

# Low scale Left-Right @ LHC through LNV

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w/ Alessio Maiezza, Miha Nemevšek, Goran Senjanović

# Are we satisfied with the SM?

- SM needs extension — in addition to DM, maybe hierarchy:

Neutrino masses  $\rightarrow$  high or low scale?

Dirac or Majorana?

SM begging for more symmetry...

- Addressed within the simplest extension, the LR model.
- Can LHC help?

Yes if parity (LR symmetry) restored at low scale,  
via Lepton Violation, with pretty low statistics

# $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$

Fields: **fermions**  $f_L, f_R$ , **bidoublet**  $\phi \sim (h_{light}, H_{heavy})$ , **triplets**  $\Delta_L, \Delta_R$ :

$$\langle \phi \rangle = \begin{pmatrix} v' & \\ & v \end{pmatrix}, \quad \langle \Delta_R \rangle = \begin{pmatrix} & \\ & v_R \end{pmatrix}, \quad \langle \Delta_L \rangle = \begin{pmatrix} \\ v_L \end{pmatrix}$$

spontaneously with  $v_L \ll v' < v \ll v_R$ . [Mohapatra Senjanovic '75]

- Quark masses from two yukawa matrices,  $\bar{\psi}_L (Y\phi + \tilde{Y}\tilde{\phi})\psi_R$ :

$$M_u = |v| Y + |v'| e^{i\alpha} \tilde{Y}$$

$$M_d = |v'| Y + |v| e^{i\alpha} \tilde{Y}$$

- **Majorana neutrino masses**, in addition to Dirac:

$$m_{LL} = Y_\Delta \langle \Delta_L \rangle \ll m_{RR} = Y_\Delta \langle \Delta_R \rangle$$

- Spectrum:  $W_R, \nu_R, \Delta_{L,R}$  may be near TeV

- $H$  should be very heavy (tree-level FC)

[Senjanović Senjanović '80, ..., Zhang et al '07]

# $M_R$ scales

Low scale  
Left-Right @  
LHC through  
LNV

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Can we test this model?

- High  $M_{W_R}$  up to  $\sim 10^{14}$  GeV: ok with GUT.  
Still  $M_{\nu_R}$  can be low – but hard to see [Kersten Smirnov '07, etc]

- Low  $M_{W_R} \gtrsim \text{TeV}$  possible and testable:

leading to striking signals

(... direct probe of new interactions)

(... of parity restoration)

(... of majorana character)

(... of additional flavour structure)

- Collider signals of  $W_R$  and  $\nu_R$ . [Keung Senjanovic '83]

- Also, lepton number violation enters in rare processes: e.g. new contributions to  $0\nu\beta\beta$   
(disentangled from neutrino masses and their (cosmological) bound)

A selection of processes...

Problem

Problem

LR

LR

Scales

Low scale  $W_R$

Processes

$W_R$ - $\nu_R$

$\Delta_{L,R}$

$0\nu\beta\beta$

Limits

$K\bar{K}$

Good mixings

L-R models

C

Outlook

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A selection of processes...

# Interesting processes

Low scale  
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Problem  
LR  
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Low scale  $W_R$

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$W_R$ - $\nu_R$   
 $\Delta_{L,R}$   
 $0\nu\beta\beta$

Limits

$K\bar{R}$   
Good mixings

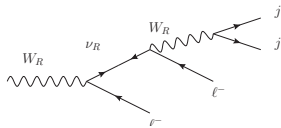
L-R models

C

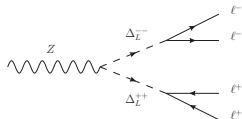
Outlook

- Premium:  $W_R$ - $\nu_R$  production

Same-sign dileptons.



- $\Delta_L^{\pm\pm}$  production (pairwise)

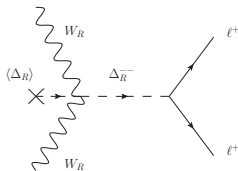


- $\Delta_R^{\pm\pm}$  production ( $W$  fusion)

- $W_R$ - $\Delta_R$  pair production

- $0\nu 2\beta$  (LR vs RR)

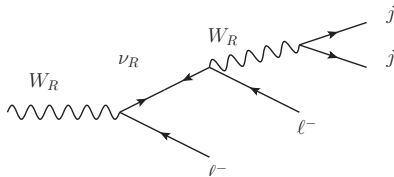
- $\mu \rightarrow e\gamma, \dots$



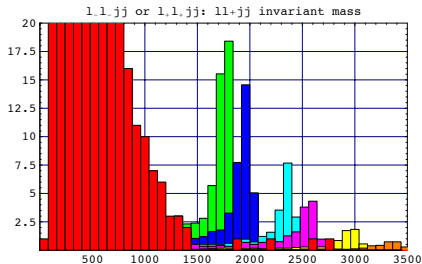
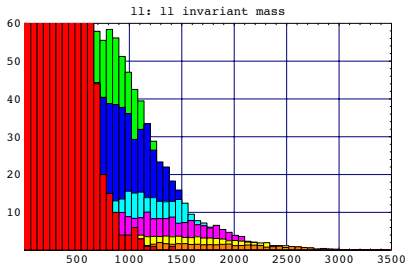
... depends of course on which particles lie at low scale.

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Yukawa-free production of  $W_R, \nu_R$  possibly on-shell.



allows reconstruction of  $W_R$  and neutrino invariant mass, probing neutrino flavour structure.



$8fb^{-1}$  @ 14 TeV, PT cuts 20GeV,  $t\bar{t}$  background

# $W_{R-\nu_R}$ cont'd

## ■ LHC reach?

$M_{W_R}$ [TeV]	$m_{\nu_R}$ [TeV]	$\int L$	energy	
4 (2)	2 (1)	30 /fb	14(7) TeV	Ferrari et al '00, Gninenko et al '07
2.1 (1.5)	2.1	100/pb	14(10) TeV	Kirsanov '09

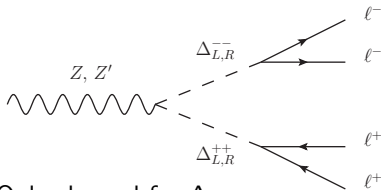
- But early signal through  $\ell^\pm \ell^\pm$  large energy (wrt to  $t\bar{t}$  ones)?
- Neutrino masses and flavour:  
yukawa-free, but probing RH neutrino matrix.  
For flavour need updated montecarlo (CalcHEP? Update Pythia?)
- Displaced Vertex?

$$\tau_{\nu_R} \gtrsim 1 \text{ cm for } m_{\nu_R} \lesssim 10 \text{ GeV } (M_{W_R} = 2.5 \text{ TeV})$$

Tuning, from the model point of view to have light  $\nu_R$ .  
On the other hand this signal would be quite unmistakable.



# $\Delta_{L,R}$



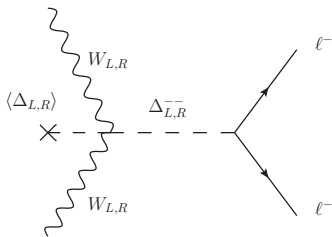
$$\propto (Y_{\Delta})_{ij}(Y_{\Delta}^*)_{kl}$$

Only channel for  $\Delta_L$

(except for  $y_{\Delta} \ll 1!$ )

Can probe neutrino masses, only assuming type-II seesaw. . .

[Kadastik Raidal Rebane '07, del Aguila et al '07, Han et al]



$$\propto (Y_{\Delta})_{ij}$$

large VEV for  $\Delta_R$  but  
suppressed for heavy  $W_R$

[Azuolos '05]

VEV suppressed for  $\Delta_L$

Reach  $< 1$  TeV

# $0\nu\beta\beta$

New contributions, that can compete with the standard LL  $0\nu\beta\beta$  amplitude  $\propto m_{ee}/p^2$  with  $m_{ee} \sim 0.1 \text{ eV}$ :

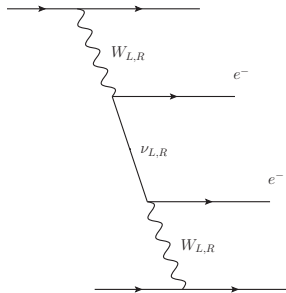
- RR important unless:

$$\left(\frac{M_{W_R}}{\text{TeV}}\right)^4 \left(\frac{m_{\nu_R}}{\text{TeV}}\right) > 2.$$

- LR important unless:

$$\left(\frac{M_{W_R}}{\text{TeV}}\right)^4 \left(\frac{m_{\nu_R}}{\text{TeV}}\right) > 0.2 (U_L O U_R^t)_{ee}^2$$

where  $O$  are orthogonal complex, maybe large! (seesaw example)



- LR can (over)dominate for large Yukawa.
- RR survives even for vanishing Yukawa.

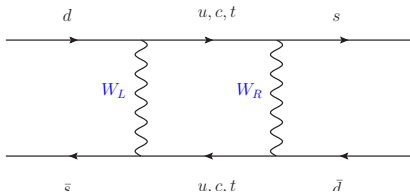
Important e.g. for  $M_{W_R} \simeq 3 \text{ TeV}$ ,  $m_{\nu_R} \simeq 25 \text{ GeV}$ !

# Limits

- Direct limits  $M_{W_R} \geq 800 \text{ GeV}$  (from dijets @  $D0$  [PRL '96, '04, '08])
- Strongest limit comes from  $K$  mass difference:
  - If disentangled  $V_{CKMR} \neq V_{CKML}$  then **no limit on  $M_{W_R}$** .
  - In models where  $V_{CKMR} \simeq V_{CKML}$ , we need  **$M_{W_R} > 2.5 \pm \dots$**   
[Beall Bander Soni '81, ..., Zhang An Ji Mohapatra '07]
- In general  $\epsilon, \epsilon'$  harmless, due to phases. (also in minimal models!)

Thus it is  $\Delta m_K$  that matters

$W_R \rightarrow$  new boxes for  $\Delta S = 2$  — largest is  $W_L-W_R$ :



- Dominant is  $c$ - $c$  loop – Correlated bound  $V_R-M_{W_R}$ :

$$M_{W_R}^2 > (2.5 \text{ TeV})^2 \left( \frac{V_{cdR}^*}{\lambda_c} \right) \left( \frac{V_{csR}}{1} \right)$$

(With hadronic matrix elements uncertainty 25–50%.)

[Baremboim, Barnabeu, Prades, Raidal, '96, Babich et al '06]

So it is  $V_R^{CKM}$  that matters...

# Good mixing matrices

Good  $V_R$  have thus one of the following forms:

$$V_R = \begin{pmatrix} e^{i\psi} & 0 & 0 \\ 0 & ce^{i\sigma} & -se^{i\gamma} \\ 0 & se^{i\theta} & ce^{i\epsilon} \end{pmatrix}, \quad \begin{pmatrix} 0 & e^{i\psi} & 0 \\ ce^{i\sigma} & 0 & -se^{i\gamma} \\ se^{i\theta} & 0 & ce^{i\epsilon} \end{pmatrix}$$

[Langacker Sankar '98, ..., Frank et al, '10]

By inspection, one checks that this is enough to relax limits from  $\Delta m_K$  as well from  $B_s, B_d$ .

Then also CP violation bounds can be satisfied, by exploiting the phases.

$$\theta_{12R} = 0 \text{ or } \pi/2$$

Can we reach this form?

Generically, if  $\alpha, Y, \tilde{Y}$  unconstrained,  $\rightarrow V_R$  free  $\rightarrow$  no limits on  $M_{W_R}$ .

# L-R models: two symmetries

## ■ Generalized Parity:

$$\mathcal{P} : f_L \leftrightarrow f_R, \phi \leftrightarrow \phi^\dagger$$

$$Y, \tilde{Y} \text{ hermitian, but} \quad \Rightarrow \quad V_R \neq V_L$$

because of the 'spontaneous' phase  $e^{i\alpha} \dots$

But how much actually different?

see Nemevšek talk

## ■ Generalized Charge conj.:

$$\mathcal{C} : f_L \leftrightarrow (f_R)^c, \phi \leftrightarrow \phi^T$$

$$Y, \tilde{Y} \text{ symmetric and} \quad \Rightarrow \quad V_R = K_1 V_L^* K_2,$$

with  $K_1, K_2$  diagonal phases. So equal mixings, and from  $\Delta m_K$ ,

$$M_{W_R} \geq 2.5 \text{ TeV}$$

Note this is gaugeable symmetry – e.g. embedded in GUT SO(10)!

# Case of $\mathcal{C}$ : Charge Conjugation

Mass matrices symmetric: same angles, only extra phases (5)

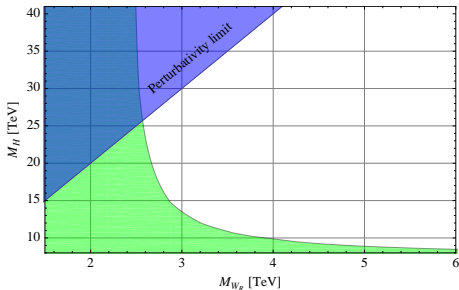
$$V_R = K_u V_L^* K_d$$

$$(K_u = \text{diag}\{e^{i\theta_u}, e^{i\theta_c}, e^{i\theta_t}\}, K_d = \text{diag}\{e^{i\theta_d}, e^{i\theta_s}, e^{i\theta_b}\})$$

- Again, from  $\Delta m_K$ :

$$M_{W_R} > 2.5 \text{ TeV.}$$

correlated with  
heavy FC higgs:



- No constraint from  $\Delta m_{B_d}$ ,  $\Delta m_{B_s}$ , but  
situation with CP violation in  $B_{d,s}$  is now curious...

# $\mathcal{C}$ , cont'd: $\epsilon$

Possible new physics in  $\epsilon$  is at most 20–30%:

$$\frac{\epsilon_{LR}}{\epsilon_{SM}} \simeq \text{Im} \left[ e^{i(\theta_d - \theta_s)} A_{cc} \right] < 0.3$$

where  $\beta = -\arg(V_{Ltd})$  and the  $c$ - $c$  term is:

$$A_{cc} \simeq \left[ 150 + 8.2 \ln \left( \frac{M_{W_R}}{2.5 \text{ TeV}} \right) \right] \left( \frac{2.5 \text{ TeV}}{M_{W_R}} \right)^2 + 84 \left( \frac{15 \text{ TeV}}{M_H} \right)^2$$

Quite large contribution from LR, however:

- For zero phases  $\theta_{d,s}$ , no CP violation (from LR graphs)
- So, no bounds, we only conclude:

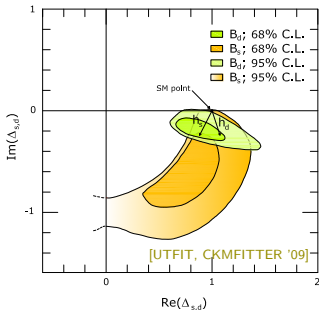
$$\theta_d - \theta_s \simeq 0.$$



# $C$ , cont'd, $B_{d,s}$

[w/ Maiezza, Nemevshek, Senjanovic]

New Physics in  $B^0-\bar{B}^0$ :



$$h_q = \frac{\langle B_q | \mathcal{H}_{LR} | \bar{B}_q \rangle}{\langle B_q^0 | \mathcal{H}_{SM} | \bar{B}_q^0 \rangle}, \quad (q = d, s)$$

Need a nonzero phase.

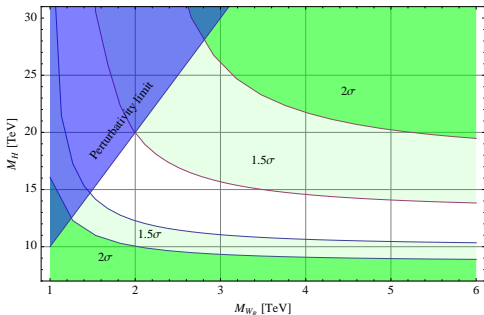
$$\theta_b - \theta_d \simeq \theta_b - \theta_s$$

(because  $\theta_d - \theta_s \simeq 0$  for  $\epsilon$ )

$\rightarrow h_{d,s}$  point toward same region.

Correlated bound:

In the interesting zone  
for LHC



# Outlook

The interesting case of TeV-scale L-R symmetry **with  $\mathcal{C}$** :

- A **symmetric extension** of the SM (embeddable in GUT)
- **LR Parity restored**, at low scale!
- Premium channel still on-shell  $W_{R-\nu_R}$  @ LHC.
- **Lepton Number Violation**.
- Possibly **very rich phenomenology** ( $W_R, \nu_R, \Delta_L, \Delta_R$ )
- Lower bound  $M_{W_R} \gtrsim 2.5 \text{ TeV}$  (from  $K^0-\bar{K}^0$ )
- No bounds from CP violation...  
... on the contrary solution of  $B_{d,s}$  CP tension
- Todo WIP: update montecarlo for flavour? LD part?  
Polarizations? Disentangling different signals...
- **Thanks!**

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# L-R Lagrangian

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$0\nu\beta\beta$

Limits

$K\bar{R}$

Good mixings

L-R models

$C$

Outlook

$$L = R$$

# $W_L$ - $W_R$ mixing

In the minimal models, tree level  $W_L$ - $W_R$  mixing angle  $\zeta$  is bound by weak decays,  $\zeta < 10^{-2}$  ( $3 \cdot 10^{-3}$ ).

This translates into a limit on the  $W_R$  mass:

$$M_{W_R} > 1.5 \text{ TeV} \sqrt{\frac{2x}{1+x^2}},$$

... quite harmless.

# Higgs spectrum

Higgs state	$m^2$
$h^0 = \sqrt{2} \operatorname{Re} (\phi_1^{0*} + x e^{-i\alpha} \phi_2^0)$	$\left(4\lambda_1 - \frac{\alpha_1^2}{\rho_1}\right) v^2 + \alpha_3 v_R^2 x^2$
$H_1^0 = \sqrt{2} \operatorname{Re} (-x e^{i\alpha} \phi_1^{0*} + \phi_2^0)$	$\alpha_3 v_R^2$
$A_1^0 = \sqrt{2} \operatorname{Im} (-x e^{i\alpha} \phi_1^{0*} + \phi_2^0)$	$\alpha_3 v_R^2$
$H_2^0 = \sqrt{2} \operatorname{Re} \delta_R^0$	$4\rho_1 v_R^2$
$H_2^+ = \phi_2^+ + x e^{i\alpha} \phi_1^+ + \frac{1}{\sqrt{2}} \epsilon \delta_R^+$	$\alpha_3 (v_R^2 + \frac{1}{2} v^2)$
$\delta_R^{++}$	$4\rho_2 v_R^2 + \alpha_3 v^2$
$H_3^0 = \sqrt{2} \operatorname{Re} \delta_L^0$	$(\rho_3 - 2\rho_1) v_R^2$
$A_2^0 = \sqrt{2} \operatorname{Im} \delta_L^0$	$(\rho_3 - 2\rho_1) v_R^2$
$H_1^+ = \delta_L^+$	$(\rho_3 - 2\rho_1) v_R^2 + \frac{1}{2} \alpha_3 v^2$
$\delta_L^{++}$	$(\rho_3 - 2\rho_1) v_R^2 + \alpha_3 v^2$

Leading order in  $\epsilon = v/v_R$  and  $x = v'/v$ , and assuming  $v_L = 0$ .  
The SM Higgs is identified with  $h^0$ . [Zhang et al '07]



# Ugly

	Lorentz	Q ( $Y + T_{3L}$ )	Y	$SU(2)_L$ $T_{3L}$			$SU(3)$
$u_L$	2	2/3	1/6	1/2			3
$d_L$	2	-1/3	1/6	-1/2			3
$\nu_L$	2	0	-1/2	1/2			1
$e_L$	2	-1	-1/2	-1/2			1
$u_R$	$\bar{2}$	2/3	2/3	0			3
$d_R$	$\bar{2}$	-1/3	-1/3	0			3
$\nu_R$	$\bar{2}$	0	0	0			1
$e_R$	$\bar{2}$	-1	-1	0			1

Plenty of symmetries to restore 'beauty', starting from the simplest, **Left-Right symmetry**, restoring a "Parity" at some scale:

$$SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

[Pati Salam '74, Mohapatra Pati '75, Senjanović Mohapatra '75]

(Then Pati-Salam  $SU(2)_L \times SU(2)_R \times SU(4)_c$ ,  $SO(10)$ , etc, even with Lorentz)

[Pati Salam '74; Georgi '75] [FN '07, FN Percacci '09]

# Nice

	Lorentz	Q ( $Y + T_{3L}$ )	Y ( $T_{3R} + \frac{(B-L)}{2}$ )	$SU(2)_L$ $T_{3L}$	$SU(2)_R$ $T_{3R}$	$B - L$	$SU(3)$
$u_L$	2	2/3	1/6	1/2	0	1/3	3
$d_L$	2	-1/3	1/6	-1/2	0	1/3	3
$\nu_L$	2	0	-1/2	1/2	0	-1	1
$e_L$	2	-1	-1/2	-1/2	0	-1	1
$u_R$	$\bar{2}$	2/3	2/3	0	1/2	1/3	3
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$\nu_R$	$\bar{2}$	0	0	0	1/2	-1	1
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# $\Delta F = 2$ Hamiltonians

Effective **Hamiltonians** from the box diagrams:

$$\mathcal{H}_{LL}^{\Delta F=2} = \frac{G_F^2 M_{WL}^2}{4\pi^2} \sum_{d,d'=d,s,b} \bar{d}' \gamma_\mu P_{Ld} \bar{d}' \gamma_\mu P_{Ld} \sum_{i,j=c,t} \lambda_i^{LL} \lambda_j^{LL} S_{LL}(x_i, x_j) \eta_{LL,ij}$$

$$\mathcal{H}_{LR}^{\Delta F=2} = \frac{G_F^2 M_{WL}^2}{4\pi^2} 8 \beta \sum_{d,d'=d,s,b} \bar{d}' P_{Ld} \bar{d}' P_{Rd} \sum_{i,j=u,c,t} \lambda_i^{LR} \lambda_j^{RL} S_{LR}(x_i, x_j, \beta) \eta_{LR,ij}$$

$$\mathcal{H}_{RR}^{\Delta F=2} = \frac{G_F^2 M_{WL}^2}{4\pi^2} \beta \sum_{d,d'=d,s,b} \bar{d}' \gamma_\mu P_{Rd} \bar{d}' \gamma_\mu P_{Rd} \sum_{i,j=c,t} \lambda_i^{RR} \lambda_j^{RR} S_{RR}(x_i, x_j, \beta) \eta_{RR,ij}$$

where

$$\lambda_i^{AB} = V_{id'}^{A*} V_{id}^B, \quad x_i = (m_i/M_{WL})^2, \quad \beta = M_{WL}^2/M_{WR}^2$$

and **Matrix elements** for meson  $M^0-\bar{M}^0$  are:

$$\langle M^0 | \bar{d}' \gamma_\mu P_{Ld} \bar{d}' \gamma_\mu P_{Ld} | \bar{M}^0 \rangle = \frac{2}{3} f_M^2 m_M \mathcal{B}_M^{LL}$$

$$\langle M^0 | \bar{d} P_{Ld} \bar{d} P_{Rd'} | \bar{M}^0 \rangle = \frac{1}{2} f_M^2 m_M \mathcal{B}_M^{LR} \left[ \left( \frac{m_M}{m_{d'} + m_d} \right)^2 + \frac{1}{6} \right].$$

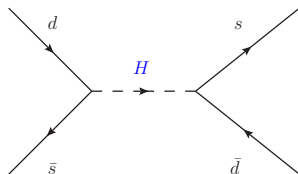
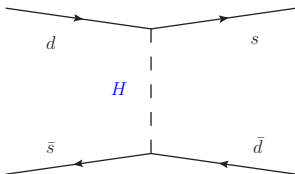
# $\Delta F = 2$ FC Higgs

Effective **Hamiltonians** from the tree level Higgs:

$$\mathcal{H}_H^{\Delta F=2} = -\frac{4G_F}{\sqrt{2}M_H^2} \sum_{d,d'=d,s,b} \bar{d}' P_L d \bar{d}' P_R d \sum_{i,j=u,c,t} \lambda_i^{LR} \lambda_j^{RL} m_i m_j,$$

where again

$$\lambda_i^{AB} = V_{id'}^{A*} V_{id}^B, \quad x_i = (m_i/M_{W_L})^2$$



# $C$ : $B$ CP violation

The last free phase is constrained:

