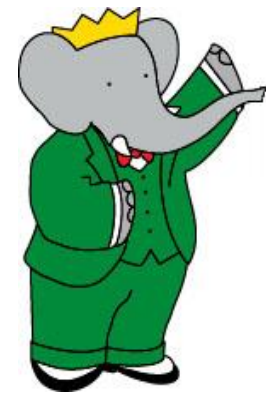


**Measurements of Semileptonic B meson decays to Charm
and the determination of the CKM matrix element $|V_{cb}|$
at BaBar**

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University and INFN, Ferrara

on behalf of
the BaBar collaboration



35th International Conference on High Energy Physics
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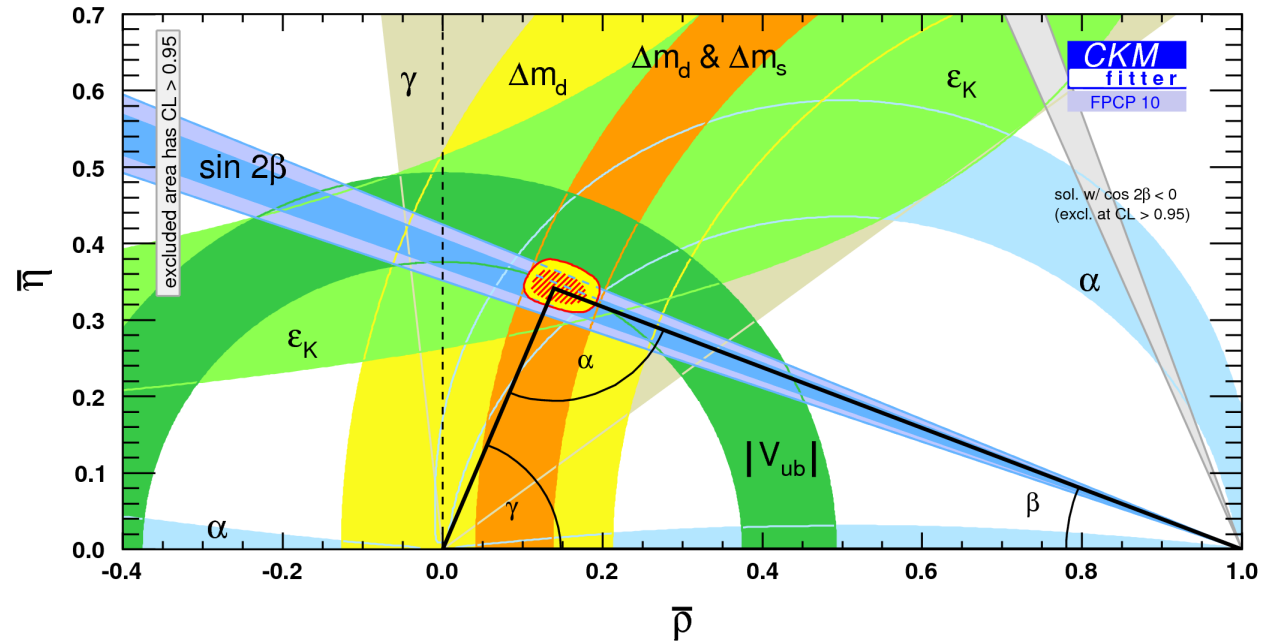
- Inclusive $|V_{cb}|$: measurement of moments
[PRD **81**, 032003 (2010)]
- Exclusive $|V_{cb}|$: $B \rightarrow Dlv$ with hadronic tag
[PRL **104**, 011802 (2010)]
- $\mathcal{B}(B \rightarrow D_s^{(*)}Klv)$ measurement



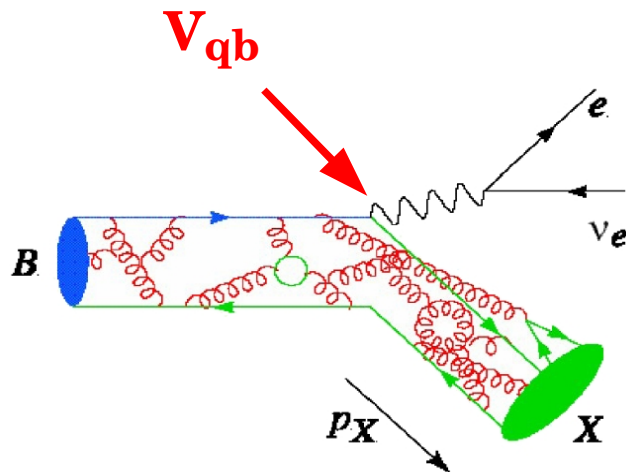
new

Measure $|V_{cb}|$ and $|V_{ub}|$ to overconstrain the Unitarity Triangle

$$\frac{\delta|V_{cb}|}{|V_{cb}|} \sim 2\%$$



Semileptonic B decays



- leptonic and hadronic current decoupled
- quark decay depends on $|V_{xb}|$, m_b . Perturbative regime
- We see mesons: QCD corrections

Inclusive approach: study distributions from $B \rightarrow X_l \nu_q$

Theory: OPE

Exclusive approach: focus on single decay channel.

Theory: Form Factors (eg. Lattice QCD)

Inclusive $|V_{cb}|$

- Total rate described in the context of Heavy Quark Expansion

$$\Gamma(\bar{B} \rightarrow X_c \ell \bar{\nu}) = \frac{G_F^2}{192\pi^3} m_b^5 |V_{cb}|^2 (1 + A_{ew}) A^{pert} F\left(r, \frac{\mu_\pi^2}{m_b^2}, \frac{\mu_G^2}{m_b^2}, \dots\right) \quad r = \frac{m_c}{m_b}$$

free quark decay

Perturbative
corrections
(expansion $1/\alpha_s^k$)

non perturbative
corrections (expansion $1/m_b^n$)

- non perturbative parameters need to be measured
- OPE relates moments and rates of inclusive distribution to heavy quark parameters

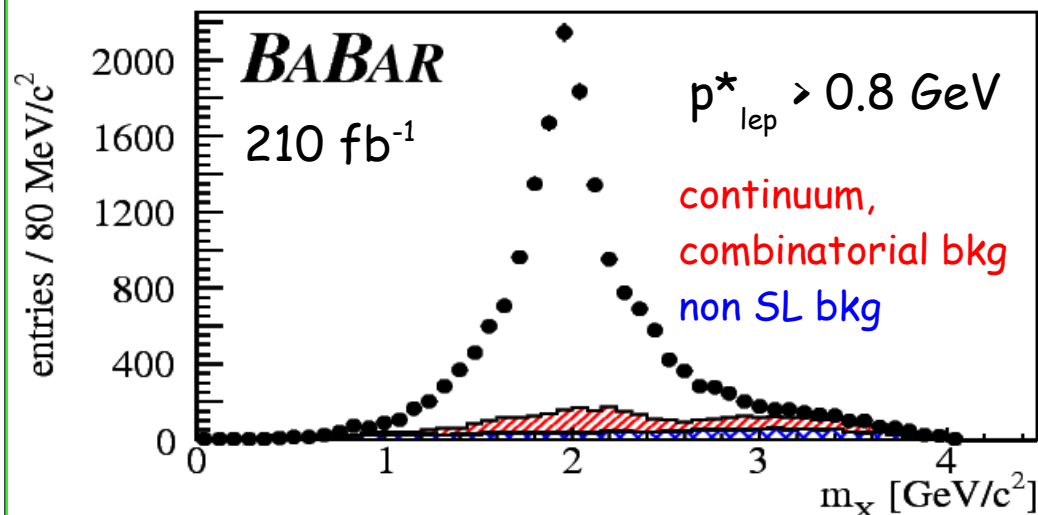
$$\begin{aligned} \langle E_\ell^n \rangle_{p_\ell^*} &= f^{(n)}(p_\ell^* \text{ cut}, m_b, \text{HQ parameters}) \\ \langle m_X^{2n} \rangle_{p_\ell^*} &= g^{(n)}(p_\ell^* \text{ cut}, m_b, \text{HQ parameters}) \\ \langle E_\gamma^n \rangle_{p_\ell^*} &= h^{(n)}(p_\ell^* \text{ cut}, m_b, \text{HQ parameters}) \end{aligned}$$

Calculations available in the "kinetic" (Benson et al. Nucl. Phys. B665:367) and "1S" (Bauer et al., Phys. Rev. D70:094017,2004) mass scheme

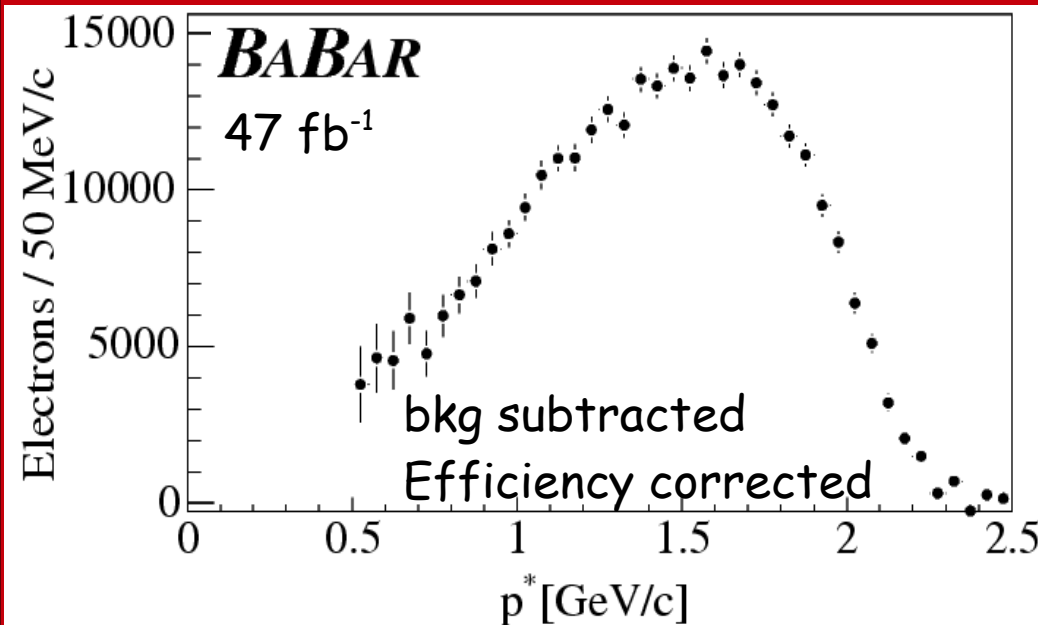
Inclusive $|V_{cb}|$: moments measurements

- Analysis performed reconstructing semileptonic B decays on the recoil of fully reconstructed B meson decays in hadronic mode (low efficiency $\sim 0.4\%$; high purity $\sim 80\%$)

- Hadronic mass moments $\langle m_x^k \rangle$



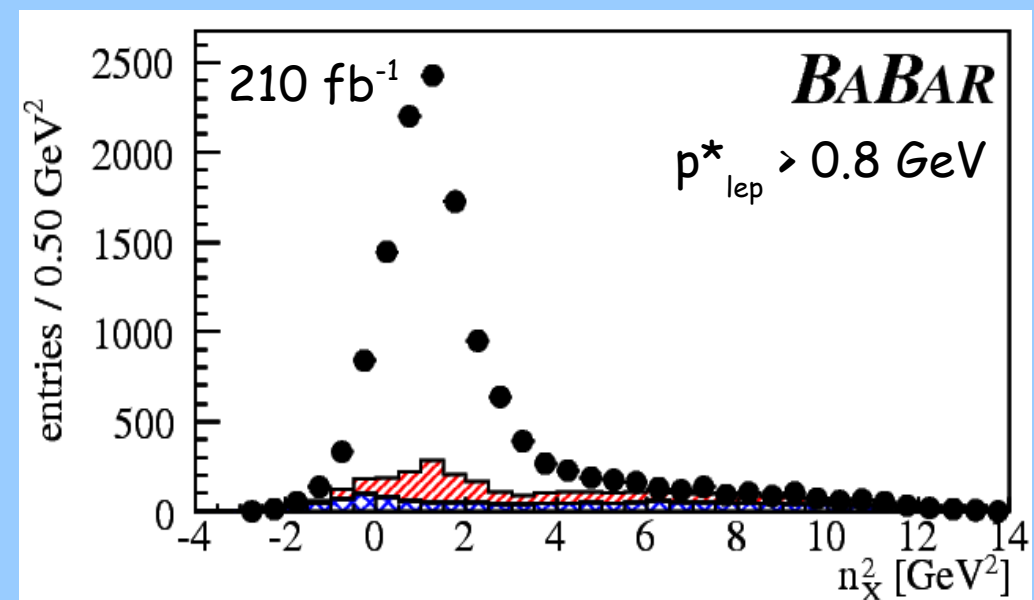
- Electron Energy moments



- Mixed mass and energy moments $\langle n_x^k \rangle$

[Gambino, Uraltsev Eur. Phys. J. C 34, 181 (2004)]

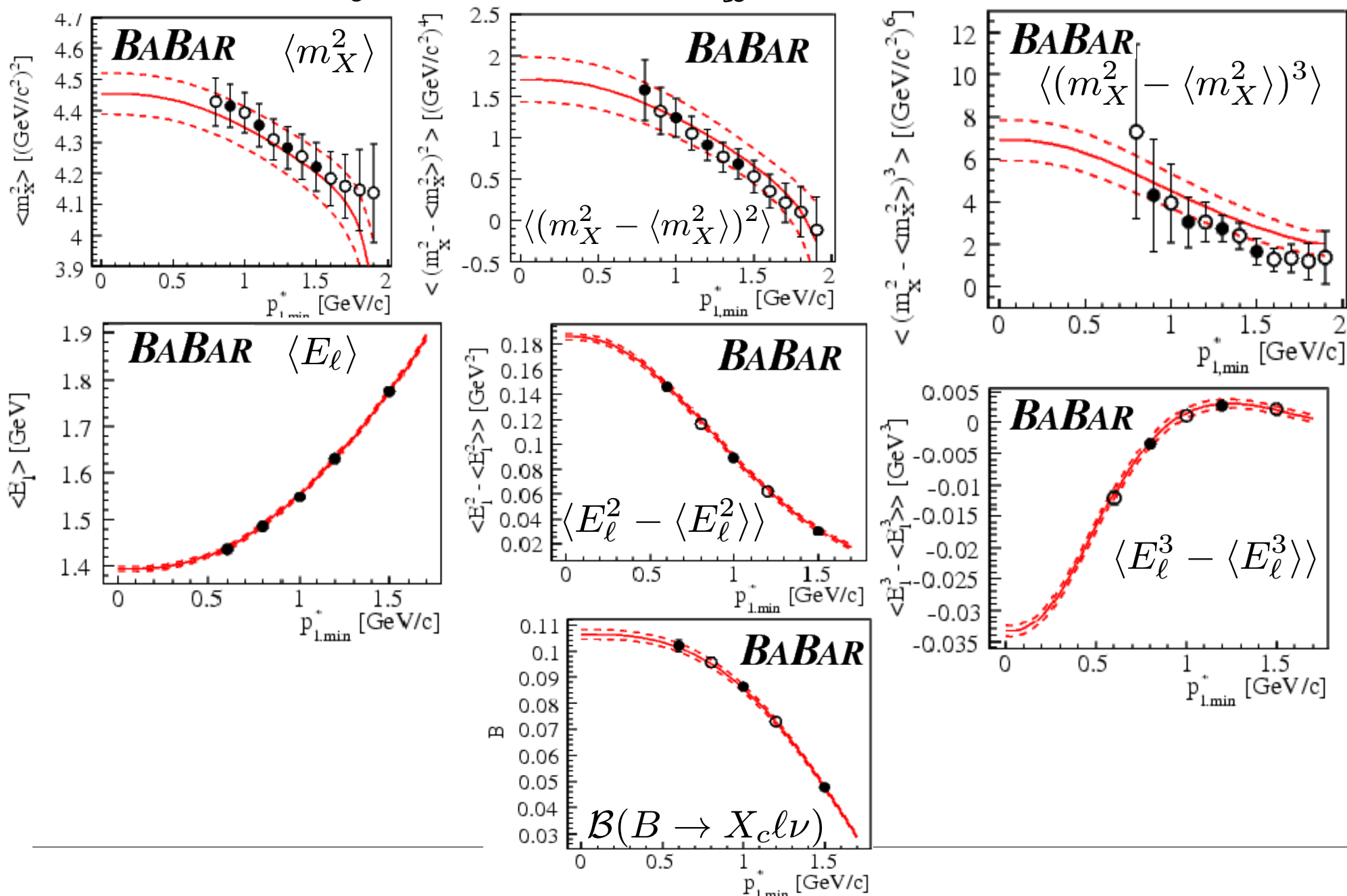
$$n_X^2 = m_X^2 c^4 - 2\tilde{\Lambda} E_X + \tilde{\Lambda}^2$$



Inclusive $|V_{cb}|$: moments measurements

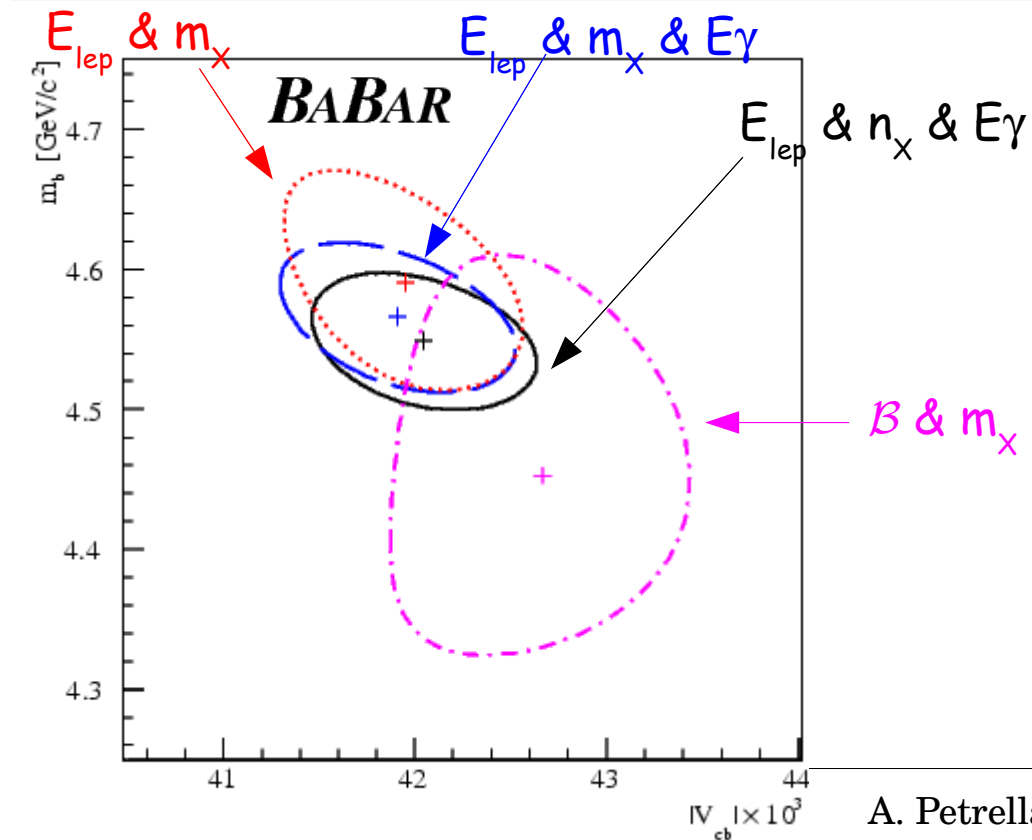
- Global Fit performed with either m_X or n_X and 10 E_{lep} moments and 3 E_γ moments ($B \rightarrow X_s \gamma$)

external constraint $\mu_G^2 = (0.35 \pm 0.07) \text{ GeV}^2$, $\rho_{LS}^3 = (-0.15 \pm 0.10) \text{ GeV}^3$



Inclusive $|V_{cb}|$: moments measurements

	Fit with Hadronic mass moments	Fit with combined mass-energy moments	HFAG Average (end 2009) ($B \rightarrow X_c l \nu$ & $B \rightarrow X_s \gamma$)
$ V_{cb} (10^{-3})$	$42.05 \pm 0.45 \pm 0.70$	$41.91 \pm 0.48 \pm 0.70$	$41.85 \pm 0.42_{(fit)} \pm 0.60$
$m_b (\text{GeV}/c^2)$	$4.549 \pm 0.031 \pm 0.038$	$4.556 \pm 0.034 \pm 0.041$	4.591 ± 0.031
$\mathcal{B}(B \rightarrow X_c l \nu) (\%)$	$10.64 \pm 0.17 \pm 0.06$	$10.64 \pm 0.17 \pm 0.06$	10.55 ± 0.14
χ^2/ndf	10.9 / 28	8.2 / 28	29.7 / 59



- Good agreement of all fit parameters
- Fits in agreement with old determinations and average
- combined mass-energy moment does not give more precise determination
- increased confidence in OPE fits
- $\delta|V_{cb}|/|V_{cb}|$ at $\sim 2\%$

Exclusive $|V_{cb}|$

$B \rightarrow Dlv$ with Hadronic tag

Exclusive $|V_{cb}|$: $B \rightarrow D\ell\nu$ with Hadronic tag

- Differential decay rate:

$$\frac{d\Gamma(B \rightarrow D\ell\nu)}{dw} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3 \hbar} M_D^3 (M_B + M_D)^2 (w^2 - 1)^{3/2} \mathcal{G}^2(w)$$

$$w = \frac{M_B^2 + M_D^2 - q^2}{2M_B M_D} \quad q^2 = (p_B - p_D)^2$$

$\mathcal{G}(w)$ form factor: Caprini et al.
Nucl. Phys. B530, 153 (1998)

- Experiment measures $\mathcal{G}(1)|V_{cb}|$ and FF slope ρ_D^2
- Hadronic tag: Neutrino is the only missing particle

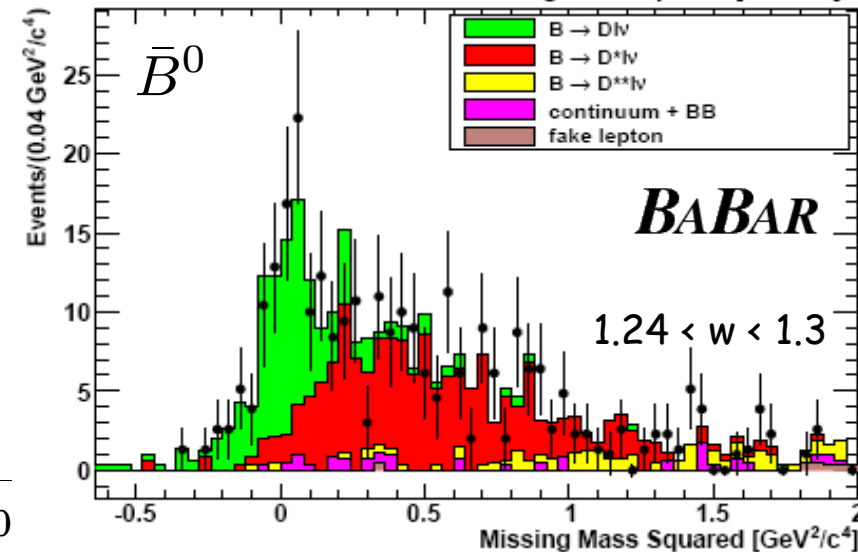
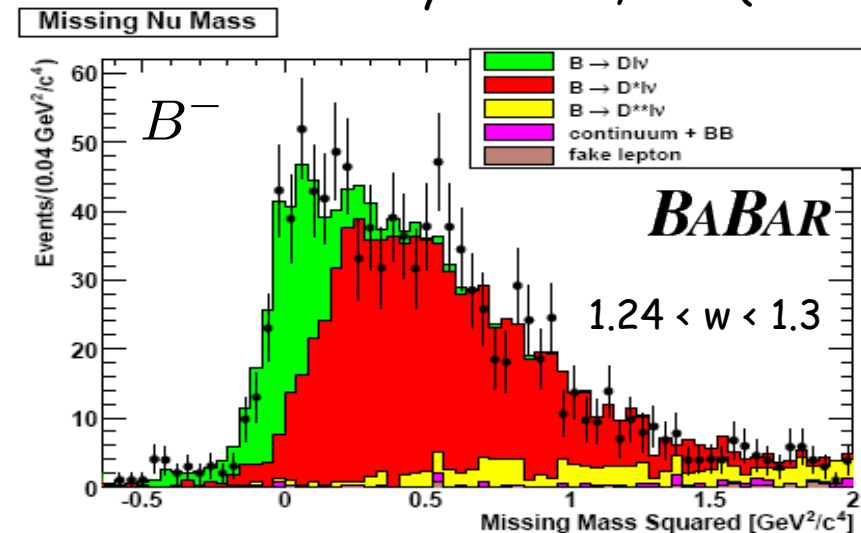
$$m_{miss}^2 = [p_{\Upsilon(4s)} - p_{B_{tag}} - p_D - p_\ell]^2$$

signal side well measured: w resolution ~ 0.01

- Background from $D^*\ell\nu$ is significant (larger BF, undetected slow π)

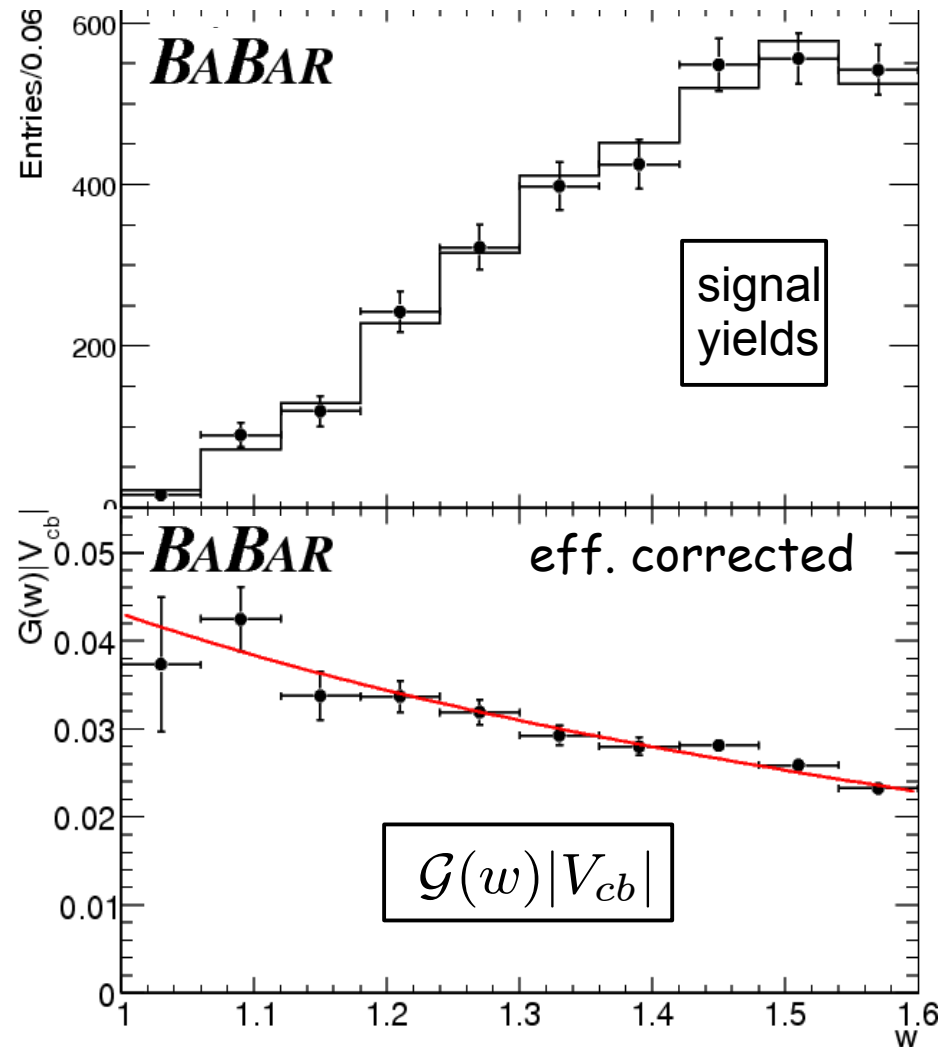
Signal Yields	2147 ± 69	$B^- \rightarrow D^0 \ell^- \bar{\nu}$
	1108 ± 45	$\bar{B}^0 \rightarrow D^+ \ell^- \bar{\nu}$

- Inclusive $B \rightarrow X\ell\nu$ used as normalization sample



Exclusive $|V_{cb}|$: $B \rightarrow D\ell\nu$ with Hadronic tag

χ^2 fit of signal yields in w distribution $1 < w < 1.6$



$$\mathcal{B}(\bar{B} \rightarrow D\ell\bar{\nu}) = (2.15 \pm 0.06 \pm 0.09)\%$$

$$\mathcal{G}(1)|V_{cb}| = (42.3 \pm 1.9 \pm 1.4) \times 10^{-3}$$

$$\rho_D^2 = 1.20 \pm 0.09 \pm 0.04$$

Unquenched lattice calculation

Okamoto et al. Nucl. Phys. B, Proc Suppl. 140, 461 (2005)

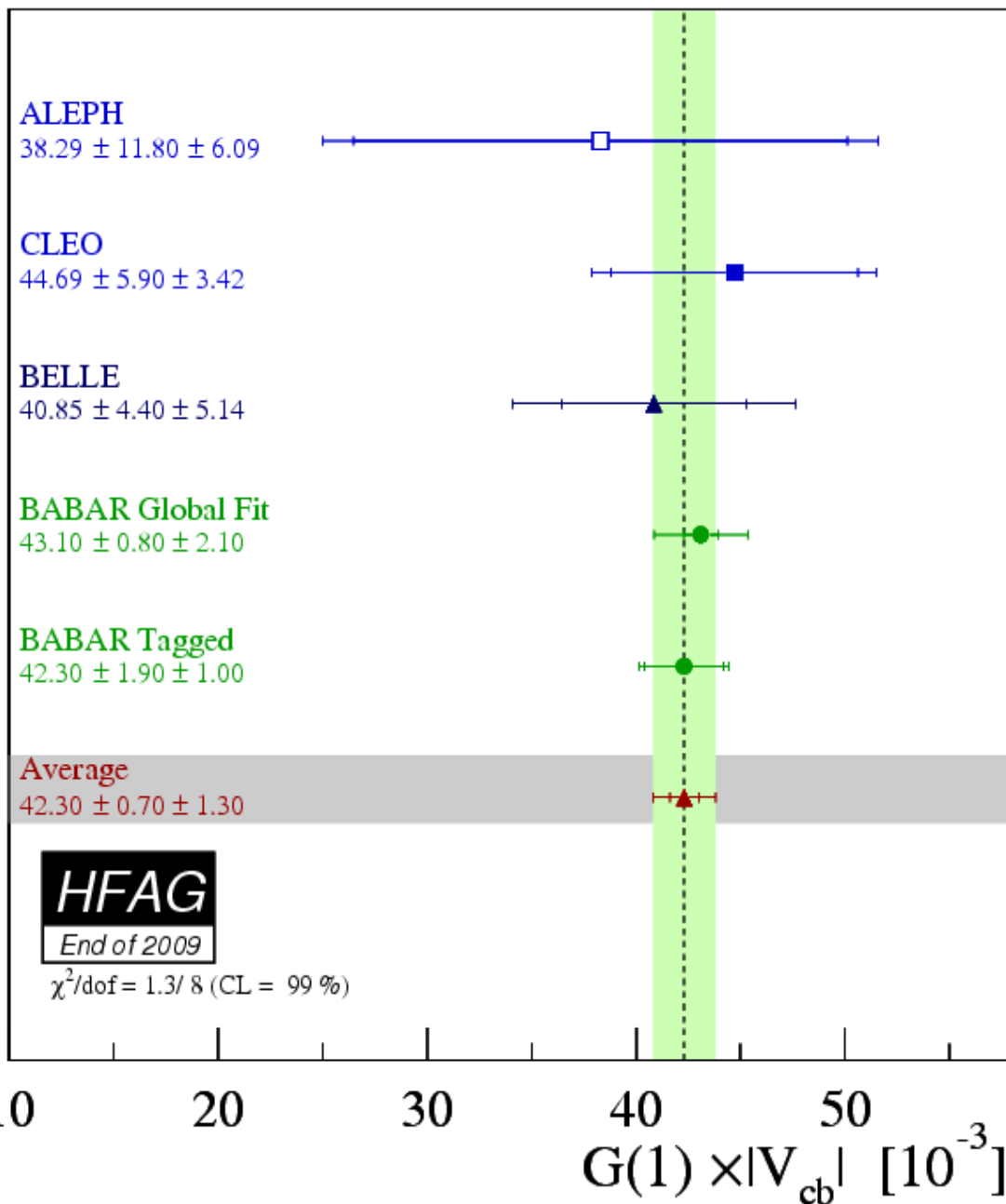
$$|V_{cb}| = (39.2 \pm 1.8 \pm 1.3 \pm 0.9_{FF}) \times 10^{-3}$$

Quenched lattice calculation

Divitiis et al. Phys. Lett. B 655, 45 (2007)

$$|V_{cb}| = (40.9 \pm 1.8 \pm 1.4 \pm 0.7_{FF}) \times 10^{-3}$$

Exclusive $|V_{cb}|$: HFAG averages



Tagged measurement is the most precise in $B \rightarrow Dlv$ channel

$|V_{cb}| = (39.2 \pm 1.4_{\text{exp}} \pm 0.9_{\text{FF}}) 10^{-3}$ ($\sim 4\%$)
 $\mathcal{G}(1) = 1.074(18)(16)$
 Nucl. Phys. B, Proc Suppl. 140, 461 (2005)

good agreement with $|V_{cb}|$ from exclusive $B \rightarrow D^*lv$
 $|V_{cb}| = (39.1 \pm 0.6 \pm 0.8_{\text{FF}}) 10^{-3}$ ($\sim 3\%$)
 $\mathcal{F}(1) = 0.921(13)(20)$
 Phys. Rev. D 79, 014506 (2009)

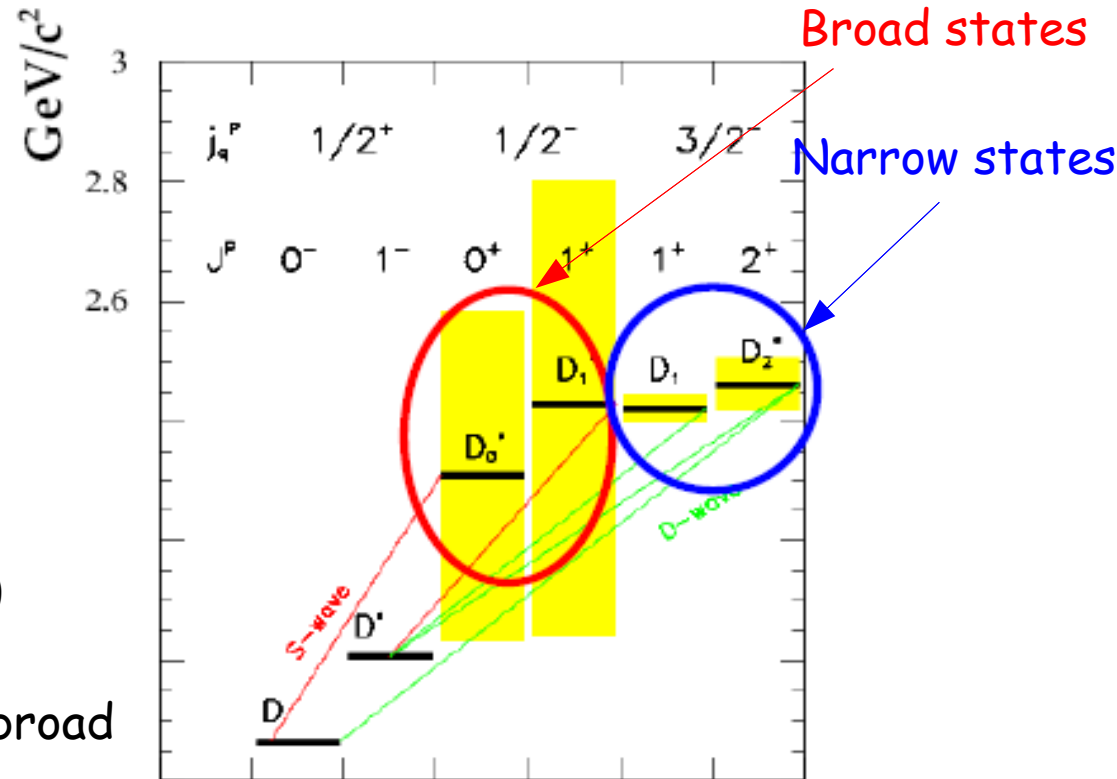
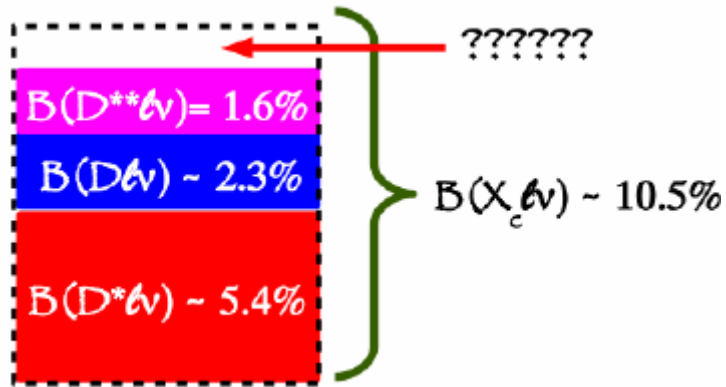
Tension with inclusive measurements
 $|V_{cb}| = (41.9 \pm 0.4 \pm 0.6) 10^{-3}$ ($\sim 2\%$)
Exclusive determinations 2σ lower than inclusive one

$\mathcal{B}(B \rightarrow D_s^{(*)} K l \nu)$ measurement

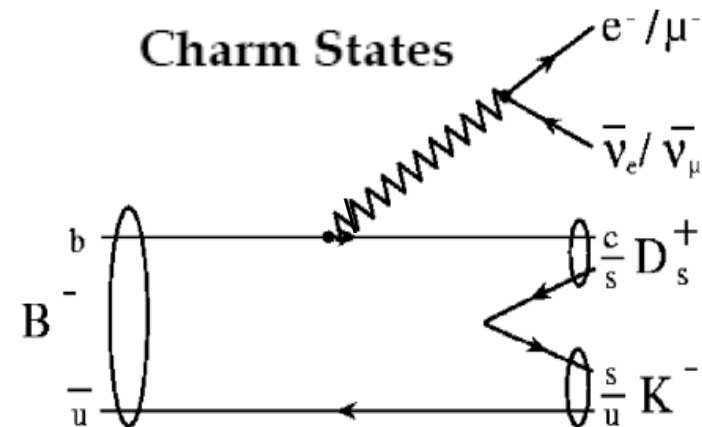
$$\mathcal{B}(B^- \rightarrow D_s^{(*)} + K^- \ell^- \bar{\nu}_\ell)$$

Puzzle in exclusive $B \rightarrow D^{(*,**)} \ell \nu$ Branching Fractions:

$$\mathcal{B}(B \rightarrow X_c \ell \nu) > \mathcal{B}(B \rightarrow D \ell \nu) + \mathcal{B}(B \rightarrow D^* \ell \nu) + \mathcal{B}(B \rightarrow D^{**} \ell \nu)$$



- experimentally: similar rate for broad and narrow (QCD sum rule: narrow \gg broad)
- small statistics doesn't allow to separate broad from non resonant
- $B \rightarrow D_s^{(*)} K \ell \nu$ similar to $B \rightarrow D^{(*)} \pi \ell \nu$. Study hadronic mass spectrum above 2.46 GeV/c²
- $\mathcal{B}(B \rightarrow D_s^{(*)} K \ell \nu)$ expected $\sim 10^{-3}$



$\mathcal{B}(B^- \rightarrow D_s^{(*)+} K^- \ell^- \bar{\nu}_\ell)$

- Exclusive reconstruction

$$D_s \rightarrow \phi(K^+ K^-) \pi$$

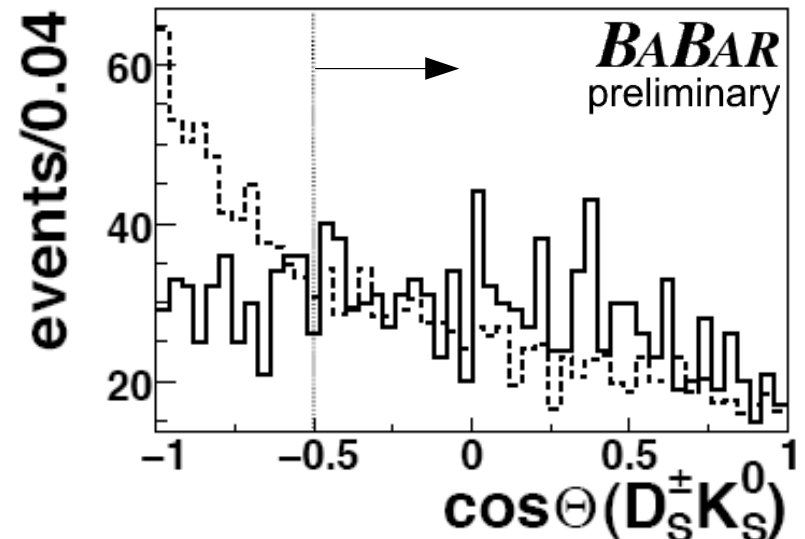
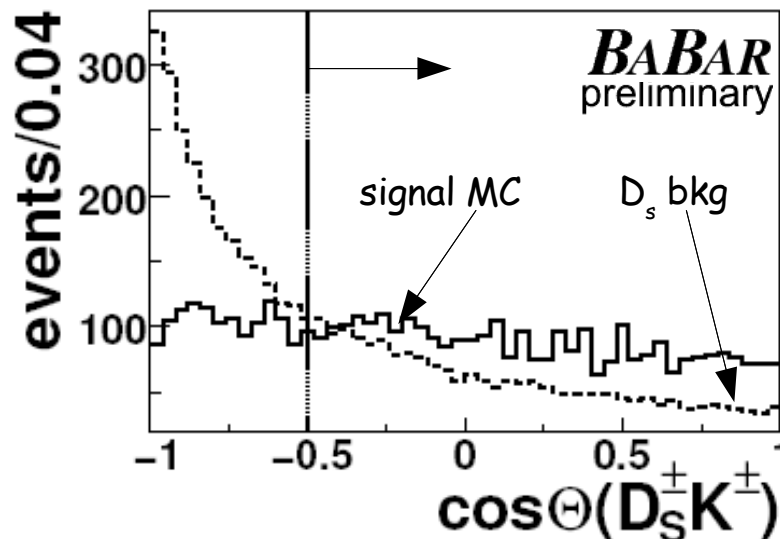
$$D_s \rightarrow \bar{K}^{*0}(K^\pm \pi^\mp) K$$

$$D_s \rightarrow K_s^0(\pi^+ \pi^-) K$$

Feed Forward NN to suppress combinatorial bkg.

- lepton ($p_{lep} > 0.8 \text{ GeV}/c$) and Kaon added to D_s candidate
- Bkg from $B \rightarrow DD_s$ reduced using angular correlation between D_s and D (signal events no correlation)

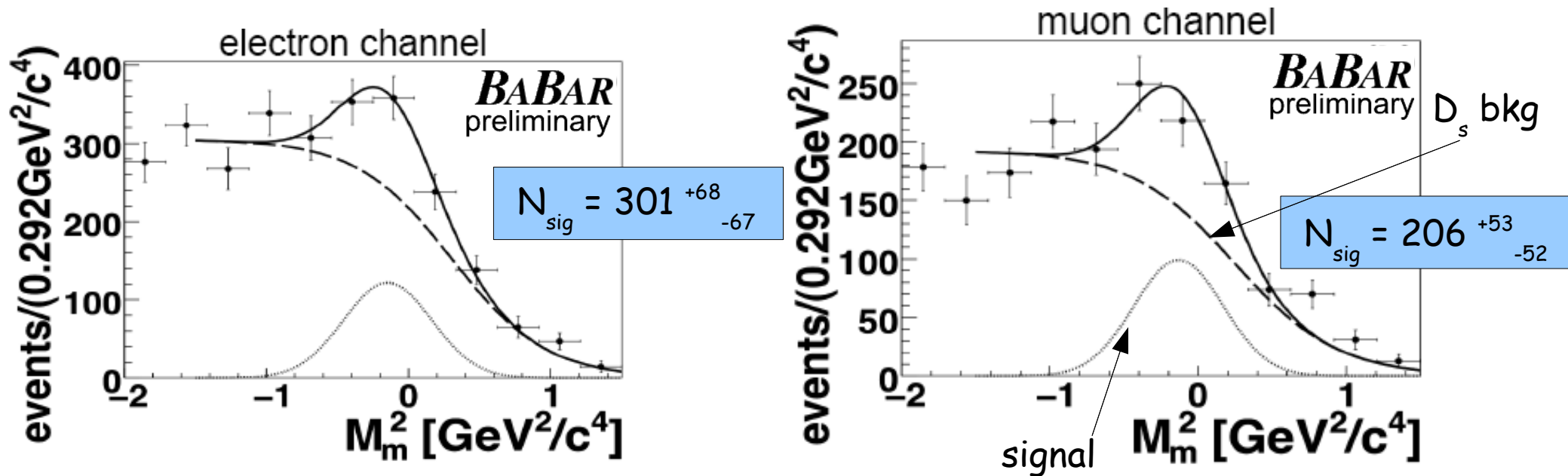
~30% of D_s bkg rejected



$\mathcal{B}(B^- \rightarrow D_s^{(*)+} K^- \ell^- \bar{\nu}_\ell)$

- Signal yields extracted via unbinned extended maximum likelihood fit to Missing mass

$$M_m^2 = (E_{beam} - E_Y)^2 - |\vec{p}_Y|^2 = m_\nu^2 \quad Y = D_s K \ell \text{ candidate}$$



- leading systematic uncertainty: signal MC modelling ($\sim 3\%$ - 8% depending on channel)
- Signal MC statistics ($\sim 2\%$)

342 fb⁻¹

$$\mathcal{B}(B \rightarrow D_s^+ K^- \ell^- \bar{\nu}_\ell) = (6.13_{-1.03}^{+1.04} \text{stat.} \pm 0.43_{\text{sys.}} \pm 0.51(\mathcal{B}(D_s))) \times 10^{-4}$$

- Result in agreement with ARGUS measurement: $\mathcal{B}(B \rightarrow D_s^+ K^- \ell^- \bar{\nu}_\ell) < 5 \times 10^{-3}$
- BR too small to solve the BR puzzle

Conclusions

- Inclusive $|V_{cb}|$ determinations precision at 2% from HQE fits to moments. Consistency check with combined energy-mass moments.
- $B \rightarrow Dlv$ tagged analyses give the most precise measurement of $\mathcal{G}(1)|V_{cb}|$.
 $|V_{cb}|$ determinations in agreement among different FF calculations.
- $|V_{cb}|$ determinations with inclusive/exclusive decays differ by $\sim 2\sigma$
- First measurement of $\mathcal{B}(B \rightarrow D_s^{(*)} Kl\nu)$ decay, 5σ significance. BR still too small to explain Incl-Excl branching ratio puzzle: more measurements needed.