The nucleon's transversity and the photon distribution amplitude probed in lepton pair photoproduction

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Motivation

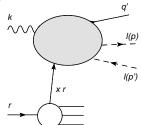
Description of the process of Drell-Yan type

$$\gamma N \to l(p)l(p')X$$

or on the partonic level

$$\gamma(k)q(xr) \to l(p)l(p')q(q')$$

in the QCD factorization approach



Real photon components

Two components of a **REAL** photon in (semi-)exclusive processes:

- a "pointlike" or perturbative electromagnetic component
- ullet a "soft"or non-perturbative component (familiar from the studies of γ structure function in DIS)

non-perturbative \longrightarrow induced by condensates:

B.L. loffe, A.V. Smilga 1984

exist WITHOUT an external field

 $\langle 0 | \ ar{q}(0) q(0) \ | 0 \rangle
eq 0$ "ferromagnetic" type

nonvanishes IN THE PRESENCE of an external e-m field ${\cal F}$

 $\langle 0|\ ar{q}(0)\sigma_{lpha\,eta}q(0)\ |0
angle_F=e_q\,\chi\langlear{q}q
angle F_{lpha\,eta}$ "paramagnetic" type

 χ - magnetic susceptibility of QCD vacuum

for
$$z^2 = 0$$

$$\langle 0 | \bar{q}(z) \sigma_{\alpha\beta} q(-z) | 0 \rangle_F = e_q \chi \langle \bar{q}q \rangle \int_0^1 du F_{\alpha\beta} ((1 - 2u)z) \phi_{\gamma}(u)$$

Real photon distribution amplitudes

ullet the perturbative, singular CHIRAL-EVEN with q- $ar{q}$ pair of opposite (equal) helicities (chiralities)

$$\langle 0|\bar{q}(0)\gamma_{+}\frac{1\pm\gamma_{5}}{2}q(x)|\gamma^{(\lambda)}(q)\rangle = \frac{iN_{c}e_{q}}{4\pi^{2}\mathbf{r}^{2}}q_{+}\int_{0}^{1}due^{-iu(qx)}\left[\left(\epsilon^{(\lambda)}\cdot\mathbf{r}\right)(2u-1)\pm i\epsilon_{ik}\mathbf{r}_{i}\epsilon_{k}^{(\lambda)}\right]$$

• the non-perturbative (due to chiral s.b.), CHIRAL-ODD with q- \bar{q} pair of equal (opposite) helicities (chiralities)

$$\langle 0|\bar{q}(0)\sigma_{\alpha\beta}q(x)|\gamma^{(\lambda)}(k)\rangle = i\,e_q\,\chi\,\langle\bar{q}q\rangle\left(\epsilon_{\alpha}^{(\lambda)}k_{\beta} - \epsilon_{\beta}^{(\lambda)}k_{\alpha}\right)\int\limits_{0}^{1}dz\,e^{-iz(qx)}\,\phi_{\gamma}(z)$$

with $\chi \langle \bar{q}q \rangle \approx 40 - 70 \, \text{MeV}$ at $\mu = 1 \, \text{GeV}$

 χ - magnetic susceptibility of the QCD vacuum

Braun et al Phys.Rev.Lett. 89, 172001 (2002); Braun et al Nucl. Phys. B 649, 263 (2003),

P. V. Buividovich et al; Nucl. Phys. B 826 (2010) 313 Dorokhov et al Phys. Rev. D 74, 054023 (2006)



Transversity h_1

- the chiral-odd objects must appear in pairs :
 - ullet Nucleon's transversity parton distribution h_1 is CHIRAL-ODD

$$\langle r, s_T | \bar{q}(-\frac{1}{2}z)\sigma^{+i}\gamma^5 q(\frac{1}{2}z) | r, s_T \rangle = \bar{u}(r, s_T)\sigma^{+i}\gamma^5 u(r, s_T) \int_0^1 du e^{-iu(rz)} (\delta q(u) - \delta \bar{q}(-u))$$

with quark $\delta q(u) = h_1(u)$

The partonic photoproduction of lepton pair

$$\gamma(k)q(xr) \to l(p)l(p')q(q')$$

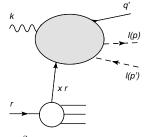
$$q = p + p' = \alpha k + \frac{Q^2 + \mathbf{Q}^2}{\alpha s} r + Q_T$$

$$p = \gamma \alpha k + \frac{(\gamma \mathbf{Q_T} + \mathbf{l_T})^2}{\gamma \alpha s} r + \gamma Q_T + l_T$$

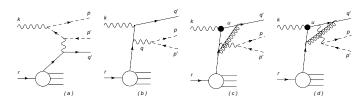
$$p' = \bar{\gamma} \alpha k + \frac{(\bar{\gamma} \mathbf{Q_T} - \mathbf{l_T})^2}{\bar{\gamma} \alpha s} r + \bar{\gamma} Q_T - l_T$$

$$q' = \bar{\alpha} k + \frac{\mathbf{Q_T}^2}{\bar{\alpha} s} r - Q_T$$

$$x = \frac{\bar{\alpha} Q^2 + \mathbf{Q_T}^2}{2\bar{\alpha} s} \qquad Q^2 = \frac{\mathbf{l_T}^2}{2\bar{\alpha} s} \qquad s = 2r \cdot k \qquad Q_T^2 = -\mathbf{Q_T}^2$$



Contributions to the process



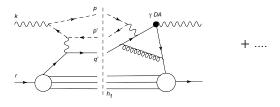
CHIRAL-EVEN: Bethe-Heitler (a) + Drell-Yan (b) AND CHIRAL-ODD (c + d) with γ DA

Crucial observation: the CHIRAL-ODD part has an absorptive part:

$$\text{e.g. } \sim \int\limits_0^1 du \frac{\phi_{\gamma}(u)}{u - \frac{Q^2\alpha}{Q^2 + \mathbf{Q_T}^2 - i\epsilon}} = PV \int\limits_0^1 du \frac{\phi_{\gamma}(u)}{u - \frac{Q^2\alpha}{Q^2 + \mathbf{Q_T}^2}} + i\pi\phi_{\gamma}(\frac{Q^2\alpha}{Q^2 + \mathbf{Q_T}^2})$$

Interference between CHIRAL-EVEN and CHIRAL-ODD parts





$$\frac{1}{2} \sum_{\lambda} d\sigma_{\phi BH}(\gamma(\lambda)p \rightarrow l^- l^+ X) = \frac{(4\pi\alpha_{em})^3}{4s} \; \frac{C_F 4\pi\alpha_s}{2N_c} \cdot \frac{\chi\left\langle \bar{q}q\right\rangle}{\bar{Q}_T^2} \int dx \sum_q Q_l^3 Q_q^3 h_1^q(x) 2\mathcal{R}e(\mathcal{I}_{\phi BH}) \; dLIPS \; , \label{eq:delta}$$

Result: INTERFERENCE DOESN'T VANISH

$$\sim \chi \phi_{\gamma}(\frac{Q^2 \alpha}{Q^2 + \mathbf{Q_T}^2}) \cdot h_1(\frac{\bar{\alpha}Q^2 + \mathbf{Q_T}^2}{\alpha \bar{\alpha}s})$$

- may be singled out by the lepton azymuthal distribution
 - only nucleon is polarized, i.e. SINGLE SPIN EFFECTS

Phenomenological perspectives

- Lepton pair photoproduction cross sec. are $\sim \alpha_{em}^3$: Is it measurable ? It IS NOT a signal of unmeasurability:
 - J. F. Davis et al., "Measurement of muon-pair photoproduction in the deep inelastic region," Phys. Rev. Lett. 29, 1356 (1972)
- \bullet The unpolarized Drell-Yan cross sec. is estimated to be a few picobarns for Q^2 values of a few ${\rm GeV}^2$
 - R. L. Jaffe, "Photoproduction Of Massive Muon Pairs At High-Energies,"
 Phys. Rev. D **4**, 1507 (1971);
- one needs to carry a detailed numerical analysis of all the kinematical domains in order to perform a judicious partial phase space integration and define less differential observables
- A single spin observable is not necessarily the most easily accessible. A
 detailed phenomenological analysis should discuss both single spin and
 double spin observables.

Conclusions

ullet We propose a new way to access the nucleon's transversity parton distr. $h_1(x)$

The basic tool is to select observables which selects the interference of the amplitude \mathcal{A}_{ϕ} , where the photon couples to quark through its chiral-odd DA with a better known amplitude such as the Bethe-Heitler or the leading Drell-Yan amplitude

The result - in the exemplary case we have studied - is proportional to $\chi\phi_{\gamma}(\frac{\alpha Q^2}{Q^2+\bar{Q}_{\perp}^2})h_1^q(\frac{Q^2}{\alpha s}+\frac{\bar{Q}_{\perp}^2}{\alpha\bar{\alpha}s}), \text{ which allows to scan both the photon DA and the transversity nucleon distribution}$

- Experimental prospects cover mostly the future JLab 12 Gev upgrade and in particular its Hall D real photon program
- Experiments at higher energy such as the Compass muon beam at CERN may open another kinematical domain.

Both set-ups will have polarized quasi real photon beams and transversely polarized nuclear targets.

• A complete phenomenological study is needed to check that the foreseen photon luminosity and a good lepton pair reconstruction will give access to the interference of the chiral odd amplitude driven by the magnetic susceptibility of the QCD vacuum and either the Bethe-Heitler or the usual Drell-Yan amplitudes.

THANK YOU FOR ATTENTION

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