

# Flavor data constraints on supersymmetry

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### Searches for New Physics

- direct detection of new physics particles
- nature of Dark Matter
- indirect evidence for new physics

### Indirect constraints

- search for new physics effects
- guideline for other searches
- check consistencies with direct observations

# Indirect Constraints

## Flavor observables

- 1 Penguin mediated observables
- 2 Neutral Higgs mediated observables
- 3 Charged Higgs mediated observables

## Other observables

- 1 Direct search limits
- 2 Anomalous magnetic moment of muon  $a_\mu = (g - 2)/2$
- 3 Relic density

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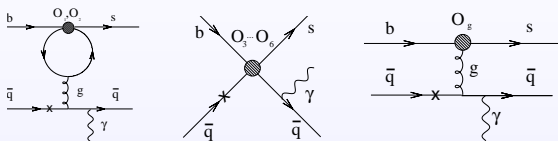
## Flavor observables

## 1) Penguin mediated observables

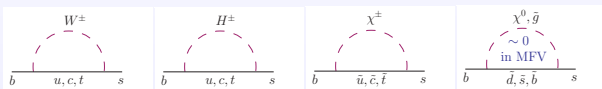
- inclusive branching ratio of  $B \rightarrow X_s \gamma$
- isospin asymmetry of  $B \rightarrow K^* \gamma$

# 1) Penguin mediated observables

## Isospin asymmetry of $B \rightarrow K^* \gamma$ at NLO



Contributing loops:



$$\Delta_{0-} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) - \Gamma(B^- \rightarrow K^{*-} \gamma)}{\Gamma(\bar{B}^0 \rightarrow \bar{K}^{*0} \gamma) + \Gamma(B^- \rightarrow K^{*-} \gamma)}$$

$$\Delta_{0-} = \text{Re}(b_d - b_u), \quad b_q = \frac{12\pi^2 f_B Q_q}{m_b T_1^{B \rightarrow K^*} a_7^c} \left( \frac{f_{K^*}^\perp}{m_b} K_1 + \frac{f_{K^*} m_{K^*}}{6\lambda_B m_B} K_2 \right)$$

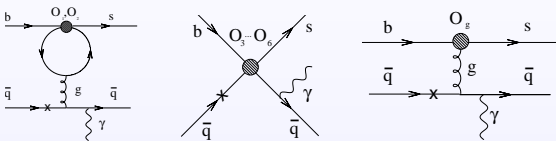
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In the Standard Model:  $\Delta_{0-} \simeq 8\%$

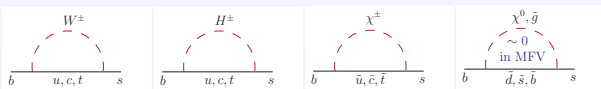
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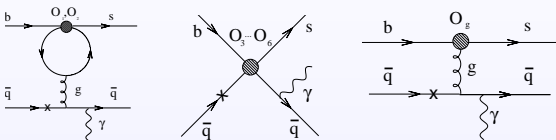
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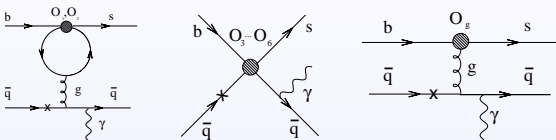
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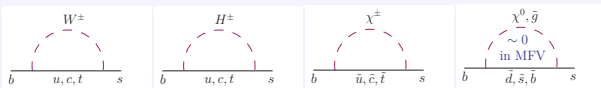
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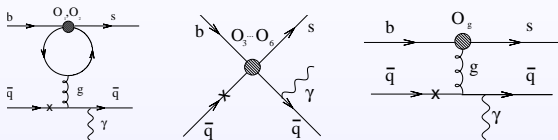
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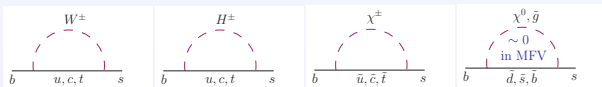
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$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma)_{E_\gamma > E_0} = \mathcal{B}(\bar{B} \rightarrow X_c e \bar{\nu})_{\text{exp}} \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right|^2 \frac{6\alpha_{\text{em}}}{\pi C} [P(E_0) + N(E_0)]$$

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SM prediction:  $\mathcal{B}[\bar{B} \rightarrow X_s \gamma] = (3.15 \pm 0.23) \times 10^{-4}$ Experimental values (HFAG 2008):  $\mathcal{B}[\bar{B} \rightarrow X_s \gamma] = (3.52 \pm 0.25) \times 10^{-4}$

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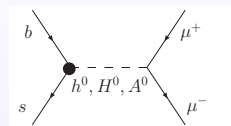
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Upper limit:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.8 \times 10^{-8}$  at 95% C.L.

SM predicted value:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{SM} \sim 3 \times 10^{-9}$

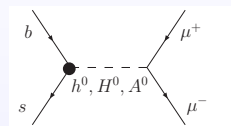
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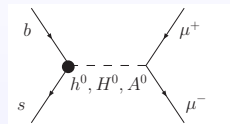
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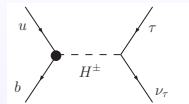
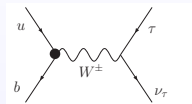
## III) Charged Higgs mediated observables

- branching ratio of  $B \rightarrow \tau\nu$
- branching ratio of  $B \rightarrow D\tau\nu$
- branching ratio of  $K \rightarrow \mu\nu$
- branching ratios of  $D_s \rightarrow \tau\nu/\mu\nu$

### III) Charged Higgs mediated observables

#### Branching ratio of $B \rightarrow \tau \nu$

Tree level process, mediated by  $W^+$  and  $H^+$ , higher order corrections from sparticles



$$\mathcal{B}(B \rightarrow \tau \nu) = \frac{G_F^2 |V_{ub}|^2}{8\pi} m_\tau^2 f_B^2 m_B \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \left|1 - \left(\frac{m_B^2}{m_{H^+}^2}\right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right|^2$$

$$\epsilon_0 = -\frac{2\alpha_s}{3\pi} \frac{\mu}{m_{\tilde{g}}} H_2 \left(\frac{m_Q^2}{m_{\tilde{g}}^2}, \frac{m_D^2}{m_{\tilde{g}}^2}\right), \quad H_2(x, y) = \frac{x \ln x}{(1-x)(x-y)} + \frac{y \ln y}{(1-y)(y-x)}$$



Large uncertainty from  $V_{ub}$

Also used:

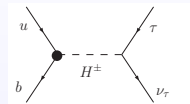
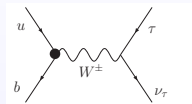
$$R_{\tau \nu \tau}^{\text{MSSM}} = \frac{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{MSSM}}}{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{SM}}} = \left[1 - \left(\frac{m_B^2}{m_{H^+}^2}\right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right]^2$$



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Tree level process, mediated by  $W^+$  and  $H^+$ , higher order corrections from sparticles



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$$\epsilon_0 = -\frac{2\alpha_s}{3\pi} \frac{\mu}{m_{\tilde{g}}} H_2 \left(\frac{m_Q^2}{m_{\tilde{g}}^2}, \frac{m_D^2}{m_{\tilde{g}}^2}\right), \quad H_2(x, y) = \frac{x \ln x}{(1-x)(x-y)} + \frac{y \ln y}{(1-y)(y-x)}$$



Large uncertainty from  $V_{ub}$

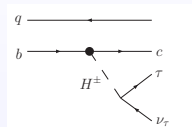
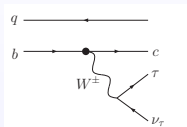
Also used:

$$R_{\tau \nu \tau}^{\text{MSSM}} = \frac{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{MSSM}}}{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{SM}}} = \left[1 - \left(\frac{m_B^2}{m_{H^+}^2}\right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right]^2$$

## III) Charged Higgs mediated observables

Branching ratio of  $B \rightarrow D\tau\nu$ 

Another tree level process:



$$\frac{d\Gamma(B \rightarrow D\ell\bar{\nu})}{dw} = \frac{G_F^2 |V_{cb}|^2 m_B^5}{192\pi^3} \rho_V(w) \left[ 1 - \frac{m_\ell^2}{m_B^2} \left| 1 - \frac{t(w)}{(m_b - m_c)} \frac{m_b}{m_{H^\pm}^2} \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|^2 \rho_S(w) \right]$$

 $w = v_B \cdot v_D$      $\rho_V$  and  $\rho_S$ : vector and scalar Dalitz density contributions

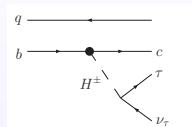
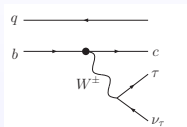
- Depends on  $V_{cb}$ , which is known to better precision than  $V_{ub}$
- Larger branching fraction than  $B \rightarrow \tau\nu$
- Experimentally challenging due to the presence of neutrinos in the final state

Branching ratios:  $\mathcal{B}(B^- \rightarrow D^0 \tau^- \nu)$  and  $\frac{\mathcal{B}(B^- \rightarrow D^0 \tau^- \nu)}{\mathcal{B}(B^- \rightarrow D^0 e^- \nu)}$

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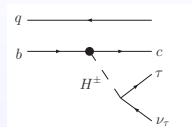
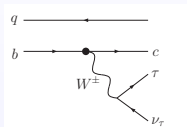
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### III) Charged Higgs mediated observables

Branching ratio of  $K \rightarrow \mu\nu$

Tree level process similar to  $B \rightarrow \tau\nu$

Two observables can be considered:

$$\frac{\Gamma(K \rightarrow \mu\nu)}{\Gamma(\pi \rightarrow \mu\nu)} = \left| \frac{V_{us}}{V_{ud}} \right|^2 \frac{f_K^2 m_K}{f_\pi^2 m_\pi} \left( \frac{1 - m_\ell^2/m_K^2}{1 - m_\ell^2/m_\pi^2} \right)^2$$

$$\times \left( 1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left( 1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right)^2 (1 + \delta_{\text{em}})$$

$$R_{\ell 23} = \left| \frac{V_{us}(K_{\ell 2})}{V_{us}(K_{\ell 3})} \times \frac{V_{us}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\ell 2})} \right| = \left| 1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left( 1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

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## III) Charged Higgs mediated observables

Branching ratio of  $D_s \rightarrow \ell \nu$ Tree level process similar to  $B \rightarrow \tau \nu$ 

$$\mathcal{B}(D_s \rightarrow \ell \nu) = \frac{G_F^2}{8\pi} |V_{cs}|^2 f_{D_s}^2 m_\ell^2 M_{D_s} \tau_{D_s} \left(1 - \frac{m_\ell^2}{M_{D_s}^2}\right)^2 \times \left[1 + \left(\frac{1}{m_c + m_s}\right) \left(\frac{M_{D_s}}{m_{H^+}}\right)^2 \left(m_c - \frac{m_s \tan^2 \beta}{1 + \epsilon_0 \tan \beta}\right)\right]^2 \text{ for } \ell = \mu, \tau$$

- Competitive with and complementary to analogous observables
- Dependence on only one lattice QCD quantity
- Interesting if lattice calculations eventually prefer  $f_{D_s} < 250$  MeV
- Promising experimental situation (BES-III)

Sensitive to  $f_{D_s}$  and  $m_s/m_c$

# Superlso

## Superlso is a public C program

- dedicated to the flavor physics observable calculations
- implemented models: SM, THDM, MSSM and NMSSM with MFV
- interfaced to spectrum calculators (2HDMC, SOFTSUSY, ISAJET, SUSPECT, SPHENO, NMSSMTOOLS)
- Superlso Relic: extension to the relic density calculation, featuring alternative cosmological scenarios

F. Mahmoudi, *Comput. Phys. Commun.* **178** (2008) 745

F. Mahmoudi, *Comput. Phys. Commun.* **180** (2009) 1579

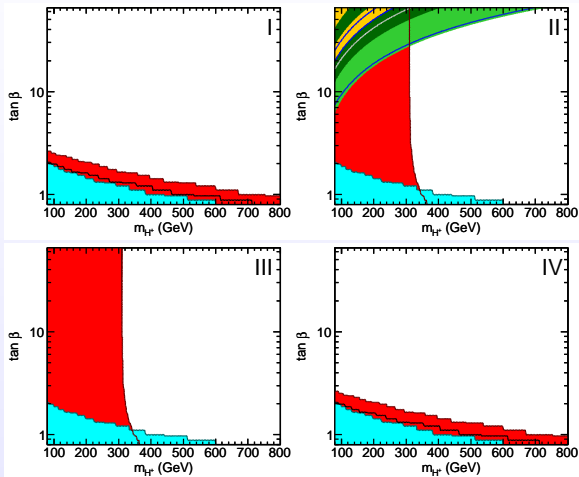
F. Mahmoudi, *Comput. Phys. Commun.* **180** (2009) 1718

A. Arbey & F. Mahmoudi, *Comput. Phys. Commun.* **181** (2010) 1277



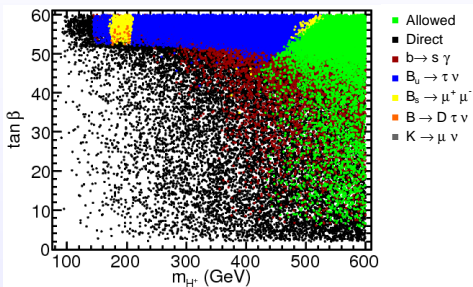
## THDM

## THDM (Types I-IV)

Red:  $b \rightarrow s\gamma$ Cyan:  $\Delta M_{B_d}$ Blue:  $B_u \rightarrow \tau\nu_\tau$ Yellow:  $B \rightarrow D l \nu_l$ Gray:  $K \rightarrow \mu\nu_\mu$ Green:  $D_s \rightarrow \tau\nu_\tau$ Dark green:  $D_s \rightarrow \mu\nu_\mu$ 

F. Mahmoudi &amp; O. Stål, Phys. Rev. D81, 035016 (2010)

## mSUGRA

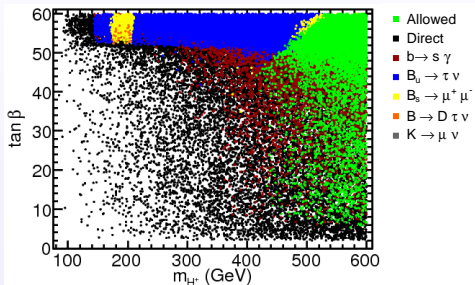


$$m_{H^+} \gtrsim 400 \text{ GeV}$$

D. Eriksson, F. Mahmoudi & O. Stål, JHEP 0811 (2008)

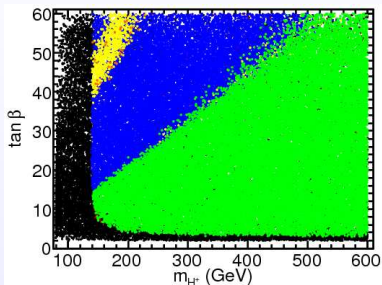
## MSSM

mSUGRA



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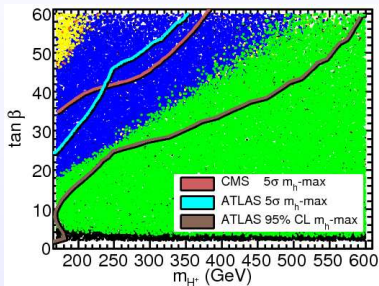
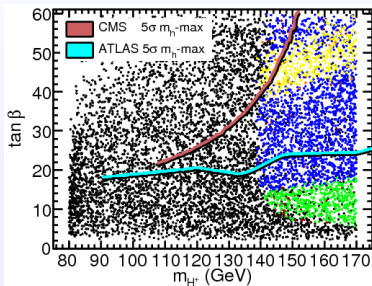
NUHM



$$m_{H^+} \gtrsim 135 \text{ GeV}$$

D. Eriksson, F. Mahmoudi & O. Stål, JHEP 0811 (2008)

## MSSM



D. Eriksson, F. Mahmoudi & O. Stål, JHEP 0811 (2008)



## Conclusion

- Indirect constraints and in particular flavor physics are essential to restrict new physics parameters
  - That will become even more interesting when combined with LHC data
  - This kind of analysis should be generalized to more new physics scenarios

## Ongoing Developments

- Extension to NMFV
- Implementation of other observables

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## Backup

## THDM types I–IV

- **Type I:** one Higgs doublet provides masses to all quarks (up and down type quarks) ( $\sim$  SM)
- **Type II:** one Higgs doublet provides masses for up type quarks and the other for down-type quarks ( $\sim$  MSSM)
- **Type III,IV:** different doublets provide masses for down type quarks and charged leptons

Type	$\lambda_U$	$\lambda_D$	$\lambda_L$
I	$\cot \beta$	$\cot \beta$	$\cot \beta$
II	$\cot \beta$	$-\tan \beta$	$-\tan \beta$
III	$\cot \beta$	$-\tan \beta$	$\cot \beta$
IV	$\cot \beta$	$\cot \beta$	$-\tan \beta$

## SuperIso

