

CKM
fitter



From the KM ansatz to the search of New Physics in $\Delta F=2$ FCNC

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CKM Matrix

In SM, weak-charged transitions mix quarks of different generations

↳ CKM matrix: free parameters determined experimentally

- Once we assume unitarity, the CKM matrix can be completely determined using only tree-level CC amplitudes: $\Gamma \propto |V_{ij}|^2$
- The only CKM elements we cannot access via tree-level processes are V_{ts} and V_{td} .

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} n \begin{array}{c} e^- \\ \bar{\nu} \\ p \end{array} & K \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} & B \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} \\ D \begin{array}{c} \ell^- \\ \bar{\nu} \\ \pi \end{array} & D \begin{array}{c} \ell^- \\ \bar{\nu} \\ K \end{array} & B \begin{array}{c} \ell^- \\ \bar{\nu} \\ D \end{array} \\ B^0 \begin{array}{c} \bar{B}^0 \end{array} & B_s \begin{array}{c} \bar{B}_s \end{array} & t \begin{array}{c} W \\ b \end{array} \end{pmatrix}$$

Four unknowns using a unitary Wolfenstein parametrization

→ Unitarity-exact to all order in λ and phase-convention independent :

Charles *et al.*
EPJC 41, 1 (2005)

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}, \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2}, \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

KM ansatz (1973): one irreducible phase with 3 families

↳ only source of CP violation in the SM



Kobayashi & Maskawa,
Prog.Theor.Phys.49 (1973) 652
Cited 6032 times (SPIRES)

Inputs

Use Frequentist significance testing to build statistical significance (p-value) functions from which estimates and confidence intervals are obtained; test statistic=likelihood-ratio test. Dedicated Rfit scheme for the treatment of theoretical systematics.

data = weak \otimes QCD \implies Need for hadronic inputs (often lattice)

$ V_{ud} $	superallowed β decays	PRC79, 055502 (2009)
$ V_{us} $	$K_{\ell 3}$ (Flavianet)	$f_+(0) = 0.963 \pm 0.003 \pm 0.005$
ϵ_K	PDG 08	$\hat{B}_K = 0.723 \pm 0.004 \pm 0.067$
$ V_{ub} $	inclusive and exclusive	$ V_{ub} \cdot 10^3 = 3.92 \pm 0.09 \pm 0.45$
$ V_{cb} $	inclusive and exclusive	$ V_{cb} \cdot 10^3 = 40.89 \pm 0.38 \pm 0.59$
Δm_d	last WA $B_d - \bar{B}_d$ mixing	$B_{B_s} / B_{B_d} = 1.05 \pm 0.01 \pm 0.03$
Δm_s	last WA $B_s - \bar{B}_s$ mixing	$B_{B_s} = 1.28 \pm 0.02 \pm 0.03$
β	last WA $J/\psi K^{(*)}$	
α	last WA $\pi\pi, \rho\pi, \rho\rho$	isospin
γ	last WA $B \rightarrow D^{(*)} K^{(*)}$	GLW/ADS/GGSZ
$B \rightarrow \tau \nu$	$(1.68 \pm 0.31) \cdot 10^{-4}$	$f_{B_s} / f_{B_d} = 1.199 \pm 0.008 \pm 0.023$ $f_{B_s} = 228 \pm 3 \pm 17 \text{ MeV}$

NEW

Inputs: γ

- **GLW** : D^0 decays into CP eigenstate
- **ADS** : D^0 decays to $K^-\pi^+$ (fav.) and $K^+\pi^-$ (sup.)
- **GGSZ** : D^0 decays to $K_S\pi^+\pi^-$ (interference in Dalitz plot)

All methods fit simultaneously:

γ , r_B and δ (different r_B and δ)

σ_γ depends significantly on the value of r_B

Coverage-adjusted 1D p-value function for γ :

$$71_{-25}^{+21} \text{ (deg)}$$

Without coverage adjustment: 71_{-17}^{+11} (deg)

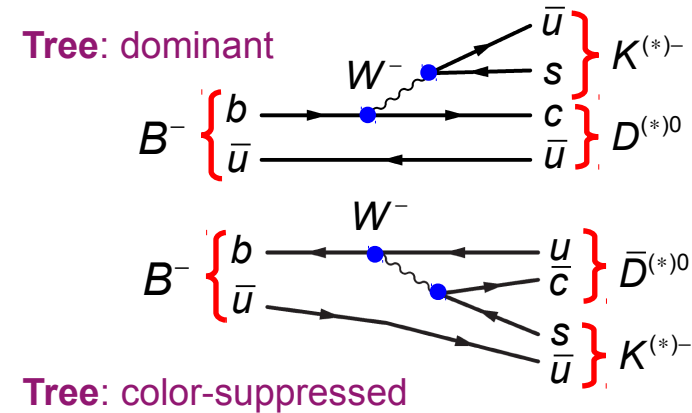


GGSZ: arXiv:1005.1096
 ADS: arXiv:1006.4241
 GLW: arXiv:1007.0504

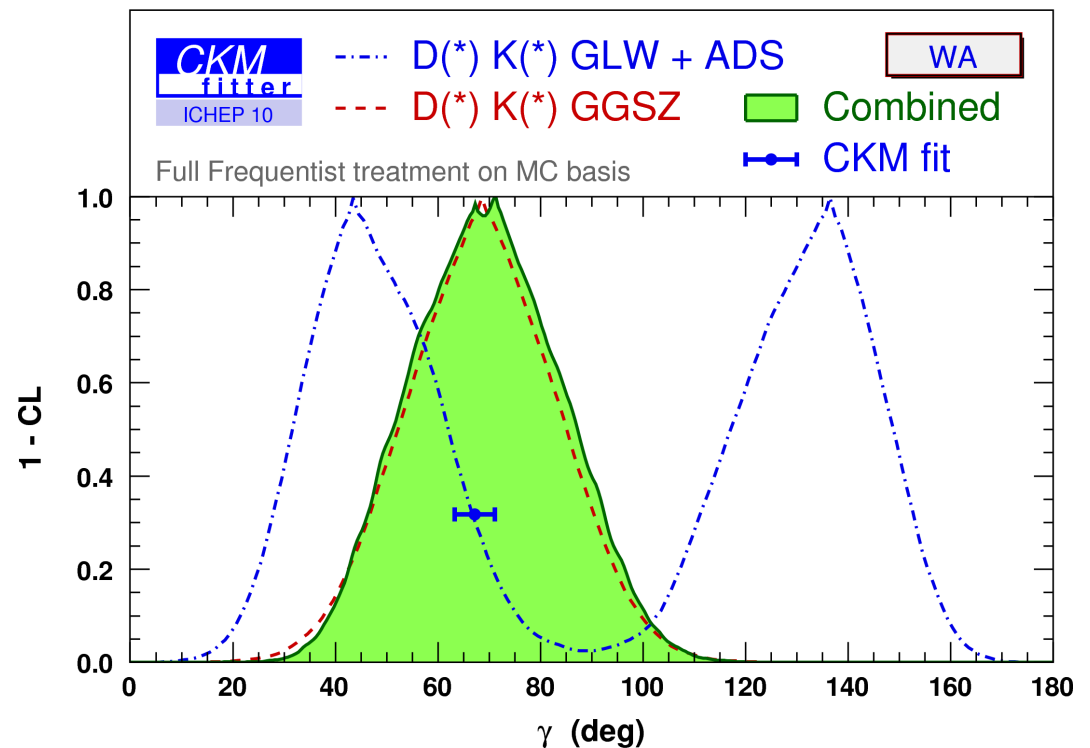


GGSZ: arXiv:1003.3360

NEW

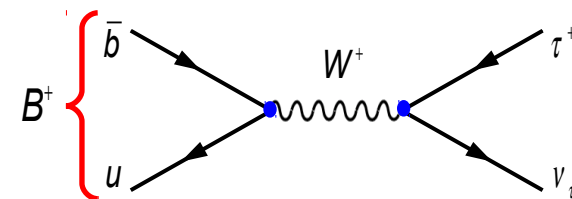


GLW: Gronau-London, PL B253, 483 (1991);
 Gronau-Wyler, PL B265, 172 (1991)
 ADS: Atwood-Dunietz-Soni, PRL 78, 3257 (1997)
 GGSZ: Giri *et al*, PRD 68, 054018 (2003)





Inputs: $B \rightarrow \tau \nu$

- helicity-suppressed annihilation decay sensitive to $f_B \times |V_{ub}|$
- Sensitive to charged Higgs replacing the W propagator

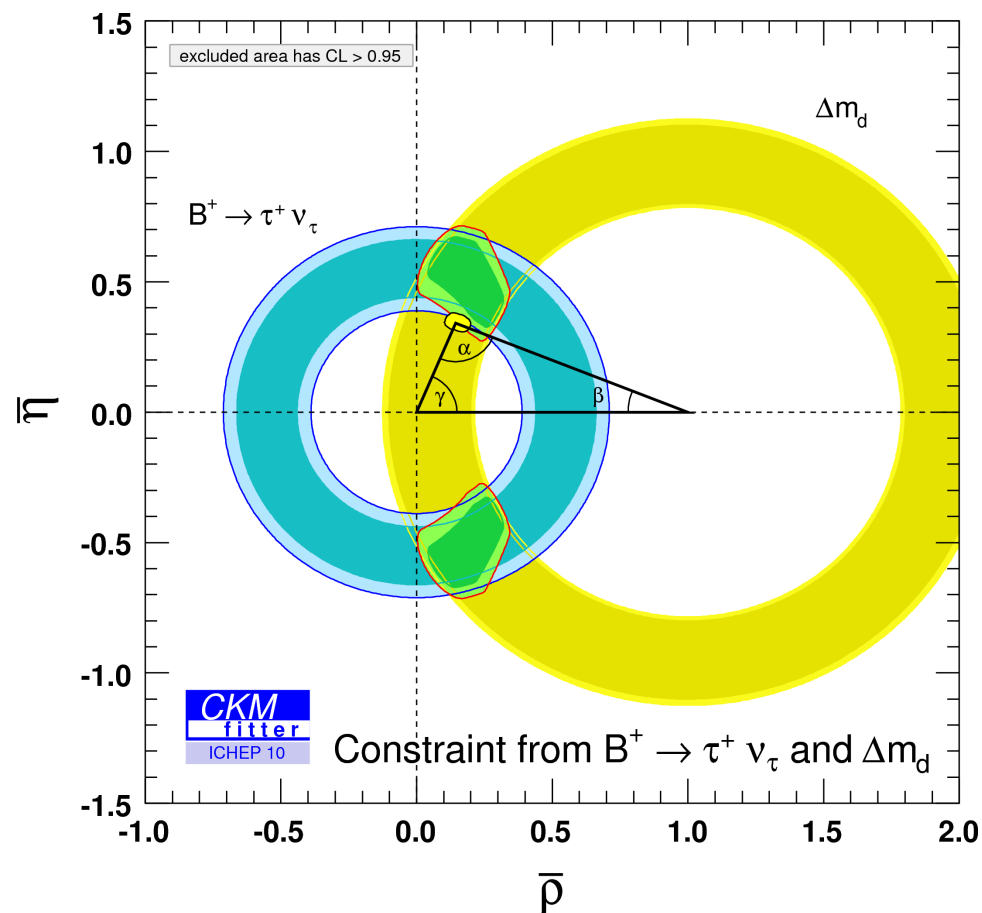


$$\text{BR}(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$

	tag	BF($\rightarrow \tau \nu$) [10^{-4}]
	SL (459M)	1.70 ± 0.82
	Had (467M)	1.80 ± 0.61 NEW
	Average	1.76 ± 0.49
	SL (657M)	1.54 ± 0.48 NEW
	Had (449M)	1.79 ± 0.71
	Average	1.62 ± 0.40
World Average		1.68 ± 0.31

Prediction from global CKM fit:

$$\text{BF}(B^+ \rightarrow \tau^+ \nu_\tau) = (0.763_{-0.061}^{+0.114}) \times 10^{-4}$$



KM ansatz: tested to be dominant source of CPV at the EW scale

Inputs (theor. uncer. under control (LQCD)):

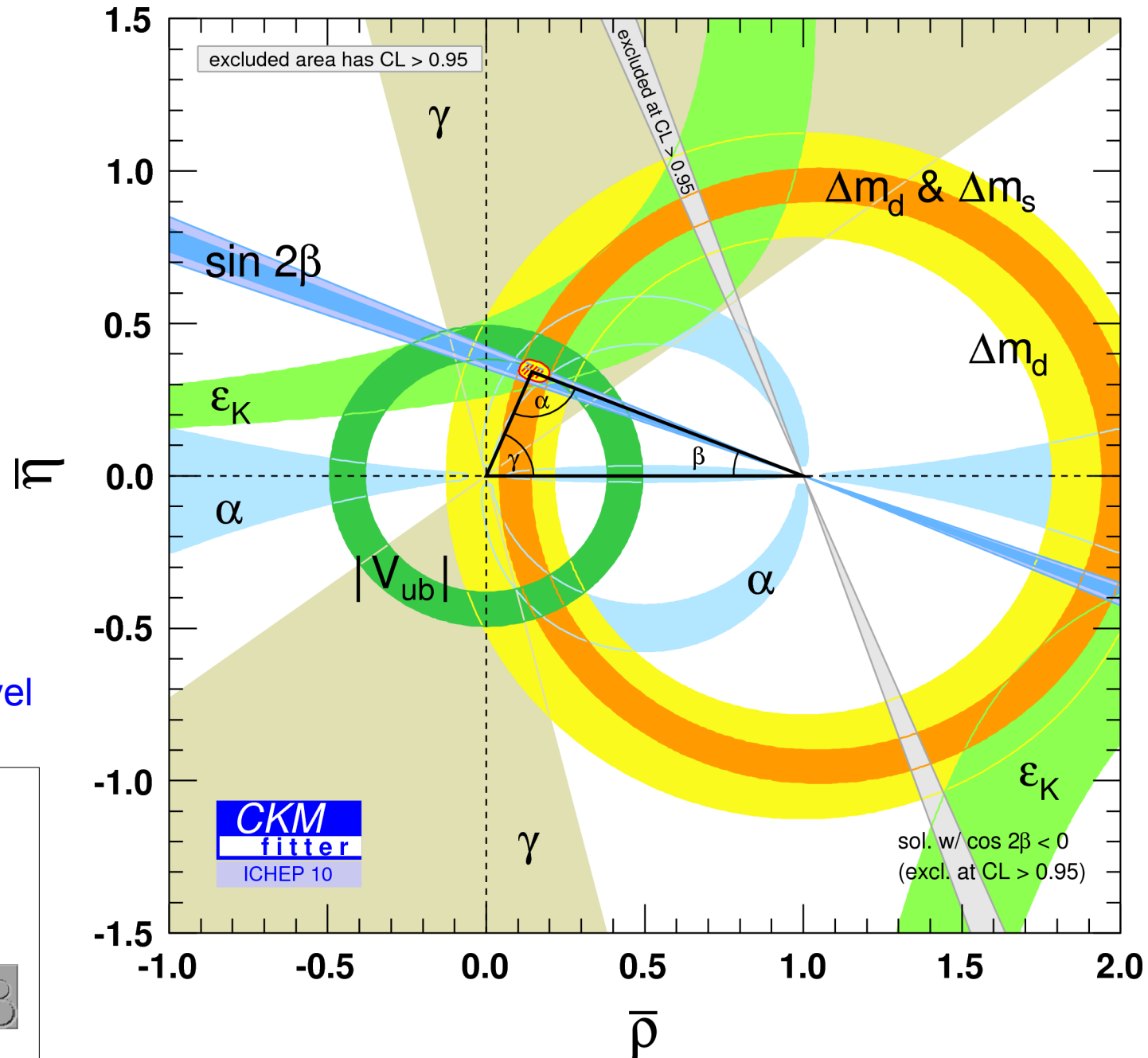
$A, \lambda: |V_{ud}|, |V_{us}|, |V_{cb}|$

$(\bar{\rho}, \bar{\eta})$:

- $|V_{ub}|$
- $B \rightarrow TV$
- γ
- Δm_d
- $\Delta m_d \& \Delta m_s$
- $|\epsilon_K|$
- $\sin 2\beta$
- α

Overall consistency at 2σ level

May '99-Apr '08
 May '99-Jun '10
 ...



Global Fit results

Wolfenstein parameters: (relative precision: 2.5%, 0.4%, 17% and 5%)

$A = 0.812^{+0.013}_{-0.027}$	$\lambda = 0.22543 \pm 0.00077$	$\bar{\rho} = 0.144 \pm 0.025$	$\bar{\eta} = 0.342^{+0.016}_{-0.015}$
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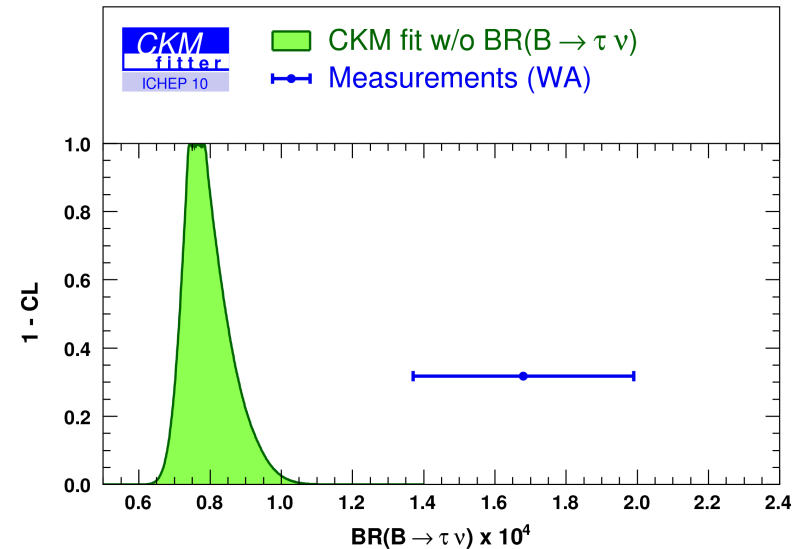
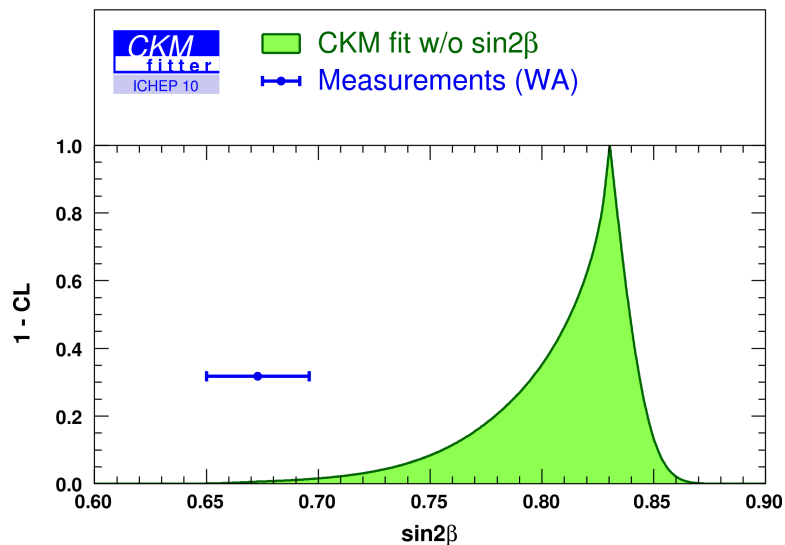
Sides and angles:

$R_u = 0.371^{+0.015}_{-0.013}$	$R_t = 0.922^{+0.025}_{-0.026}$	$\alpha = (91.0 \pm 3.9)^\circ$	$\beta = (21.76^{+0.92}_{-0.82})^\circ$	$\gamma = (67.2 \pm 3.9)^\circ$
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B_s system

$\beta_s = (1.041^{+0.050}_{-0.048})^\circ$	$BF(B_s \rightarrow \mu\mu) [10^{-9}] = 3.073^{+0.070}_{-0.190}$
---------------------------------------------	------------------------------------------------------------------

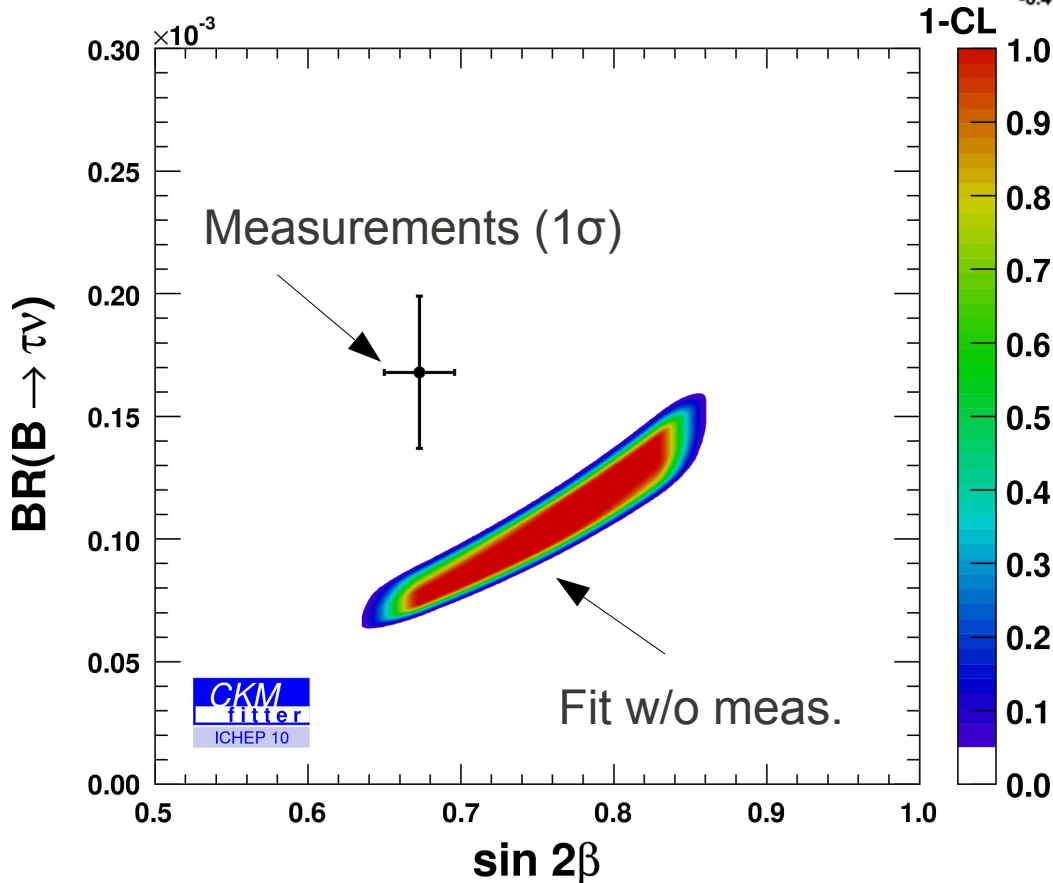
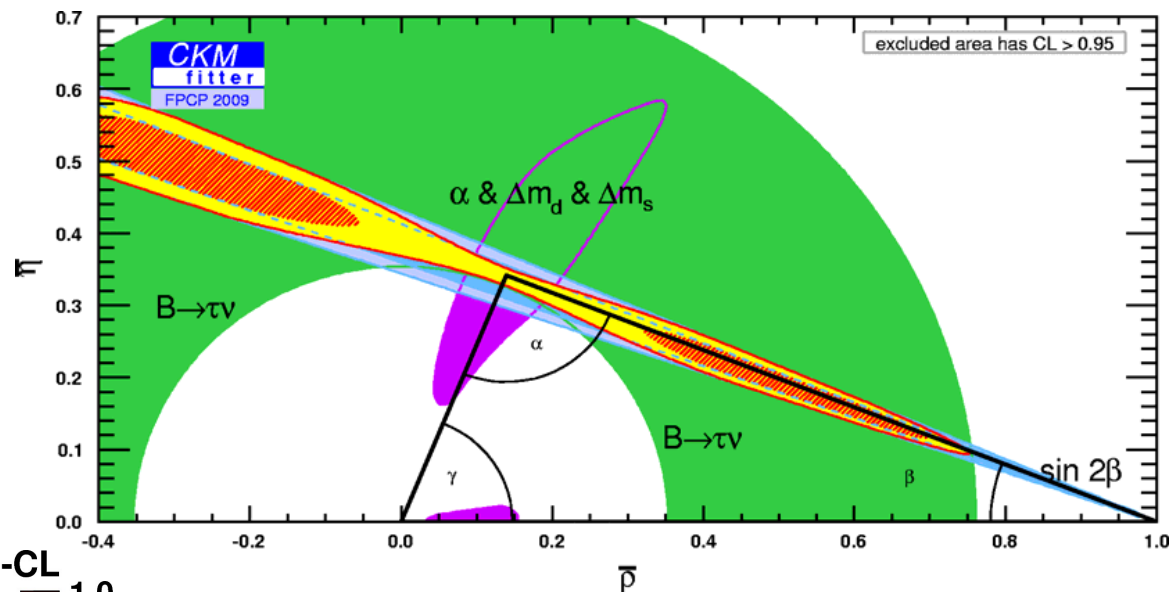
All measurements consistent with their predictions within $\pm 1\sigma$ except $\sin 2\beta$: 2.6σ and $B \rightarrow \tau\nu$: 2.8σ



A closer look at the discrepancies

Sin2 β and $B \rightarrow \tau\nu$ discrepancies

- The combination $\sin 2\beta$ and $B \rightarrow \tau\nu$ favors 2 solutions in contradictions with other inputs.
- One cannot accommodate both inputs simultaneously in the global fit.



Non-trivial correlation of indirect constraints on $\sin 2\beta$ and $B \rightarrow \tau\nu$.

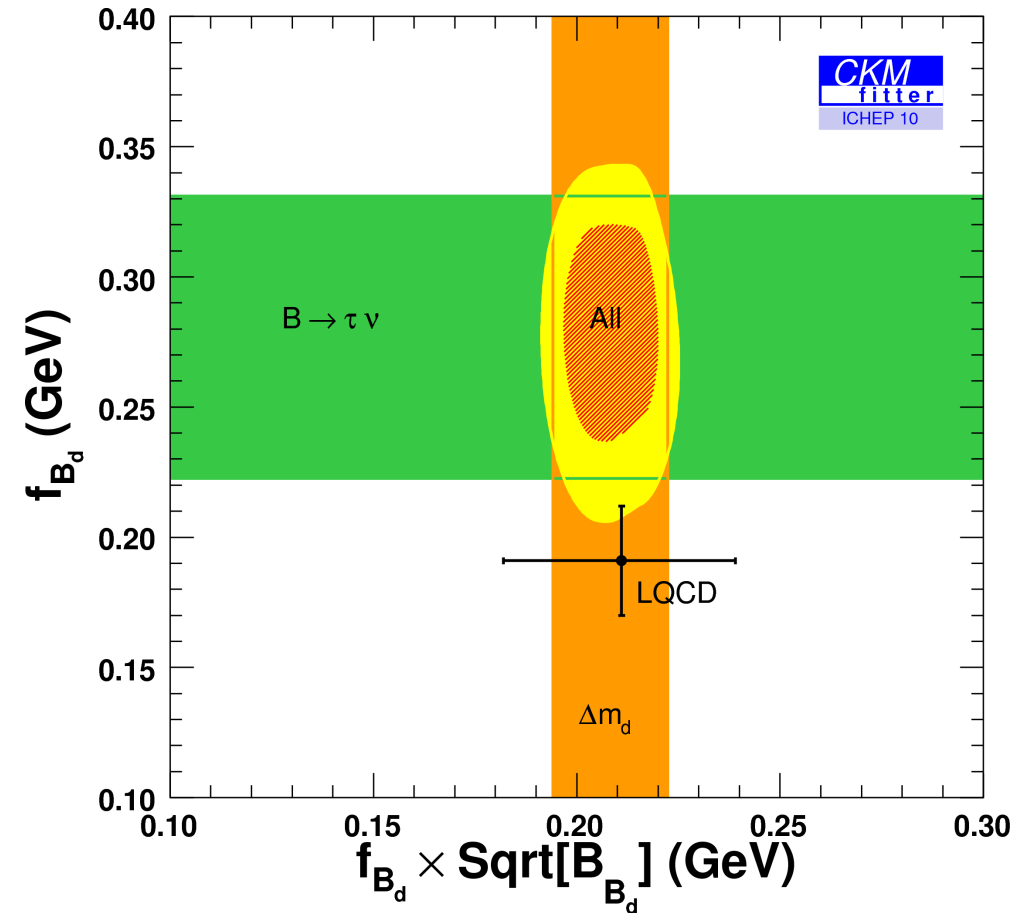
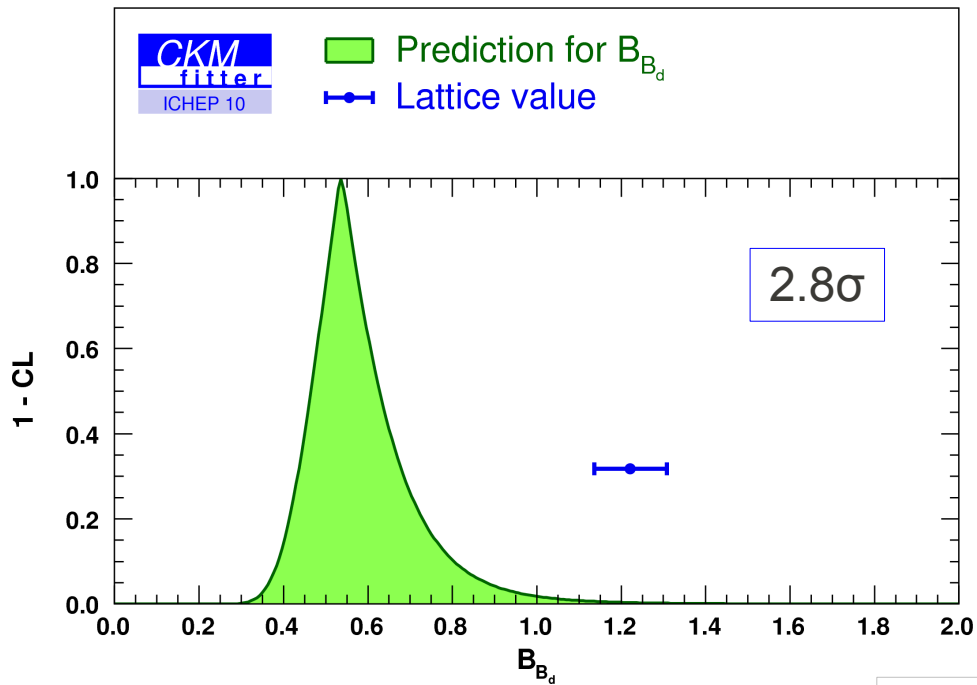
The low value of the prediction of $B \rightarrow \tau\nu$ is mainly driven by the measured value of $\sin 2\beta$

Sources of discrepancies:

- 1) Measurements (stat. fluctuations)?
- 2) Lattice estimate of f_B ?
- 3) New Physics in $B \rightarrow \tau\nu$ and/or $\sin 2\beta$?

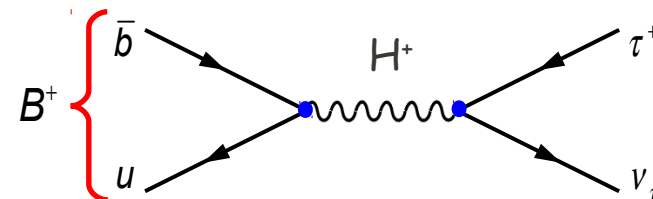
$$\frac{BR(B \rightarrow \tau \nu)}{\Delta m_d} = \frac{3\pi}{4} \frac{m_\tau^2 \tau_B}{m_W^2 \eta_B S(x_t) |V_{ud}|^2} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \frac{\sin^2(\beta)}{\sin^2(\gamma)} \frac{1}{B_{B_d}}$$

“Theory-free” estimation of B_{B_d} :



The global fit is accommodated keeping $f_{B_d}^2 \times B_{B_d} \approx$ constant to fit Δm_d while increasing f_{B_d} to fit $B \rightarrow \tau \nu$ 10

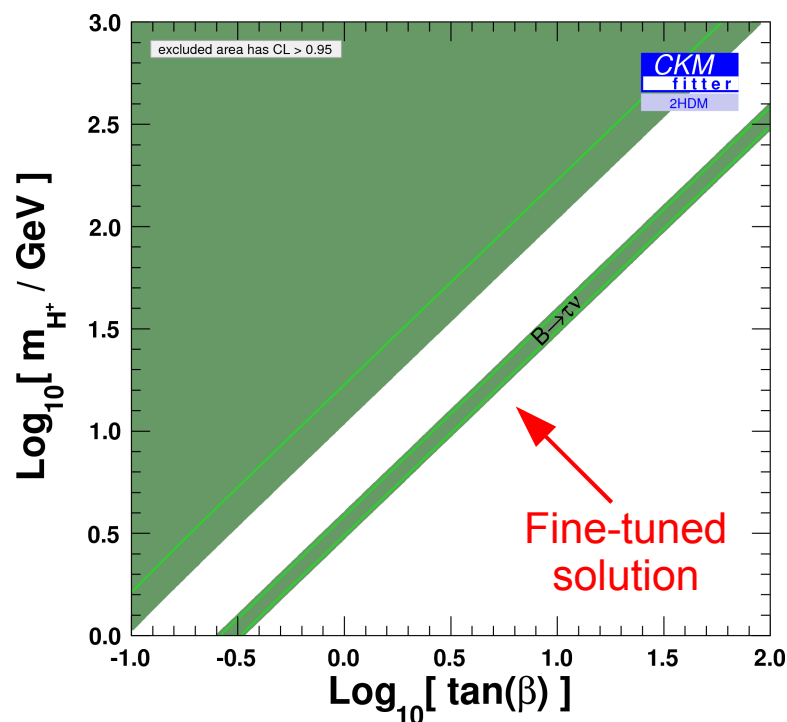
$$\frac{\mathcal{B}[M \rightarrow l\nu]}{\mathcal{B}[M \rightarrow l\nu]_{\text{SM}}} = (1 + r_H)^2 \quad r_H = \left(\frac{m_{q_u} - m_{q_d} \tan^2 \beta}{m_{q_u} + m_{q_d}} \right) \left(\frac{m_M}{m_{H^+}} \right)^2$$



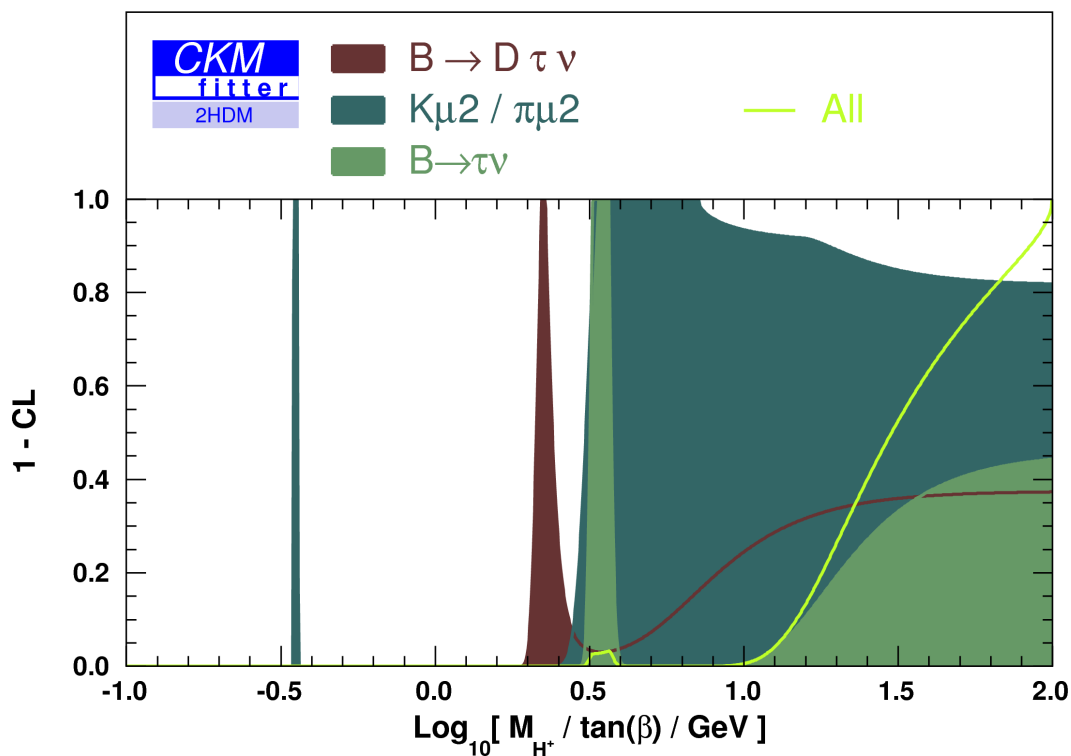
If perfect agreement SM-data, two distinct solutions in 2HDM(II)

- decoupling : $r_H = 0$ ($m_{H^+} \rightarrow \infty$, $\tan \beta$ small)
- fine-tuned : $r_H = -2$ (linear correlation between m_{H^+} and large $\tan \beta$, depends on meson mass)

Deschamps *et al.*
ArXiv:0907.5135 [hep-ph]



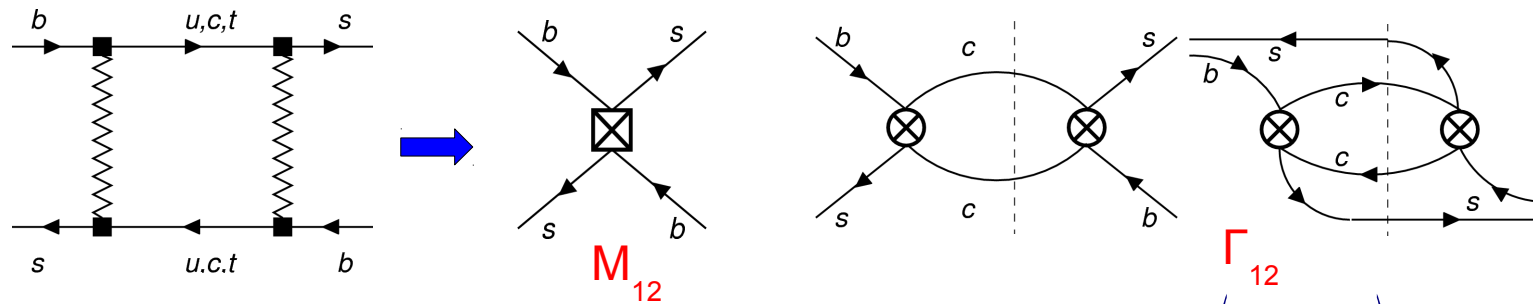
BF($B \rightarrow \tau\nu$) meas. favors fine-tuned solution



Fine-tuned solution ruled out at 95% CL by other leptonic+semileptonic observables

Bounds on NP in $\Delta F=2$ FCNC

Neutral-B Mixing and New Physics



Nierste&Lenz,
JHEP 706 (2007) 72

3 physical quantities in B-B mixing: $|M_{12}^q|$, $|\Gamma_{12}^q|$, $\phi_q = \arg\left(-\frac{M_{12}^q}{\Gamma_{12}^q}\right)$

Observables to determine them:

- Mass and width difference: $\Delta m_q = M_H^q - M_L^q \simeq 2|M_{12}^q|$, $\Delta \Gamma_q = \Gamma_L^q - \Gamma_H^q \simeq 2|\Gamma_{12}^q| \cos(\phi_q)$
- CP Asymmetry in flavor-specific B decays: $A_{SL}^q = \left| \frac{\Gamma_{12}^q}{M_{12}^q} \right| \sin(\phi_q) = \frac{\Delta \Gamma_q}{\Delta m_q} \tan(\phi_q)$

Standard Model:

- M_{12} from **dispersive** part of the box, only internal t relevant
- Γ_{12} from **absorptive** part of the box, only c,u contribute (u's are negligible). Γ_{12} is a **CKM-favored tree-level** effect associated with final states containing a $(c\bar{c})$ pair.

New physics:

- Γ_{12} can barely be affected, stems from tree-level decays
- M_{12} is very sensitive to virtual effects of new heavy particles

Generic New Physics in B_q Mixing: Assumptions

Nierste&Lenz,
JHEP 706 (2007) 72

Assume that NP only affects short distance physics in $\Delta B = 2$: M_{12}

Model-independent param. with a complex parameter Δ_q through:

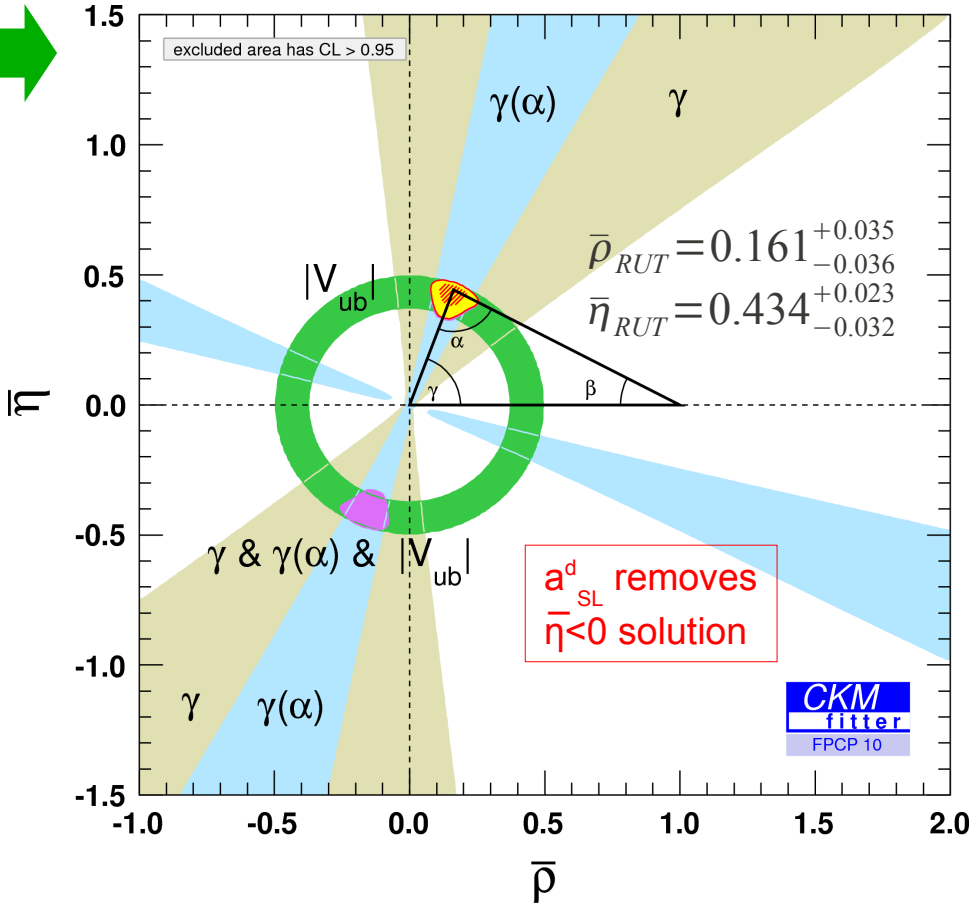
$$M_{12}^q = M_{12}^{SM,q} \cdot \Delta_q$$

In the SM, $\Delta_q = 1$.

→ To identify or constrain new physics: measure both the magnitude and phase of M_{12}

Reference UT (fix SM param.):
 $|V_{ud}|, |V_{us}|, |V_{cb}|, |V_{ub}|, B \rightarrow \tau \nu, \gamma, \gamma(\alpha) = \pi - \beta_{cc} - \alpha$

parameter	prediction in the presence of NP
Oscil. Δm_q	$ \Delta_q^{NP} \times \Delta m_q^{SM}$
Phases 2β	$2\beta^{SM} + \Phi_d^{NP}$
$2\beta_s$	$2\beta_s^{SM} - \Phi_s^{NP}$
2α	$2(\pi - \beta^{SM} - \gamma) - \Phi_d^{NP}$
$\Phi_{12,q} = \text{Arg}[-\frac{M_{12,q}}{\Gamma_{12,q}}]$	$\Phi_{12,q}^{SM} + \Phi_q^{NP}$
Asym SL A_{SL}^q	$\frac{\Gamma_{12,q}}{M_{12,q}^{SM}} \times \frac{\sin(\Phi_{12,q}^{SM} + \Phi_q^{NP})}{ \Delta_q^{NP} }$
Lifetime diff. $\Delta\Gamma_q$	$2 \Gamma_{12,q} \times \cos(\Phi_{12,q}^{SM} + \Phi_q^{NP})$



Bounds from the B_d sector

Constraining Δ_d :

Δm_d
 Δm_d & Δm_s
 $\sin 2\beta$
 α
 A_{SL}^d & A_{SL}^s & A_{SL}
 +Reference UT

$$\text{Re}\Delta_d = +0.732^{+0.216}_{-0.056}$$

$$\text{Im}\Delta_d = -0.156^{+0.039}_{-0.087}$$

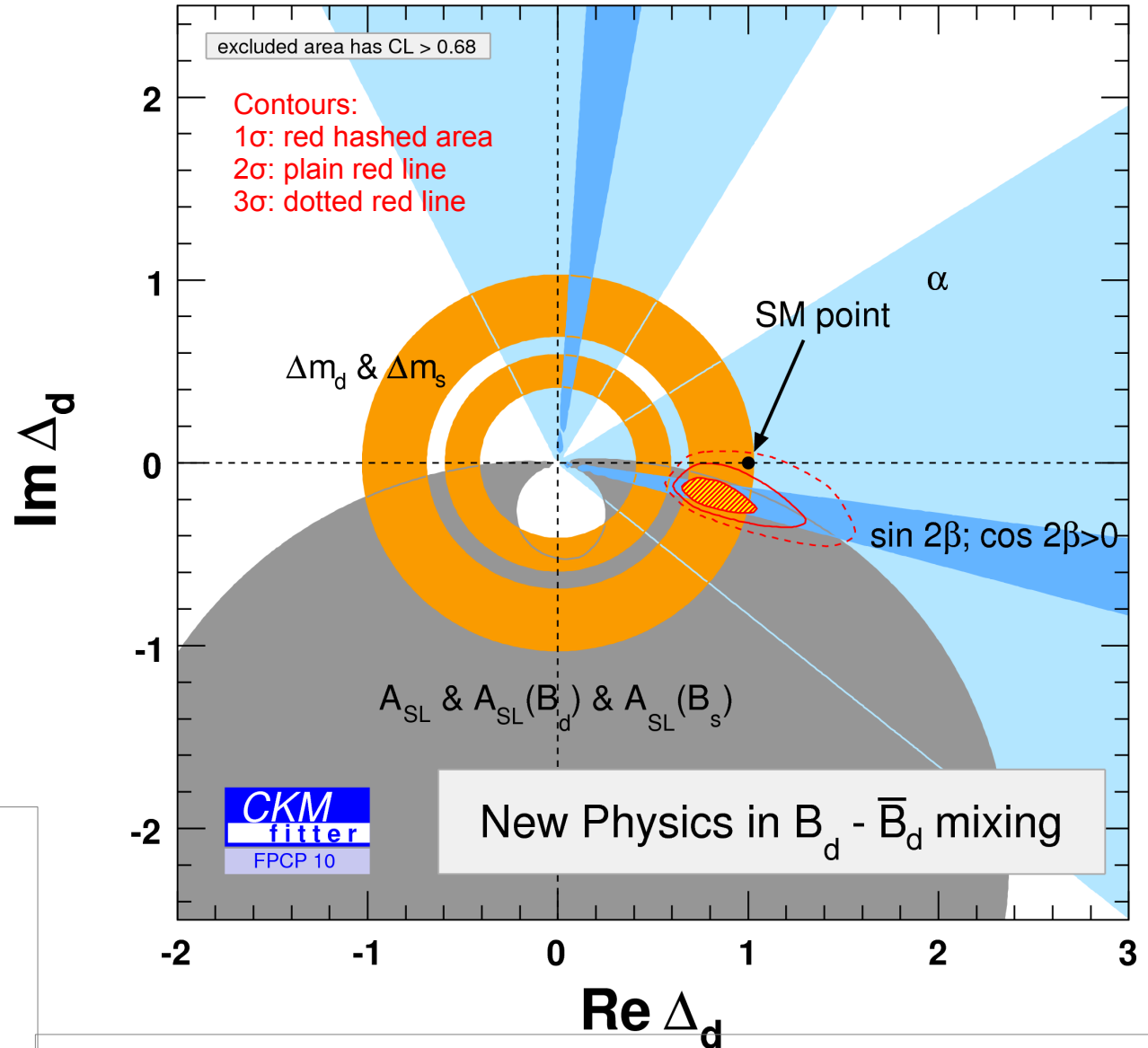
- Dominant constraints from $\sin 2\beta$ and Δm_d (2 rings from 2 sol. for apex of Reference UT)

- $B \rightarrow \tau \nu$ part of Reference UT

$$\rightarrow \sin 2\beta_{SM} = 0.825^{+0.014}_{-0.051}$$

$$> \sin 2\beta_{meas} = \sin(2\beta_{SM} + \Phi_d^{NP})$$

- $\rightarrow \Phi_d^{NP} < 0$ preferred



- Disagreement with SM driven in same direction by $\sin 2\beta$ and A_{SL}
- 2D SM hypothesis ($\Delta_d=1$): 2.5σ (w/o $B \rightarrow \tau \nu$: 1.1σ).
- Still sizable NP contribution possible: $\sim 40\%$

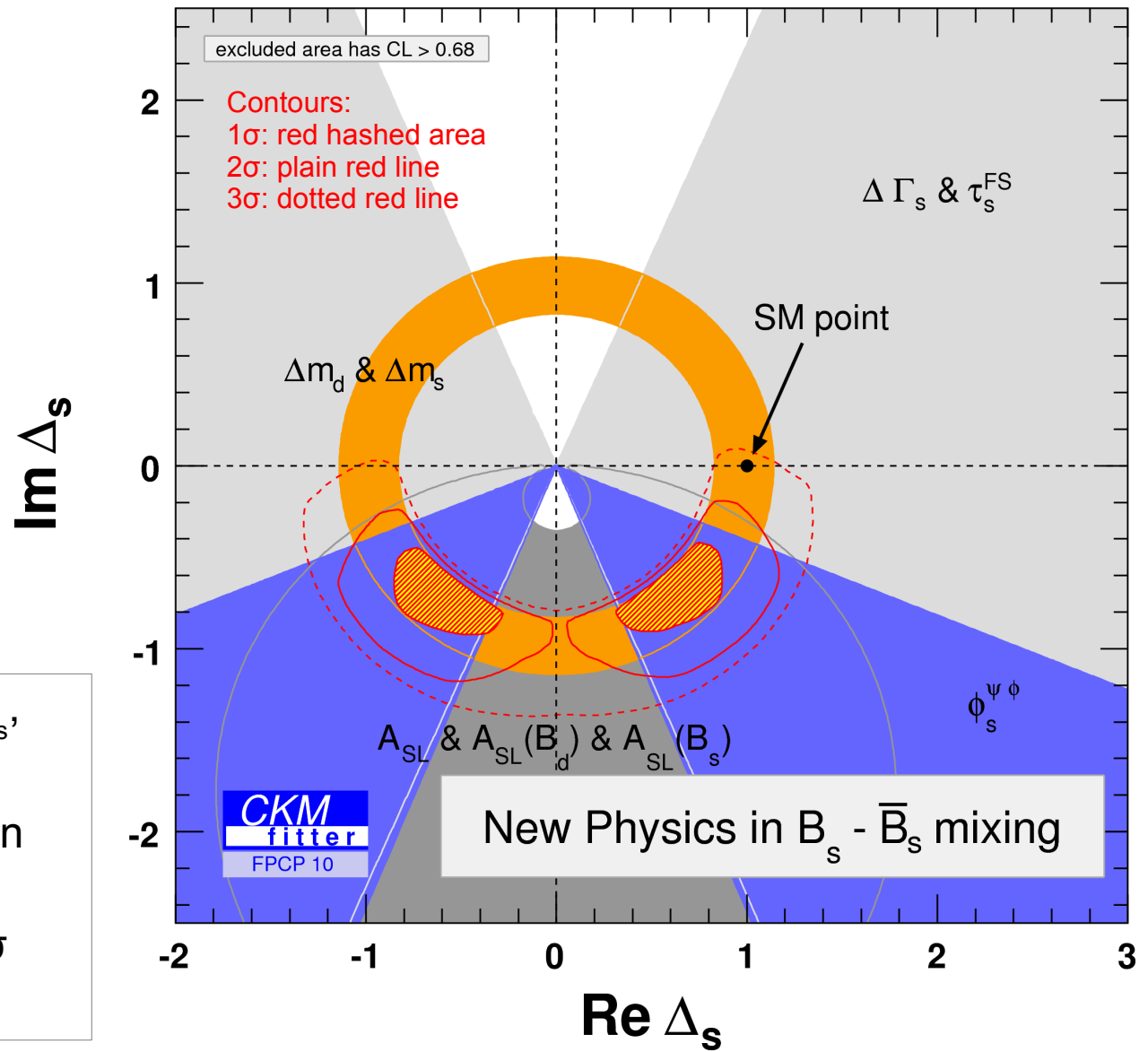
Constraining Δ_s :

Δm_d & Δm_s
 $a_{CP}(\psi\Phi)$
 A_{SL}^d & A_{SL}^s & A_{SL}
 $\Delta\Gamma_s$ & τ_s^{FS}
 +Reference UT

$$\text{Re}\Delta_s = +0.55^{+0.21}_{-0.14}$$

$$\text{Im}\Delta_s = -0.68^{+0.15}_{-0.14}$$

- Dominant constraints from Δm_s , $\Phi_s^{\psi\Phi}$ and A_{SL}
- Disagreement with SM driven in same direction by $\Phi_s^{\psi\Phi}$ and A_{SL}
- 2D SM hypothesis ($\Delta_s=1$): 2.7σ (w/o $B \rightarrow \tau\nu$: 2.7σ).



Still 1.3σ discrepancy between the NP in M_{12} fit prediction: $A_{SL}(\text{NP})(\text{meas. not in fit}) = -0.0041 \pm 0.0019$ and the measurement $A_{SL}(\text{WA w/ new } D\emptyset) = -0.0085 \pm 0.0028$.

KM mechanism at work at the EW scale.

Unitarity Triangle:

- Overall consistency at 2σ level
- Ongoing discrepancy between $\sin 2\beta$ and $B \rightarrow \tau\nu$ \rightarrow Super Flavor Factory

New Physics in $\Delta F=2$ mixing:

- The discrepancy $B \rightarrow \tau\nu$ vs $\sin 2\beta$ can be accommodated by a new CPV phase in the B_d mixing, in agreement with the latest $A_{SL}(D\bar{0})$ measurement.
- Still a lot of room for NP in the B_s , even with the latest CDF measurement of Φ_s

Precision flavor physics: unraveling the flavor structure of New Physics

- Will require a second “quantum jump”: going from $O(1)$ to $O(0.1)$ precision is not the same as going from $O(0.1)$ to $O(0.01)$. Many assumptions will need to be revisited.
- An average representing a consensus of the lattice community will be mandatory (“HFAG lattice?”).

Let's check that any (so long awaited) deviation from the SM is a true one and let's hope that the next decade will be even more successful than the B-factory decade.

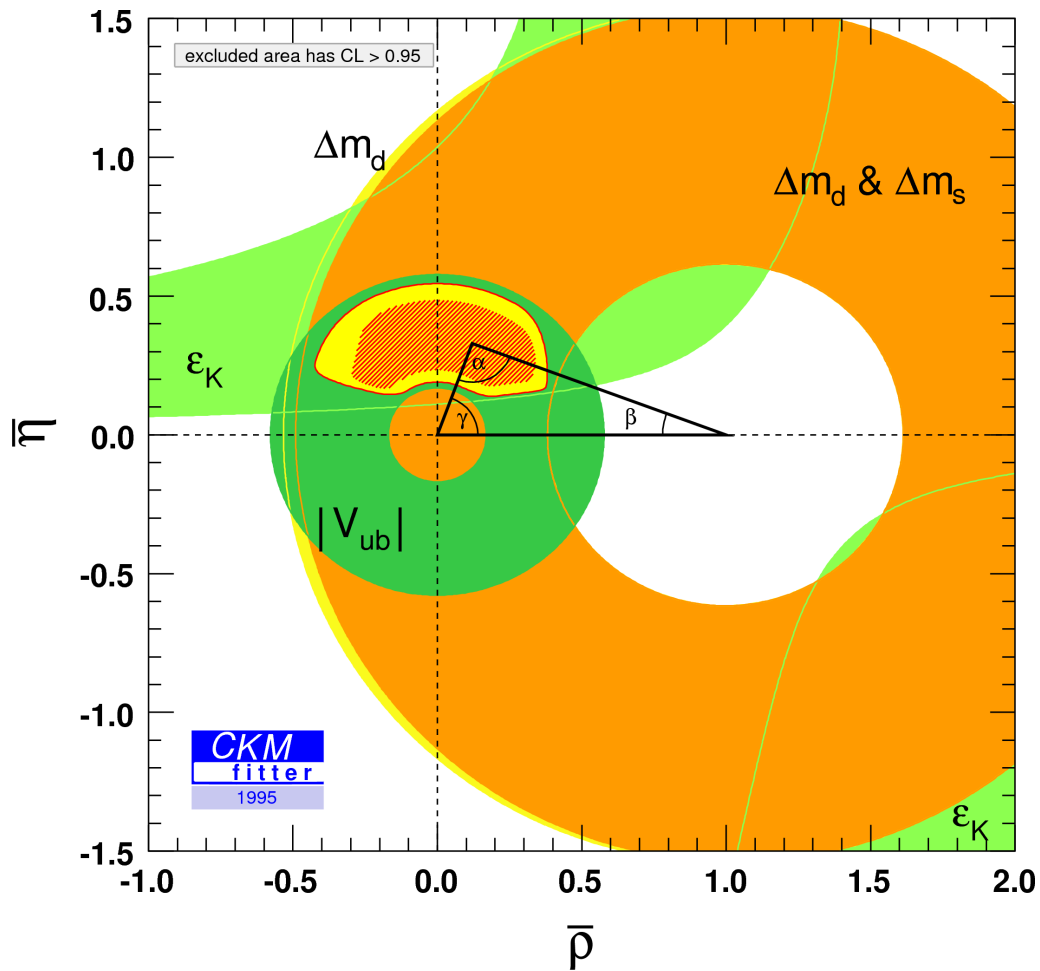


BACKUP SLIDES

Digression: a bit of history

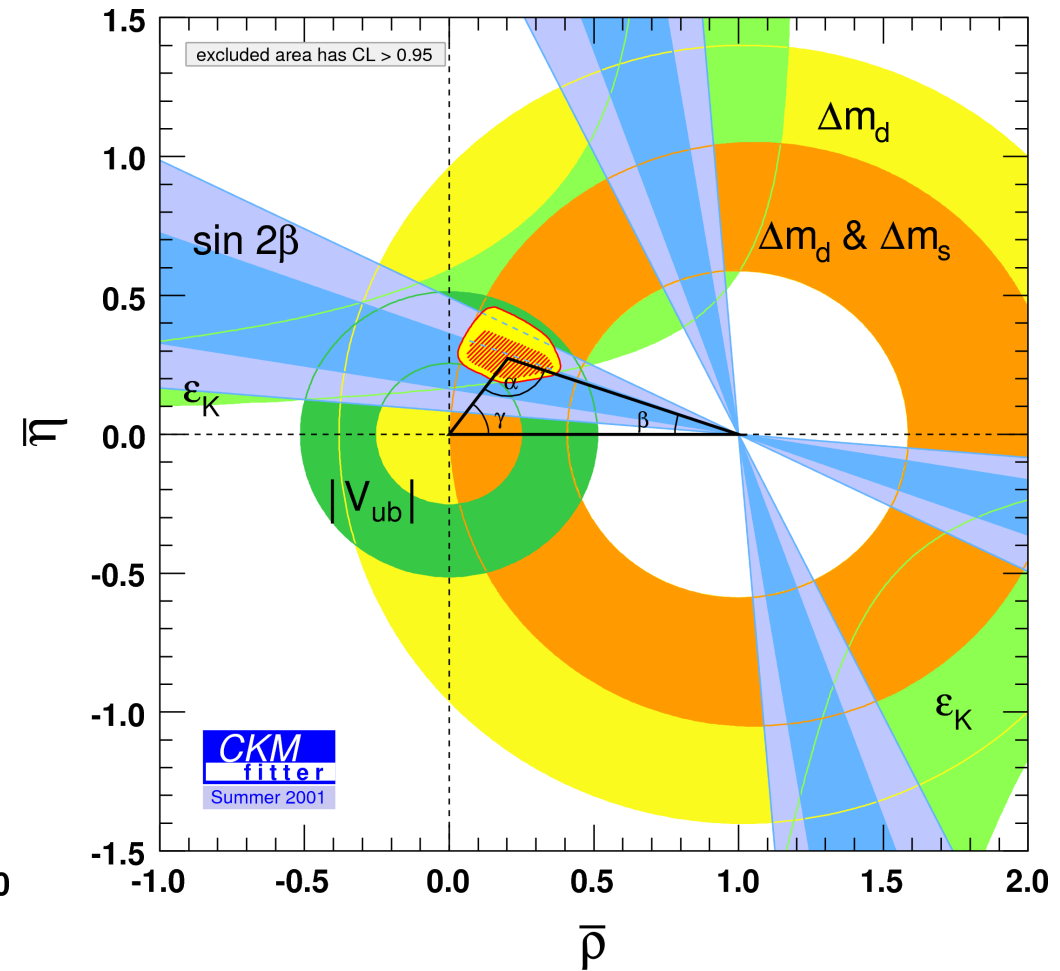
~1995

LEP, TeVatron (top),
NA48, KTeV, ...



S2001

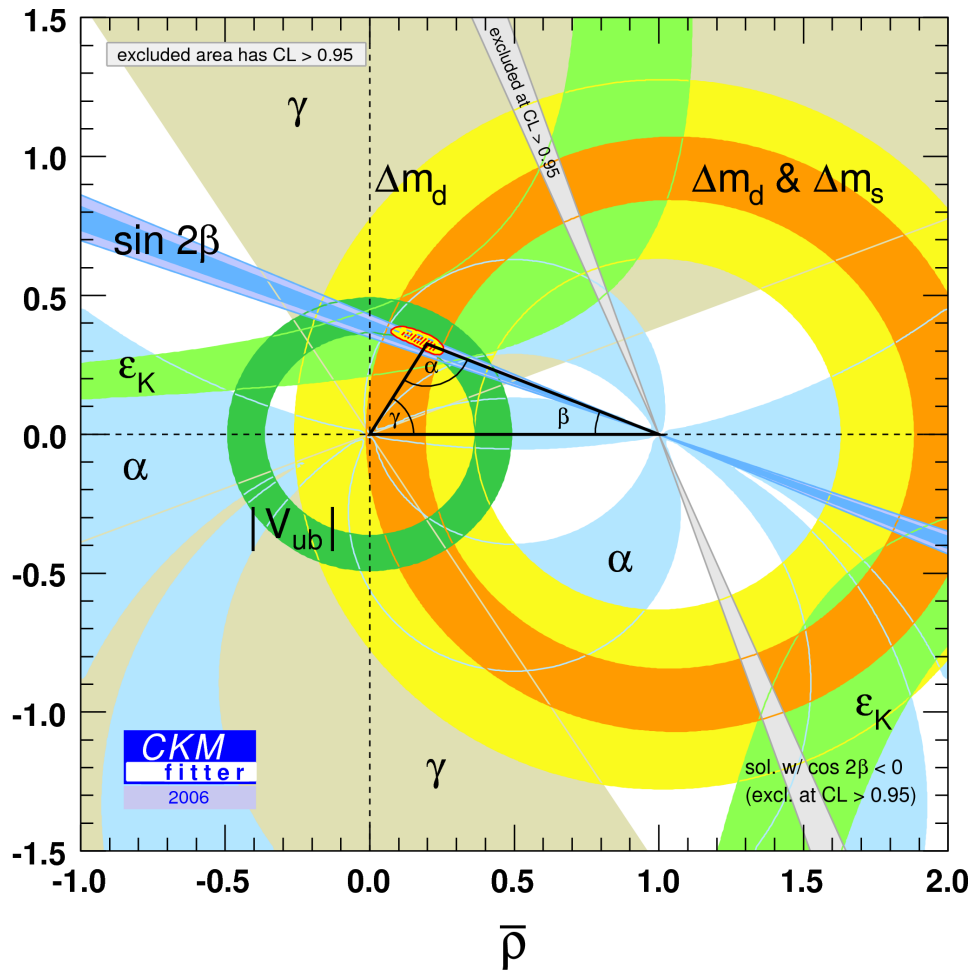
BaBar (SLAC),
Belle (KEK), ...



Digression: a bit of history

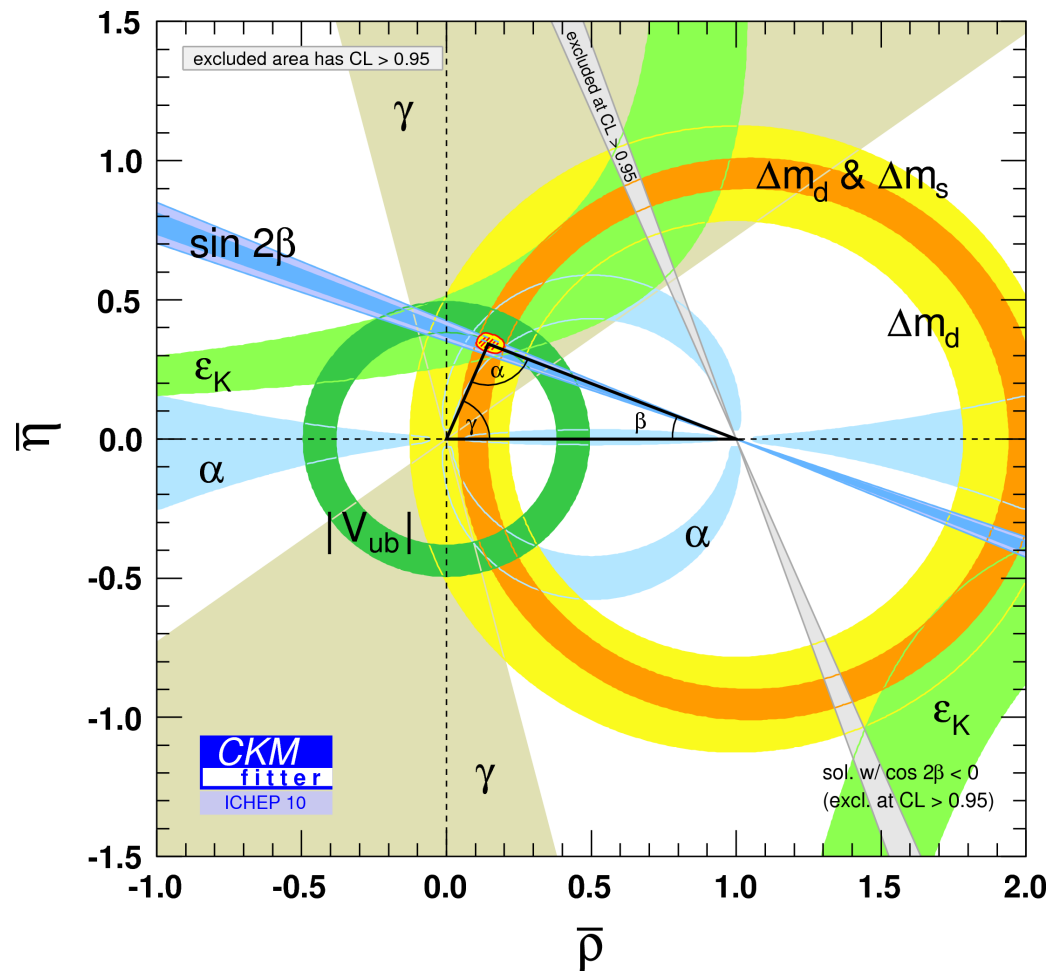
2006

BaBar, Belle and CDF/DØ (TeVatron Bs), ...

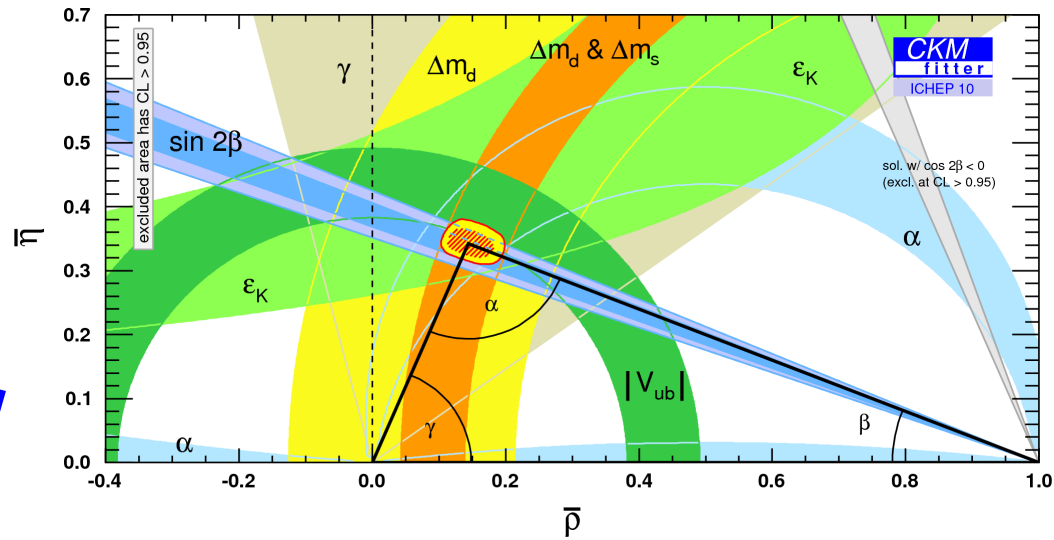


2010

BaBar, Belle and LQCD, ...



Sin2 β and $B \rightarrow \tau\nu$ discrepancies

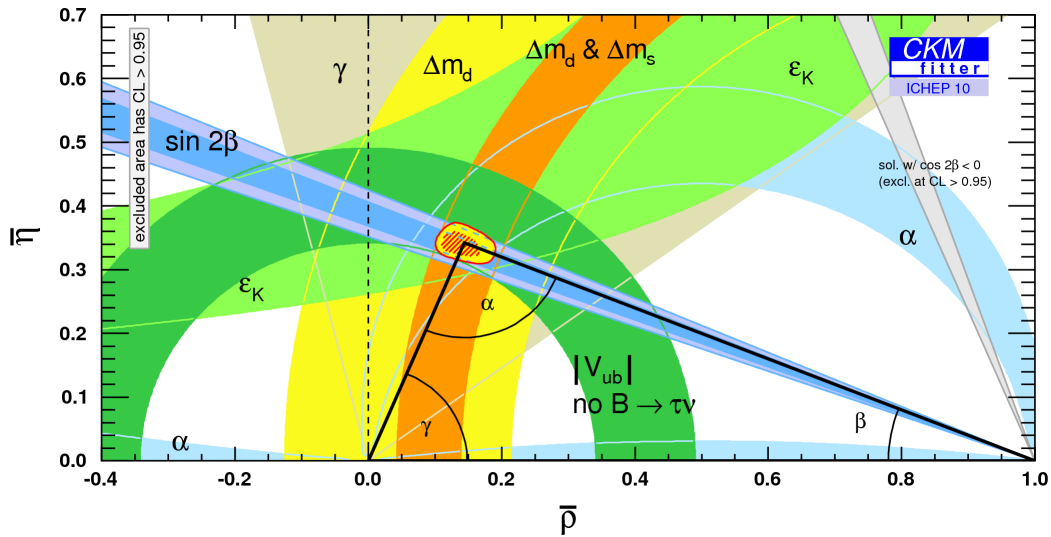
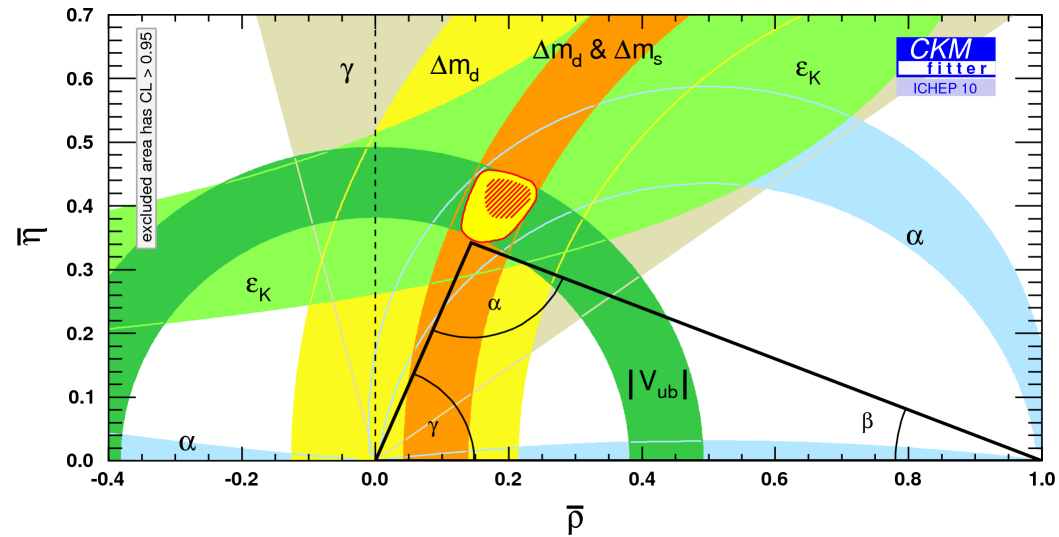


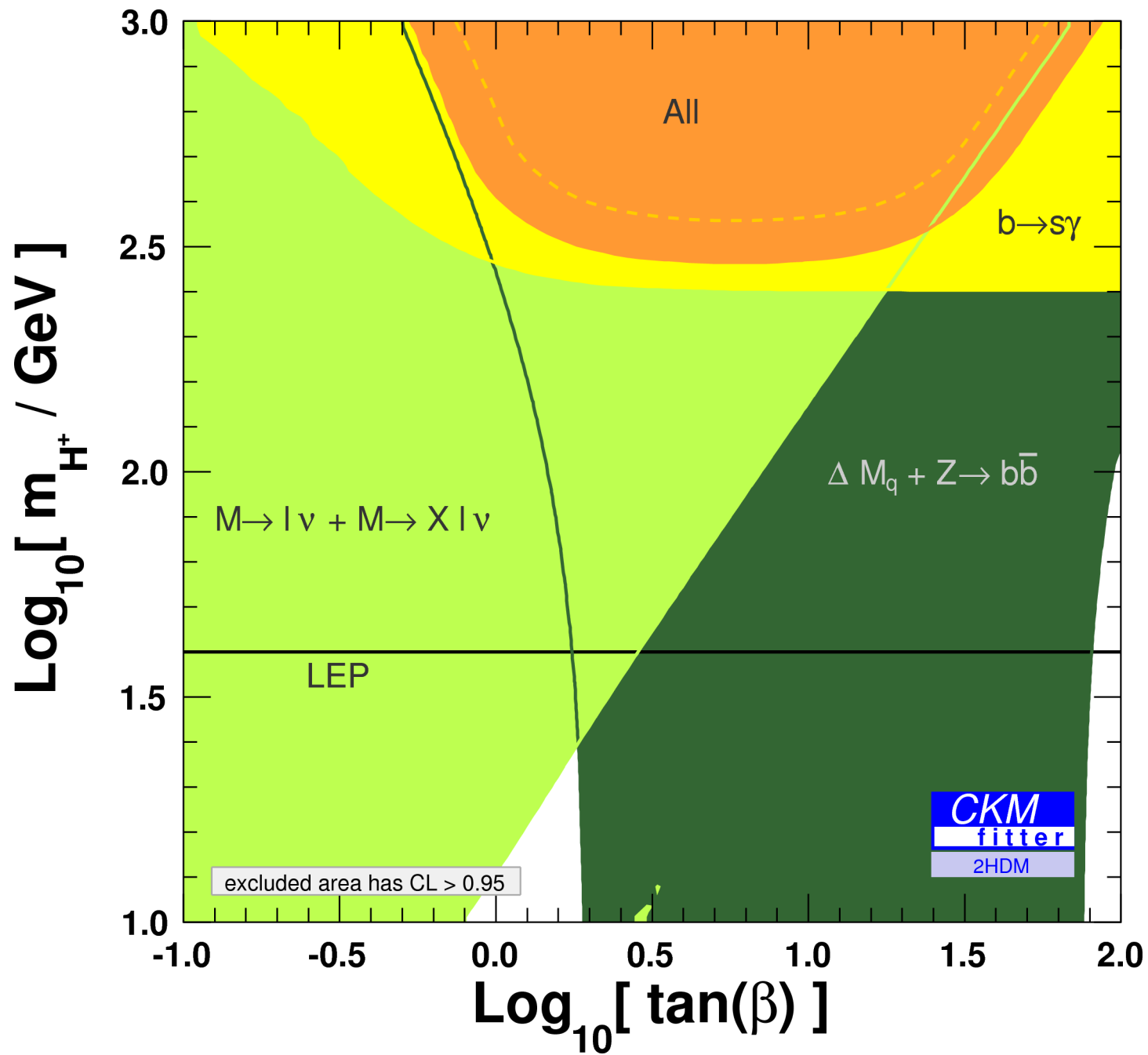
removing
sin2 β

removing
 $B \rightarrow \tau\nu$

$$\Delta \chi^2_{min} = 6.94$$

$$\Delta \chi^2_{min} = 7.68$$





Prediction of Φ_s from the fit

