

Special features  
of the complete one-loop  
MSSM SUSY effects  
in charged and neutral  
semi inclusive Higgs  
production at LHC.

Charged Higgs 2010, Uppsala 27/09.

C.Verzegnassi  
Dept.of Physics, University, Trieste.

Terminology: follows Dawson,  
Jackson, Reina and Wackerroth  
(Mod.Phys.Lett. A21,89 -2006)  
for bottom- neutral Higgs  
and Berger,Han, Jing Jiang  
and Plehn  
(Phys.Rev.D71,115012-2005)  
for top- charged Higgs  
("semi-inclusive"="associated")  
production.

Apologies to the very large number  
of unquoted authors.....

The results that I will show have been obtained working in the 5FNS and considering the 4 “semi-inclusive” processes:

$bg \rightarrow bh$  ( $h=h_0, H_0, A_0$  MSSM)

$bg \rightarrow tH$  ( $H=\text{charged MSSM Higgs}$ ).

in the MSSM and also in the 2HDM, Type 2, approach, for  $MH > m_{\text{top}}$ .

The theoretical group that performed the calculations is mostly constituted by the members of the Italian INFN supported LE21 “Iniziativa Specifica” i.e.

Matteo Beccaria, Giacomo Dovier, Guido Macorini, Luca Panizzi, C.V. (green ones previously p.h.d. students of mine) with the extra essential contribution of Fernand Renard, Edoardo Mirabella. and (for the last paper) Abdelhak Djouadi.

At the lowest tree level order,  
the four considered processes are  
described by the following  
Feynman diagrams (next page):

To understand the main goals of the  
theoretical efforts to be described,  
a good starting point is to derive  
the MSSM expression of the relevant  
(t,b H=Higgs) Yukawa Lagrangian.  
In the notation of Carena, Garcia,  
Nierste and Wagner (Nucl.Phys.B577,  
577-2000) this reads:

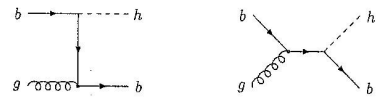


FIG. 2: Tree level Feynman diagram for  $bg \rightarrow bh$  in the 5FNS.

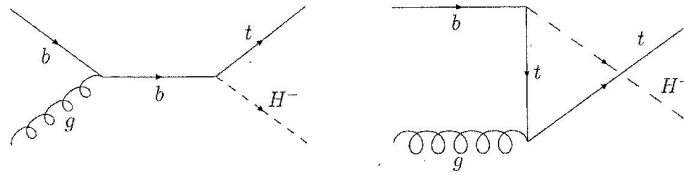


Figure 1: Born diagrams: s-channel bottom exchange and u-channel top exchange.

$$\begin{aligned}
 -\mathcal{L}_{\text{YU}}^{(0)}(b, t, H) = & \left\{ \frac{\sqrt{2}}{v} \left[ m_b \frac{t}{\beta} \bar{b}_L b_R H^+ + \right. \right. \\
 & \left. \left. + \frac{m_t}{t\beta} \bar{b}_L t_R H \right] + \text{h.c.} \right\} \\
 & + \left\{ \frac{m_b}{v \cos \beta} \left[ \bar{b} b \left( -\sin \alpha h_0 + \cos \alpha H_0 \right) - \right. \right. \\
 & \left. \left. - i \bar{b} \gamma_5 b A_0 \frac{t}{\beta} \right] \right. \\
 & \left. + \frac{m_t}{v \sin \beta} \left[ \bar{t} t \left( \cos \alpha h_0 + \sin \alpha H_0 \right) \right. \right. \\
 & \left. \left. + i \bar{t} \gamma_5 t A_0 \cos \beta \right] \right\}
 \end{aligned}$$

Here  $\beta, \alpha$  are the usual MSSM Higgs sector angles,  $v \equiv \sqrt{v_1^2 + v_2^2} \approx 174 \text{ GeV}$  and  $\mathcal{L}^{(0)}$  does not contain (future) radiative corrections. The Yukawa couplings  $h_{b,t}$  are defined as

$$h_b = \frac{m_b}{v_2}, \quad h_t = \frac{m_t}{v_2}, \quad t \beta \equiv \frac{v_2}{v_1}$$

( $v_{1,2}$  are the neutral Higgses vevs).

More precisely:

$$h_0 = \cos \alpha h_u^0 - \sin \alpha h_d^0$$

$$H_0 = \sin \alpha h_u^0 + \cos \alpha h_d^0$$

$$A_0 = \cos \beta \chi_u^0 + \sin \beta \chi_d^0$$

$$H^+ = \cos \beta h_u^+ + \sin \beta h_d^{+*}$$

$h_u^0, \chi_u^0, h_u^+$  are the neutral (real and Imaginary) and charged members of the  $H_u$  doublet (coupled to up quarks)

The  $(\ )_d$  fields are those coupled to down quarks.



In the previous expression (where I assumed  $V_{tb}=1$ ),  $h_0$ ,  $H_0$ ,  $A_0$  are the physical neutral CP even and odd Higgses (CP is assumed to be conserved),  $H^\pm$  is the physical charged Higgs. In principle, there are six free parameters (the four masses and the two angles). In the MSSM at this lowest order only two parameters are independent, usually taken as  $M_{A_0}$  and  $\tan\beta$ .

In a model with one more (extra SM) Higgs Doublet and two different vevs like in the MSSM (2HDM) the six parameters are free.

Looking at the LO Lagrangian of page 7 one sees that taking large values (e.g.  $>10$ ) of  $\tan\beta$  the term proportional to  $M_t$  in the  $b_tH$  interaction can be ignored.

The four processes  $bg \rightarrow bh$  and  $bg \rightarrow tH$  are therefore described in this regime by the same parameters,  $\tan\beta$ ,  $M_A$  and  $m_b$ . This suggests the criterion of making a common study and comparison of the four reactions, that must necessarily involve the higher order “radiative” corrections and, also, the “poor boy” small  $\tan\beta$  (e.g.  $<10$ ) region.

Moving to higher orders.

Moving to higher orders in the MSSM requires first of all a choice of the SUSY parameters description. Next, strong and EW interactions effects must be computed (in a possibly terrifying way, where a number  $N \gg 1$  of infinities must be exactly cancelled) and suitable definitions for certain parameters must be adopted.

A particularly relevant example of the latter sentence is that of the choice of the bottom mass.

At the lowest order, page 7,  $m_b$  is taken as the “pole mass”. But as soon as one moves to higher orders, this definition is not always safe and other renormalization schemes are preferable, see e.g. Beneke and Singer, Phys.Lett.B471, 233 (1999).

In the specific MSSM case, a particularly convenient choice for  $m_b$  is that of the Dimensional Reduction renormalization scheme, (Siegel, Phys.Lett.B84, 193 (1979)), as discussed in detail by Heinemeyer, Hollik, Rzehak and Weiglein, Eur.Phys.J C39, 465 (2005). Different “mixed” choices are however allowed (with some care).

In the 5FNS treatment of the four considered "semi-inclusive" production processes one finds two types of QCD corrections, that might be called of "diagrammatic" and "bottom pdf" origin.

The latter ones originate from the (known) fact that in the 5FNS the bottom parton is described by a proper pdf that resums collinear logarithms and is already of  $O(\alpha_s)$  (see discussion and references of Dawson et al., page 2).

Moving to NLO replaces the LO version (CTEQ6L) with the NLO one ( ).

## The SM and SUSY QCD NLO

“diagrammatic” corrections for the considered “associated” processes in the 5FNS have been computed by a number of honourable authors, to my knowledge:

Zhu, Phys.Rev.D67,075006 (2003);

Plehn, Phys.Rev. D67, 014018, (2003)

Gao,Lu,Xiong, Yang, Phys.Rev.D66, 015007(2002);

Berger et al., page 2;

Campbell,Ellis,Maltoni and Willenbrock, Phys.Rev.D67,095002 (2003);

Dawson et al., page 2.

As a general feature, SM QCD corrections to the total rates are large and positive, while SUSY QCD effects are negative and sizeable for large values, e.g.  $>10$ , of  $\tan\beta$ . This can be relatively easily understood as a consequence of the special large  $\tan\beta$  parametrization of these effects originally proposed by Carena et al. (page 5), with the introduction of an “Effective” Yukawa Lagrangian replacing that of Page 7 and containing the “glorious” parameter  $\Delta\tilde{t}$ .

At the origin of the formalism there is the simple observation (Carena et al., page 5) that in the lowest order Yukawa Lagrangian (page 7) the bottom quark only interacts with d-type Higgses, while at higher MSSM order an interaction of SUSY QCD origin with u-type Higgses is introduced by the following diagram (next page).

Starting from this observation and after bright steps one is led to a description of the 4 processes valid in the large  $\tan\beta$  range (in fact, the leading  $\tan\beta$  effects are resummed to all orders) and based on an “effective” Yukawa Lagrangian where a modified bottom mass enters:



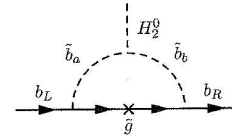


Figure 1: One-loop SUSY-QCD diagram contributing to the effective coupling  $\Delta h_b$ . The solid lines inside the loop denote the gluino propagator, the dashed lines correspond to sbottom propagators. The cross represents the  $M_{\tilde{g}}$  insertion coming from the gluino propagator.

$$\mathcal{L}_{\text{eff}}^{(q\bar{q})} = \frac{1}{v} \frac{\overline{m}_b(Q)}{1 + \Delta m_b}.$$

$$\begin{aligned} & \left\{ \left[ \frac{\sin \alpha}{\cos \beta} - \Delta m_b \frac{\cos \alpha}{\sin \beta} \right] \bar{b} b h_0 + \right. \\ & + \left[ -\frac{\cos \alpha}{\cos \beta} + \Delta m_b \frac{\sin \alpha}{\sin \beta} \right] \bar{b} b H_0 + \\ & + \left[ \tan \beta \right] i \bar{b} \gamma_5 b A_0 + \\ & \left. + \left[ \sqrt{2} \tan \beta (H^+ \bar{t}_L b_R + H^- \bar{b}_R t_L) \right] \right\} \end{aligned}$$

where  $Q$  is the "typical" energy scale of the process ( $\sim M_{H^\pm + t}$  or  $M_h$ ) and  $\overline{m}_b$  is computed in a safe renormalization scheme (e.g.  $\overline{DR}$ ).

( $V_{tb}$  assumed to be  $\pm 1$  ...) (in  $H^\pm V_{tb} \bar{t}_L b_R$ )

The SUSY QCD contribution to  $\Delta_{ab}$  depends on the values of the involved MSSM parameters. For certain choices one sees that  $\Delta_{ab}$  can be positive, proportional to  $\tan\beta$  and thus large. The denominator  $(1+\Delta_{ab})$  therefore decreases the rates of the processes.

In conclusion, NLO QCD effects are known (with their related theoretical uncertainty, due to factorization and renormalization scale dependence, discussed in the quoted references).

What about NLO electroweak corrections?<sup>19</sup>

For the considered processes, NLO MSSM EW radiative corrections have been computed in the following ways:

Dawson et al., page 2, (bh) have used a “generalized  $\Delta_{\text{tab}}$ ” approach. Beyond the gluino-sbottom graph of page 17, there are similar SUSY EW graphs, e.g. one with chargino-stop. This can be resummed and provides a “ $\Delta_{\text{tabEW}}$ ” effect which is also enhanced for large  $\tan\beta$  and is supposed to be the dominant SUSY EW contribution. Numerical results are given in this approximation.

Berger et al., page 2, add to the SUSY QCD Deltab term other NLO “Supersymmetric contributions”. In the (usual) large tanbeta limit, these extra MSSM “non SUSY QCD Deltab” effects are small and negligible. MSSM EW effects seem not to be relevant.

The “dignity” of MSSM EW effects is reconsidered in the “fully inclusive” process of h production by bottom fusion in a paper By Dittmaier, Kramer, Muck and Schluter (JHEP 0703, 114(2007) ).

This paper performs the complete NLO MSSM EW calculation for the process and separates the resummed extra “EW Deltab” effects (wino-higgsino-stop, wino-higgsino-sbottom,..) from the “remaining” ones.

The result is that the EW Deltab effects are well competitive with the SUSY QCD ones, and of opposite sign. The “remaining” ones give a smaller (relative few percent) effect.

Our conclusion is that these NLO MSSM EW effects must be accurately computed.

This is what we did.

For top-charged Higgs calculation:  
Beccaria, Macorini, Panizzi, Renard,  
C.V., Phys.Rev.D80,053011,(2009).

For bottom-neutral Higgs calculation  
Beccaria, Davier, Macorini, Mirabella,  
Renard, C.V., arXiv:1005.0759(hep-  
ph). A more recent version with extra  
calculations and the same authors  
exists, arXiv:

For the top polarization in tH  
production , a preliminary version  
exists, Beccaria, Djouadi, Davier,  
Macorini, Renard, C.V.

In all papers, the complete one-loop MSSM EW effects (including QED) have been computed.

NLO QCD has not been included (it already exists).

The resummed SUSY QCD  $\Delta_{\text{tab}}$  term has been inserted in the  $bh$  production processes, and omitted in the  $tH$  production case.



The EW calculation is valid for all  $\tan\beta$  values, including the usually neglected “small” ones. SM entry alpha, MW, MZ.

For bh we chose the Dimensional Reduction Renormalization scheme, with the (kinematical) bottom mass defined in the OS system.

For tH we chose the Wan, Ma, Zhang, Yang (Phys.Rev. D 64, 115004-2001-) Renormalization scheme, with the b, t masses on shell.

The bottom pdf has been computed in the  $\overline{\text{MS}}$  system at scale  $(M_t + M_H)$  or  $M_h$ .

All the definitions of the various counterterms can be found in the two first quoted papers (a partial illustrative set of figures is enclosed).

We have calculated invariant mass distributions and total rates with only EW (and SUSY QCD for  $bh$ ) NLO effects for different parameter space scenarios, for the MSSM and for the 2HDM.

tH

The c.t. appearing in the above expressions are obtained in terms of self-energies as follows:

**b and t quark**

$$\delta Z_L^b = \delta Z_L^t \equiv \delta Z_L = -\Sigma_L^b(m_b^2) - m_b^2[\Sigma_L^b(m_b^2) + \Sigma_R^b(m_b^2) + 2\Sigma_S^b(m_b^2)] \quad (\text{A16})$$

$$\delta Z_R^b = -\Sigma_R^b(m_b^2) - m_b^2[\Sigma_L^b(m_b^2) + \Sigma_R^b(m_b^2) + 2\Sigma_S^b(m_b^2)] \quad (\text{A17})$$

$$\delta Z_R^t = \delta Z_L + \Sigma_L^t(m_t^2) - \Sigma_R^t(m_t^2) \quad (\text{A18})$$

$$\delta \Psi_t = -\{\Sigma_L^t(m_t^2) + \delta Z_L + m_t^2[\Sigma_L^t(m_t^2) + \Sigma_R^t(m_t^2) + 2\Sigma_S^t(m_t^2)]\} \quad (\text{A19})$$

$$\delta m_b = \frac{m_b}{2} \text{Re}[\Sigma_L^b(m_b^2) + \Sigma_R^b(m_b^2) + 2\Sigma_S^b(m_b^2)] \quad (\text{A20})$$

$$\delta m_t = \frac{m_t}{2} \text{Re}[\Sigma_L^t(m_t^2) + \Sigma_R^t(m_t^2) + 2\Sigma_S^t(m_t^2)] \quad (\text{A21})$$

**gauge boson**

$$\delta Z_1^W - \delta Z_2^W = \frac{\Sigma^{\gamma Z}(0)}{s_W c_W M_Z^2} \quad (\text{A22})$$

$$\delta Z_2^W = -\Sigma^{\gamma\gamma}(0) + 2\frac{c_W}{s_W M_Z^2} \Sigma^{\gamma Z}(0) + \frac{c_W^2}{s_W^2} \left[ \frac{\delta M_Z^2}{M_Z^2} - \frac{\delta M_W^2}{M_W^2} \right] \quad (\text{A23})$$

$$\delta M_W^2 = \text{Re} \Sigma^{WW}(M_W^2) \quad \delta M_Z^2 = \text{Re} \Sigma^{ZZ}(M_Z^2) \quad (\text{A24})$$

**Higgs boson**

We need  $\delta Z_{j1}^*$  which means  $\delta Z_{H^-H^-}^*$  and  $Z_{G^-H^-}^*$ . We use the on-shell procedure of Wan et al [18] in which

$$\delta Z_{H^-H^-} = -\Sigma'_{H^-}(p^2 = m_{H^-}^2) \quad (\text{A25})$$

and

$$\delta Z_{G^-H^-}^* = \delta Z_{G^+H^+} = -\frac{2\Sigma_{H^-W^-}^*(m_{H^-}^2)}{M_W} = \frac{2\Sigma_{H^+W^+}(m_{H^+}^2)}{M_W} \quad (\text{A26})$$

**Couplings**

The Yukawa  $btH^-$  coupling leads to the c.t.  $\delta c^L$  and  $\delta c^R$ , computed in terms of  $\delta g$ ,  $\delta m_{t,b}$ ,  $\delta M_W$  (given above) and  $\delta \tan \beta$ . For the latter, we have adopted the renormalization scheme of [18].

calculations are collected in Appendix B.

### Higgs sector

As anticipated we performed the calculation using two different renormalization schemes: the  $\overline{\text{DR}}$  scheme [14] is defined by the following renormalization conditions

$$\begin{aligned}
\delta Z_{H_1}^{\overline{\text{DR}}} &= - \left[ \text{Re} \frac{\partial \Sigma_{H^0}(k^2)}{\partial k^2} \Big|_{k^2=M_{H^0}^2, \alpha=0} \right]_{\text{div}} \\
\delta Z_{H_2}^{\overline{\text{DR}}} &= - \left[ \text{Re} \frac{\partial \Sigma_{h^0}(k^2)}{\partial k^2} \Big|_{k^2=M_{h^0}^2, \alpha=0} \right]_{\text{div}} \\
\delta T_{h^0} &= -T_{h^0} \\
\delta T_{H^0} &= -T_{H^0} \\
\delta M_{A^0}^2 &= \text{Re} \Sigma_{A^0}(M_{A^0}^2) - M_{A^0}^2 \Sigma'_{A^0}(M_{A^0}^2) \\
\delta \tan \beta^{\overline{\text{DR}}} &= \frac{1}{2} (\delta Z_{H_2}^{\overline{\text{DR}}} - \delta Z_{H_1}^{\overline{\text{DR}}}) \tan \beta.
\end{aligned} \tag{10}$$

$\delta Z_{H_i}^{\overline{\text{DR}}}$  define the wave function renormalization constant of the Higgs field  $H_i$ , the third and fourth line fix the tadpole renormalization and the last one the  $\tan \beta$  renormalization constant.  $[\mathcal{A}]_{\text{div}}$  means keeping the UV divergent part of  $\mathcal{A}$ , discarding the finite contribution. In the DCPR scheme [15, 16] the independent parameters are the same, and the renormalization conditions of the Higgs wavefunctions change as follows

$$\begin{aligned}
\delta Z_{H_1}^{\text{DCPR}} &= -\text{Re} \frac{\partial \Sigma_{A^0}(k^2)}{\partial k^2} \Big|_{k^2=M_{A^0}^2} - \frac{1}{\tan \beta M_Z} \text{Re} \Sigma_{A^0 Z}(M_{A^0}^2) \\
\delta Z_{H_2}^{\text{DCPR}} &= -\text{Re} \frac{\partial \Sigma_{A^0}(k^2)}{\partial k^2} \Big|_{k^2=M_{A^0}^2} + \frac{\tan \beta}{M_Z} \text{Re} \Sigma_{A^0 Z}(M_{A^0}^2) \\
\delta T_{h^0} &= -T_{h^0} \\
\delta T_{H^0} &= -T_{H^0} \\
\delta M_{A^0}^2 &= \text{Re} \Sigma_{A^0}(M_{A^0}^2) - M_{A^0}^2 \Sigma'_{A^0}(M_{A^0}^2) \\
\delta \tan \beta^{\text{DCPR}} &= \frac{1}{2} (\delta Z_{H_2}^{\text{DCPR}} - \delta Z_{H_1}^{\text{DCPR}}) \tan \beta
\end{aligned} \tag{11}$$

We choose to impose on-shell (OS) condition for the mass of CP-odd  $A^0$  Higgs in both schemes.

The renormalization constants of the Higgs bosons wavefunctions and of the  $c^\eta(bb\mathcal{H}^0)$  couplings can be written in terms of the renormalization constants defined above.

## A few illustrative Figures.

In the  $bh$  process we have (also) determined the EW K factor, defined as the ratio of the computed one-loop (BORN +SUSY QCD + MSSM EW) rate to the (BORN +SUSY QCD) one. We have considered a “SPP2” scenario with fixed  $M_A=250$  GEV and input parameters shown in next Table. The sparticle masses and mixing angles have been obtained with the code FeynHiggs. The results for  $A_0, H_0, h_0$  production are shown in the next Figure.

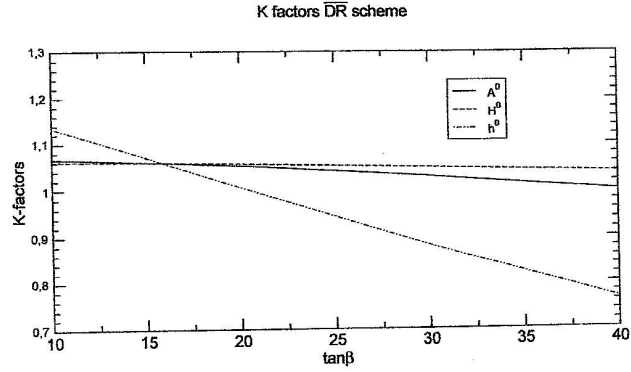


FIG. 14:  $K$ -factors for  $A^0$ ,  $H^0$  and  $h^0$  production,  $\overline{\text{DR}}$  scheme.  $M_{A^0} = 250$  GeV,  $p_{b,T} > 20$  GeV,  $|y_b| < 2$ .

Scenario	$\tan \beta$	$M_{A^0}$	$M_{\tilde{q},1}$	$M_{\tilde{q},2}$	$M_{\tilde{q},3}$	$M_1$	$M_2$	$M_{\tilde{g}}$
SPP <sub>1</sub>	15	350	350	350	250	90	150	800
SPP <sub>2</sub>	variable	250	500	500	400	90	200	800

TABLE I: Inputs parameters for the SUSY scenarios considered in our numerical discussion.  $M_{\tilde{q},j}$  is the common value of the breaking parameters in the sector of the squarks belonging to the  $j^{\text{th}}$  generation. The dimensionful parameters are given in GeV.

## What about tH?

We have computed the purely EW (no SUSY QCD) MSSM K factor in two mSugra scenarios +SUSPECT ( tables).

The EW effect is modest for  $\tan\beta = 10$ . For  $\tan\beta = 50$ , it reaches a relative 20 percent size (to be compared with possible 30-40 percent effects for Berger et al.)

Again, it appears that MSSM EW NLO effects can be relevant and should be fully computed.

As one sees from the Figure, the NLO MSSM EW effect is indeed “modest” (a few percent) for  $A_0$  and  $H_0$ . But for  $h_0$  it becomes large and negative (a relative 20 percent) when  $\tan\beta$  approaches 40, and is of opposite sign (a relative 10 percent) and apparently increasing when  $\tan\beta$  approaches 10 (smaller  $\tan\beta$  values are being computed...).

Certainly, for  $bh_0$  production the NLO MSSM EW effect should not be “assumed” to be negligible.



mSUGRA scenario	$m_0$	$m_{1/2}$	$A_0$	$\tan \beta$	sign $\mu$	$H^-$	$\alpha_s(Q)$
LS2	300	150	-500	50	+	229.6	0.0965325
SPS1a	100	250	-100	10	+	412.1	0.0922963

Table II: input parameters for the mSUGRA benchmark points and mass of the charged Higgs  $H^-$  (all values with mass dimension are in GeV)

mSUGRA scenario	$\sigma_{Born}$	SUSY		2HDM	
		$\sigma_{1-loop}$	K-factor	$\sigma_{1-loop}$	K-factor
LS2	5.589	4.545	0.813	5.867	1.050
SPS1a	0.04207	0.04145	0.985	0.04170	0.991

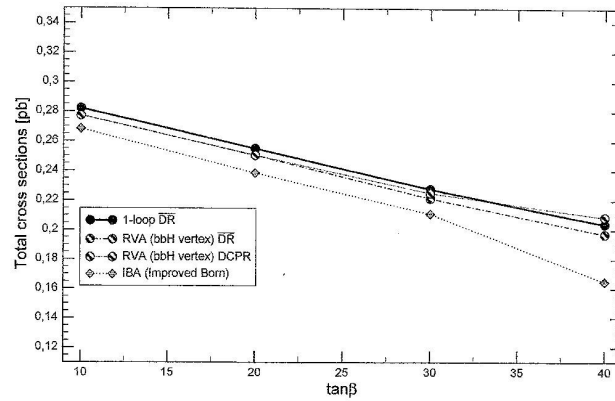
Table III: Total cross sections (in pb) at Born and loop level and K-factors

A reasonable question that arises at this point, having verified the possible relevance of the complete NLO EW MSSM effects, is the following one:

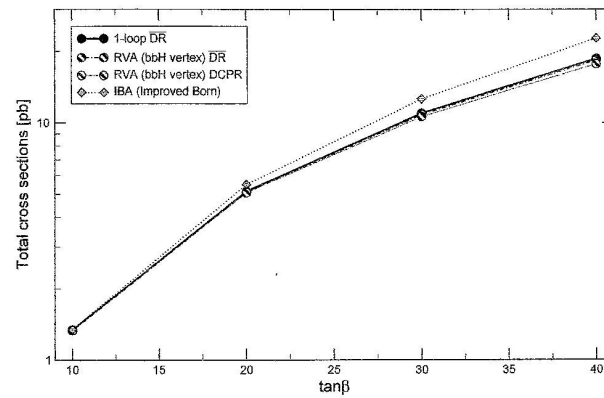
Are the EW effects of “non Deltab type” really important? In other words, could one use the (much simpler) “Improved Born Approximation” with only resummed SUSY QCD and (all) EW Deltab terms, like in the Dittmaier et al. b-fusion paper, where these contributions seem to be by far the leading ones?

To find an answer to this question, we have compared our full one-loop calculation with the mentioned IBA, keeping in both terms the full resummed SUSY QCD  $\Delta_{ab}$  term and allowing as in the previous example  $\tan\beta$  to vary in the SPP2 scenario with  $M_A = 250$  GEV. The results are shown in the following Figures.

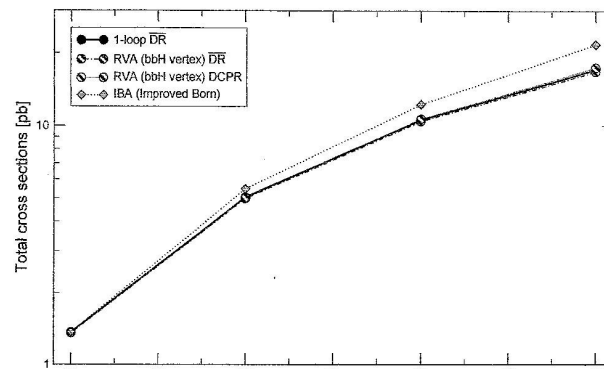
$h_0$  production, total cross sections, NLO  $\overline{\text{DR}}$  and approximations



$H_0$  production, total cross sections, NLO  $\overline{\text{DR}}$  and approximations



$A_0$  production, total cross sections, NLO  $\overline{\text{DR}}$  and approximations



As one sees from the Figure, there is a rather strong difference between the complete one-loop calculation and the IBA, that reaches a relative 25 percent size for large  $\tan\beta$ .

In the same Figures, one sees the result of a different “Reduced Vertex Approximation”, RVA, that sums at one loop effects of a larger number of bottom vertices and reproduces much better the complete calculation.

So for bh IBA seems to be in trouble.

Which special information can be obtained by NLO MSSM effects?

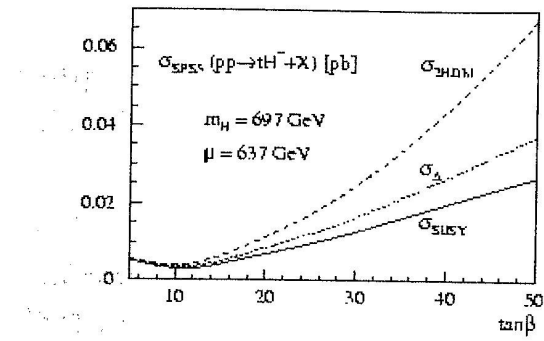
As a first example, we considered the ratio of the MSSM and 2HDM rates at variable  $\tan\beta$  (with another parameter e.g.  $M_{A0}$  kept fixed).

This ratio should be SM QCD independent, and would therefore provide the size of the “Genuine” SUSY content (including SUSY QCD) of the MSSM with reasonable accuracy.

This ratio has already been computed for  $tH$  by Berger et al. in a certain scenario and has provided a Figure containing only a part of the MSSM EW NLO with the SUSY QCD  $\Delta b$  term. (see next page).

As one sees, the 2HDM rate is much larger for large  $\tan\beta$  (almost a factor 2 for  $\tan\beta = 40$ ) but coincides with the MSSM when  $\tan\beta$  becomes smaller.

This is what one would expect from the presence of the  $\Delta b$  term.

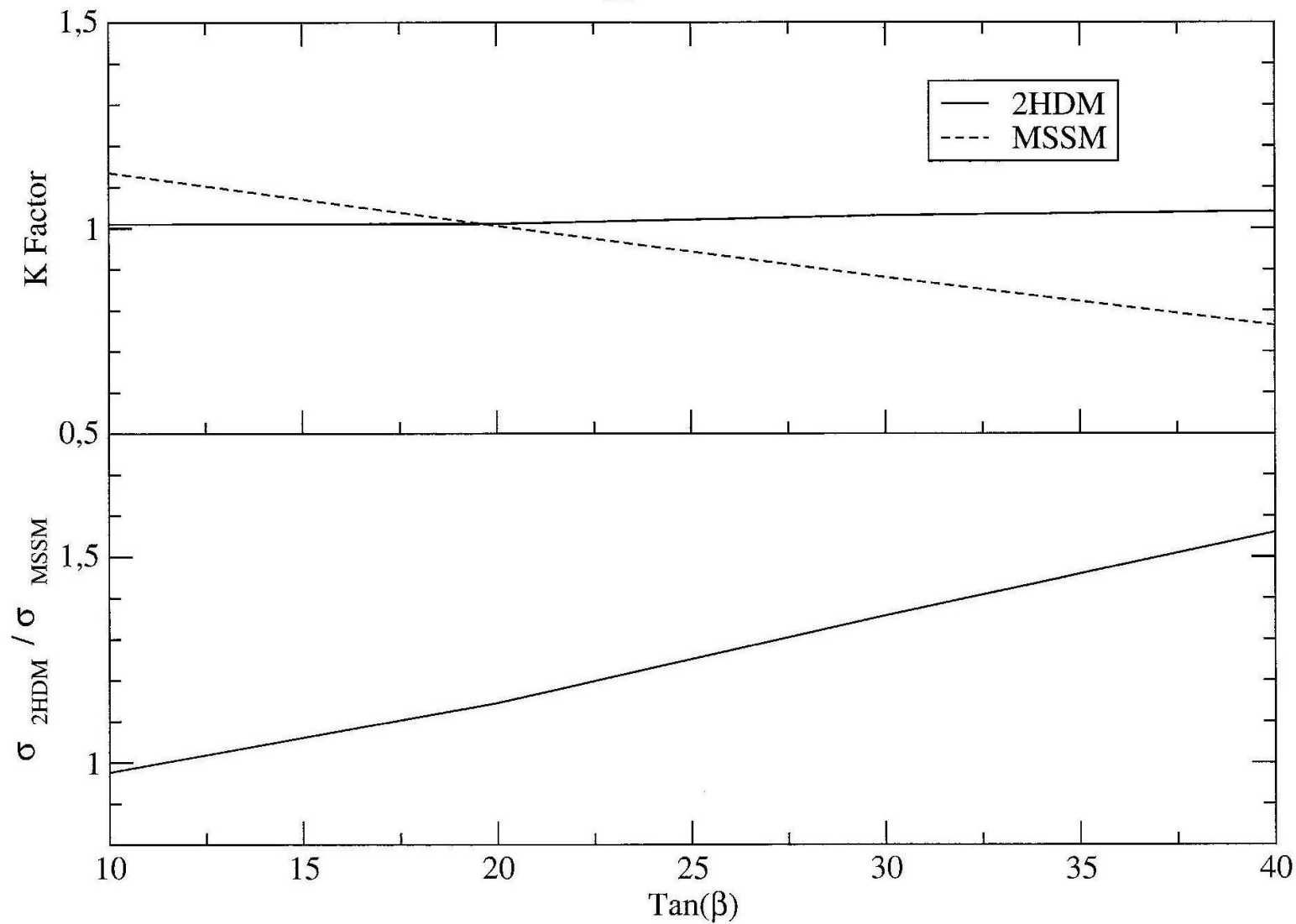




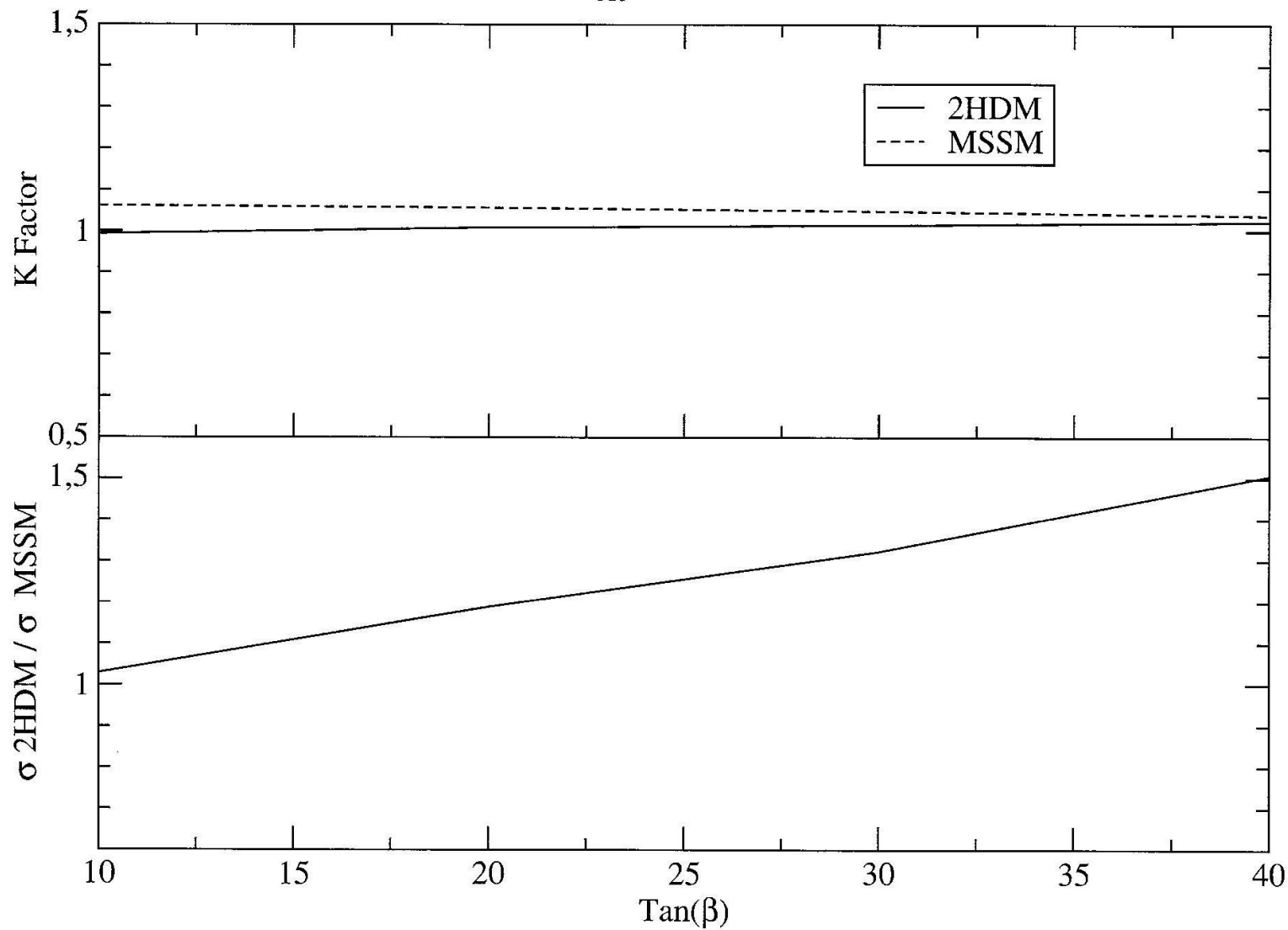
We have performed the same comparison for bh, again allowing tanbeta to vary for fixed MA at different values. Only the MA=250 Figures are shown.

# h0 Production

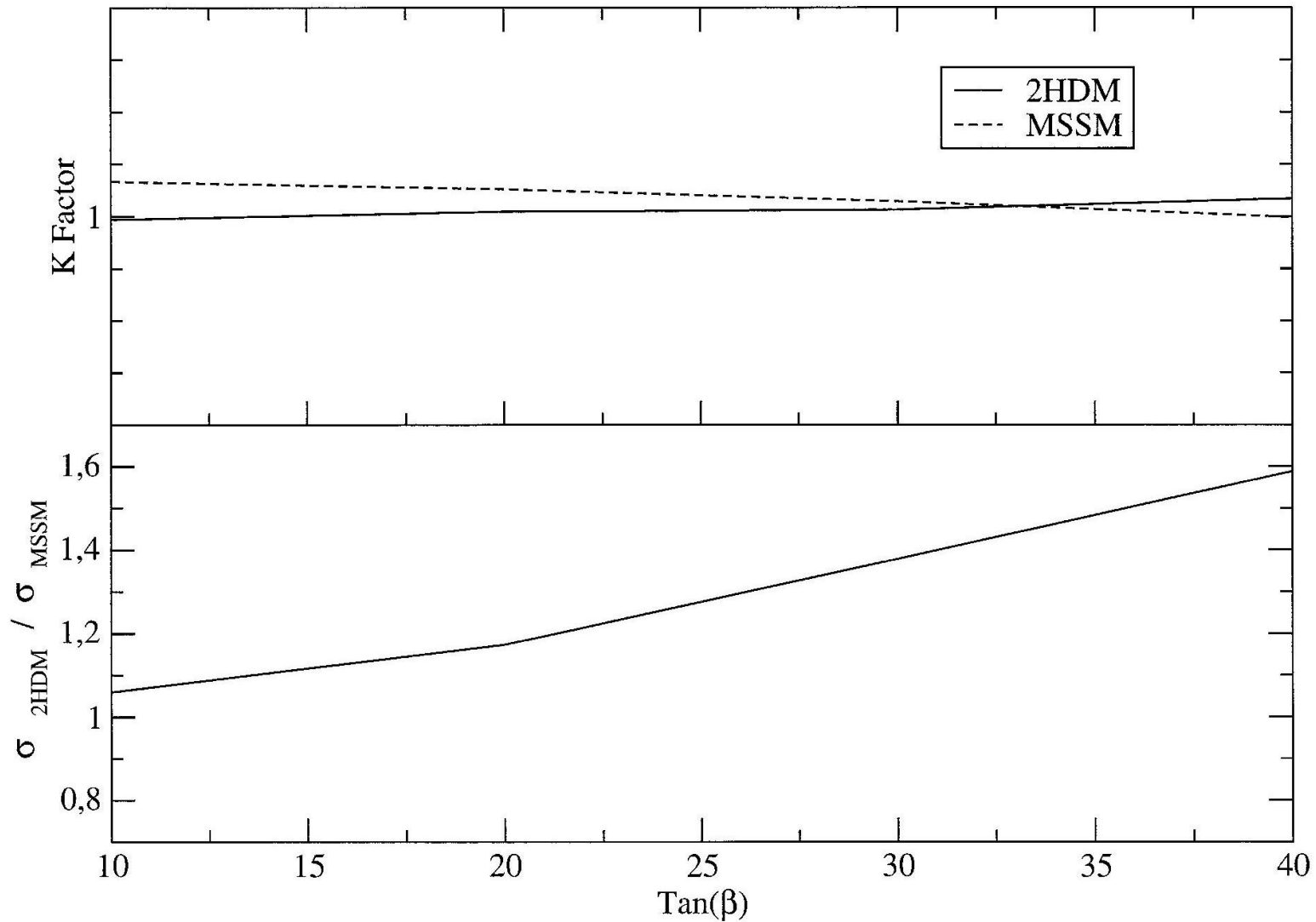
$M_{A0} = 250 \text{ GeV}$



$H_0$  Production  
 $M_{A0} = 250$  GeV



$A_0$  Production  
 $M_{A0} = 250$  GeV



As one sees from the Figures, the 2HDM provides a rate whose ratio with the MSSM one follows the identical  $\tan\beta$  behaviour in all neutral Higgs cases. For large  $\tan\beta$  the 2HDM rate is definitely larger, moreless like in the Berger plot.

If  $\tan\beta$  were known, it might be possible to identify the “true” Model.

This leads to the last question of my presentation: could  $\tan\beta$  be measured?

A problem to identify SUSY parameters is the presence of strong interactions that introduce in the theoretical estimate a “scale” uncertainty that is sometimes as large as the SUSY effect to be measured.

On the other hand, strong interactions increase the value of the rates, which produces more statistics----> they are “useful”.

The situation appears to me somehow similar to the old case of LEP1 Hadron production at the Z resonance.

The idea was to define an observable that was independent of strong interactions (Lynn, C.V., Phys.Rev-D35,3326-1987)

i.e.:

The Longitudinal Polarization Asymmetry ( $A_{lr}(MZ)$ ).

First question: does such an observable exist in one of the considered processes? In principle, Yes for the tH process (rates for tl and tr production are certainly different).

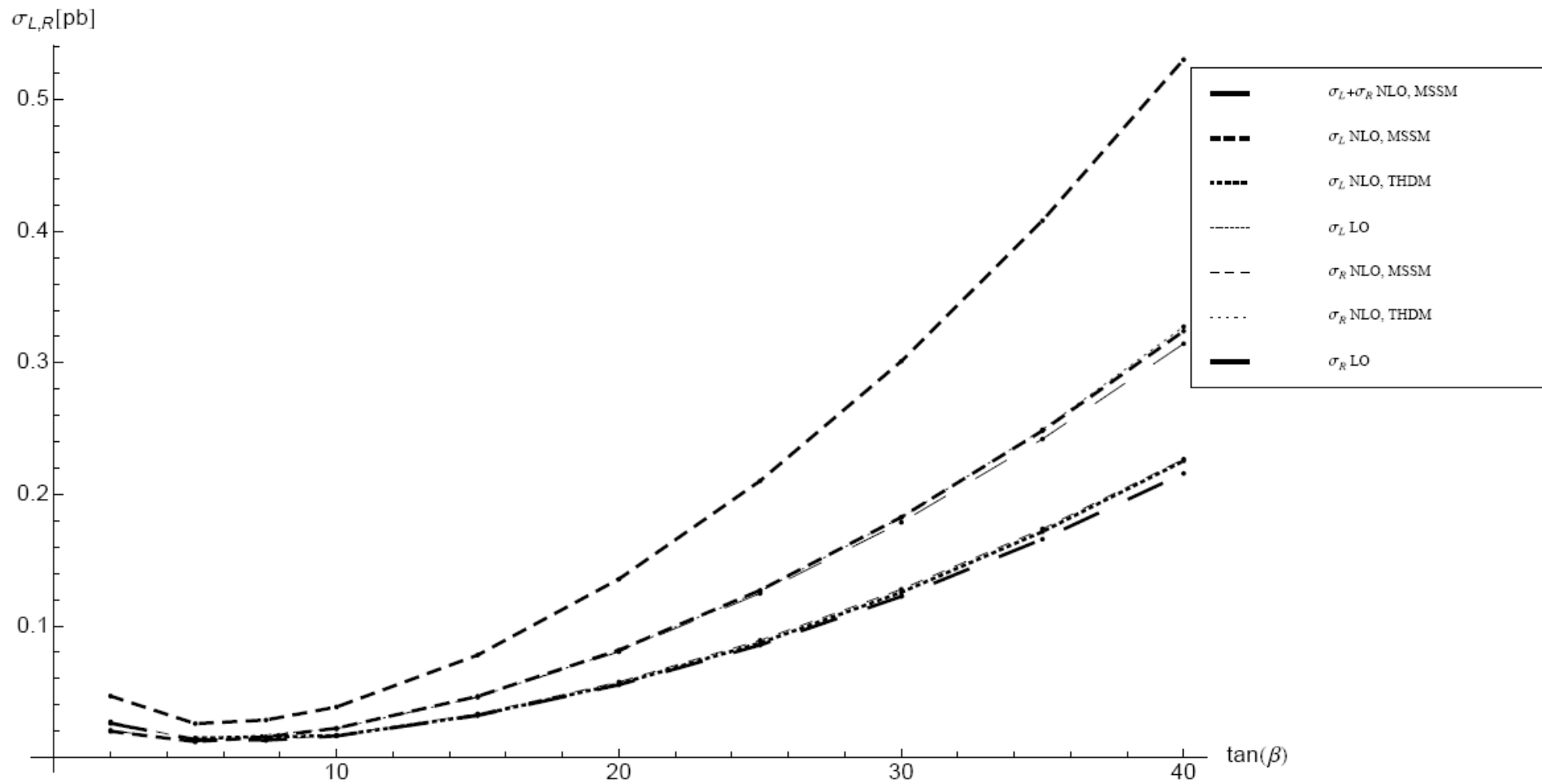
A detailed discussion of possible measurements of top polarization asymmetry from charged slepton production, suggesting the “natural extension” of the work to the process of  $tH$  production, has very recently been provided by

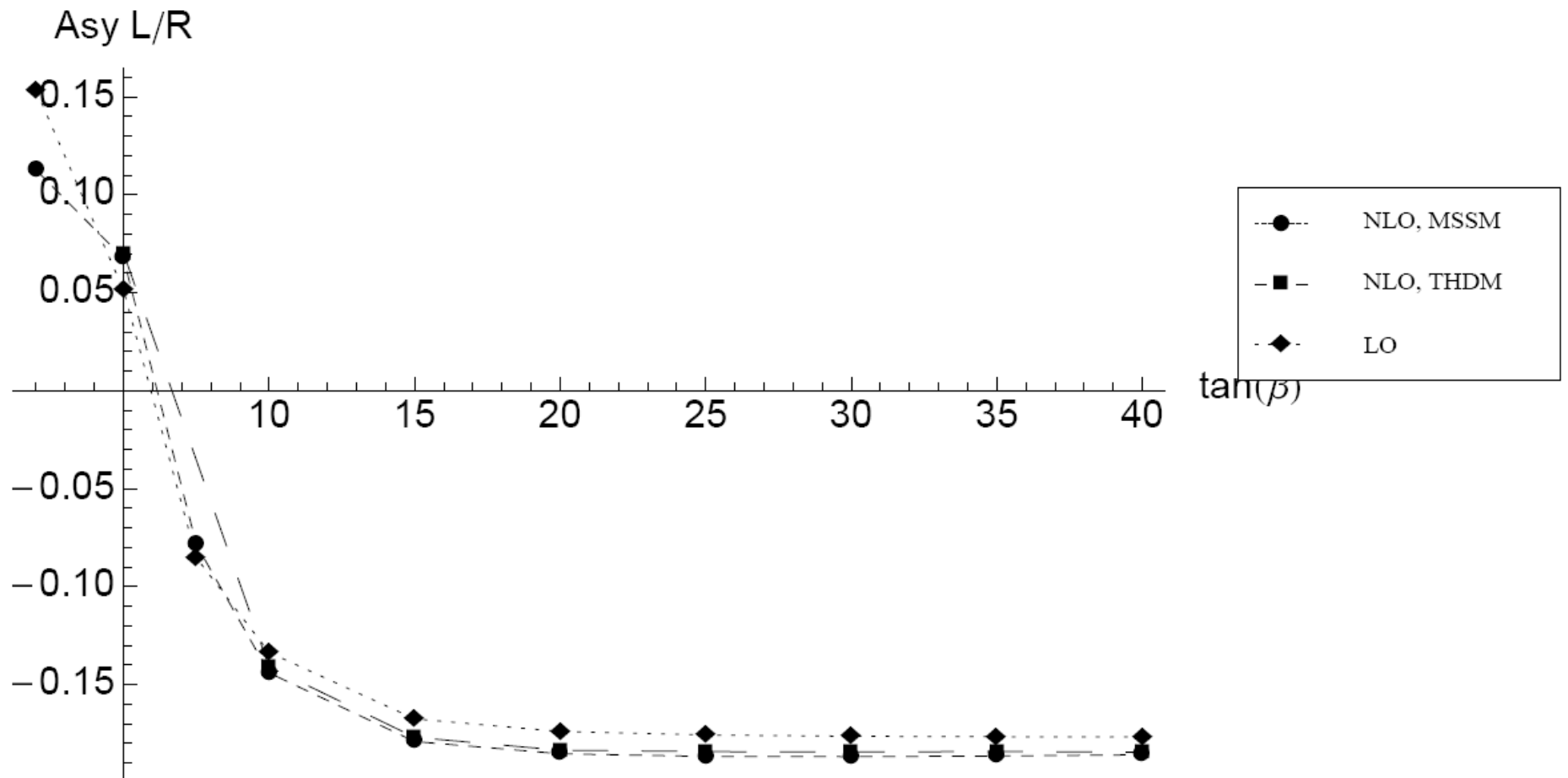
Arai, Huitu, Rai and Rao,  
ArXiv: 1003.4708V2, (August 2010).



Could a certain longitudinal polarization asymmetry be SM QCD independent (i.e. SUSY detector)?

Before tackling this problem, we computed the purely EW NLO value of this asymmetry, defined as the ratio of difference and sum of the polarized rates, starting from the previously defined tH benchmark point (SPS1) and allowing  $\tan\beta$  to vary with SUSPECT. Next (preliminary!!) Figures show the tH rates and left-right asymmetry.





Qualitatively : one sees a potentially relevant feature in the low  $\tan\beta$  region ( $2 < \tan\beta < 10$ ) , with a drastic change of sign. But SUSY QCD could be also relevant, and should be computed (Beccaria, Djouadi, Dovier, Macorini, Renard, C.V., in progress).

Our hope: SM QCD might cancel in the ratio (to be checked).

Then  $A_{lr}$  might be considered as a possible “ SUSY measurement ” in the all  $\tan\beta$  region, if combined with measurements of all  $tH$  and  $bh$  rates.

# Conclusions.

The role of the NLO MSSM SUSY corrections appears to be relevant both at the QCD and at EW level in the production of tH and bh.

It seems appropriate to compute the  $\Delta_{\text{tab}}$  QCD effect, correctly resummed, independently of the complete NLO EW contribution: no separation of “privileged” resummed  $\Delta_{\text{tabEW}}$  terms and “poor people” remaining NLO EW ones:

**DEMOCRACY MUST WIN!!!**

A lot of work on these processes has been done.

A lot of work on these processes has still to be (and is being) done.