2).$$



- Uncertainties from PDG & numerical calculation of D factors

# B $\rightarrow$ s $\gamma$ Spectral Moments

HFAG Fit in Kinetic Mass Scheme (2010)

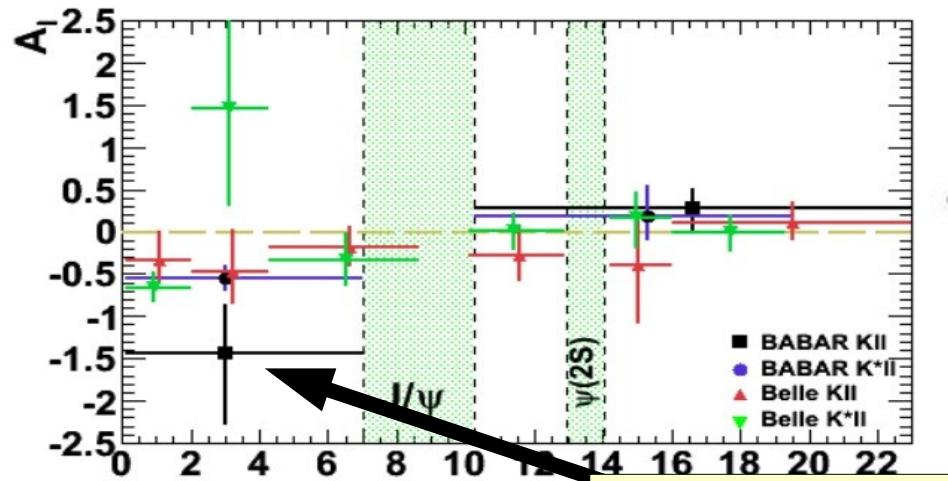
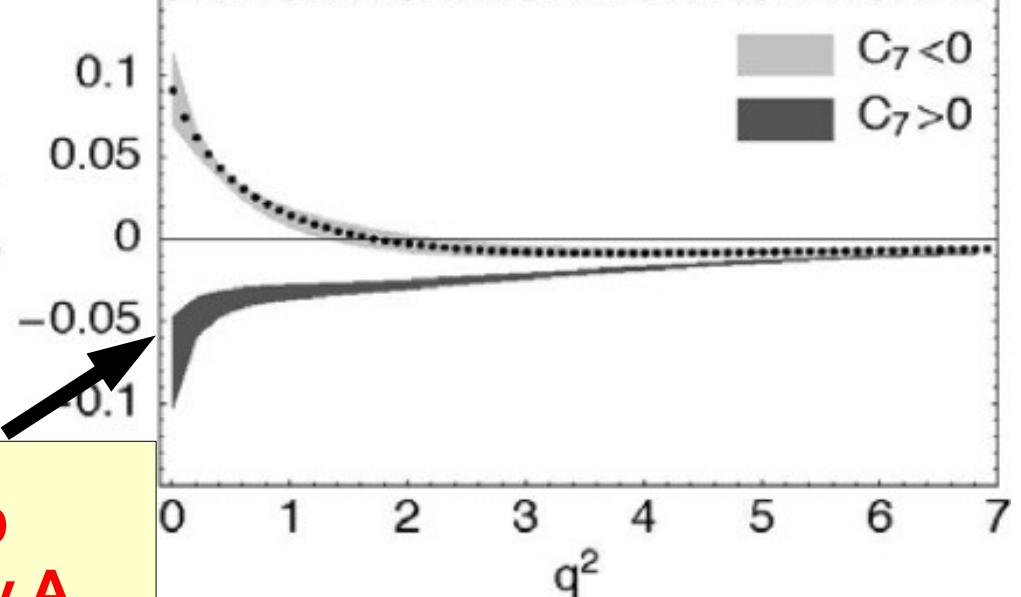


$|V_{ub}|$  From Inclusive BR in different Theoretical Frameworks using  $X_s \gamma$  Moments [HFAG2010]

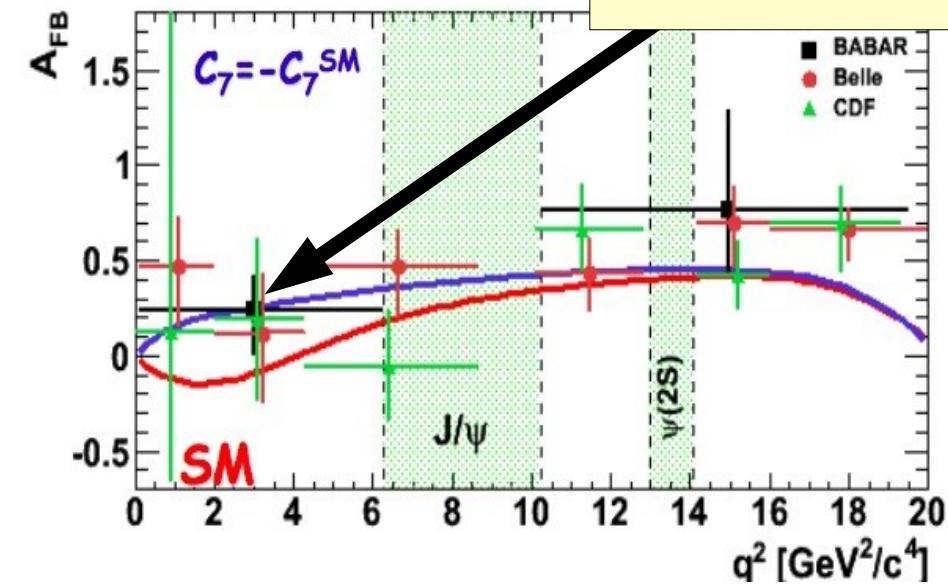
Framework	$ V_{ub} [10^{-3}]$
BLNP	$4.32 \pm 0.16^{+0.22}_{-0.23}$
DGE	$4.46 \pm 0.16^{+0.18}_{-0.17}$
GGOU	$4.34 \pm 0.16^{+0.15}_{-0.22}$
ADFR	$4.16 \pm 0.14^{+0.25}_{-0.22}$
BLL ( $m_X/q^2$ only)	$4.87 \pm 0.24 \pm 0.38$
LLR (BABAR) [394]	$4.43 \pm 0.45 \pm 0.29$
LLR (BABAR) [395]	$4.28 \pm 0.29 \pm 0.29 \pm 0.26 \pm 0.28$
LNP (BABAR) [395]	$4.40 \pm 0.30 \pm 0.41 \pm 0.23$

Data	$\chi^2/\text{dof}$	$ V_{cb} (10^{-3})$	$m_b^{\text{kin}}(\text{GeV})$	$\mu_\pi^2(\text{GeV}^2)$
All moments ( $X_c \ell \nu_\ell$ and $X_s \gamma$ )	$29.7/(66 - 7)$	$41.85 \pm 0.73$	$4.591 \pm 0.031$	$0.454 \pm 0.038$
$X_c \ell \nu_\ell$ only	$24.2/(55 - 7)$	$41.68 \pm 0.74$	$4.646 \pm 0.047$	$0.439 \pm 0.042$

# $A_{\text{ISOSPIN}}$ vs $q^2$


 $dA_I / dq^2$ 


**C7 sign-flip  
Not rejected by  $A_{\text{FB}}$**



$$C_7 = -C_7^{\text{SM}}$$

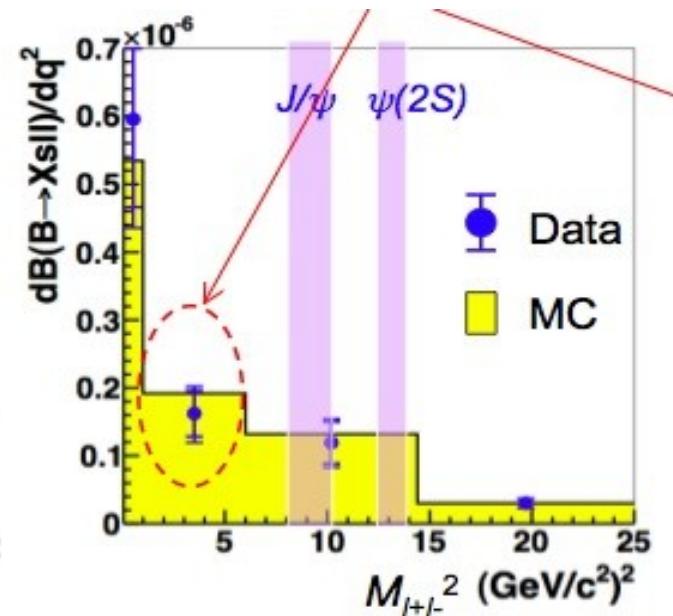
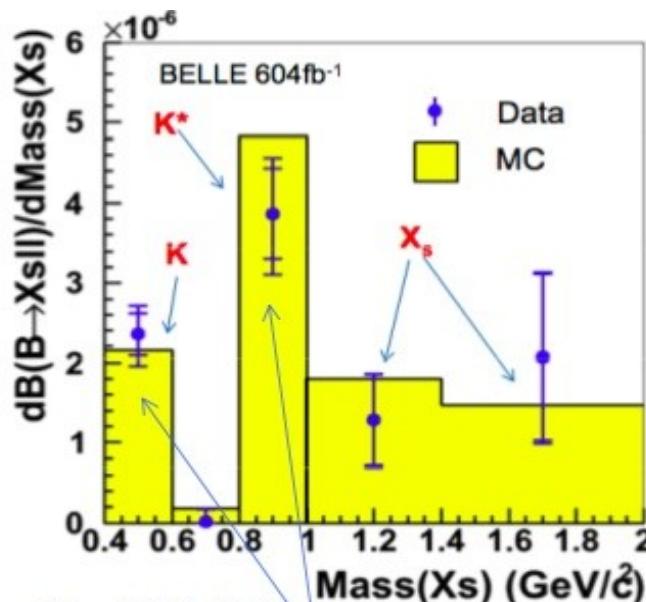
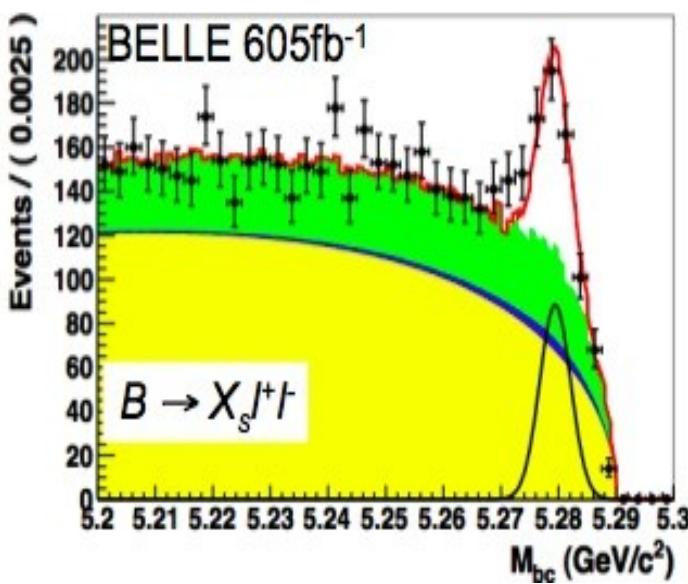
Feldman et al. JHEP 0301,074  
Hubert et al., Nucl. Phys. B802 40]

# Belle $B \rightarrow X_s l^+ l^-$ (605 fb $^{-1}$ )

PRELIMINARY

**Improved Analysis, sum up 36 exclusive modes (~80% coverage)**

- Continuum Suppressed by event shape variables
- Cascades  $b \rightarrow c \rightarrow s/d$  rejected exploiting missing mass & energy



Mode	Yield	BF (x 10 $^{-6}$ )
$B \rightarrow X_s e^+ e^-$	$121.6 \pm 19.3(\text{stat.}) \pm 2.0(\text{syst.})$	$4.56 \pm 1.15(\text{stat.})^{+0.33}_{-0.40}(\text{syst.})$
$B \rightarrow X_s \mu^+ \mu^-$	$118.5 \pm 17.3(\text{stat.}) \pm 1.5(\text{syst.})$	$1.91 \pm 1.02(\text{stat.})^{+0.16}_{-0.18}(\text{syst.})$
$B \rightarrow X_s l^+ l^-$	$238.3 \pm 26.4(\text{stat.}) \pm 2.3(\text{syst.})$	$3.33 \pm 0.80(\text{stat.})^{+0.19}_{-0.24}(\text{syst.})$

ps:  $\text{BF}(X_s e^+ e^-) / \text{BF}(X_s \mu^+ \mu^-) = 2.39 \pm 1.41$

SM:  
 $\text{BF} = (4.2 \pm 0.7) \times 10^{-6}$   
 [Ali et al.]

C<sub>7</sub> sign-flip:  
 $\text{BF} = (8.8 \pm 1.0) \times 10^{-6}$   
 [Gambino et al.]

# Transversity Amplitudes

[Bobeth et al., arXiv:1006.5013]

- HQET Calculations give possibility to disentangle QCD Effects from possible New Physics Effects at high  $q^2 = m_{l^+l^-}^{-2}$  in  $B \rightarrow K^* l^+ l^-$  angular analyses
- New Observables defined which **do not depend on FF** at low recoil and cleanly test SM:

$$H_T^{(1)} = \frac{\text{Re}(A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)}}$$

$$H_T^{(2)} = \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}}$$

$$H_T^{(3)} = \frac{\text{Re}(A_{\parallel}^L A_{\perp}^{L*} - A_{\parallel}^{R*} A_{\perp}^R)}{\sqrt{(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}}$$

Computed in terms of left & right Transversity Amplitudes:

$$A_{\perp}^{L,R} = +i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_{\perp},$$

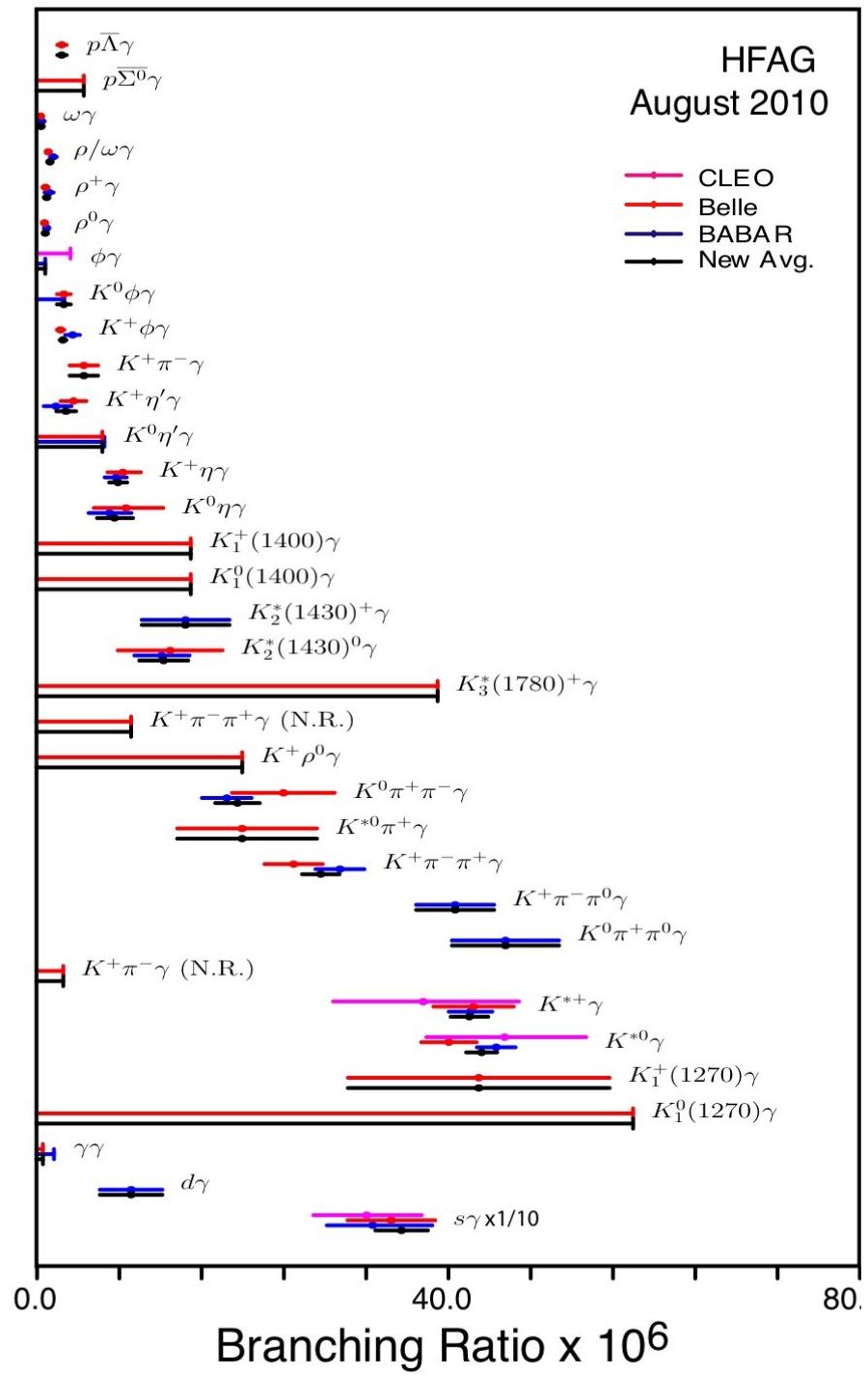
$$A_{\parallel}^{L,R} = -i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_{\parallel},$$

$$A_0^{L,R} = -i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_0,$$

Form Factors

- Other Observables which do not depend on Wilson Coefficients at low recoil probe some  $B \rightarrow K^*$  FF combinations

$\mathcal{B}(B \rightarrow X_{s d} \gamma)$



$\mathcal{B}(B \rightarrow X \ell^+ \ell^-)$

