

# Flavor Physics in a Warped Extra Dimension

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# Standard Model and Beyond

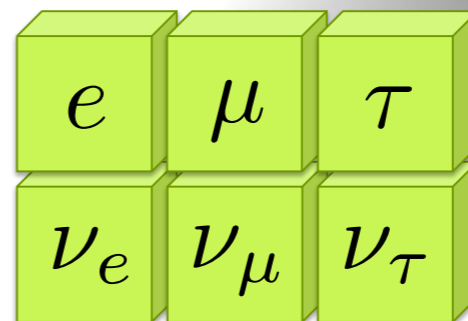
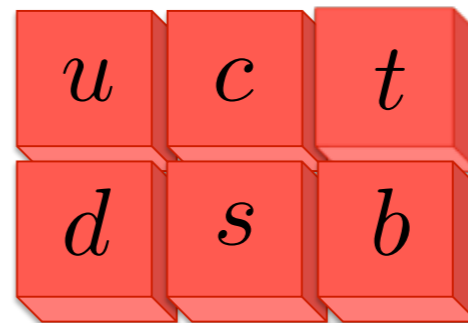
Fundamental laws derived from few, basic guiding principles:

- **Symmetries** (gauge theories)
- **Simplicity** and beauty (few parameters)
- **Naturalness** (avoid fine-tuning)
- **Anarchy** (everything is allowed)

But many questions remain unanswered:

- Origin of generations and structure of Yukawa interactions?
- Matter-antimatter asymmetry?
- Unification of forces? Neutrino masses?
- Dark matter and dark energy?

Quarks

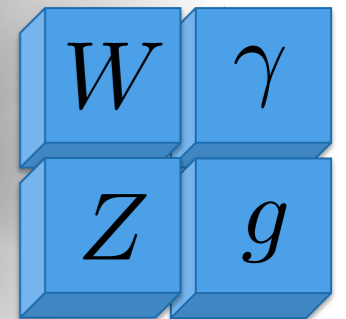


Leptons

*H*

Higgs boson

Forces



**Strong prejudice that there must be “New Physics”**

# Standard Model and Beyond: The Gordian Knot

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What is the “New Physics” and how to find it ?

# Standard Model and Beyond



4<sup>th</sup> generation



extended Higgs sectors



extended technicolor



left-right symmetry



leptoquarks



universal extra dimensions



large extra dimensions



warped extra dimensions



gauge-Higgs unification



Higgsless models



MSSM



CMSSM



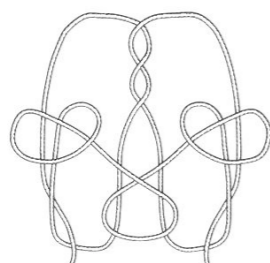
NMSSM



vMSSM



SUSY GUTs



unparticles



Little Higgs



hidden valleys



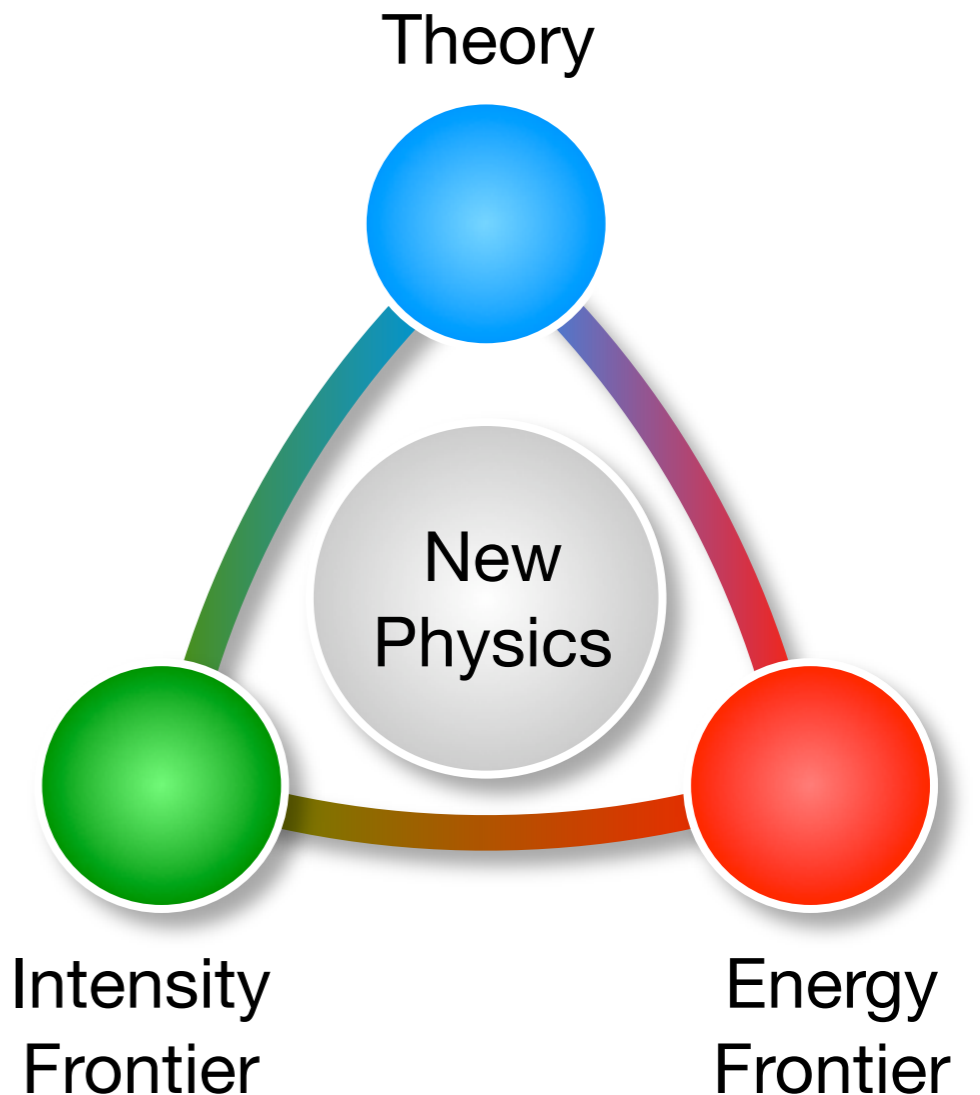
not yet thought of ...

# Searches for New Physics: Interplay

## Complementarity and synergy:

Answering the open questions of elementary particle physics requires a joint effort:

- **Theory:** precision calculations in the SM, studies of New Physics, model-building, ...
- **High-energy experiments:** Tevatron, LHC, ILC (?), CLIC (?), Muon Collider (?), ...
- **Low-energy experiments:** BaBar, Belle, Super-B, NA62, J-PARC, Project X, neutrino physics, EDMs,  $(g-2)_\mu$ , ...



**Quark flavor physics is a crucial component in this program, which provides surgical probes of subtle corrections to fundamental interactions**

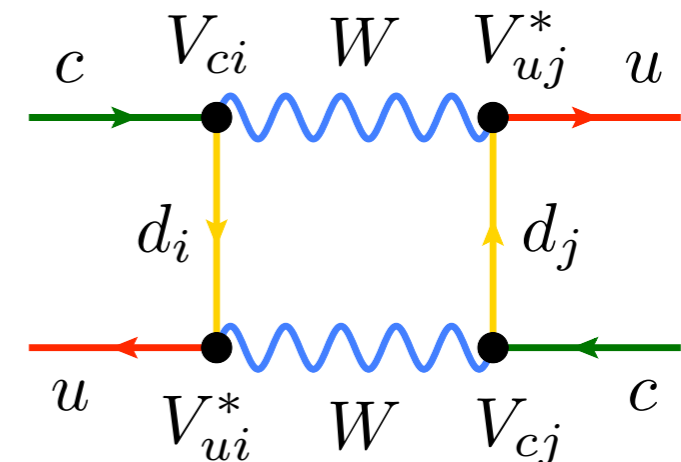
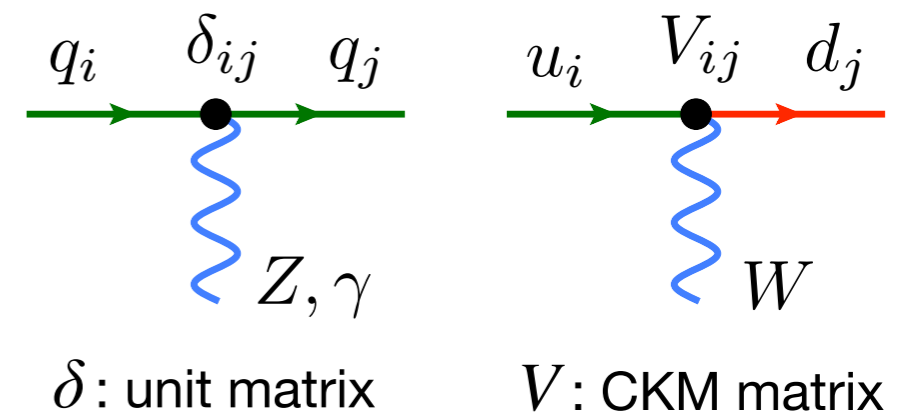


# Flavor Structure in the SM and Beyond

**Flavor physics** means phenomena related to Yukawa couplings and generation-changing interactions in the fermion sector

In SM:

- all flavor-violating interactions encoded in Yukawa couplings to Higgs boson
- suppression of flavor-changing neutral currents (FCNCs) and CP violation in quark sector due to unitarity of CKM matrix, small mixing angles, and GIM mechanism



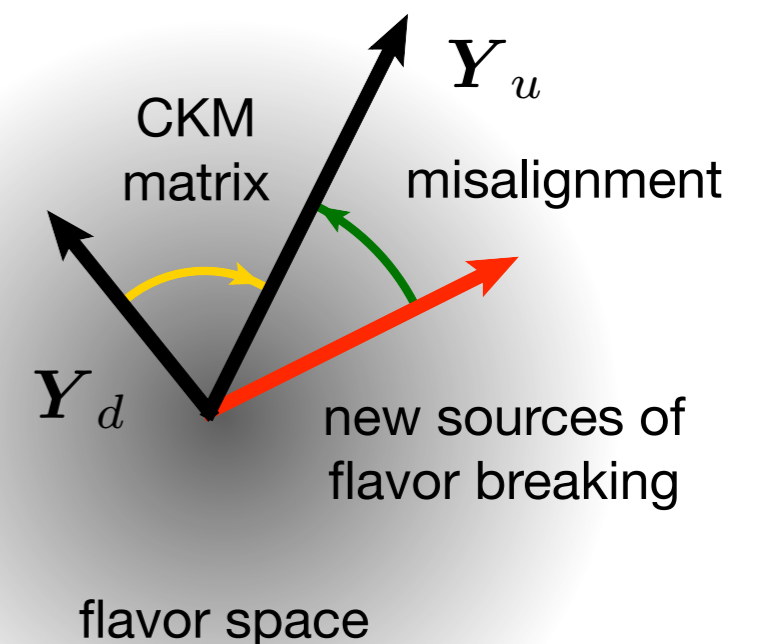
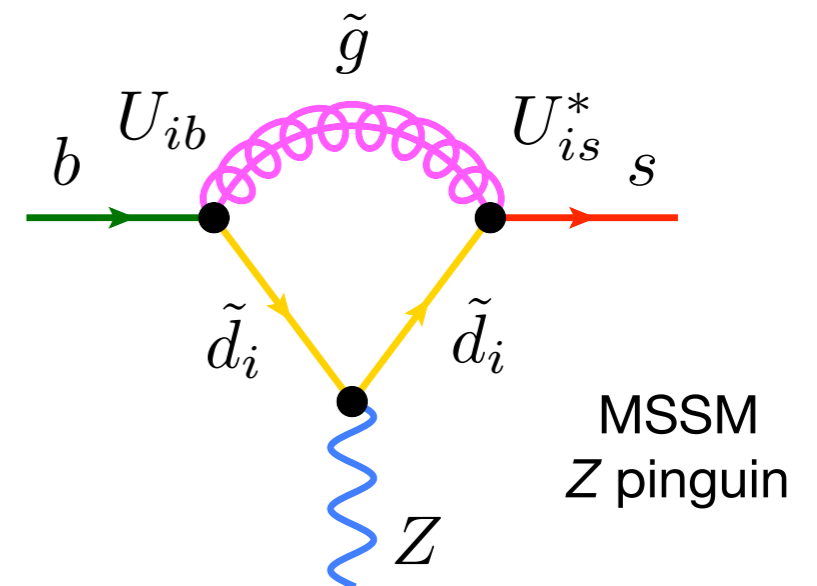
$$\sum_{i,j} \lambda_i \lambda_j f(m_i, m_j) \approx \lambda_b^2 \frac{m_b^2 - m_d^2}{M_W^2} + \lambda_s^2 \frac{m_s^2 - m_d^2}{M_W^2} \approx \lambda_b^2 \frac{m_b^2}{M_W^2}, \quad \lambda_i \equiv V_{ui}^* V_{ci}$$

# Flavor Structure in the SM and Beyond

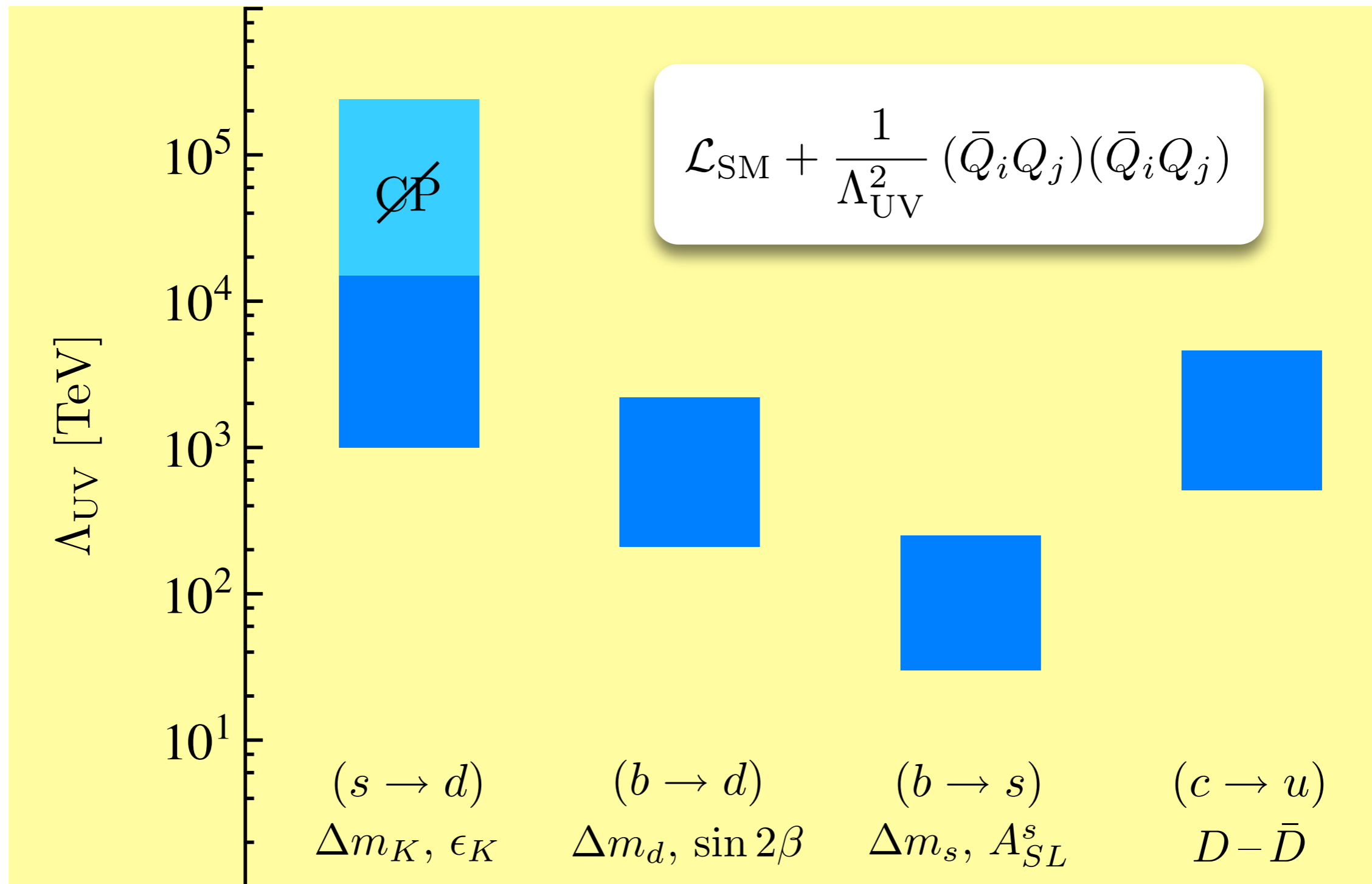
In extensions of SM, additional flavor and CP violation can arise from exchange of new scalar ( $H^+$ ,  $\tilde{q}$ , ...), fermionic ( $\tilde{g}$ ,  $t'$ ,  $t^{(1)}$ , ...), or gauge ( $Z'$ ,  $g^{(1)}$ , ...) degrees of freedom

- new flavor-violating terms in general not aligned with SM Yukawa couplings  $Y_u$ ,  $Y_d$
- can lead to excessive FCNCs, unless:
  - new particles are heavy:  $\tilde{m}_i \gg 1 \text{ TeV}$
  - masses are degenerate:  $\Delta\tilde{m}_{ij} \ll \tilde{m}_i$
  - mixing angles are very small:  $U_{ij} \ll 1$

**Absence of clear New Physics signals in FCNCs implies strong constraints on flavor structure of TeV-scale physics (if it exists)**



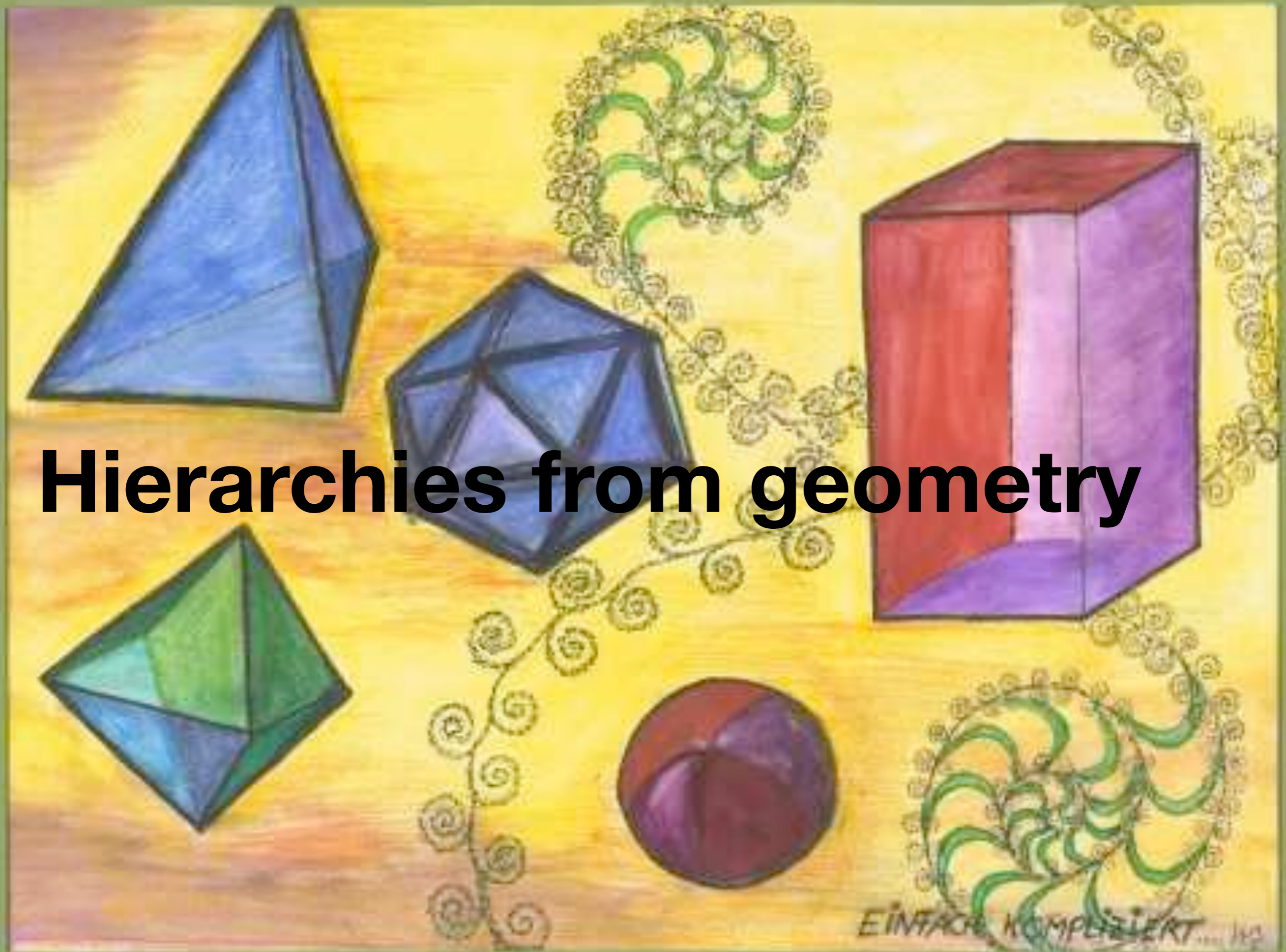
# Flavor Structure in the SM and Beyond



Generic bounds without flavor symmetry



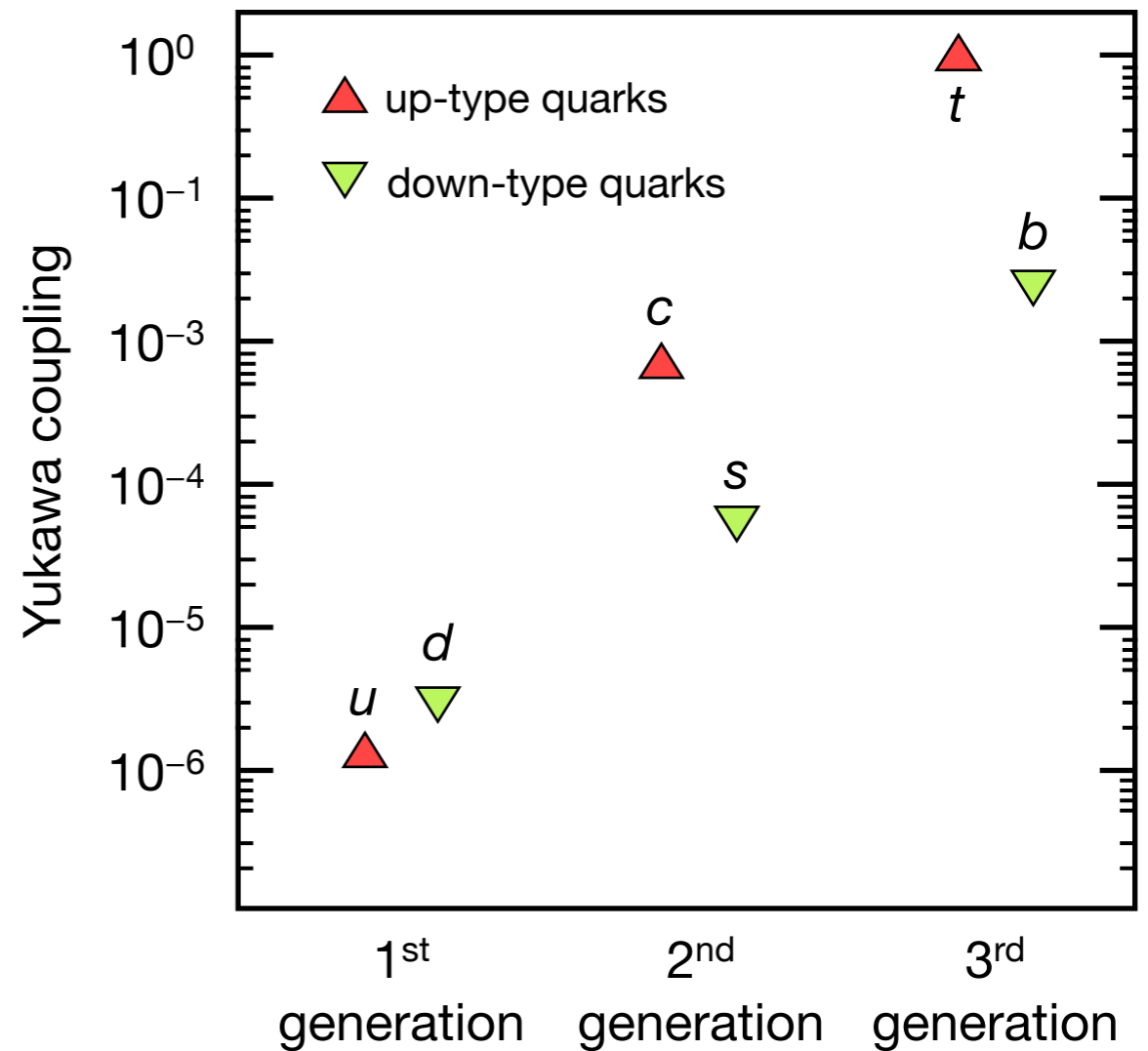
# Hierarchies from geometry



# What is the Dynamics of Flavor?

While SM describes flavor physics very accurately, it does not explain its mysteries:

- Why are there three generations in nature?
- Why does the spectrum of fermion masses cover many orders of magnitude (1<sup>st</sup> hierarchy)?

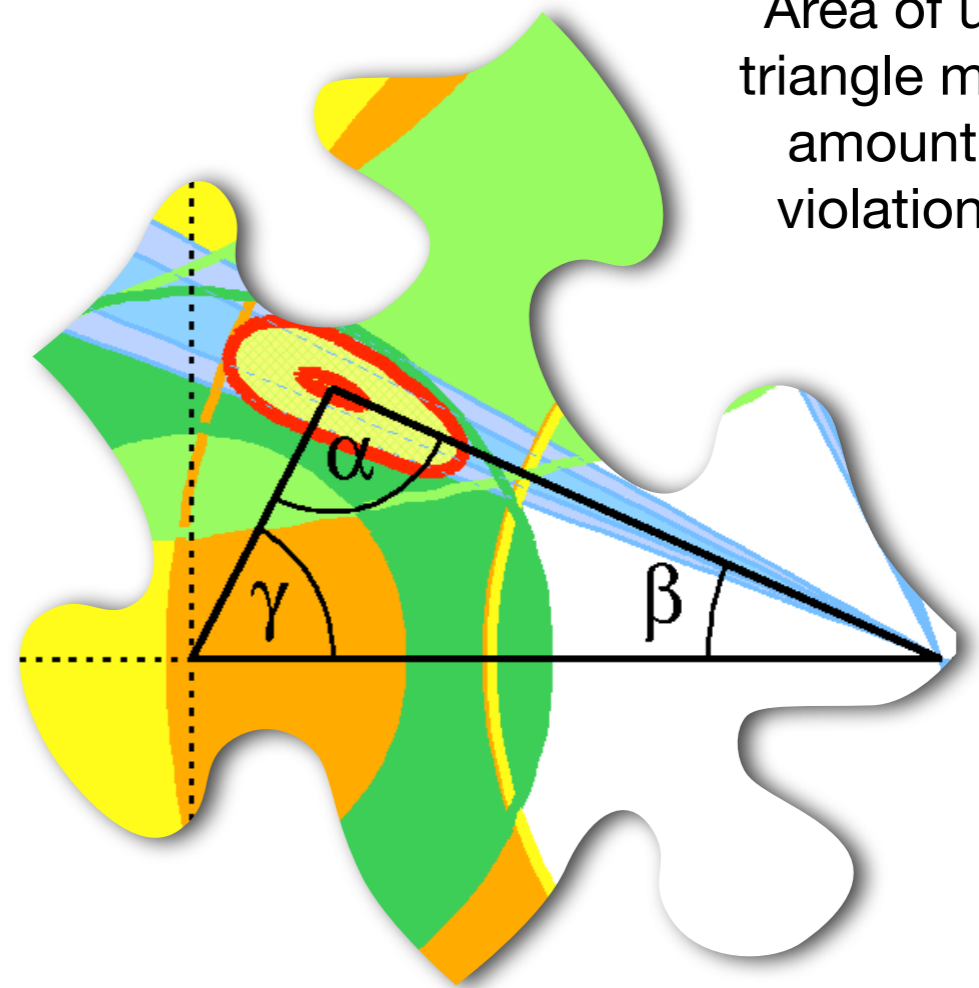


# What is the Dynamics of Flavor?

While SM describes flavor physics very accurately, it does not explain its mysteries:

- Why are there three generations in nature?
- Why does the spectrum of fermion masses cover many orders of magnitude (1<sup>st</sup> hierarchy)?
- Why is the mixing between different generation governed by small mixing angles (2<sup>nd</sup> hierarchy)?
- Why is the CP-violating phase of the CKM matrix unsuppressed?

Answers to these questions necessarily require going beyond the SM -- an interesting approach is offered by **Randall-Sundrum models with warped extra dimensions**



Area of unitarity triangle measures amount of CP violation in SM

# Flavor Structure in RS Models

Randall, Sundrum (1999)

ultraviolet (UV) brane

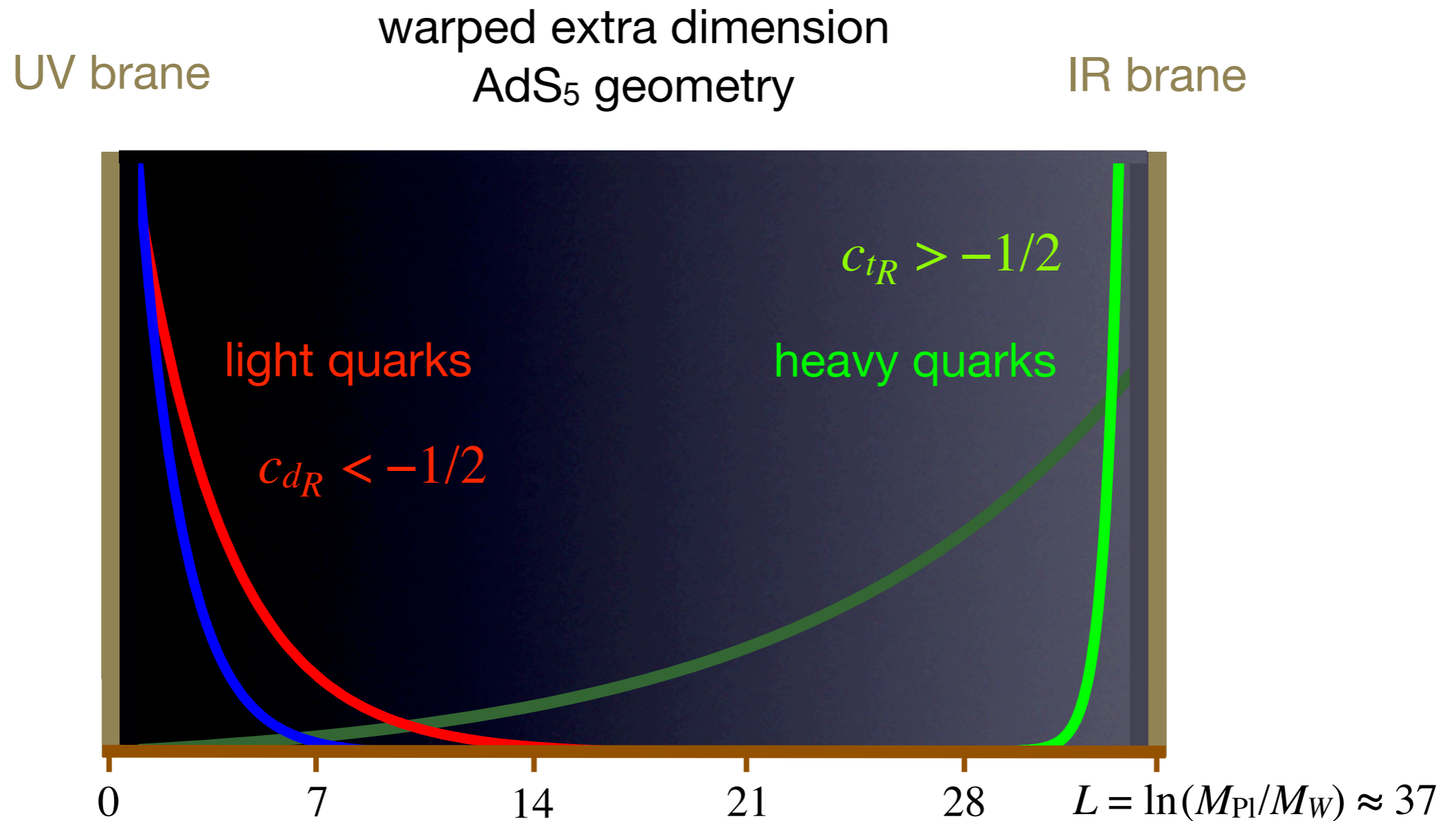
$$ds^2 = \left(\frac{R}{z}\right)^2 (\eta_{\mu\nu} dx^\mu dx^\nu - dz^2)$$

infrared (IR) brane

$R$   $z$   $R'$

- Solution to gauge hierarchy problem via gravitational redshift
- AdS/CFT calculable strong electroweak-symmetry breaking: holographic technicolor, composite Higgs
- Unification possible due to logarithmic running of couplings

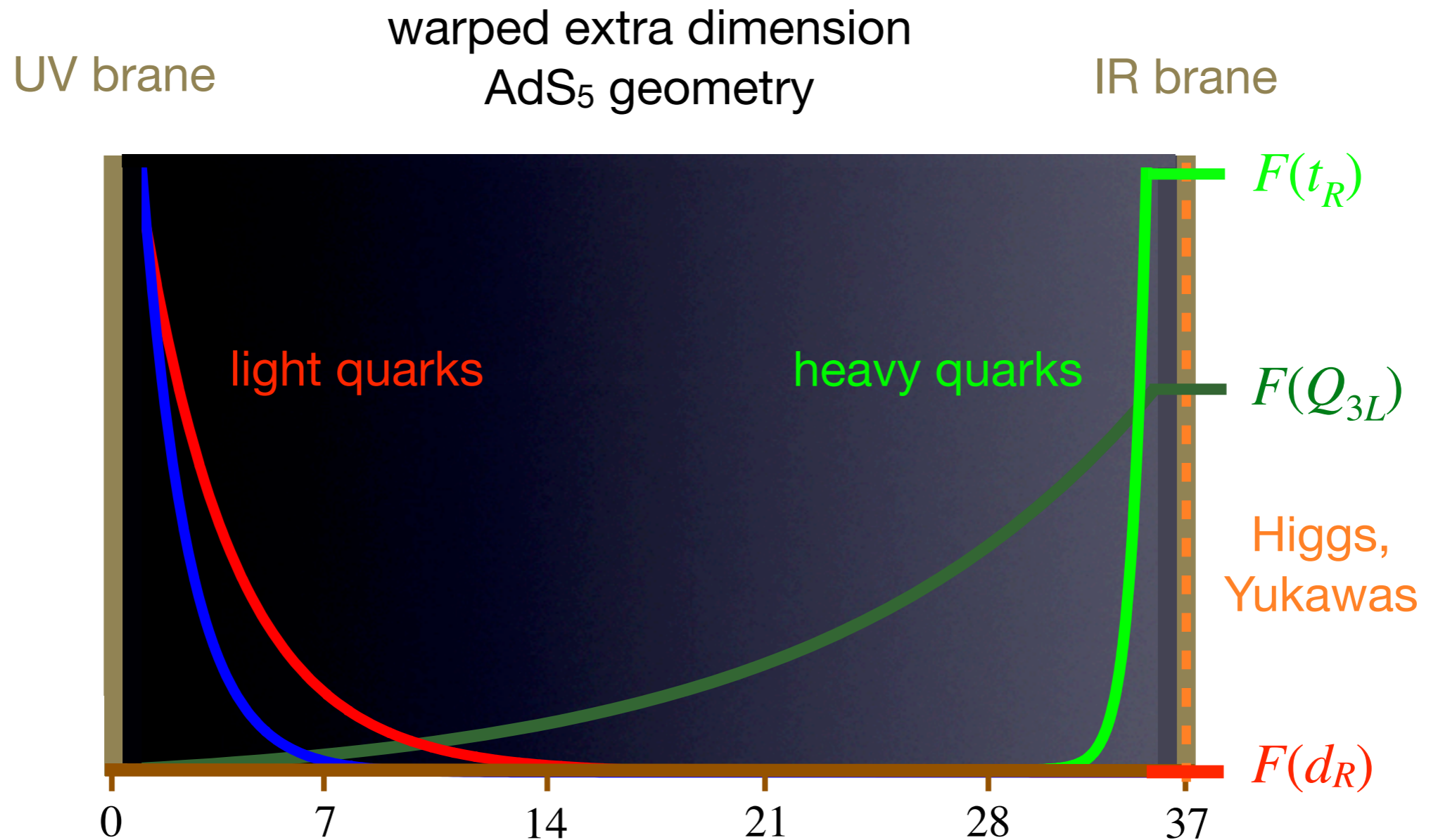
# Flavor Structure in RS Models



Localization of fermions in extra dimension depends exponentially on O(1) parameters: five-dimensional **bulk masses parameters**  $c_q$

Grossman, Neubert (1999); Ghergetta, Pomarol (2000)

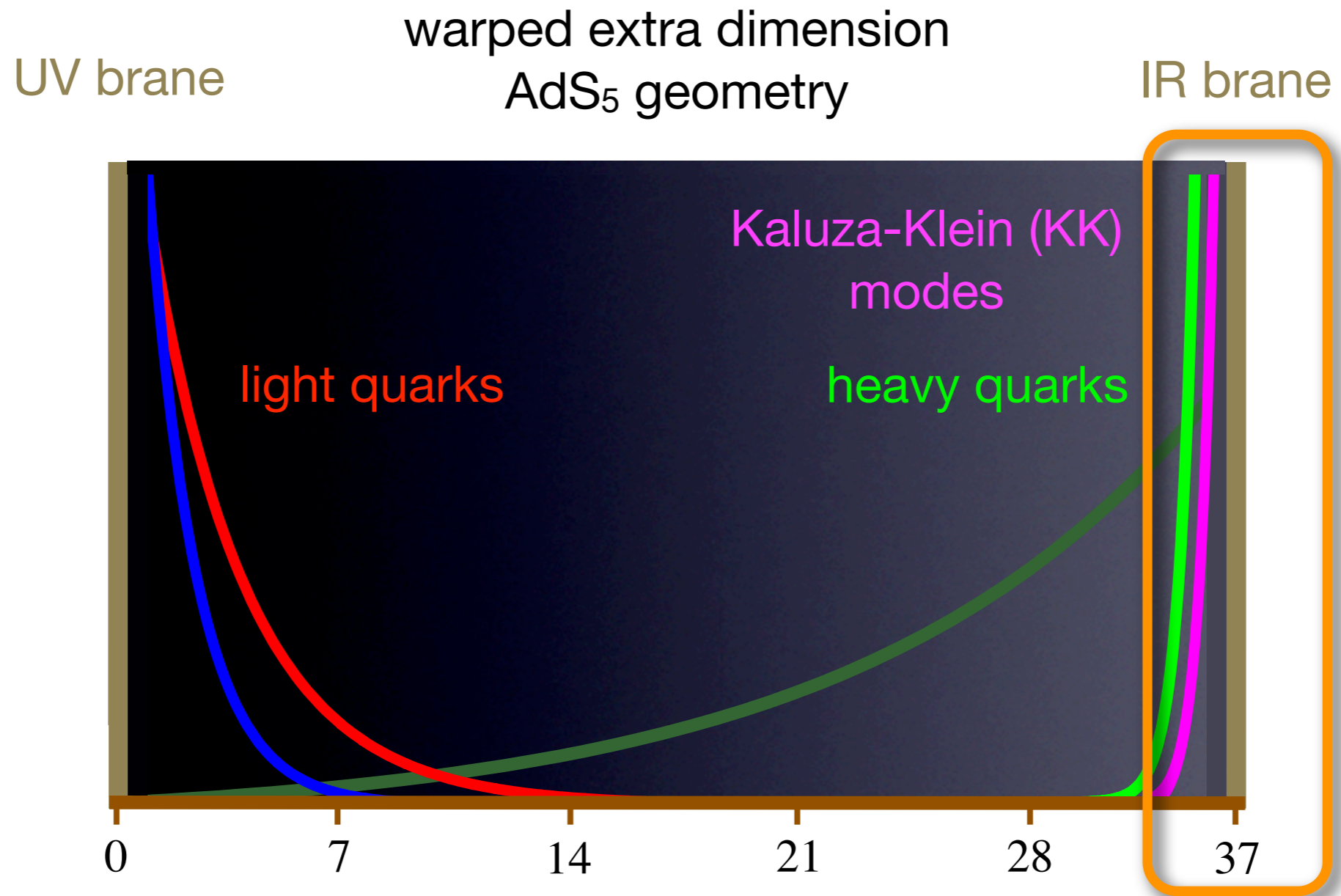
# Flavor Structure in RS Models



Overlaps  $F(Q_L)$ ,  $F(q_R)$  with IR-localized Higgs sector and Yukawa couplings are **exponentially small** for light quarks, while O(1) for top quark

Grossman, Neubert (1999); Ghergetta, Pomarol (2000)

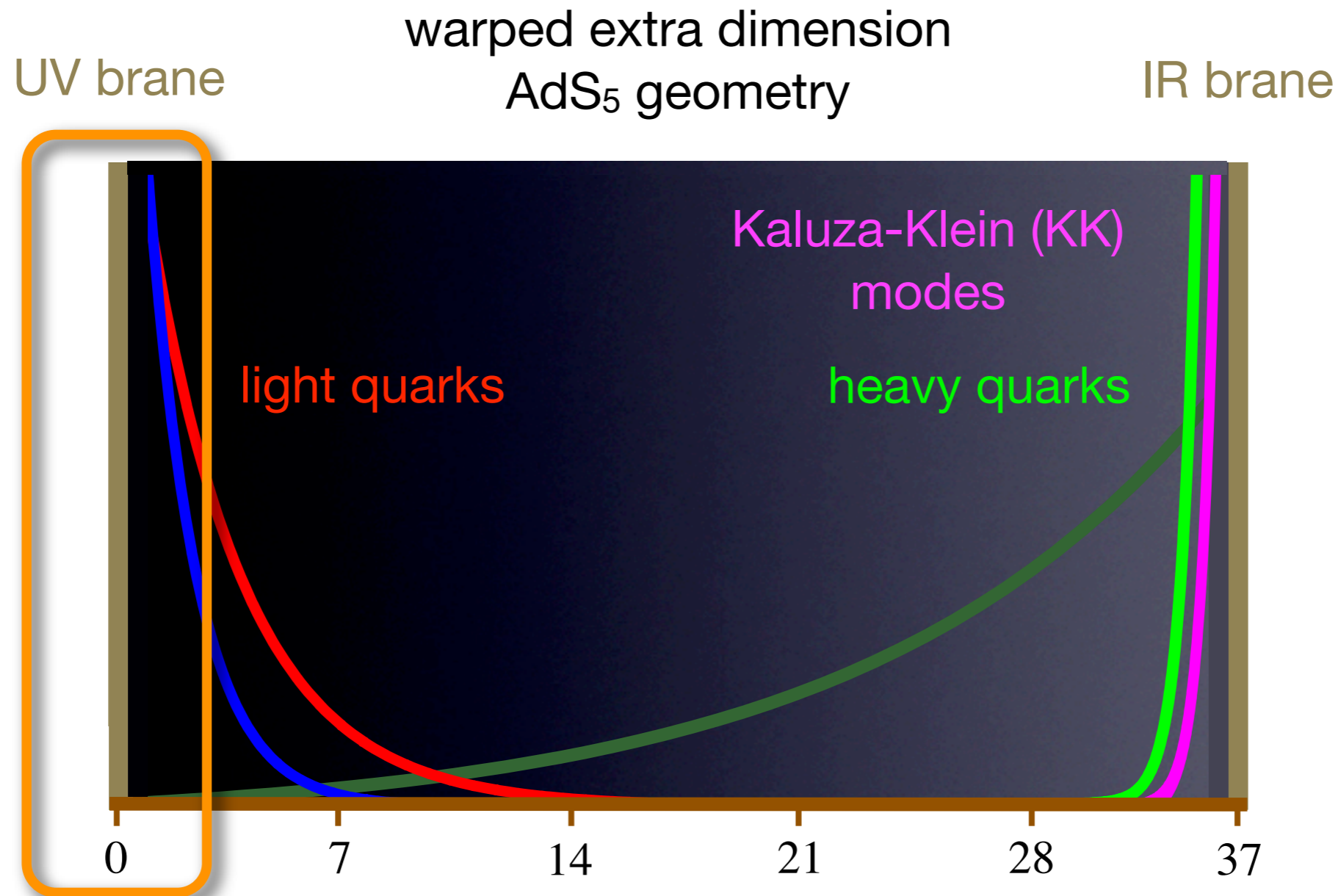
# Flavor Structure in RS Models



Kaluza-Klein (KK) excitations of SM particles live close to IR brane

Davoudiasl, Hewett, Rizzo (1999); Pomarol (1999)

# Flavor Structure in RS Models



Since light quarks live in UV, their couplings to  $W$  and  $Z$  bosons, as well as to KK gauge bosons, are almost flavor-independent

Gherghetta, Pomarol (2000)



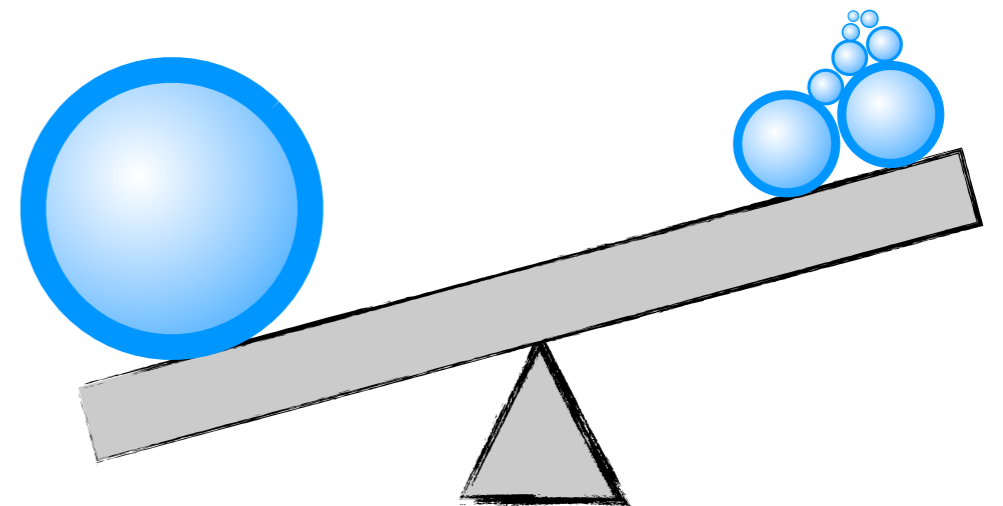
# Hierarchies of Quark Masses and CKM Angles

- SM mass matrices can be written as Huber (2003)

$$m_q^{\text{SM}} = \frac{v}{\sqrt{2}} \text{diag} [F(Q_i)] \mathbf{Y}_q \text{diag} [F(q_i)] = \begin{pmatrix} \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{pmatrix}$$

where  $\mathbf{Y}_q$  with  $q = u, d$  are **structureless, complex Yukawa matrices with  $O(1)$  entries**, and  $F(Q_i) \ll F(Q_j)$ ,  $F(q_i) \ll F(q_j)$  for  $i < j$

- In analogy to seesaw mechanism for neutrinos, matrices of this form give rise to hierarchical mass eigenvalues and mixing matrices



**Warped-space Froggatt-Nielsen mechanism!**

Froggatt, Nielsen (1979); Casagrande *et al.* (2008); Blanke *et al.* (2008)

# Hierarchies of Quark Masses and CKM Angles

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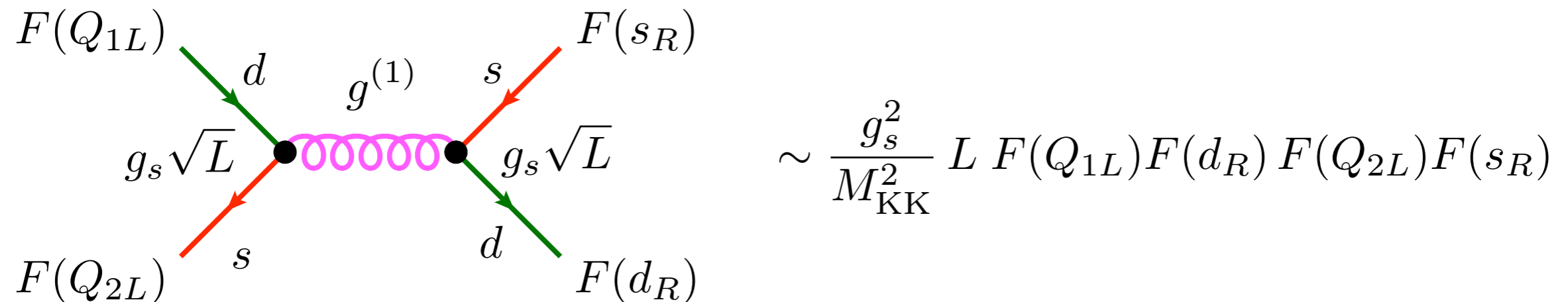
- Thus:

$$\mathbf{m}_q \sim \frac{v}{\sqrt{2}} \text{diag} [F(Q_i)F(q_i)] = \begin{pmatrix} \cdot & & \\ & \cdot & \\ & & \blacksquare \end{pmatrix}$$

$$(V_{\text{CKM}})_{ij} \sim \begin{cases} \frac{F(Q_i)}{F(Q_j)}, & i \leq j \\ \frac{F(Q_j)}{F(Q_i)}, & i > j \end{cases} = \begin{pmatrix} \blacksquare & \blacksquare & \cdot \\ \blacksquare & \blacksquare & \blacksquare \\ \cdot & \blacksquare & \blacksquare \end{pmatrix}$$

- **Hierarchies predicted** and readily adjusted by  $O(1)$  variations of bulk masses
- CP violating phase is predicted to be **unsuppressed!** Casagrande *et al.* (2008); Blanke *et al.* (2008)

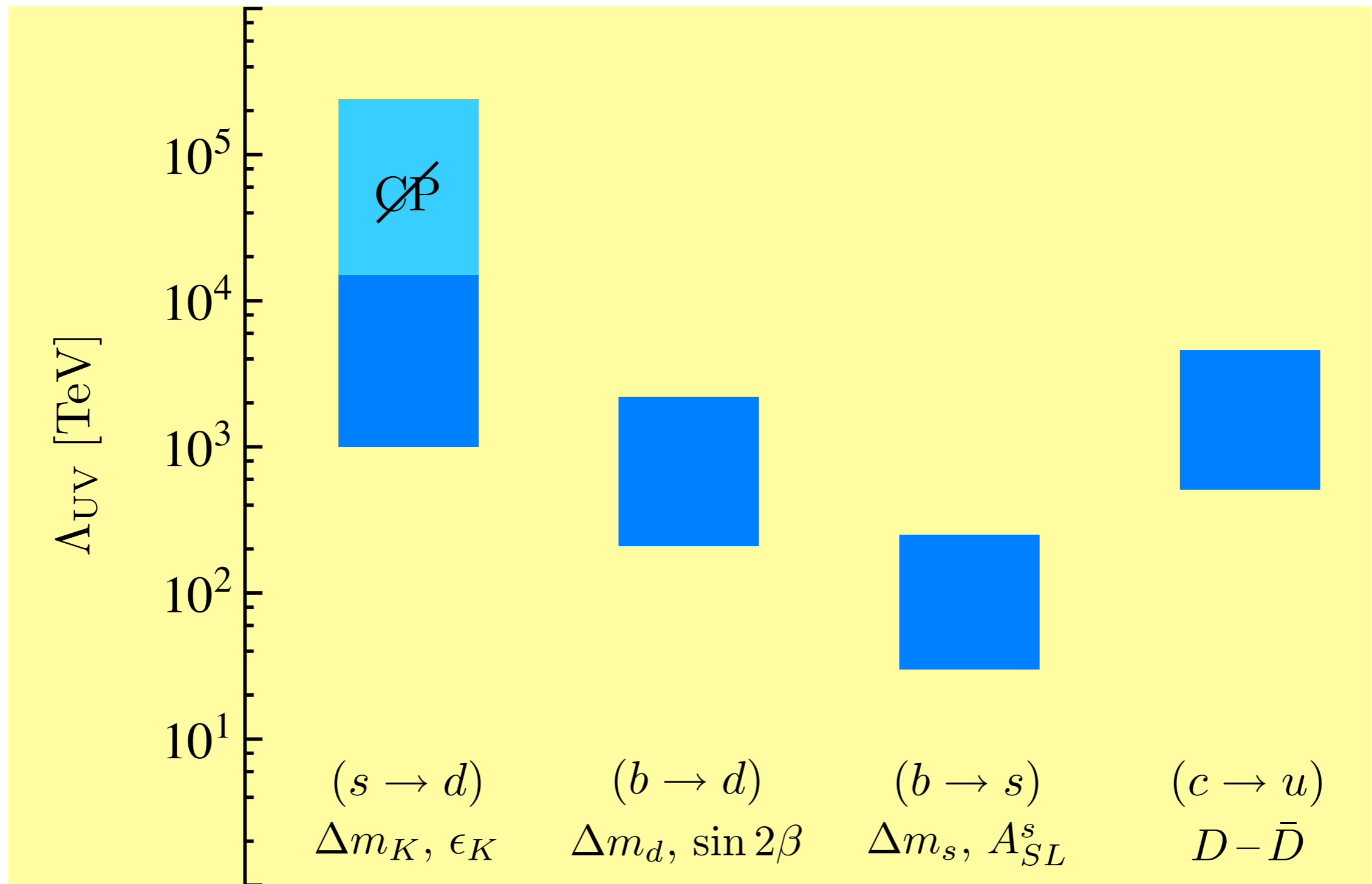
# RS-GIM Protection of FCNCs



- Quark FCNCs are induced at tree-level through virtual exchange of KK gauge bosons (including KK gluons!) [Huber \(2003\)](#); [Burdman \(2003\)](#); [Agashe et al. \(2004\)](#); [Casagrande et al. \(2008\)](#)
- Resulting FCNC couplings depend on same exponentially small overlaps  $F(Q_L)$ ,  $F(q_R)$  that generate fermion masses
- FCNCs involving quarks other than top are strongly suppressed! (true for all induced FCNC couplings) [Agashe et al. \(2004\)](#)

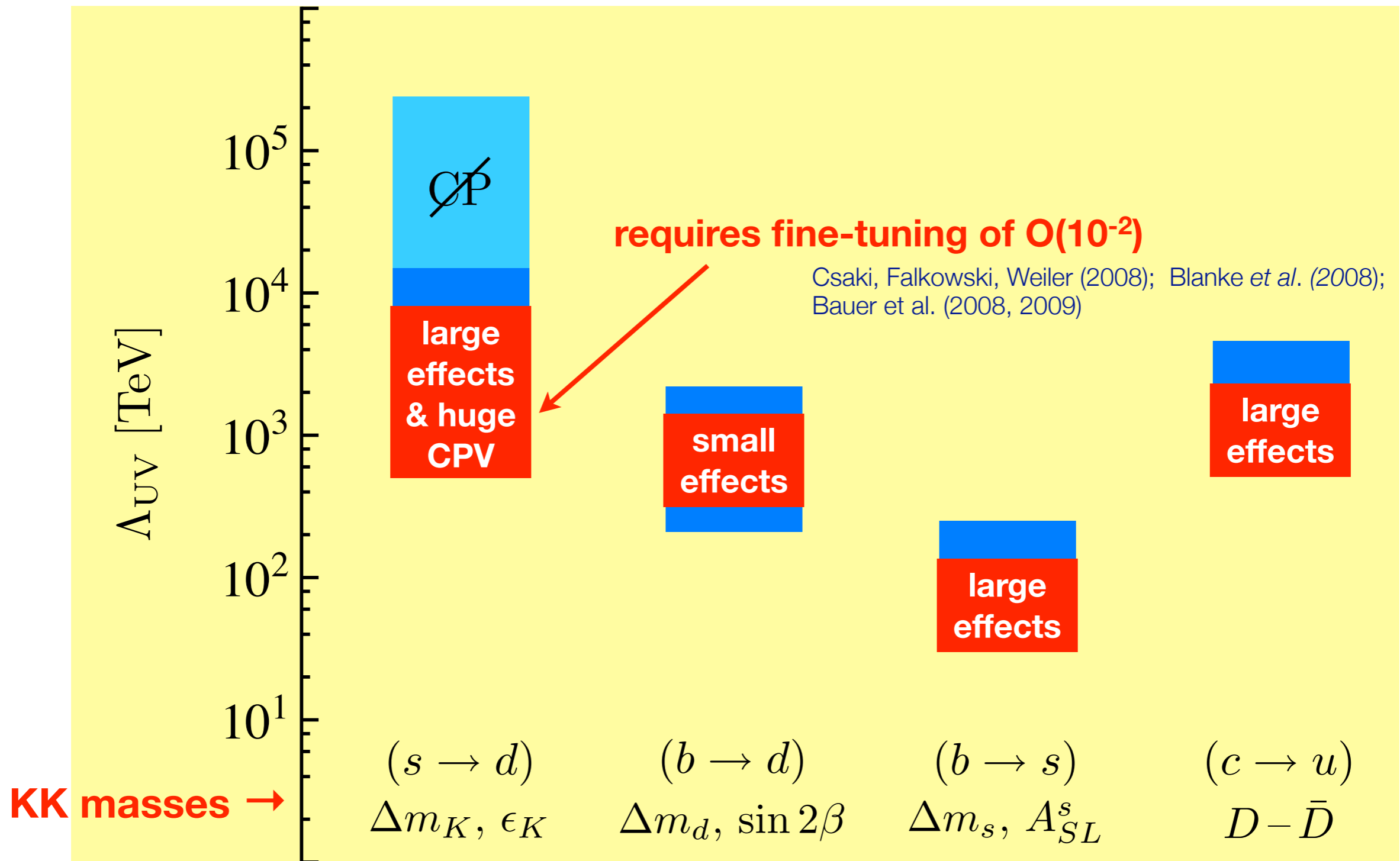
**This mechanism suffices to suppress all but one of the dangerous FCNC couplings!**

# RS-GIM Protection of FCNCs



RS-GIM protection with KK masses of order few TeV

# RS-GIM Protection of FCNCs

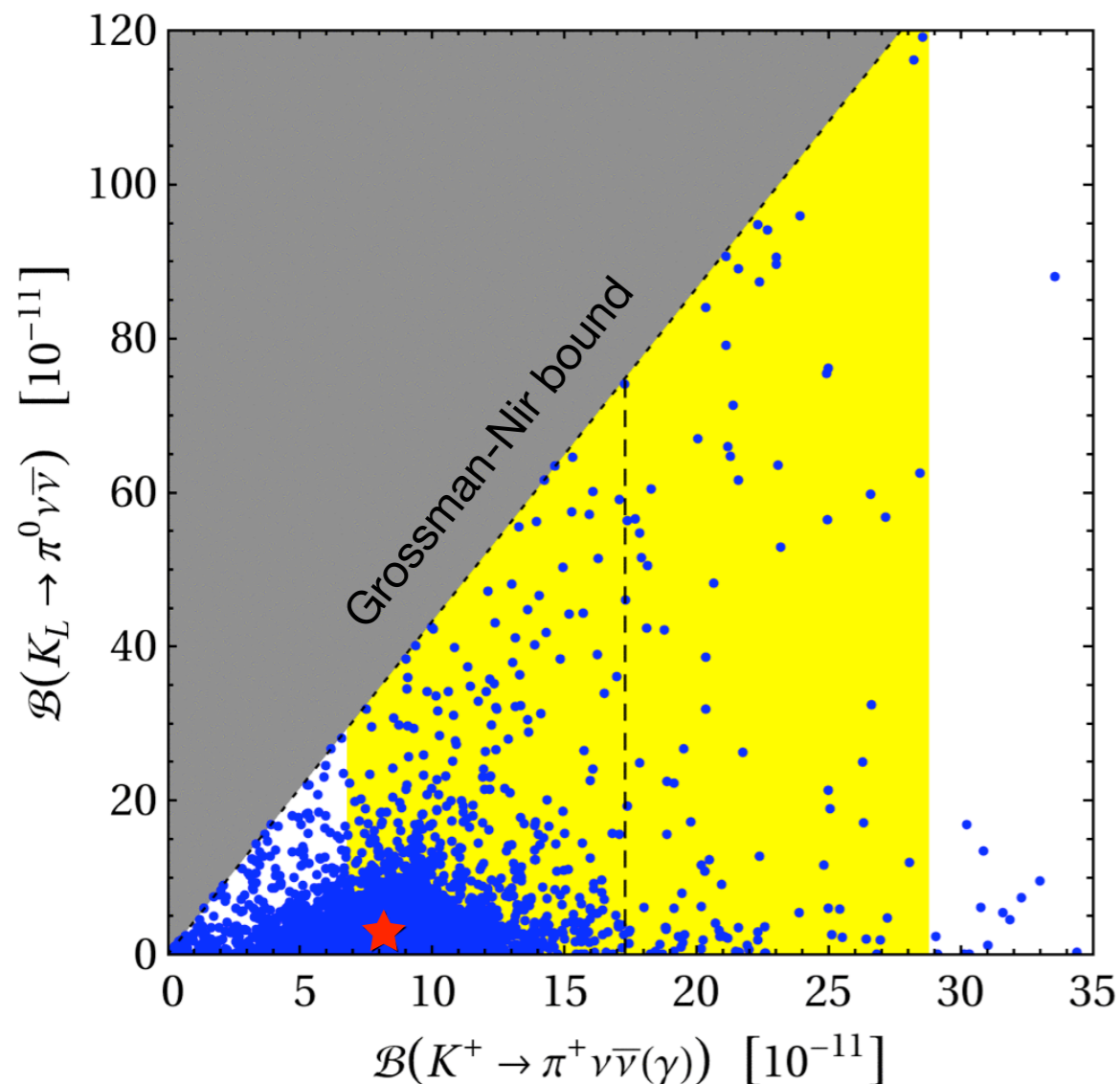


RS-GIM protection with KK masses of order few TeV

# Golden Modes: Rare Kaon Decays

- Spectacular corrections are possible in very clean  $K \rightarrow \pi\nu\bar{\nu}$  decays, even saturating the Grossman-Nir bound,  $\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu}) < 4.4 \mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})$

Blanke *et al.* (2008); Bauer *et al.* (2009)



★ SM:  $\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu}) \approx 8.3 \cdot 10^{-11}$ ,  
 $\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu}) \approx 2.7 \cdot 10^{-11}$

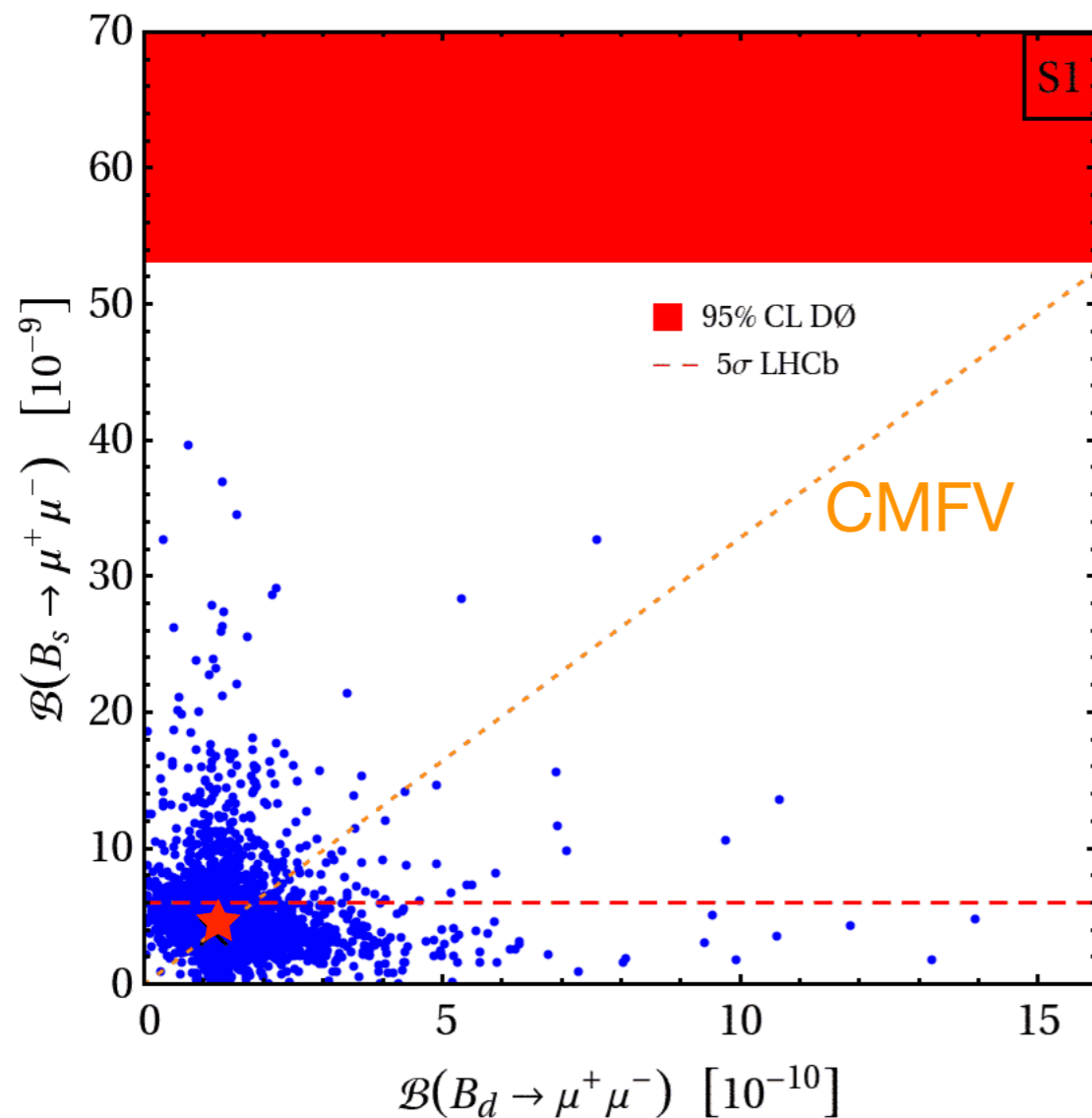
--- central value and 68% CL limit  
 $\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu}) = (17.3_{-10.5}^{+11.5}) \cdot 10^{-11}$   
 from E949

- consistent with quark masses, CKM parameters, and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

# Golden Modes: Rare B Decays

- Factor  $\sim 10$  enhancements possible in rare  $B_{d,s} \rightarrow \mu^+ \mu^-$  modes without violation of  $Z \rightarrow b\bar{b}$  constraints; effects largely uncorrelated with  $|\varepsilon_K|$

Blanke *et al.* (2008); Bauer *et al.* (2009)



★ SM:  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) \approx 1.2 \cdot 10^{-10}$ ,  
 $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) \approx 3.9 \cdot 10^{-9}$

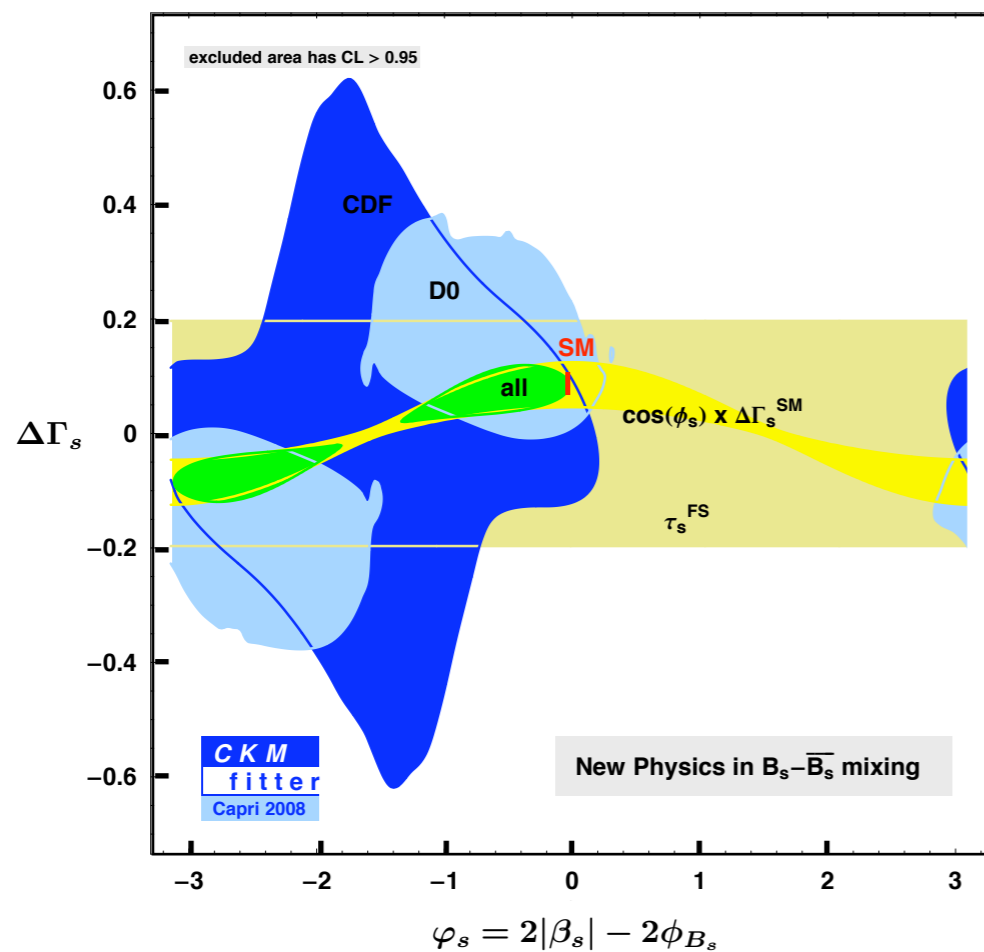
--- minimum of  $5.5 \cdot 10^{-9}$  for 5σ discovery by LHCb,  $2 \text{ fb}^{-1}$

■ 95% CL upper limit from CDF:  
 $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.8 \cdot 10^{-8}$

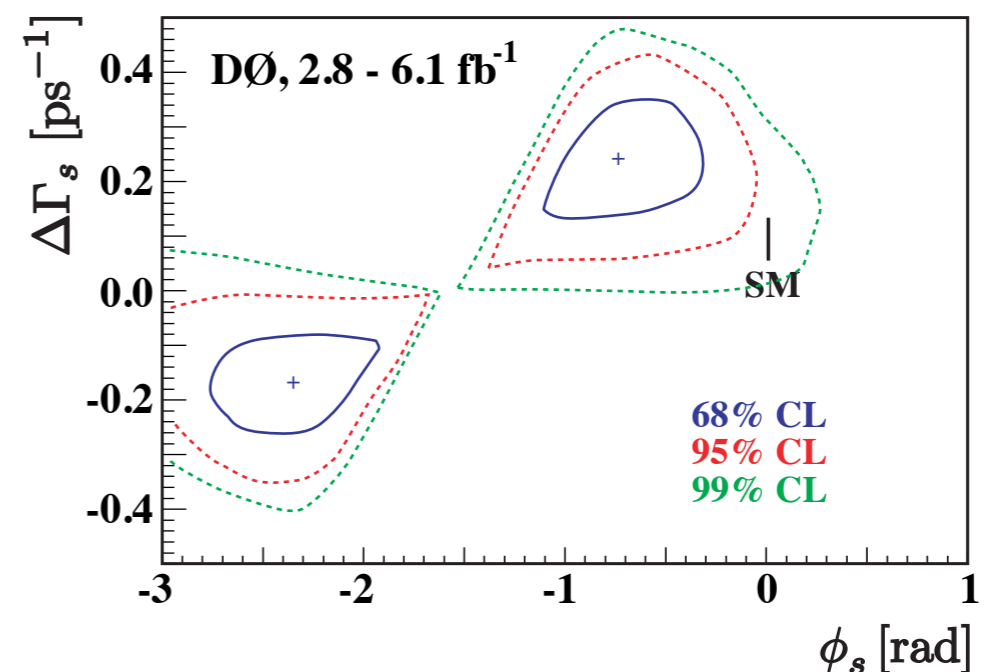
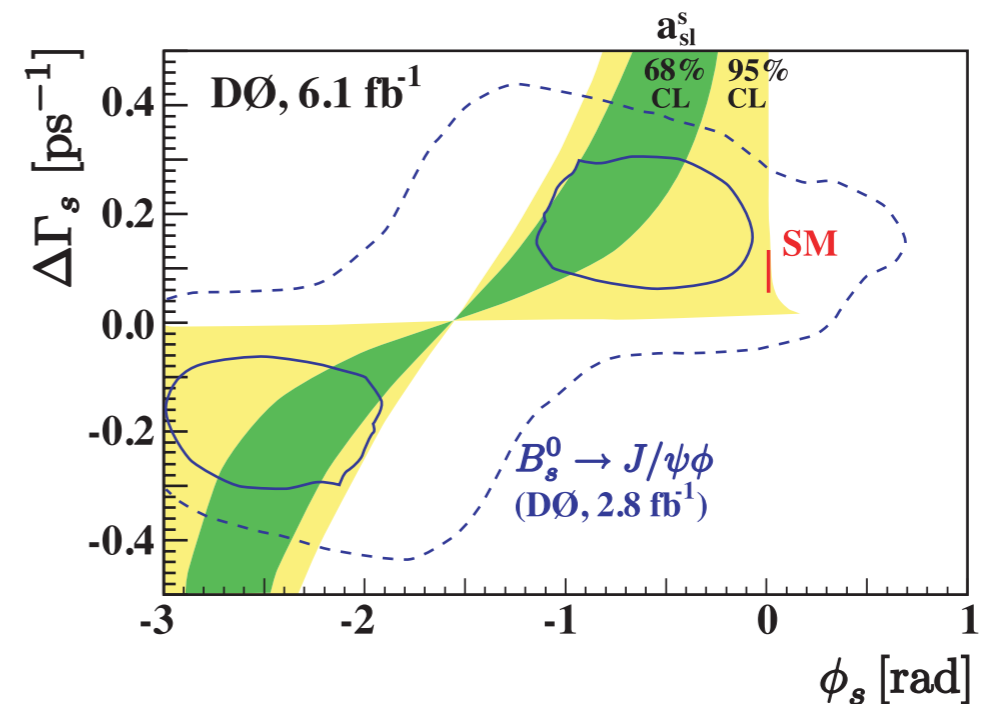
● consistent with quark masses, CKM parameters,  $Z \rightarrow b\bar{b}$ , and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

# New Physics in $B_s - \bar{B}_s$ mixing?

- Tantalizing hints for new physics phase in  $B_s - \bar{B}_s$  mixing from flavor-tagged analysis of mixing-induced CP violation in  $B_s \rightarrow J/\psi\phi$  by CDF and DØ, and more recently from anomalous like-sign di-muon charge asymmetry at DØ



Discrepancy of  $\varphi_s = 2|\beta_s| - 2\phi_{B_s}$  with respect to SM value  $\varphi_s \approx 2^\circ$  at around  $2-3\sigma$  level

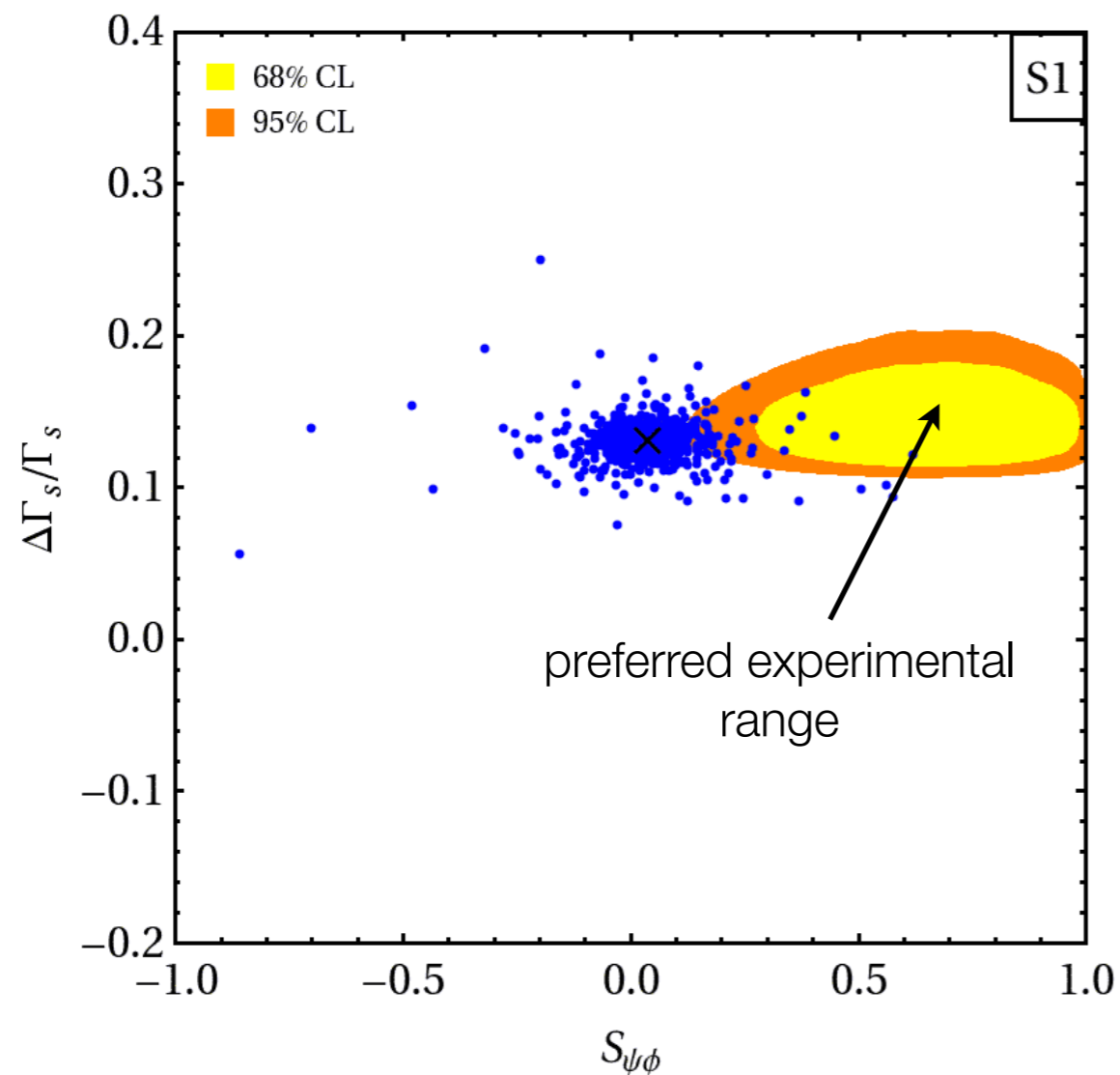




# New Physics in $B_s$ - $\bar{B}_s$ mixing?

- Constraint from  $|\varepsilon_K|$  does not exclude O(1) effects in width difference  $\Delta\Gamma_s/\Gamma_s$  of  $B_s$  system, but difficult to account for central values of data

Blanke *et al.* (2008); Bauer *et al.* (2009)



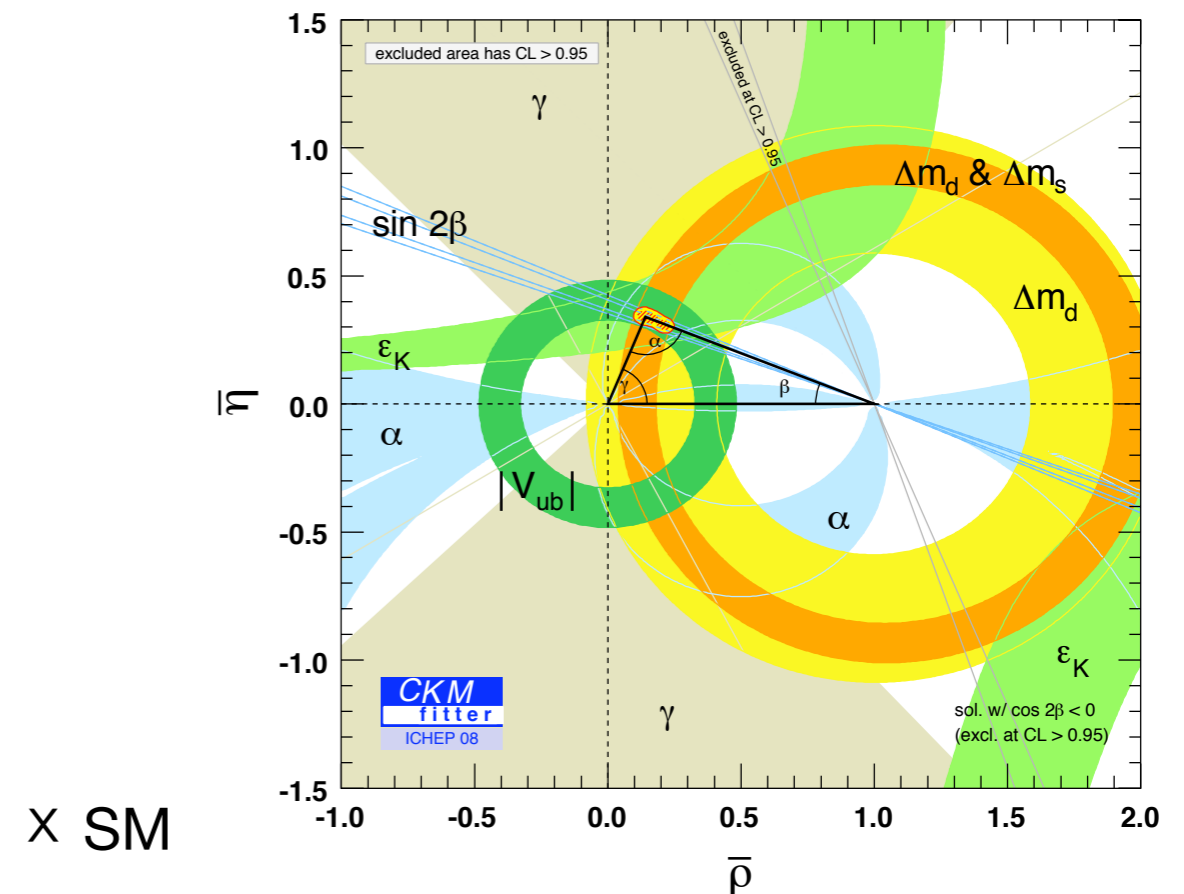
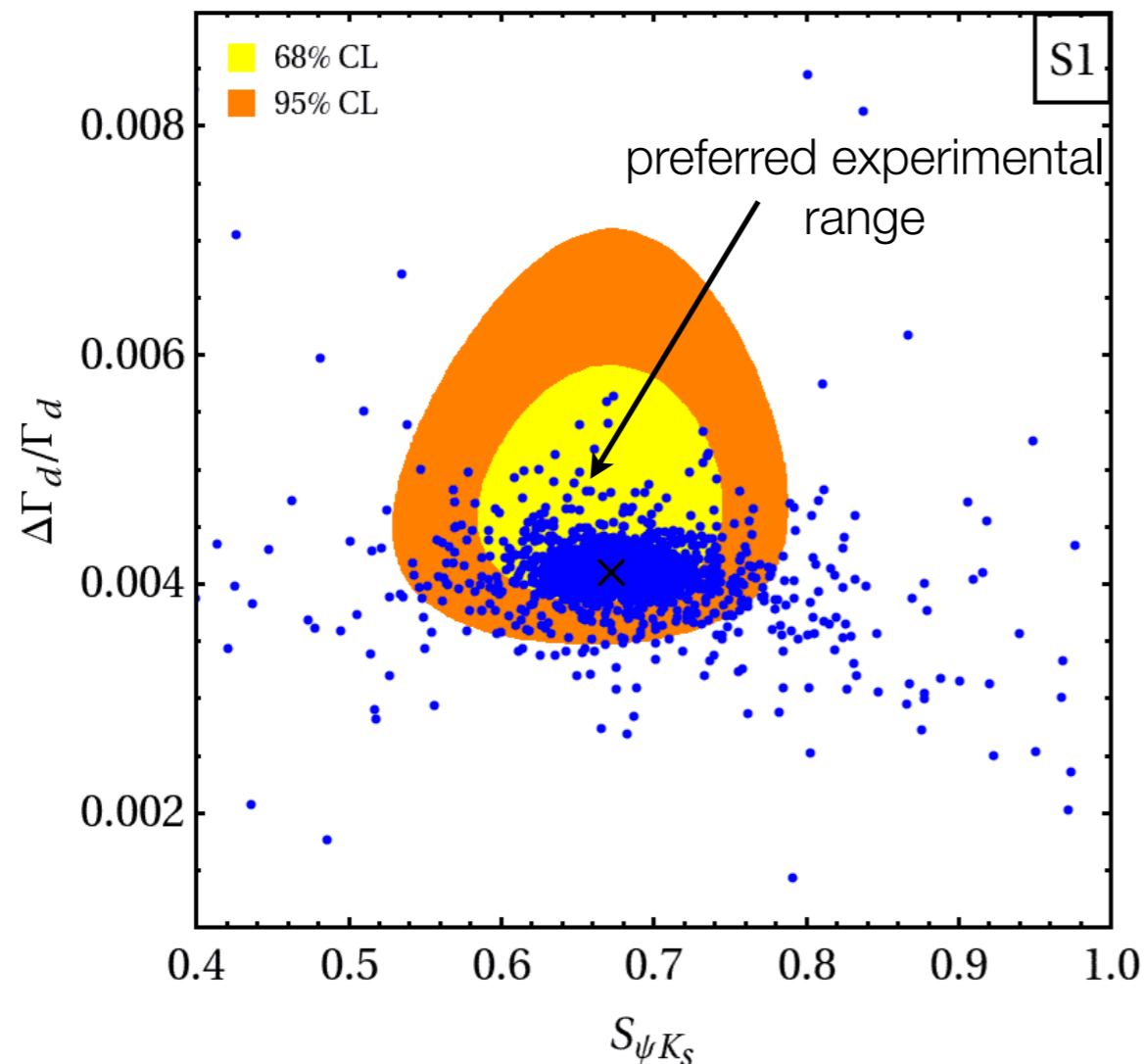
× SM:  $\Delta\Gamma_s/\Gamma_s \approx 0.13$ ,  $S_{\psi\phi} \approx 0.04$

- consistent with quark masses, CKM parameters,  $Z \rightarrow b\bar{b}$ , and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

# New Physics in $B_d$ - $\bar{B}_d$ mixing?

- Constraint from  $|\varepsilon_K|$  does not exclude significant modifications of the CP asymmetry in  $B \rightarrow \psi K_S$ , which could relax the  $|V_{ub}|$  -  $\sin 2\beta$  tension

Blanke *et al.* (2008); Bauer *et al.* (2009)

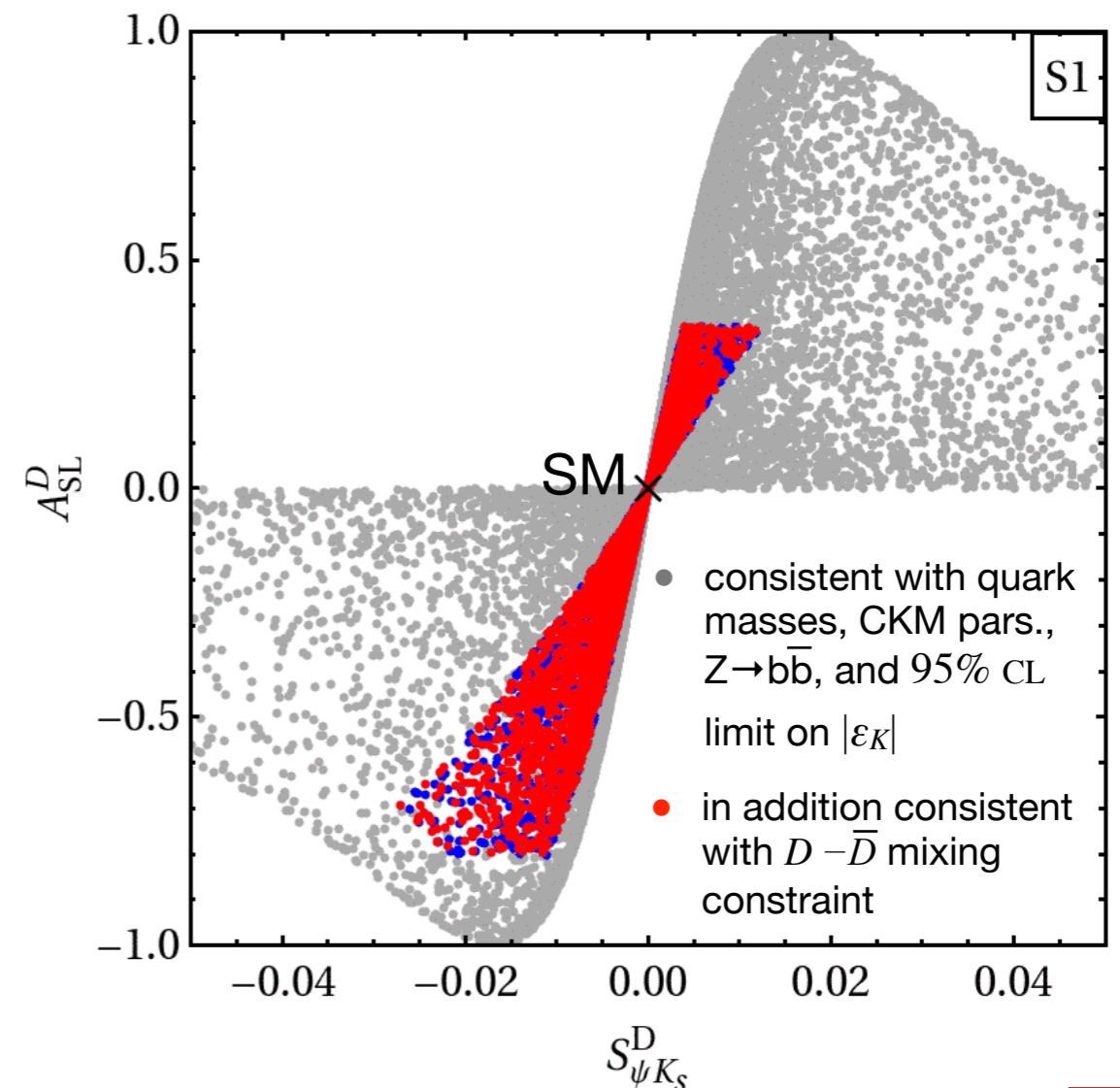
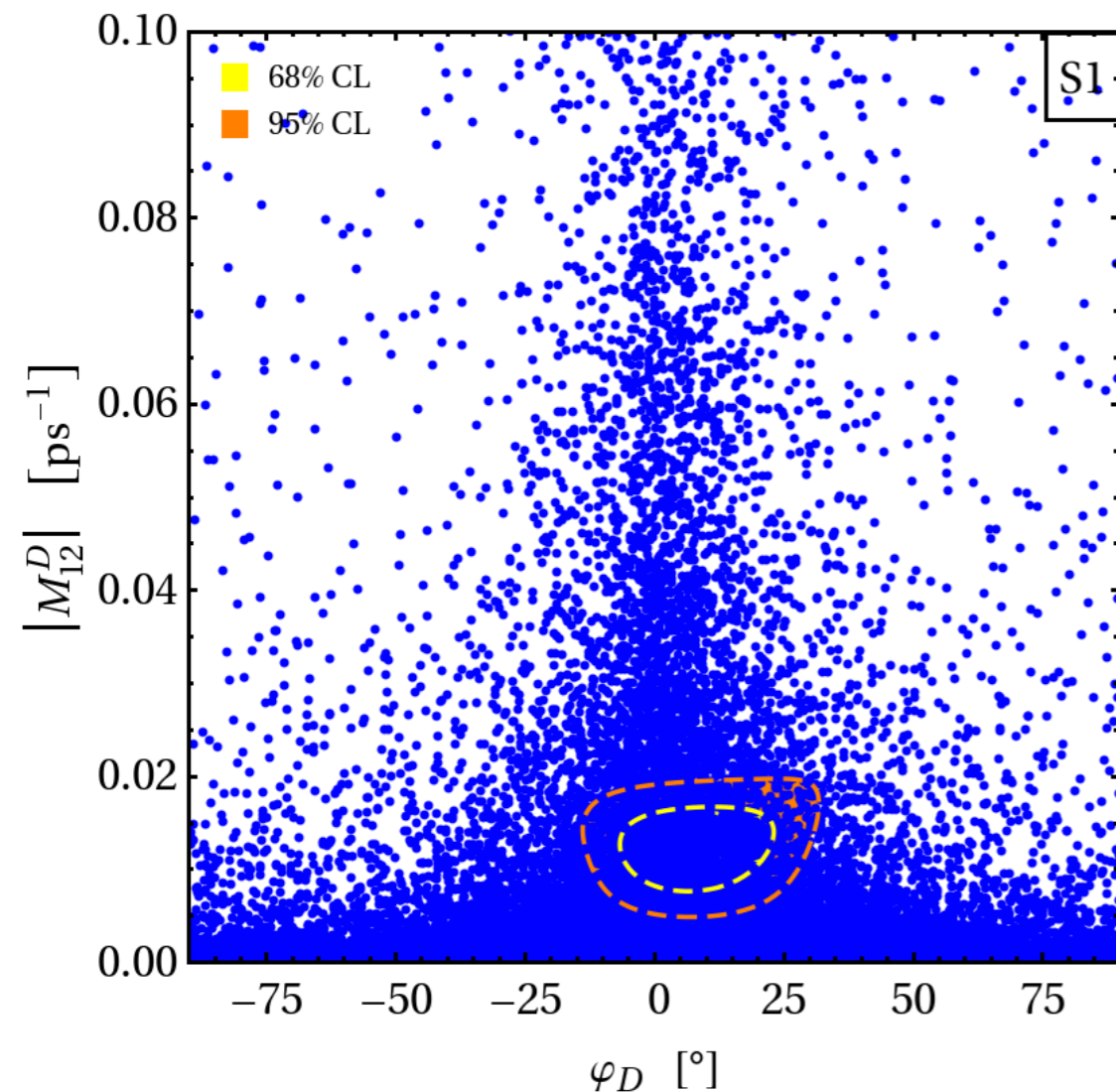


- consistent with quark masses, CKM parameters,  $Z \rightarrow b\bar{b}$ , and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

# D- $\bar{D}$ Mixing

- Very large effects possible, including large CP violation; predictions might be testable at LHCb

Bauer et al. (2009)

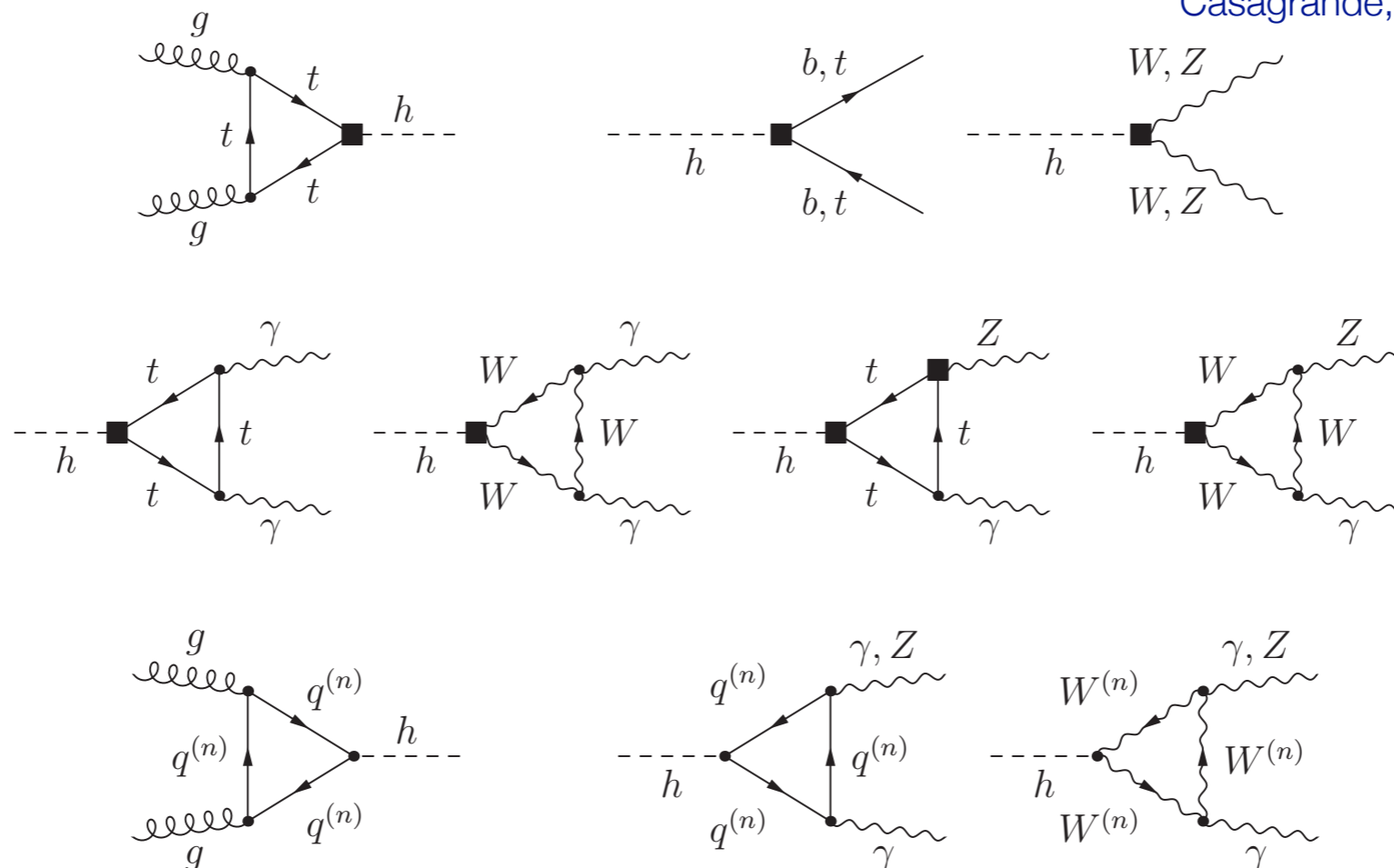


- consistent with quark masses, CKM parameters,  $Z \rightarrow b\bar{b}$ , and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

# Correlations with Higgs physics

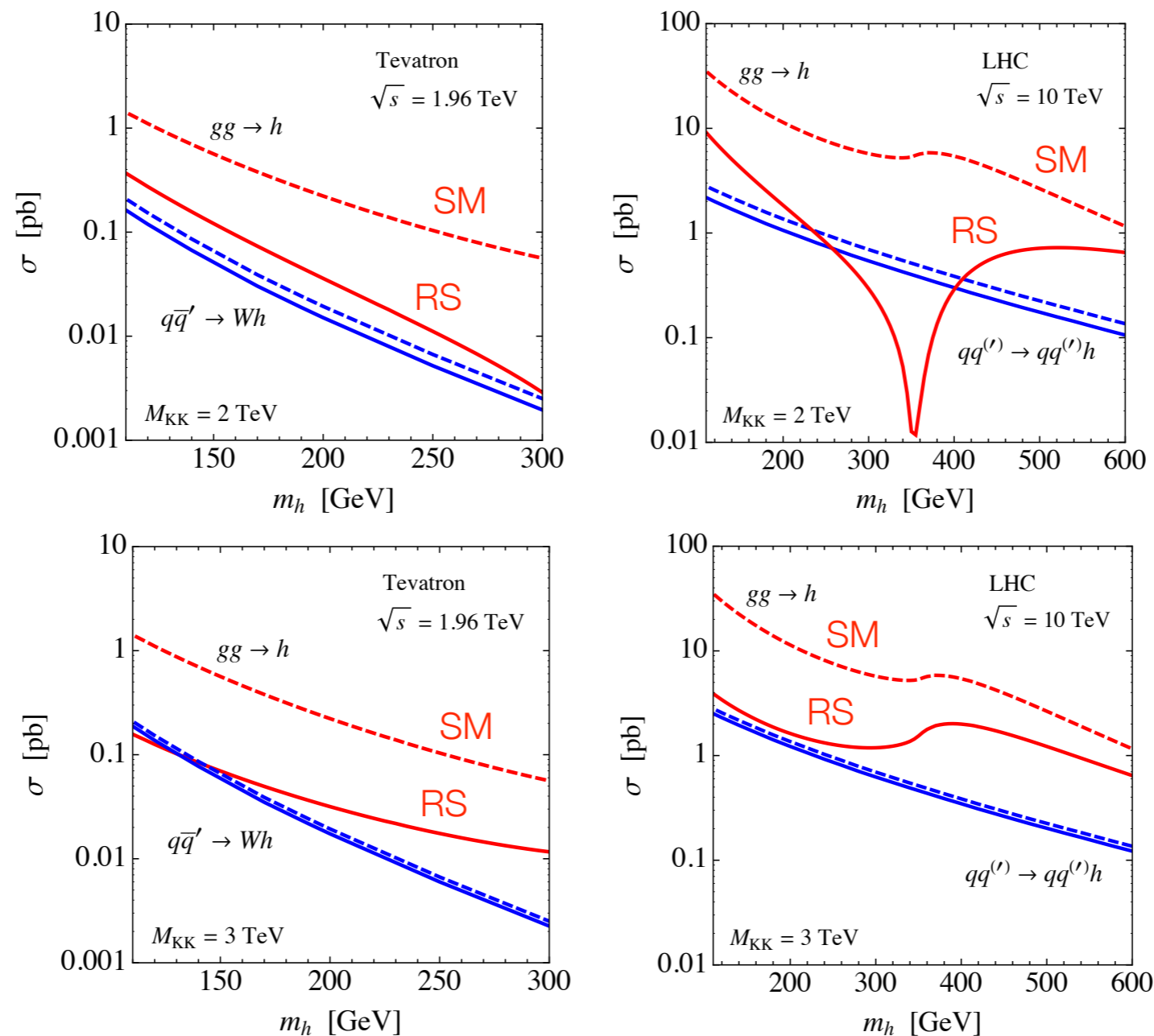
- Properties of the Higgs boson offer alternative ways to probe, via modifications of SM couplings and virtual effects from heavy KK states, the structure of warped extra-dimension models
- Recently, we have performed the first complete one-loop analysis of Higgs production and decays in the RS model with custodial symmetry

Casagrande, Goertz, Haisch, MN, Pfoh (2010)



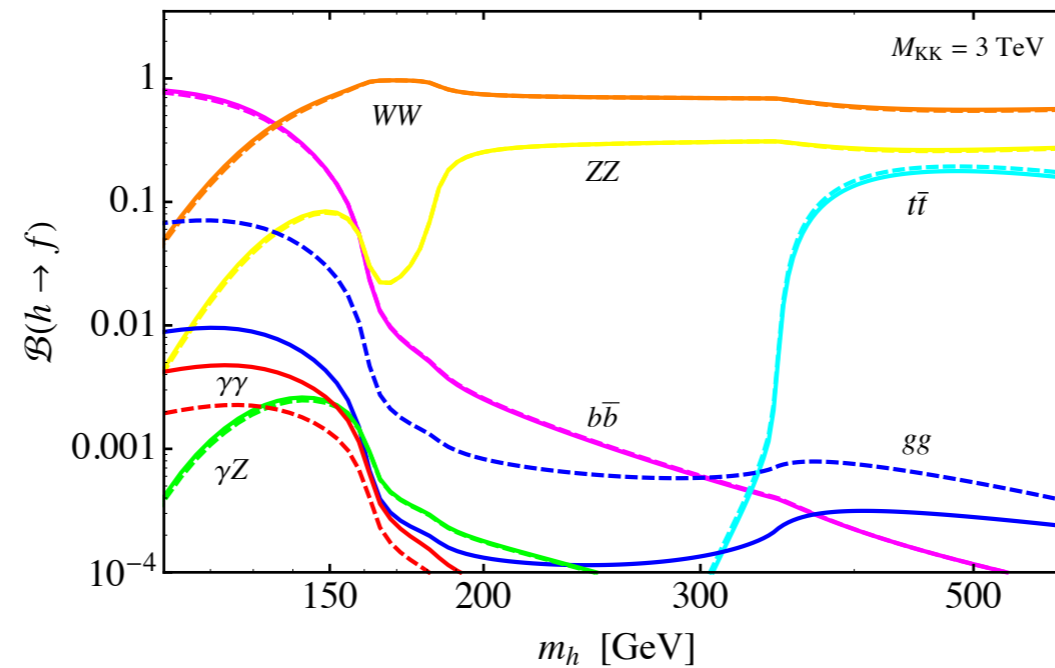
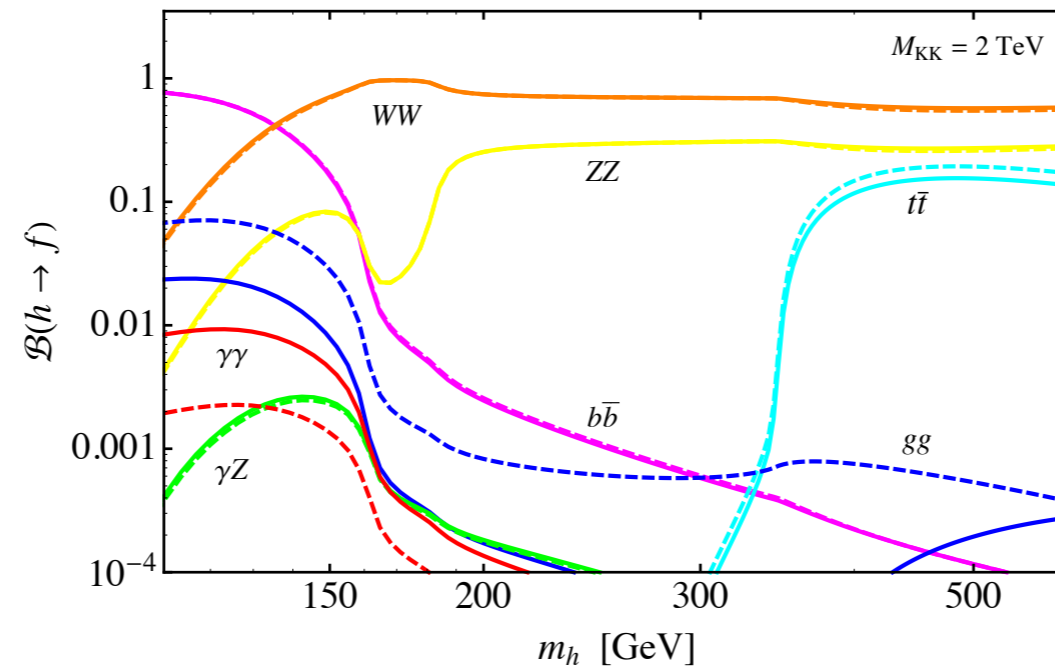
# Higgs production cross sections

- Find possibly spectacular effects on Higgs production via gluon fusion, even for high KK masses ( $m_{G_{\text{KK}}^{(1)}} \approx 2.45 M_{\text{KK}}$ ):



# Higgs decay branching fractions

- Correspondingly, find possibly significant impact on  $h \rightarrow gg$  and  $h \rightarrow \gamma\gamma$  branching ratios:



# Puzzles in the Flavor Sector: **Facts or Fiction?**

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Several observables don't look quite right ... ( $\sim 2\sigma$  effects)

# Puzzles in the Flavor Sector: Facts or Fiction?

$\sin 2\beta$  from  
tree vs. loop  
processes

$|V_{cb}|$  and  $|V_{ub}|$   
exclusive vs.  
inclusive

$|V_{ub}|$  vs.  
 $\sin 2\beta$  and  $\epsilon_K$

$\Delta A_{CP}(B \rightarrow \pi K)$   
puzzle



CP violation  
in  $B_s$  mixing

enhanced  
 $B \rightarrow \tau \nu$  rate

$A_{FB}$   
asymmetry in  
 $B \rightarrow K^* l^+ l^-$

not yet  
measured ...

Several observables don't look quite right ... ( $\sim 2\sigma$  effects)



# Summary and Outlook

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The first collisions at the LHC mark the beginning of a fantastic era for particle physics, which holds promise of ground-breaking discoveries

ATLAS and CMS discoveries alone are unlikely to provide a complete understanding of the observed phenomena

Flavor physics (more generally, low-energy precision physics) will play a key role in unravelling what lies beyond the Standard Model, providing access to energy scales and couplings inaccessible at the energy frontier

Only the synergy of LHC and high-precision experiments may give us the key to solving the puzzles of fundamental physics

