### **Top-Antitop Production at Hadron Colliders**

#### Roberto BONCIANI

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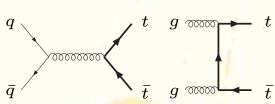
### Plan of the Talk

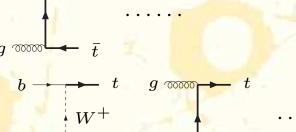
- General Introduction
  - Top Quark at the Tevatron and LHC Perspectives
- Status of the Theoretical calculations
  - Total Cross Section at NLO
  - Analytic Two-Loop QCD Corrections
- Conclusions

## Top Quark

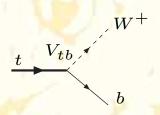
- With a mass of  $m_t = 173.1 \pm 1.3$  GeV, the TOP quark (the up-type quark of the third generation) is the heaviest elementary particle produced so far at colliders.
- Because of its mass, top quark is going to play a unique role in understanding the EW symmetry breaking ⇒ Heavy-Quark physics crucial at the LHC.
- Two production mechanisms

  - $pp(\bar{p}) \to t\bar{b}, tq'(\bar{q}'), tW^-$





- Top quark does not hadronize, since it decays in about  $5 \cdot 10^{-25}$ s (one order of magnitude smaller than the hadronization time)  $\Longrightarrow$  opportunity to study the quark as single particle
  - Spin properties
  - Interaction vertices
  - Top quark mass
- Decay products: almost exclusively  $t \to W^+ b$   $(|V_{tb}| \gg |V_{td}|, |V_{ts}|)$



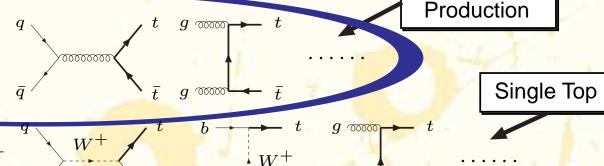
Pair

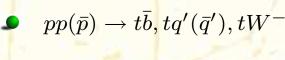
**Production** 

Single Top

### Top Quark

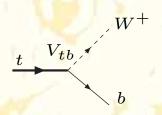
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  - $lacksquare pp(\bar p) o t \bar t$



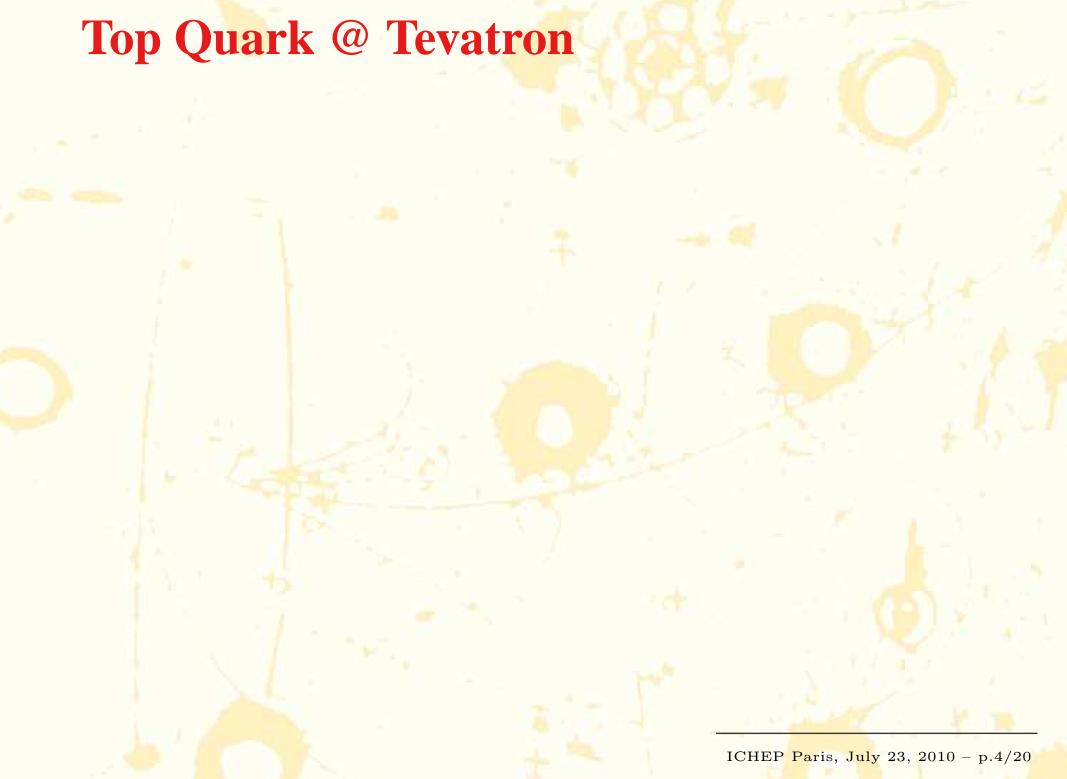




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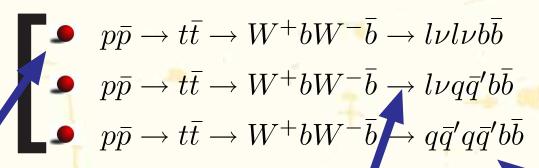


Pair



### **Events measured at Tevatron**

 $\sigma_{tar{t}}\sim7 extsf{pb}$ 



Dilepton  $\sim 10\%$ 

Lep+jets  $\sim 44\%$ 

All jets  $\sim 46\%$ 

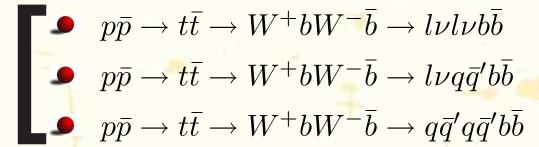
2 high- $p_T$  lept,  $\geq$  2 jets and ME

NO lept,  $\geq$  6 jets and low ME

1 isol high- $p_T$  lept,  $\geq$  4 jets and ME

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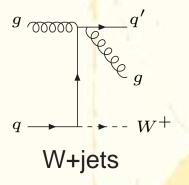
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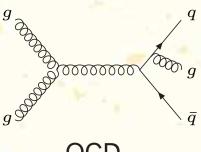
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NO lept, ≥ 6 jets and low ME

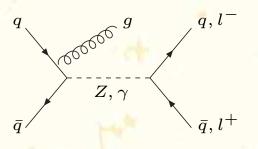
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### **Background Processes**

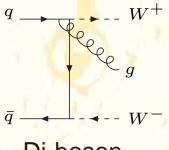




QCD



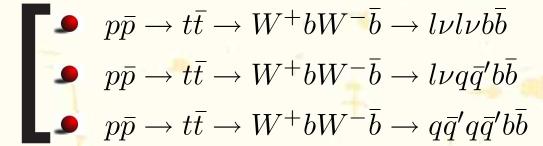
Drell-Yan



Di-boson

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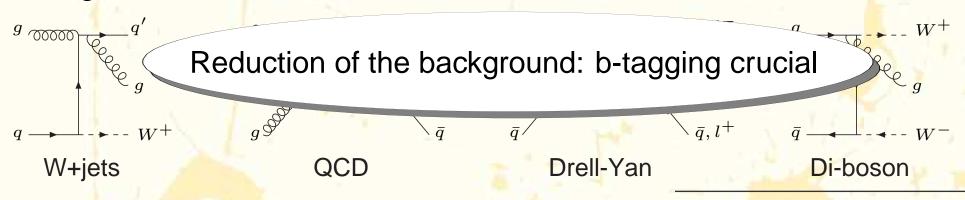
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### **Background Processes**



Total Cross Section

$$\sigma_{t\bar{t}} = \frac{N_{data} - N_{bkgr}}{\epsilon L} = 7.0 \pm 0.6 \, \mathrm{pb}$$
  $(m_t = 175 \, \mathrm{GeV})$ 

Top-quark Mass

$$m_t = 173.1 \pm 1.3 \,\text{GeV} \,(0.75\%)$$

lacksquare W helicity fractions  $F_i=B(t o bW^+(\lambda_W=i=-1,0,1))$   $(F_0+F_++F_-=1)$ 

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta^*} = \frac{3}{4} F_0 \sin^2\theta^* + \frac{3}{8} F_- (1 - \cos\theta^*)^2 + \frac{3}{8} F_+ (1 + \cos\theta^*)^2$$

$$F_0 = 0.66 \pm 0.16 \pm 0.05$$
  $F_+ = -0.03 \pm 0.06 \pm 0.03$ 

Spin correlations measured fitting the double distribution

$$\frac{1}{N} \frac{d^2 N}{d \cos \theta_1 d \cos \theta_2} = \frac{1}{4} (1 + \kappa \cos \theta_1 \cos \theta_2)$$

$$-0.455 < \kappa < 0.865 (68\% CL)$$

Forward-Backward Asymmetry

$$A_{FB} = (19.3 \pm 6.5(\text{sta}) \pm 2.4(\text{sys}))\%$$

### LHC Perspectives

#### Cross Section

- ▶ With  $100\,{\rm pb}^{-1}$  of accumulated data an error of  $\Delta\sigma_{t\bar{t}}/\sigma_{t\bar{t}}\sim15\%$  is expected (dominated by statistics!)
- After 5 years of data taking an error of  $\Delta \sigma_{t\bar{t}}/\sigma_{t\bar{t}} \sim 5\%$  is expected

#### Top Mass

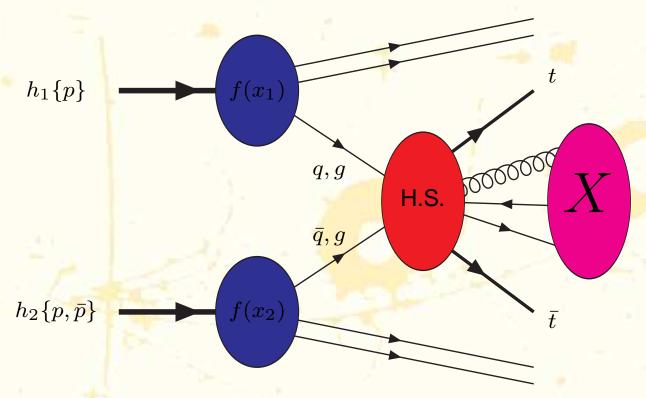
- With 1 fb<sup>-1</sup> Mass accuracy:  $\Delta m_t \sim 1-3$  GeV
- Top Properties
  - ▶ W helicity fractions and spin correlations with  $10 \, \text{fb}^{-1} \Longrightarrow 1-5\%$
  - Top-quark charge. With  $1\,{\rm fb}^{-1}$  we could be able to determine  $Q_t=2/3$  with an accuracy of  $\sim 15\%$
- Sensitivity to new physics
  - all the above mentioned points
  - Narrow resonances: with  $1\,{\rm fb}^{-1}$  possible discovery of a Z' of  $M_{Z'}\sim 700\,{\rm GeV}$  with  $\sigma_{pp\to Z'\to t\bar t}\sim 11\,{\rm pb}$

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## **Top-Anti Top Pair Production**

According to the factorization theorem, the process  $h_1 + h_2 \rightarrow t\bar{t} + X$  can be sketched as in the figure:

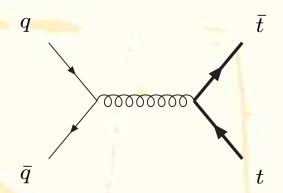


$$\sigma_{h_1,h_2}^{t\bar{t}} = \sum_{i,j} \int_0^1 dx_1 \int_0^1 dx_2 f_{h_1,i}(x_1,\mu_F) f_{h_2,j}(x_2,\mu_F) \ \hat{\sigma}_{ij} \left(\hat{s}, m_t, \alpha_s(\mu_R), \mu_F, \mu_R\right)$$

$$s = (p_{h_1} + p_{h_2})^2, \, \hat{s} = x_1 x_2 s$$

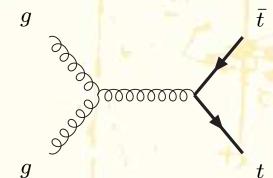
### The Partonic Cross Section: Tree-Level

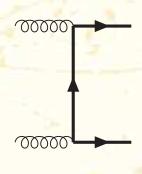
$$q(p_1) + \bar{q}(p_2) \longrightarrow t(p_3) + \bar{t}(p_4)$$

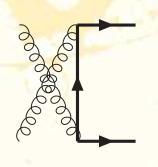




$$g(p_1) + g(p_2) \longrightarrow t(p_3) + \bar{t}(p_4)$$









$$\sigma_{t\bar{t}}^{LO}(LHC, m_t = 171 \, \text{GeV}) = 583 \, \text{pb} \pm 30\%$$

$$\sigma_{t\bar{t}}^{LO}(Tev, m_t = 171 \, \text{GeV}) = 5.92 \, \text{pb} \pm 44\%$$

### The Partonic Cross Section: NLO

#### Fixed Order

- The NLO QCD corrections are quite sizable: + 25% at Tevatron and +50% at LHC.

  Scales variation ±15%.

  Nason, Dawson, Ellis '88-'90; Beenakker, Kuijf, van Neerven, Smith '89-'91;

  Mangano, Nason, Ridolfi '92; Frixione et al. '95; Czakon and Mitov '08.
- Mixed NLO QCD-EW corrections are small: 1% at Tevatron and -0.5% at LHC.

Beenakker *et al.* '94 Bernreuther, Fuecker, and Si '05-'08 Kühn, Scharf, and Uwer '05-'06; Moretti, Nolten, and Ross '06.

#### All-order Soft-Gluon Resummation

- Leading-Logs (LL)
- Next-to-Leading-Logs (NLL)

Laenen et al. '92-'95; Berger and Contopanagos '95-'96; Catani et al. '96.

Kidonakis and Sterman '97; R. B., Catani, Mangano, and Nason '98.

Next-to-Next-to-Leading-Logs (NNLL) under study.

Moch and Uwer '08; Beneke et al. '09; Czakon et al. '09; Kidonakis '09

$$\sigma_{t\bar{t}}^{\text{NLO+NLL}}(\text{Tev}, m_t = 171 \text{ GeV}, \text{CTEQ6.5}) = 7.61^{+0.30(3.9\%)}_{-0.53(6.9\%)} \text{ (scales)} + 0.53(7\%)_{-0.36(4.8\%)} \text{ (PDFs) pb}$$

$$\sigma_{t\bar{t}}^{\text{NLO+NLL}}(\text{LHC}, m_t = 171 \text{ GeV}, \text{CTEQ6.5}) = 908^{+82(9.0\%)}_{-85(9.3\%)} \text{ (scales)} + 30(3.3\%)_{-29(3.2\%)} \text{ (PDFs) pb}$$

M. Cacciari, S. Frixione, M. Mangano, P. Nason, and G. Ridolfi, JHEP 0809:127,2008

## Measurement Requirements for $\sigma_{t\bar{t}}$

Experimental requirements for  $\sigma_{t\bar{t}}$ :

- **P** Tevatron  $\Delta \sigma / \sigma \sim 10\% \Longrightarrow \sim$  ok with the theory!
- LHC (14 TeV, high luminosity)  $\Delta \sigma / \sigma \sim 5\%$  ≪ NLO theoretical prediction!!

Kidonakis-Vogt and Moch-Uwer, Langenfeld-Moch-Uwer, presented recently approximated NNLO results for  $\sigma_{t\bar{t}}$  including

- scale dependence at NNLO
- NNLL soft-gluon contributions
- Coulomb corrections

This drastically reduces the uncertainty (factorization/renormalization scale dependence) to the level predicted for LHC:  $\sim 4-6\%$ , and indicate that a COMPLETE NNLO computation is indeed needed in order to match the experimental precision of LHC.

### **Next-to-Next-to-Leading Order**

The NNLO calculation of the top-quark pair hadro-production requires several ingredients:

- Virtual Corrections
  - ullet two-loop matrix elements for qar q o tar t and gg o tar t
  - interference of one-loop diagrams

Körner et al. '05-'08; Anastasiou and Aybat '08

#### Real Corrections

- one-loop matrix elements for the hadronic production of  $t\bar{t} + 1$  parton
- tree-level matrix elements for the hadronic production of  $t\bar{t} + 2$  partons

Dittmaier, Uwer and Weinzierl '07-'08

#### Subtraction Terms

- Both matrix elements known for  $t\bar{t}+j$  calculation, BUT subtraction up to 1 unresolved parton, while in a complete NNLO computation of  $\sigma_{t\bar{t}}$  we need subtraction terms with up to 2 unresolved partons.
  - → Need an extension of the subtraction methods at the NNLO.

Gehrmann-De Ridder, Ritzmann '09, Daleo et al. '09, Boughezal et al. '10, Glover, Pires '10

Very recently: for double real in  $\sigma_{t\bar{t}}$ , method proposed by Czakon, arXiv:1005.0274

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# Two-Loop Corrections to $q \bar q o t \bar t$

$$|\mathcal{M}|^{2}(s, t, m, \varepsilon) = \frac{4\pi^{2}\alpha_{s}^{2}}{N_{c}} \left[ \mathcal{A}_{0} + \left(\frac{\alpha_{s}}{\pi}\right) \mathcal{A}_{1} + \left(\frac{\alpha_{s}}{\pi}\right)^{2} \mathcal{A}_{2} + \mathcal{O}\left(\alpha_{s}^{3}\right) \right]$$

$$\mathcal{A}_{2} = \mathcal{A}_{2}^{(2 \times 0)} + \mathcal{A}_{2}^{(1 \times 1)}$$

$$\mathcal{A}_{2}^{(2 \times 0)} = N_{c}C_{F} \left[ N_{c}^{2}A + B + \frac{C}{N_{c}^{2}} + N_{l} \left( N_{c}D_{l} + \frac{E_{l}}{N_{c}} \right) + N_{l}^{2}F_{l} + N_{l}N_{h}F_{lh} + N_{h}^{2}F_{h} \right]$$

$$+N_{h} \left( N_{c}D_{h} + \frac{E_{h}}{N_{c}} \right) + N_{l}^{2}F_{l} + N_{l}N_{h}F_{lh} + N_{h}^{2}F_{h} \right]$$

218 two-loop diagrams | contribute to the | 10 | different color coefficients

lacksquare The whole  $\mathcal{A}_2^{(2\times0)}$  is known numerically

Czakon '08.

The coefficients  $D_i$ ,  $E_i$ ,  $F_i$ , and A are known analytically (agreement with num res)

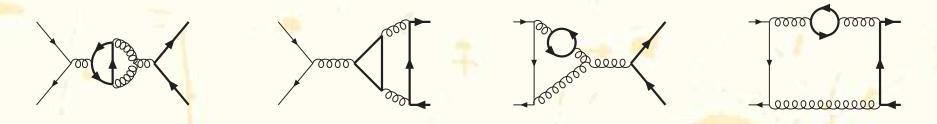
R. B., Ferroglia, Gehrmann, Maitre, and Studerus '08-'09

In the poles of  $\mathcal{A}_2^{(2 imes 0)}$  (and therefore of B and C) are known analytically

Ferroglia, Neubert, Pecjak, and Li Yang '09

# **Two-Loop Corrections to** $q\bar{q} \rightarrow t\bar{t}$

 $D_i$ ,  $E_i$ ,  $F_i$  come from the corrections involving a closed (light or heavy) fermionic loop:

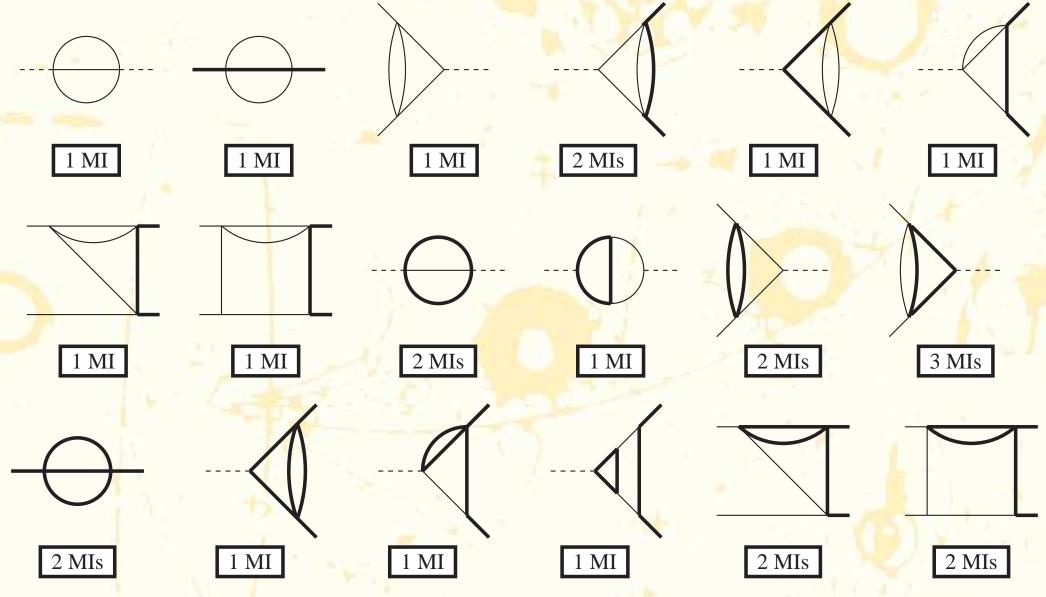


the leading-color coefficient, comes from the planar diagrams:



- The calculation is carried out analytically using:
  - Laporta Algorithm for the reduction of the dimensionally-regularized scalar integrals (in terms of which we express the  $|\mathcal{M}|^2$ ) to the Master Integrals (MIs)
  - Differential Equations Method for the analytic solution of the MIs

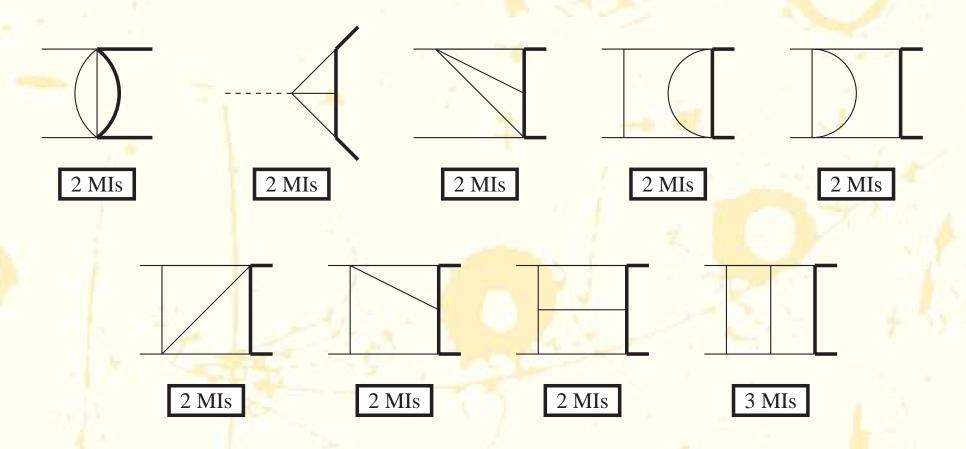
# Master Integrals for $N_l$ and $N_h$



18 irreducible two-loop topologies (26 Mls)

R. B., A. Ferroglia, T. Gehrmann, D. Maitre, and C. Studerus, JHEP 0807 (2008) 129.

### Master Integrals for the Leading Color Coeff



For the leading color coefficient there are 9 additional irreducible topologies (19 Mls)

R. B., A. Ferroglia, T. Gehrmann, and C. Studerus, JHEP 0908 (2009) 067.

### **Example: Box for the Leading Color Coeff**

$$= \frac{1}{m^6} \sum_{i=-4}^{-1} A_i \epsilon^i + \mathcal{O}(\epsilon^0)$$

$$\begin{array}{lll} A_{-4} & = & \dfrac{x^2}{24(1-x)^4(1+y)}\,, \\ A_{-3} & = & \dfrac{x^2}{96(1-x)^4(1+y)} \Big[ -10G(-1;y) + 3G(0;x) - 6G(1;x) \Big]\,, \\ A_{-2} & = & \dfrac{x^2}{48(1-x)^4(1+y)} \Big[ -5\zeta(2) - 6G(-1;y)G(0;x) + 12G(-1;y)G(1;x) + 8G(-1,-1;y) \Big]\,, \\ A_{-1} & = & \dfrac{x^2}{48(1-x)^4(1+y)} \Big[ -13\zeta(3) + 38\zeta(2)G(-1;y) + 9\zeta(2)G(0;x) + 6\zeta(2)G(1;x) - 24\zeta(2)G(-1/y;x) \\ & + 24G(0;x)G(-1,-1;y) - 24G(1;x)G(-1,-1;y) - 12G(-1/y;x)G(-1,-1;y) \\ & -12G(-y;x)G(-1,-1;y) - 6G(0;x)G(0,-1;y) + 6G(-1/y;x)G(0,-1;y) + 6G(-y;x)G(0,-1;y) \\ & + 12G(-1;y)G(1,0;x) - 24G(-1;y)G(1,1;x) - 6G(-1;y)G(-1/y,0;x) + 12G(-1;y)G(-1/y,1;x) \\ & -6G(-1;y)G(-y,0;x) + 12G(-1;y)G(-y,1;x) + 16G(-1,-1,-1;y) - 12G(1,0,-1;y) \\ & -12G(0,-1,-1;y) + 6G(0,0,-1;y) + 6G(1,0,0;x) - 12G(1,0,1;x) - 12G(1,1,0;x) + 24G(1,1,1;x) \\ & -6G(-1/y,0,0;x) + 12G(-1/y,0,1;x) + 6G(-1/y,1,0;x) - 12G(-1/y,1,1;x) + 6G(-y,1,0;x) \\ & -12G(-y,1,1;x) \Big] \end{array}$$

## **Example: Box for the Leading Color Coeff**

-12G(-y,1,1;x)

$$= \frac{1}{m^6} \sum_{i=-4}^{-1} A_i \epsilon^i + \mathcal{O}(\epsilon^0)$$

$$A_{-4} = \frac{x^2}{24(1-x)^4(1+y)},$$

$$A_{-3} = \frac{x^2}{96(1-x)^4(1+y)} \Big[ -10G(-1;y) + 3G(0;x) - 6G \Big]$$

$$A_{-2} = \frac{x^2}{48(1-x)^4(1+y)} \Big[ -5\zeta(2) - 6G(-1;y)G(0;x) + \Big]$$

$$A_{-1} = \frac{x^2}{48(1-x)^4(1+y)} \Big[ -13\zeta(3) + 38\zeta(2)G(-1;y) + 9\zeta(2)G(0;x) + \frac{6\zeta(2)}{\beta} \underbrace{(1;x)}_{\beta} - 24\zeta(2)G(-1/y;x) + 24G(0;x)G(-1,-1;y) - 24G(1;x)G(-1,-1;y) - 12G(-1/x)G(-1,-1;y) - 12G(-1/x)G(-1,-1;y) + 6G(-1/x)G(-1,-1;y) + 6G(-1/x)G(-1$$

### **GHPLs**

One- and two-dimensional Generalized Harmonic Polylogarithms (GHPLs) are defined as repeated integrations over set of basic functions. In the case at hand

$$f_w(x) = \frac{1}{x - w}, \quad \text{with} \quad w \in \left\{0, 1, -1, -y, -\frac{1}{y}, \frac{1}{2} \pm \frac{i\sqrt{3}}{2}\right\}$$
 $f_w(y) = \frac{1}{y - w}, \quad \text{with} \quad w \in \left\{0, 1, -1, -x, -\frac{1}{x}, 1 - \frac{1}{x} - x\right\}$ 

The weight-one GHPLs are defined as

$$G(0;x) = \ln x$$
,  $G(w;x) = \int_0^x dt f_w(t)$ 

Higher weight GHPLs are defined by iterated integrations

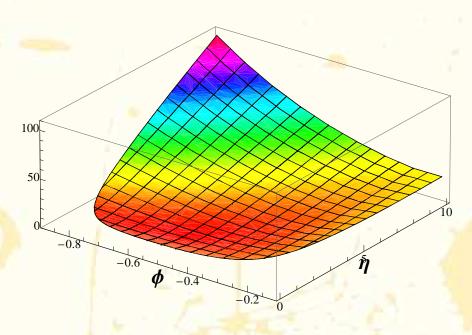
$$G(\underbrace{0,0,\cdots,0};x) = \frac{1}{n!} \ln^n x, \qquad G(w,\cdots;x) = \int_0^x dt f_w(t) G(\cdots;t)$$

Shuffle algebra. Integration by parts identities

Remiddi and Vermaseren '99, Gehrmann and Remiddi '01-'02, Aglietti and R. B. '03, Vollinga and Weinzierl '04, R. B., A. Ferroglia, T. Gehrmann, and C. Studerus '09

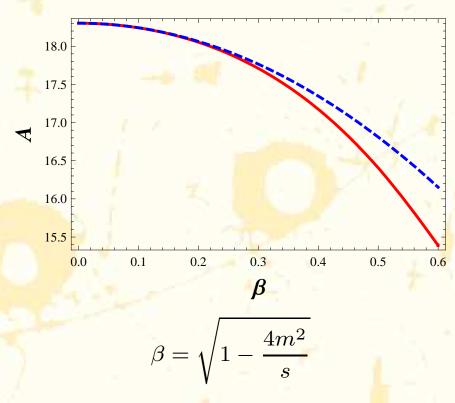
### **Coefficient A**

Finite part of A



$$\eta = \frac{s}{4m^2} - 1, \quad \phi = -\frac{t - m^2}{s}$$

#### Threshold expansion versus exact result



partonic c.m. scattering angle =  $\frac{\pi}{2}$ 

Numerical evaluation of the GHPLs with GiNaC C++ routines.

Vollinga and Weinzierl '04

# Two-Loop Corrections to $gg \rightarrow t\bar{t}$

$$|\mathcal{M}|^{2}(s,t,m,\varepsilon) = \frac{4\pi^{2}\alpha_{s}^{2}}{N_{c}} \left[ \mathcal{A}_{0} + \left(\frac{\alpha_{s}}{\pi}\right) \mathcal{A}_{1} + \left(\frac{\alpha_{s}}{\pi}\right)^{2} \mathcal{A}_{2} + \mathcal{O}\left(\alpha_{s}^{3}\right) \right]$$

$$\mathcal{A}_{2} = \mathcal{A}_{2}^{(2\times0)} + \mathcal{A}_{2}^{(1\times1)}$$

$$\mathcal{A}_{2}^{(2\times0)} = (N_{c}^{2} - 1) \left( N_{c}^{3} A + N_{c} B + \frac{1}{N_{c}} C + \frac{1}{N_{c}^{3}} D + N_{c}^{2} N_{l} E_{l} + N_{c}^{2} N_{h} E_{h} + N_{l} F_{l} + N_{h} F_{h} + \frac{N_{l}}{N_{c}^{2}} G_{l} + \frac{N_{h}}{N_{c}^{2}} G_{h} + N_{c} N_{l}^{2} H_{l} + N_{c} N_{h}^{2} H_{h} + N_{c} N_{h}^{2} H_{h} + \frac{N_{l} N_{h}}{N_{c}^{2}} I_{l} + \frac{N_{h}}{N_{c}^{2}} I_{h} + \frac{N_{l} N_{h}}{N_{c}^{2}} I_{lh} \right)$$

789 two-loop diagrams contribute to 16 different color coefficients

- No numeric result for  $\mathcal{A}_2^{(2 imes0)}$  yet
- ullet The poles of  $\mathcal{A}_2^{(2\times0)}$  are known analytically

Ferroglia, Neubert, Pecjak, and Li Yang '09

The coefficients A,  $E_l$ – $I_l$  can be evaluated analytically as for the  $q\bar{q}$  channel

R. B., Ferroglia, Gehrmann, von Manteuffel and Studerus, in prep.

### **Conclusions**

- In the last 15 years, Tevatron explored top-quark properties reaching a remarkable experimental accuracy. The top mass could be measured with  $\Delta m_t/m_t=0.75\%$  and the production cross section with  $\Delta \sigma_{t\bar{t}}/\sigma_{t\bar{t}}=9\%$ . Other observables could be measured only with bigger errors.
- At the LHC the situation will further improve. The production cross section of  $t\bar{t}$  pairs is expected to reach the accuracy of  $\Delta\sigma_{t\bar{t}}/\sigma_{t\bar{t}}=5\%!!$
- This experimental precision demands for more accurate theoretical predictions. Quantum corrections have to be unavoidably taken into account.
- For the production cross section,  $\sigma_{t\bar{t}}$ , a complete NNLO analysis is mandatory in order to reach the experimental accuracy expected in 3-4 years from now.
- In spite of a big activity of different groups, many ingredients are still missing.
- In this talk I briefly reviewed the analytic evaluation of the two-loop matrix elements, afforded using the Laporta algorithm for the reduction to the MIs and the Differential Equations method for their analytic evaluation. To date, the corrections involving a fermionic loop (light or heavy) in the  $q\bar{q}$  channel are completed, together with the leading color coefficient. Analogous corrections in the gg channel can be calculated with the same technique and are at the moment under study.