

**Dedicated to the memory  
of Alexei Sissakian**

## Energy Loss in Heavy Ion Collisions

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# In Memoriam

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Alexei Norairovich Sissakian

14.10.1944 – 01.05.2010



# Contents

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- Introduction (motivation & goals)
- Self-similarity in hadron production
  - z-Scaling - ideas, definitions, properties,...
- Energy scan of spectra at RHIC
- Energy loss in HIC vs.  $s^{1/2}$ , centrality,  $p_T$
- Conclusions



# Motivation

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“Scaling” and “Universality” are concepts developed to understanding critical phenomena. Scaling means that systems near the critical points exhibiting self-similar properties are invariant under transformation of a scale. According to universality, quite different systems behave in a remarkably similar fashion near the respective critical points. Critical exponents are defined only by symmetry of interactions and dimension of the space. H.Stanley, G.Barenblat,...

**z-Scaling** reveals self-similar properties in hadron, jet and direct photon production in high energy hadron and nucleus collisions.

**z-Scaling** can be used as a tool for searching for new physics in particle production at high energies.



# Goals

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Development of **z**-scaling approach for description of hadron production in inclusive reactions to search for signatures of new state of nuclear matter (phase transitions, critical point, ...)

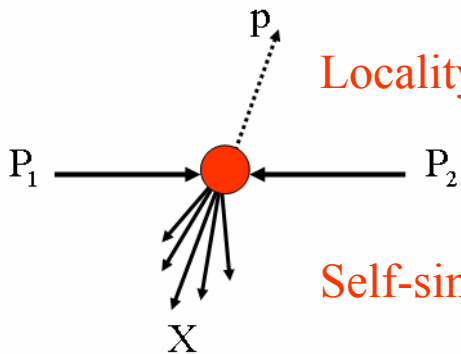
Analysis of **AA** experimental data obtained at RHIC & SPS to verify properties of **z**-scaling observed in **pp** &  $\bar{p}p$  collisions at U70, ISR,  $S\bar{p}pS$ , SPS and Tevatron.

Estimation of constituent energy loss in central **AA** collisions vs. collision energy, centrality, transverse momentum over the range  $s_{NN}^{1/2} = 9\text{-}200$  GeV



# z-Scaling

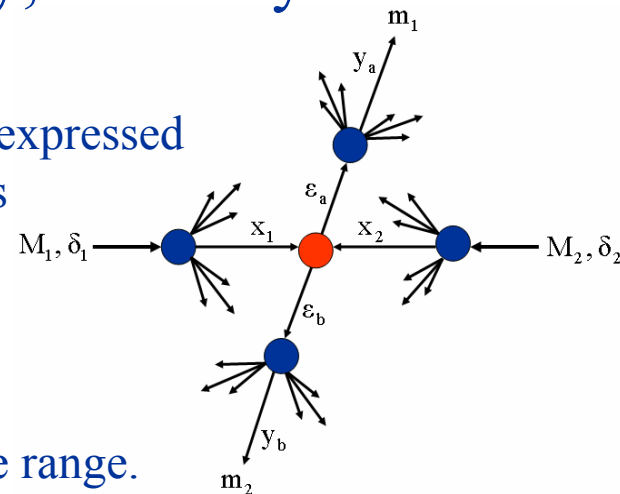
**Principles:** locality, self-similarity, fractality



**Locality:** collisions of hadrons and nuclei are expressed via interactions of their constituents (partons, quarks and gluons,...).

**Self-similarity:** interactions of the constituents are mutually similar.

**Fractality:** the self-similarity over a wide scale range.



## Hypothesis of z-scaling :

$s^{1/2}, p_T, \theta_{\text{cms}}$  Inclusive particle distributions can be described in terms of constituent sub-processes and parameters characterizing bulk properties of the system.

$x_1, x_2, y_a, y_b$   
 $\delta_1, \delta_2, \epsilon_a, \epsilon_b, c$

$Ed^3\sigma/dp^3$  Scaled inclusive cross section of particles depends in a self-similar way on a single scaling variable  $z$ .

$\Psi(z)$



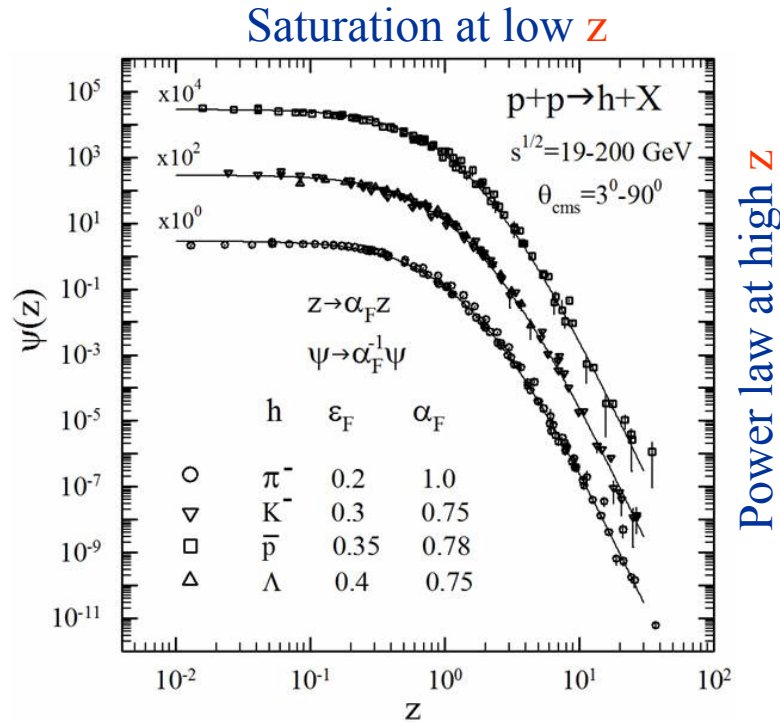
# Scaling & Universality

$\pi^-, K^-, \bar{p}, \Lambda$   
in pp collisions

FNAL:  
PRD 75 (1979) 764

ISR:  
NPB 100 (1975) 237  
PLB 64 (1976) 111  
NPB 116 (1976) 77  
(low  $p_T$ )  
NPB 56 (1973) 333  
(small angles)

STAR:  
PLB 616 (2005) 8  
PLB 637 (2006) 161  
PRC 75 (2007) 064901



- Energy & angular independence
- Flavor independence ( $\pi, K, p, \Lambda$ )
- Saturation for  $z < 0.1$
- Power law for high  $z > 4$

Energy scan of spectra  
at U70, ISR, SppS, SPS, HERA,  
FNAL(fixed target),  
Tevatron, RHIC, LHC

MT & I.Zborovsky  
Phys.Rev.D75,094008(2007)  
Int.J.Mod.Phys.A24,1417(2009)  
J. Phys.G: Nucl.Part.Phys.  
37,085008(2010)

- $\psi(z) \sim z^{-\beta}$  at high  $z$
- $\epsilon_F, \alpha_F$  independent  
of  $p_T, s^{1/2}, \theta_{\text{cms}}$

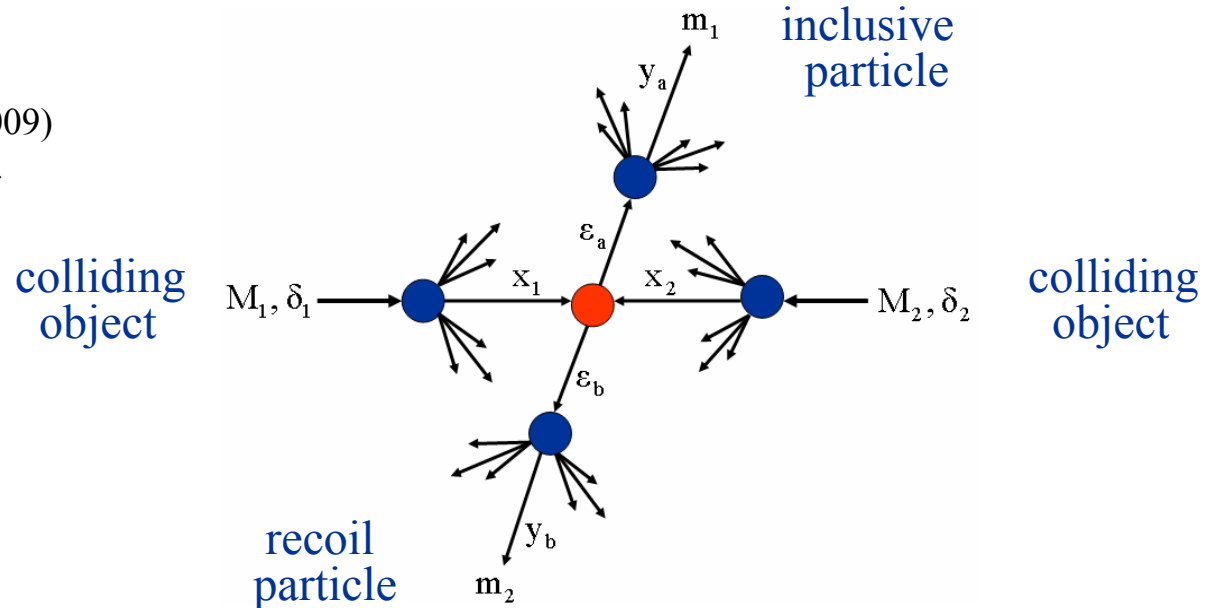
Scaling – “collapse” of data points onto a single curve.  
Scaled particle yield ( $\Psi$ ) vs. scaled transverse momentum ( $z$ ).  
Universality classes – hadron species ( $\epsilon_F, \alpha_F$ ).





# Locality of hadron interactions

M.T. & I.Zborovský  
 Part.Nucl.Lett.312(2006)  
 PRD75,094008(2007)  
 Int.J.Mod.Phys.A24,1417(2009)  
 J.Phys.G: Nucl.Part.Phys.  
 37,085008(2010)



## Constituent subprocess

$$(x_1 M_1) + (x_2 M_2) \Rightarrow (m_1 / y_a) + (x_1 M_1 + x_2 M_2 + m_2 / y_b)$$

Kinematical condition (4-momentum conservation law):

$$(x_1 P_1 + x_2 P_2 - p / y_a)^2 = M_X^2$$

Recoil mass:  $M_X = x_1 M_1 + x_2 M_2 + m_2 / y_b$

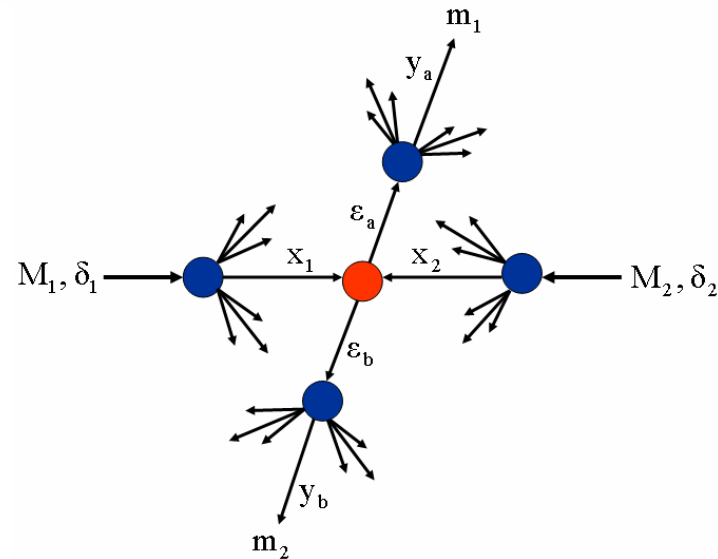




# Self-similarity parameter $z$

$$z = z_0 \cdot \Omega^{-1}$$

$$z_0 = \frac{s_{\perp}^{1/2}}{(dN_{\text{ch}}/d\eta|_0)^c m}$$



- $\Omega^{-1}$  is the minimal resolution at which a constituent subprocess can be singled out of the inclusive reaction
- $s_{\perp}^{1/2}$  is the transverse kinetic energy of the subprocess consumed on production of  $m_1$  &  $m_2$
- $dN_{\text{ch}}/d\eta|_0$  is the multiplicity density of charged particles at  $\eta = 0$
- $c$  is a parameter interpreted as a “specific heat” of created medium
- $m$  is an arbitrary constant (fixed at the value of nucleon mass)

# Fractal measure $z$

The fractality is reflected in definition of  $z$

$$z = z_0 \Omega^{-1}$$

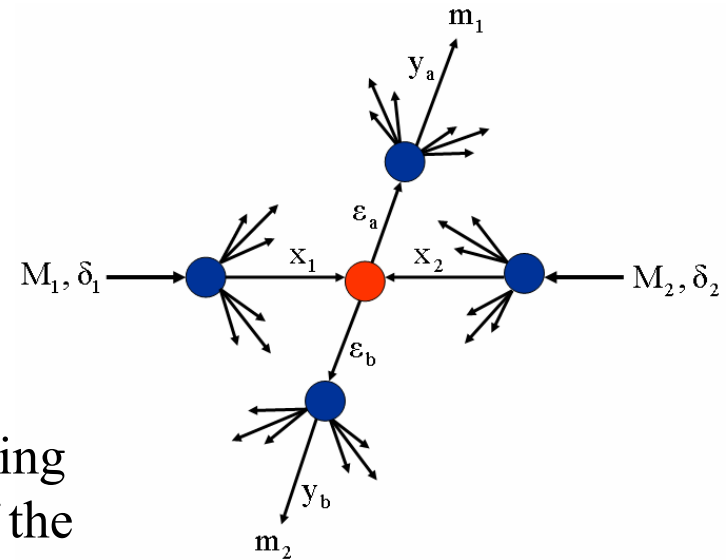
$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

$\Omega$  is relative number of configurations containing a sub-process with fractions  $x_1, x_2, y_a, y_b$  of the corresponding 4-momenta

$\delta_1, \delta_2, \varepsilon_a, \varepsilon_b$  are parameters characterizing structure of the colliding objects and fragmentation process, respectively

$\Omega^{-1}(x_1, x_2, y_a, y_b)$  characterizes resolution at which a constituent sub-process can be singled out of the inclusive reaction

$z(\Omega) \Big|_{\Omega^{-1} \rightarrow \infty} \rightarrow \infty$  The fractal measure  $z$  diverges as the resolution  $\Omega^{-1}$  increases.



# Momentum fractions $x_1, x_2, y_a, y_b$

**Principle of minimal resolution:** The momentum fractions  $x_1, x_2$  and  $y_a, y_b$  are determined in a way to minimize the resolution  $\Omega^{-1}$  of the fractal measure  $z$  with respect to all constituent sub-processes taking into account 4-momentum conservation:

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

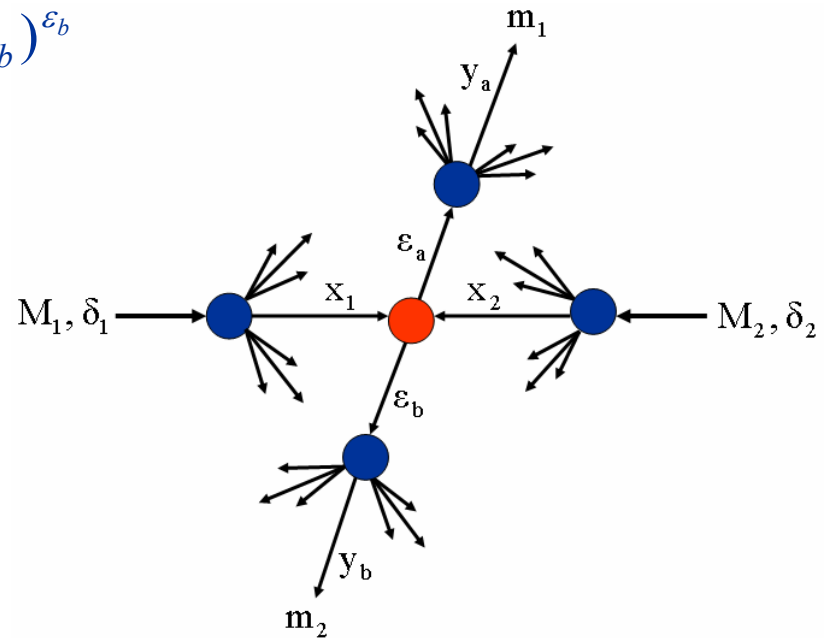
$$\begin{cases} \partial\Omega / \partial x_1 \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial x_2 \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \\ \partial\Omega / \partial y_b \big|_{y_a=y_a(x_1, x_2, y_b)} = 0 \end{cases}$$

**Momentum conservation law)**

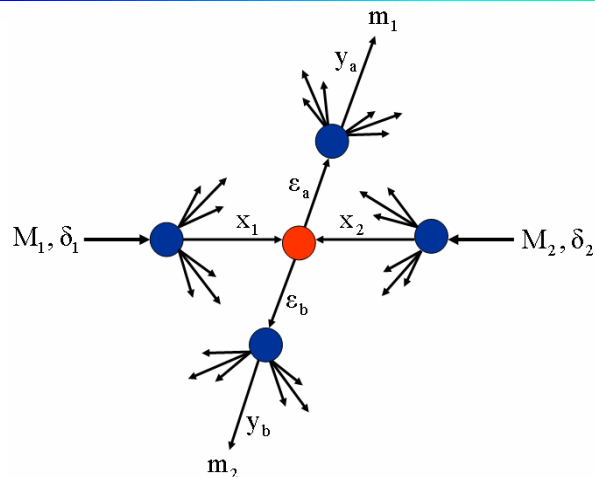
$$(x_1 P_1 + x_2 P_2 - p / y_a)^2 = M_X^2$$

**Recoil mass**

$$M_X = x_1 M_1 + x_2 M_2 + m_2 / y_b$$

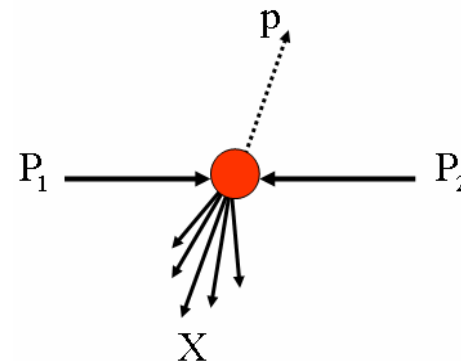


# Scaling function $\Psi(z)$



$$\int_0^{\infty} \Psi(z) dz = 1$$

$$z \rightarrow \alpha_F z, \quad \Psi \rightarrow \alpha_F^{-1} \Psi$$



$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3} \iff \int E \frac{d^3\sigma}{dp^3} dy d^2p_{\perp} = \sigma_{inel} \cdot N$$

- $\sigma_{in}$  - inelastic cross section
- $N$  - average multiplicity of the corresponding hadron species
- $dN/d\eta$  - pseudorapidity multiplicity density at angle  $\theta$  ( $\eta$ )
- $J(z, \eta; p_T^2, y)$  - Jacobian
- $E d^3\sigma/dp^3$  - inclusive cross section

The scaling function  $\Psi(z)$  is probability density to produce an inclusive particle with the corresponding  $z$ .

# Properties of $\Psi(z)$ in $pp$ & $\bar{p}p$ collisions

- Energy independence of  $\Psi(z)$  ( $s^{1/2} > 20$  GeV)
- Angular independence of  $\Psi(z)$  ( $\theta_{\text{cms}} = 3^\circ - 90^\circ$ )
- Multiplicity independence of  $\Psi(z)$  ( $dN_{\text{ch}}/d\eta = 1.5 - 26$ )
- Power law,  $\Psi(z) \sim z^{-\beta}$ , at high  $z$  ( $z > 4$ )
- Flavor independence of  $\Psi(z)$  ( $\pi, K, \phi, \Lambda, \dots, D, J/\psi, B, Y, \dots$ )
- Saturation of  $\Psi(z)$  at low  $z$  ( $z < 0.1$ )

These properties reflect self-similarity, locality, and fractality of the hadron interaction at constituent level. It concerns the structure of the colliding objects, interactions of their constituents, and fragmentation process.

M.T. & I.Zborovsky

Phys.At.Nucl. 70,1294(2007)

Phys.Rev. D75,094008(2007)

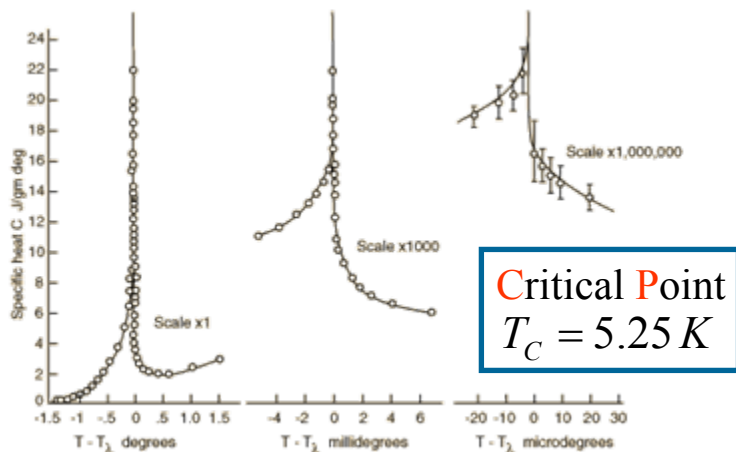
Int.J.Mod.Phys. A24,1417(2009)

J. Phys.G: Nucl.Part.Phys. 37,085008(2010)



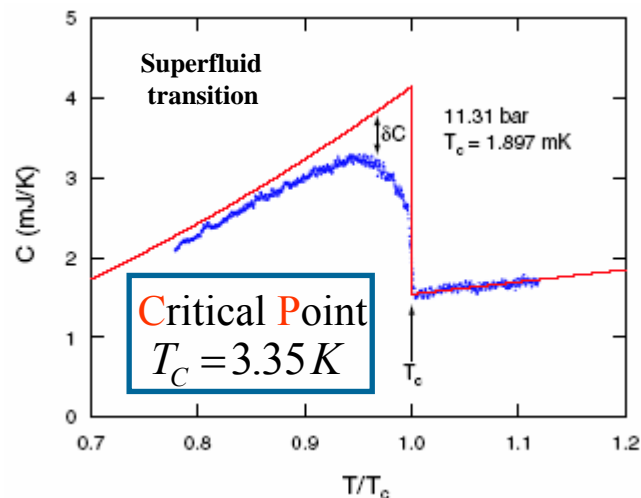
# Discontinuity of specific heat near a critical point

## Specific heat of liquid $^4\text{He}$



H.E. Stanley, 1971

## Heat capacity of liquid $^3\text{He}$



H. Choi et al., PRL 96, 125301 (2006)

- Near a critical point the singular part of thermo-dynamic potentials is a Generalized Homogeneous Function (GHF).
- The Gibbs potential  $G(\lambda^{a_\varepsilon} \varepsilon, \lambda^{a_p} p) = \lambda G(\varepsilon, p)$  is GHF of  $(\varepsilon, p)$ .

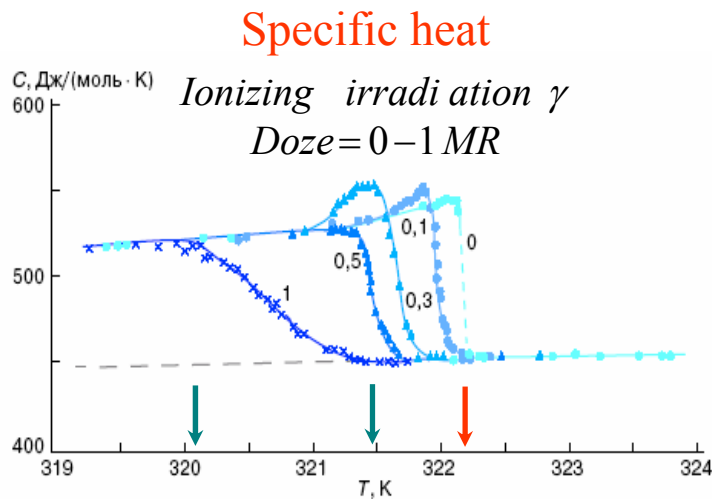
$$c_V \sim |\varepsilon|^{-\alpha} \quad \varepsilon \equiv (T - T_c) / T_c \quad c_V = -T(\partial^2 G / \partial T^2)_V$$

Critical exponents define the behavior of thermodynamical quantities close to the **Critical Point**

# Defects influence upon phase transition

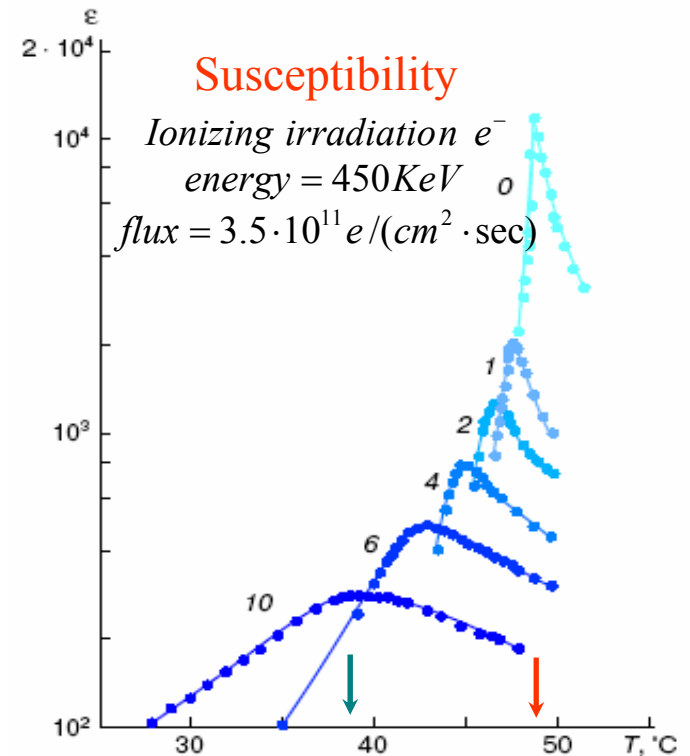
## Defects smear phase transitions

Ferroelectric crystal  
 $(CH_2NH_2COOH)_3 \cdot H_2SO_4$



**Critical Point**  
 $T_C = 49.2^0 C$

*Ferroelectric crystals*  
 $BaTiO_3$   
 $KNaC_4H_4O_6 \cdot 4H_2O$   
 $(CH_2NH_2COOH)_3 \cdot H_2SO_4$



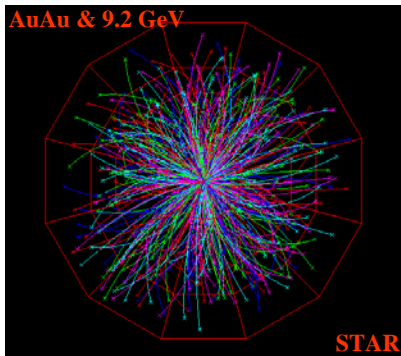
- Modification of crystal properties due to directed implantation of impurities or ionizing irradiation
- Anomalies of the properties in the region of the phase transitions

B.A.Strukov, Phase transitions,...(1996)





# Energy scan of spectra in AuAu collisions



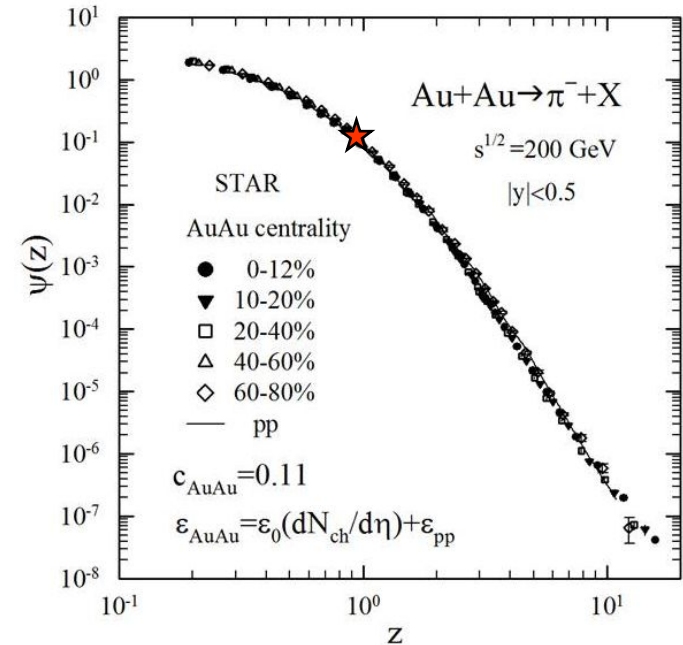
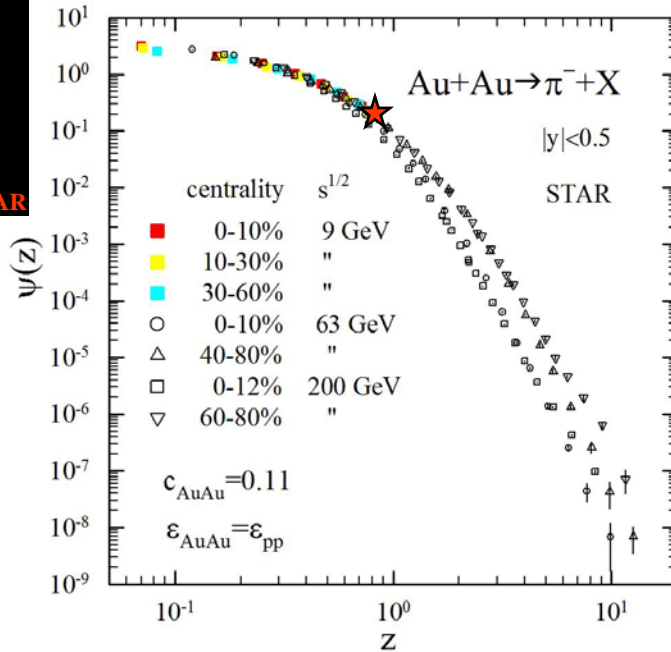
STAR

PLB 637 (2006) 161  
PRL 97 (2006) 152301  
PLB 655 (2007) 104

STAR

PRC 81 (2010) 024911

$\pi^-$  in AuAu at 9.2 & 63, 200 GeV



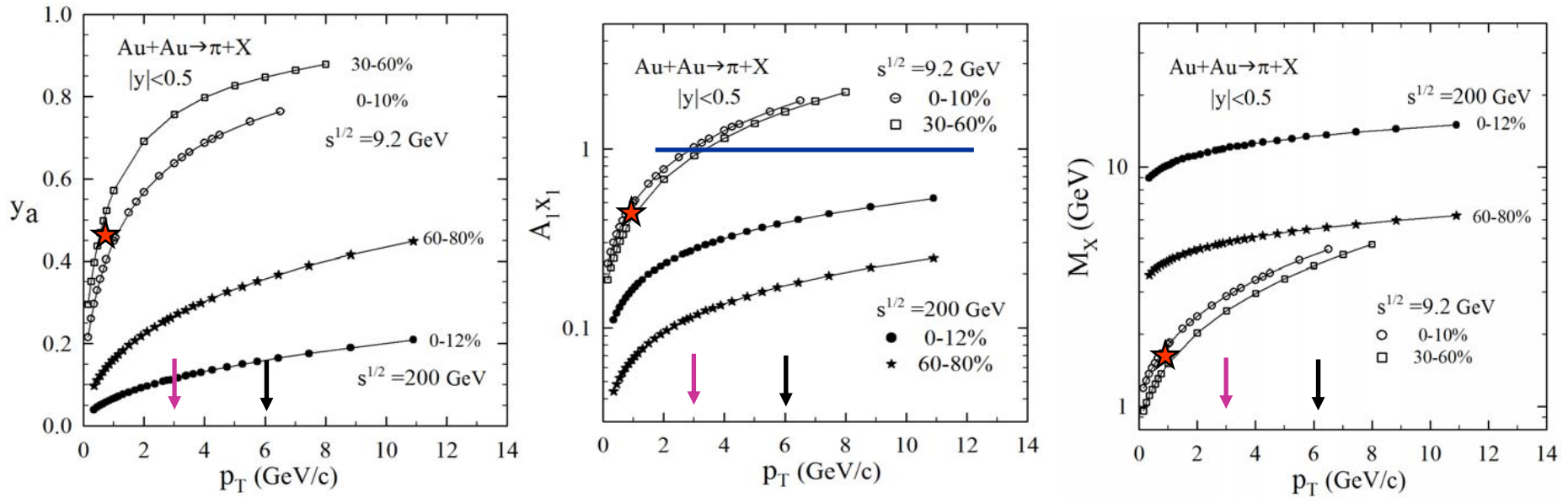
$$z = \frac{s_{\perp}^{1/2}}{(dN_{\text{ch}}/d\eta|_0)^c} \Omega^{-1}$$

- Saturation of  $\Psi(z)$  for  $z < 0.1$
- Power law for  $z > 4$
- Centrality dependence of  $\Psi(z)$  at high  $z$
- Fractal dimension  $\epsilon_{\text{AA}}$  depends on centrality



# Energy loss vs. energy, centrality, $p_T$

## $\pi^-$ in AuAu at 9.2 & 200 GeV



- $y_a$  increases with  $p_T \Rightarrow$  energy losses decreases with  $p_T$
- $y_a$  decreases with centrality  $\Rightarrow$  energy losses increase with centrality
- $x_1$  is independent of centrality at 9.2 GeV
- $M_X$  increases with  $p_T$ ,  $s^{1/2}$  and centrality

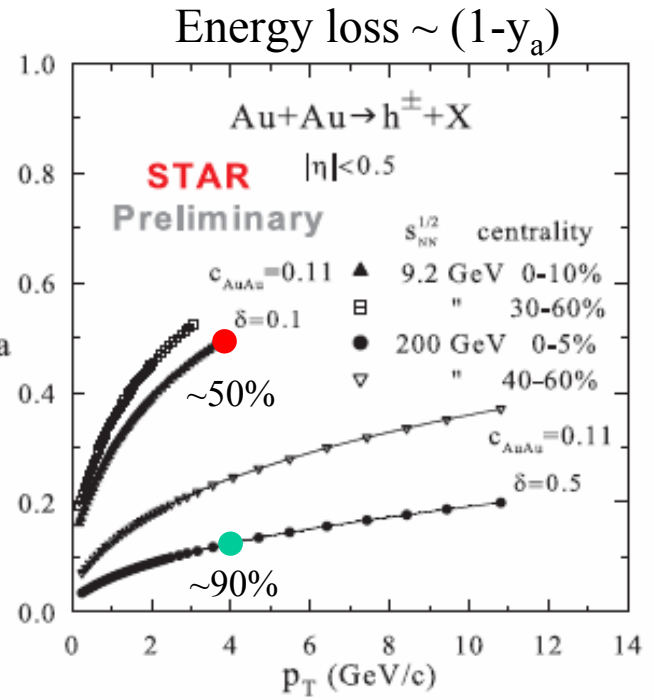
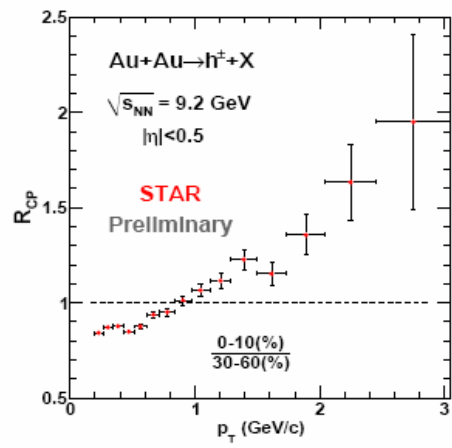
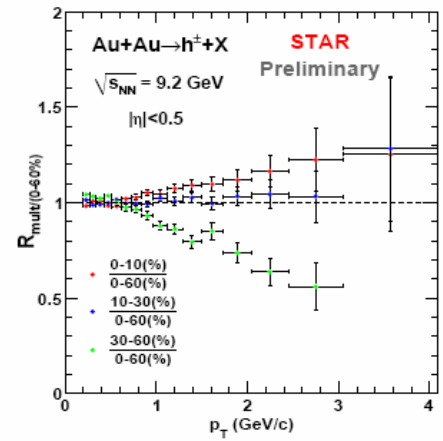
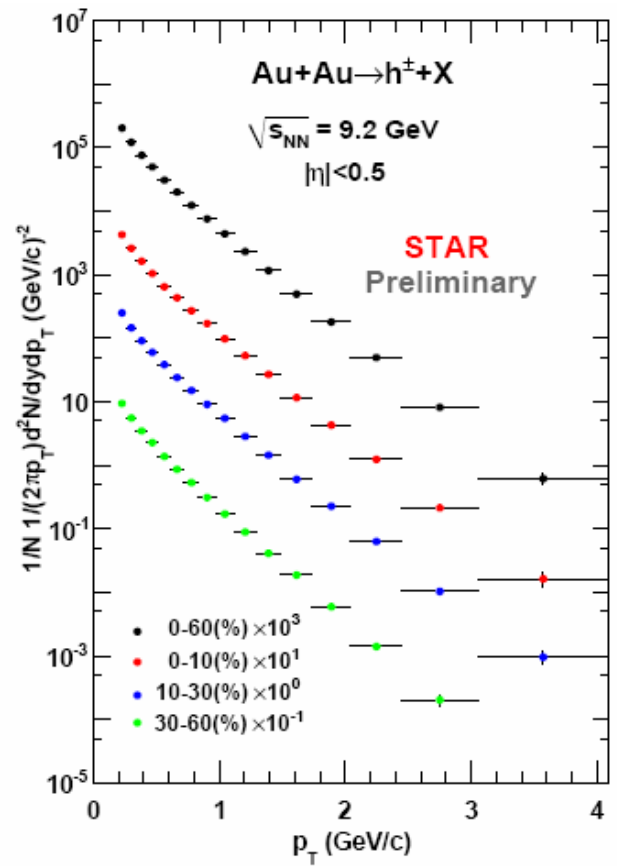
Smaller energy losses  $\Rightarrow$  better localization of a **Critical Point**  
 Cumulative region ( $A_1 x_1 > 1$ ) is most preferable to search for a **Critical Point**





# High- $p_T$ Spectra of Charged Hadrons in Au+Au Collisions at $\sqrt{s_{NN}} = 9.2$ GeV in STAR

STAR nucl-ex/1004.5582



Data sample (2008)

~ 4000 events

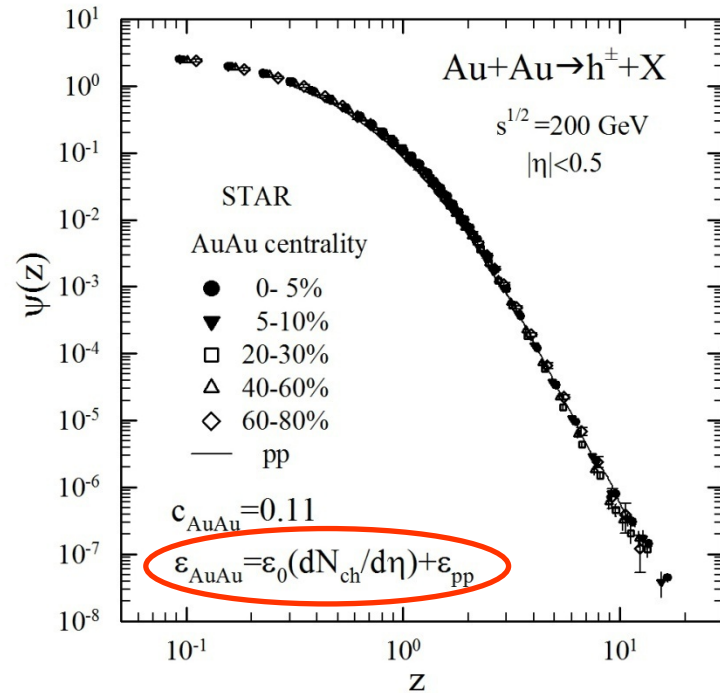
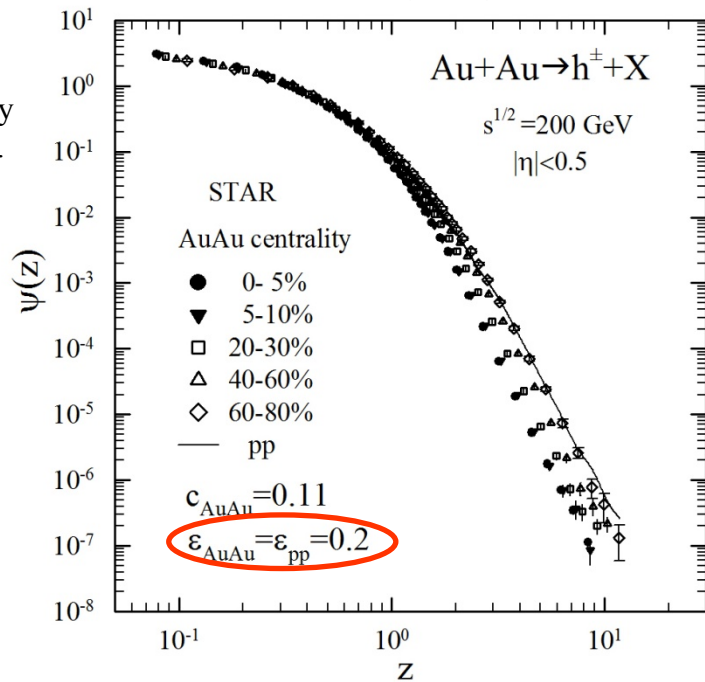
- High- $p_T$  spectra vs. centrality
- $R_{CP}$  ratio vs.  $p_T$
- Energy loss vs.  $p_T$ ,  $dN/d\eta$



# Multiplicity dependence of fragmentation dimension $\epsilon_{AA}$

## Charged hadrons in central AuAu collisions at 200 GeV

STAR: PRL 91 (2003) 172302



Suppression of  $\Psi(z)$   
in central AuAu collisions  
for  $\epsilon_{AuAu} = \epsilon_{pp}$

- The same  $\Psi(z)$  in pp & AuAu for all centralities
- Dimension  $\epsilon_{AuAu}$  depends on multiplicity
- “Specific heat”  $c_{AuAu} = 0.11$  for all centralities

Multiplicity dependence of fragmentation process in HIC



# Energy scan of spectra in AuAu collisions

## Charged hadrons in central AuAu collisions at 200, 130, 62.4, 9.2 GeV

STAR:

PRL 89 (2002) 202301

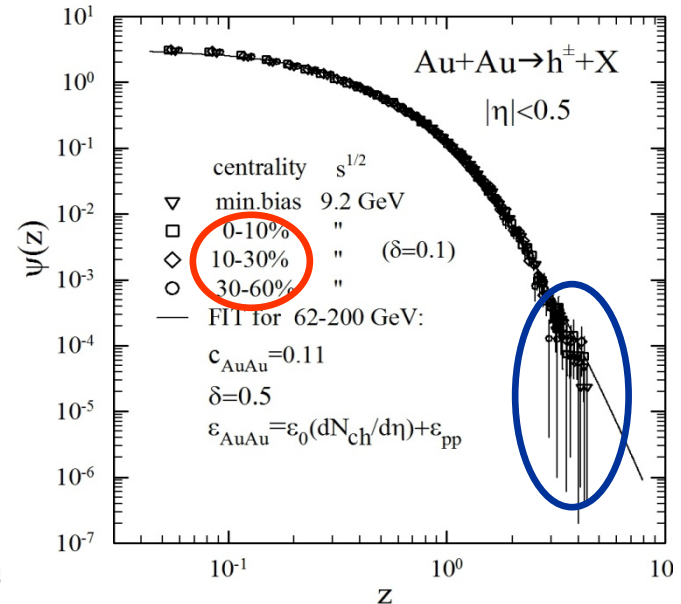
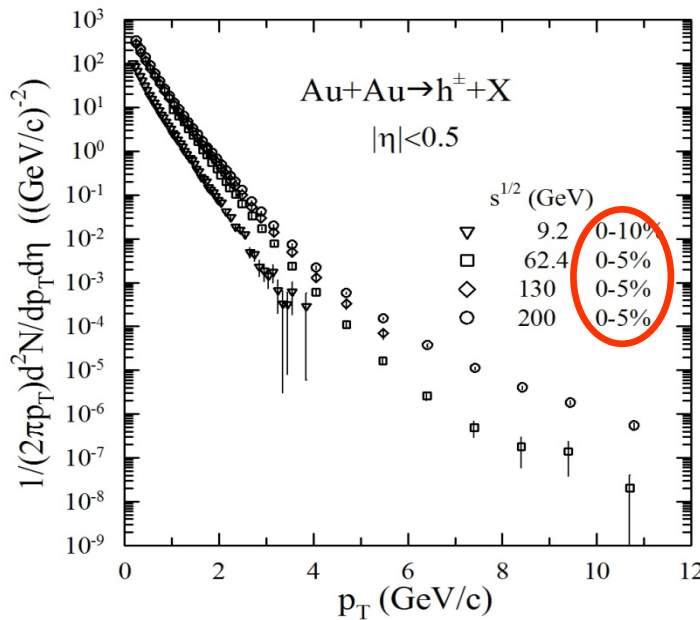
PRL 91 (2003) 172302

arXiv:1004.5582

$\pi$  at SPS & RHIC



MT & I.Zborovsky  
Phys.Part.Nucl.Lett.  
7(2010)171



- Energy scan of the spectra:  $s^{1/2} = 9 - 200$  GeV
- Centrality dependence of the spectra at high  $p_T$
- Power law for all centralities for  $p_T > 2$  GeV/c
- Fragmentation ( $\epsilon_{AA}$ ) depends on centrality

Change of the parameters  $c, \delta, \epsilon \Rightarrow$  indication on new properties of matter

Discontinuity of the parameters  $c, \delta, \epsilon \Rightarrow$  indication of existence of CP

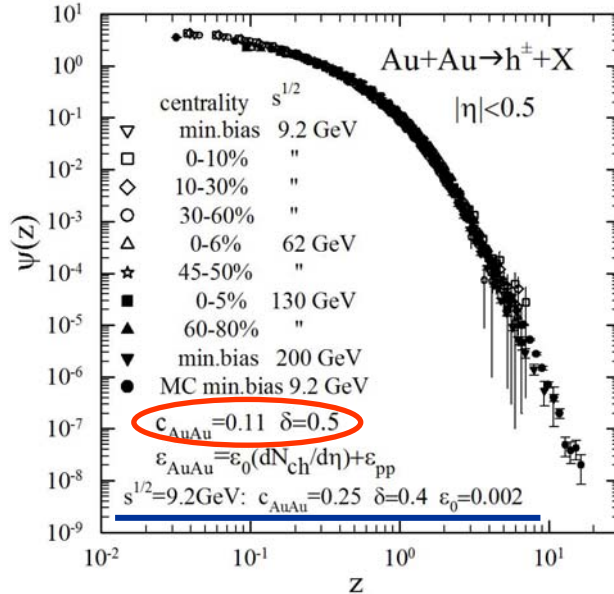




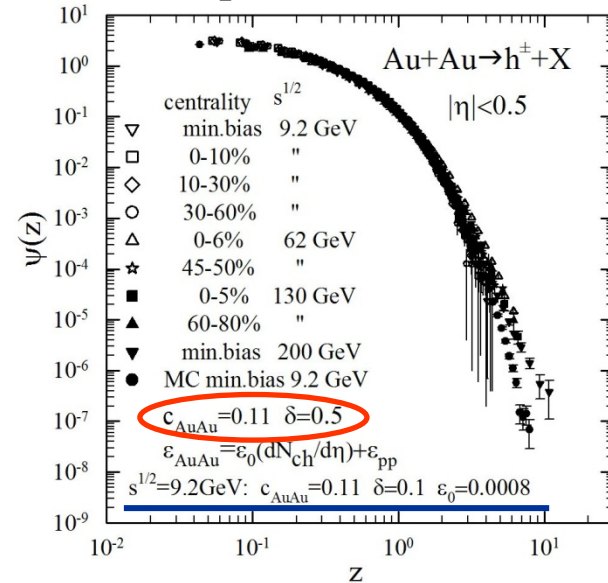
# Charged hadrons in central AuAu collisions

## Spectra in $z$ presentation - Different Scenarios

Large specific heat & large  $\delta$



Small specific heat & small  $\delta$



$$z = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N} \cdot \Omega^{-1}$$

$$\Omega = (1-x_1)^{\delta_1} (1-x_2)^{\delta_2} (1-y_a)^{\epsilon_a} (1-y_b)^{\epsilon_b}$$

- The same  $\Psi(z)$  for all centralities & energy (universality)  
 $\epsilon_{AuAu}$  depends on multiplicity density
- Scenarios of interaction: large vs. small “specific heat”
- Correlation of  $c$ ,  $\epsilon$ ,  $\delta$
- Centrality dependence of the spectra constraints  $c_{AuAu}$
- Different scenarios in high- $z$  range ( $p_T > 6$  GeV/c)



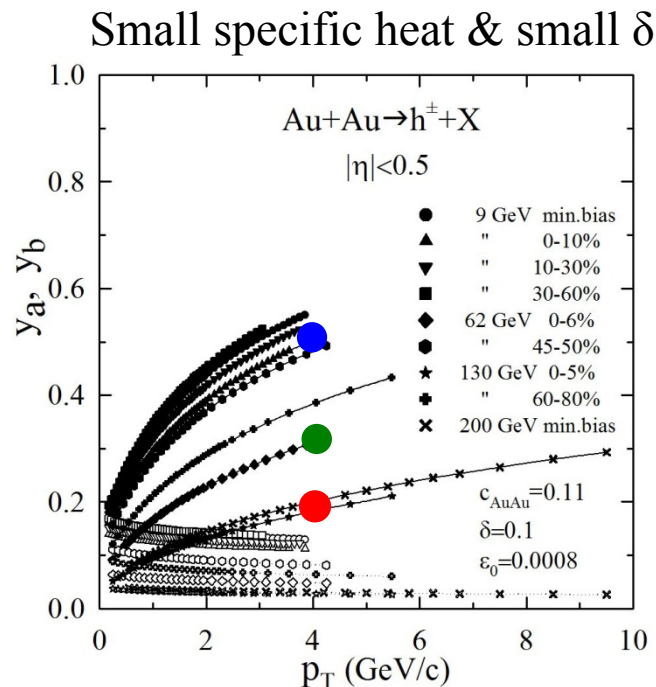
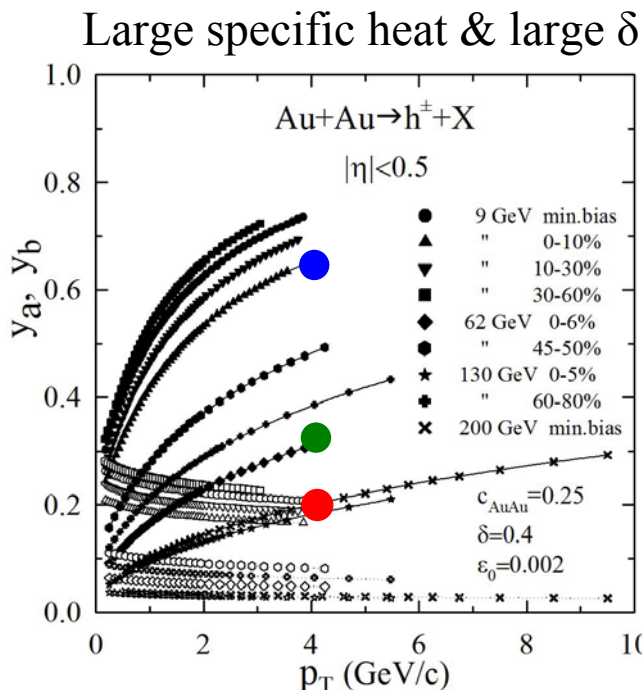
# Energy loss in AuAu collisions

## Momentum fractions $y_a, y_b$ in different scenarios

35%  
energy loss  
 $q \approx 6$  GeV

70%  
energy loss  
 $q \approx 13$  GeV

82%  
energy loss  
 $q \approx 22$  GeV



50%  
energy loss  
 $q = 8$  GeV

70%  
energy loss  
 $q \approx 13$  GeV

82%  
energy loss  
 $q \approx 22$  GeV

- $y_a$  increases with  $p_T \Rightarrow$  energy losses decrease with  $p_T$
- $y_a$  decreases with  $s^{1/2} \Rightarrow$  energy losses increase with  $s^{1/2}$
- $y_a$  decreases as centrality increases  $\Rightarrow$  energy losses increase with centrality
- $y_b$  is flat with  $p_T \Rightarrow$  weak dependence of  $M_X$  on  $p_T$
- $y_b \ll y_a$  for  $p_T > 1$  GeV/c  $\Rightarrow$  soft (high multiplicity) recoil  $M_X$

Energy losses ( $c=0.25, \delta=0.4$ ) < energy losses ( $c=0.11, \delta=0.1$ )  
 Smaller energy losses  $\Rightarrow$  better localization of a Critical Point....

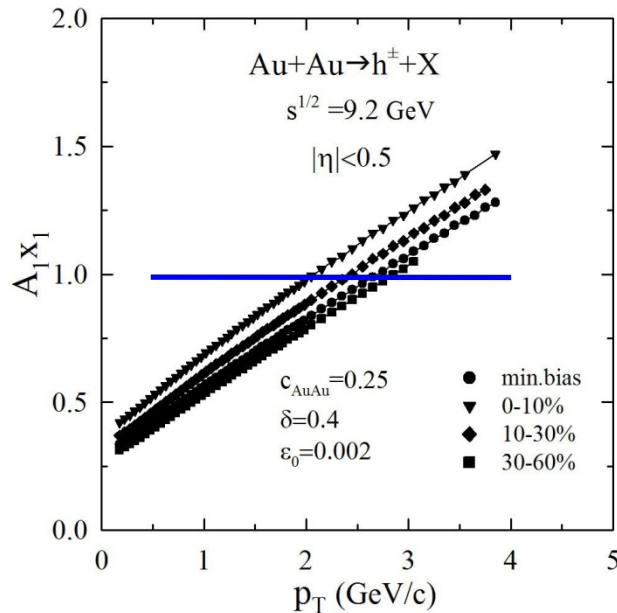




# Momentum fraction $x_1 A_1$ in AuAu collisions

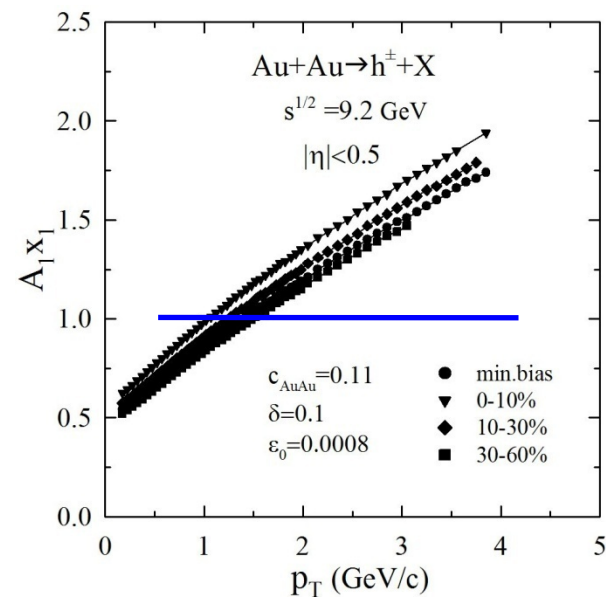
## Momentum fraction $x_1 A_1$ in different scenarios

Large specific heat & large  $\delta$



- Cumulative region at  $p_T > 2$  GeV/c
- Smaller energy loss
- Not smeared sub-structure

Small specific heat & small  $\delta$



- Cumulative region at  $p_T > 1$  GeV/c
- Larger energy loss
- Smeared sub-structure

Smaller energy losses  $\Rightarrow$  better localization of a **Critical Point**

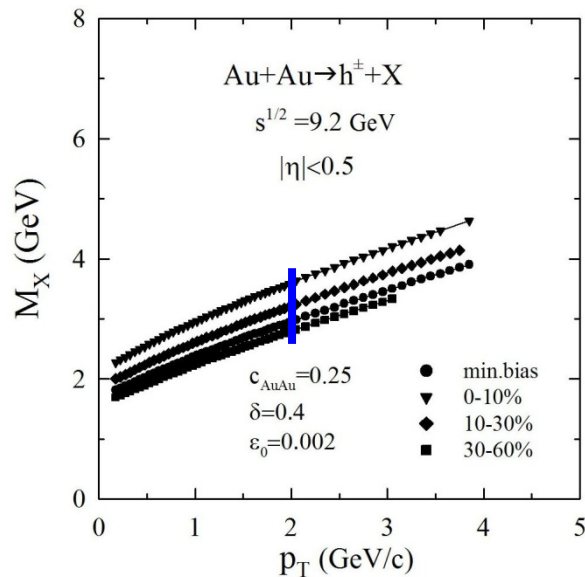
Cumulative region ( $x_1 A_1 > 1$ ) is most preferable to search for a **Critical Point**



# Recoil mass $M_X$

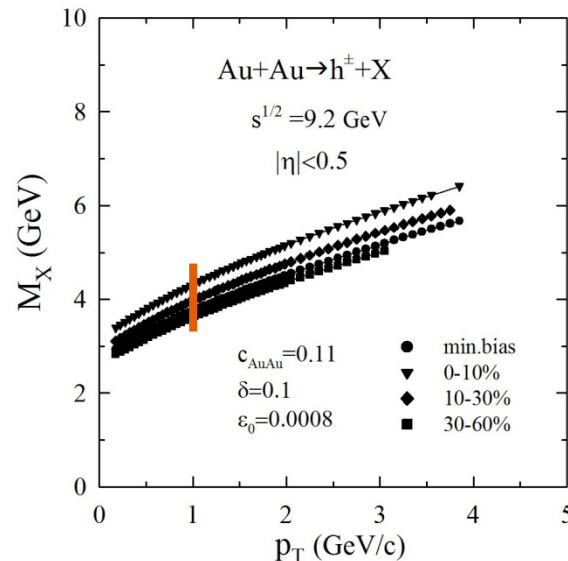
Recoil mass in different scenarios  $M_X = x_1 M_1 + x_2 M_2 + m/y_b$

Large specific heat & large  $\delta$



- Cumulative region at  $p_T > 2$  GeV/c
- Smaller energy loss
- Not smeared sub-structure
- Smaller multiplicity in the way-side

Small specific heat & small  $\delta$



- Cumulative region at  $p_T > 1$  GeV/c
- Larger energy loss
- Smeared sub-structure
- Larger multiplicity in the way-side

$M_X$  increases with  $p_T$ ,  $s^{1/2}$ , centrality due to decrease of the fraction  $y_b$

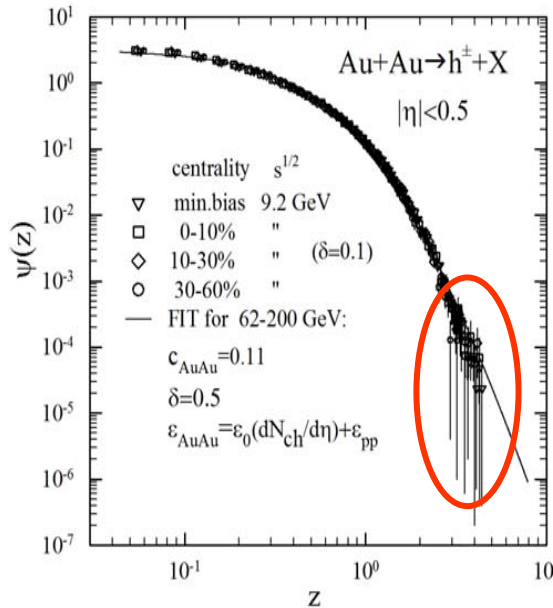


# Self-similarity restoration & Search for location of CP

## Self-similarity parameter $z$

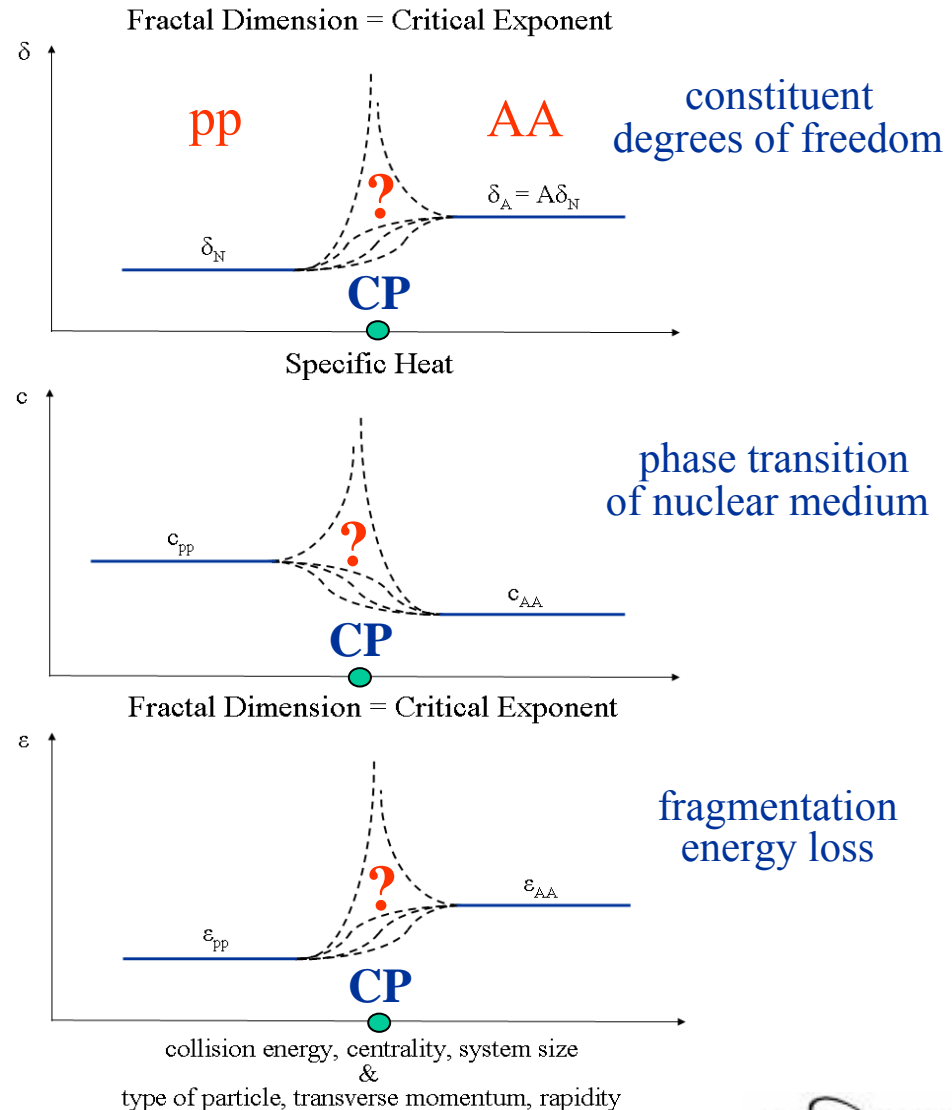
$$z = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N} \cdot \Omega^{-1}$$

$$\Omega = (1-x_1)^{\delta_1} (1-x_2)^{\delta_2} (1-y_a)^{\varepsilon_a} (1-y_b)^{\varepsilon_b}$$



Correlation of  $\delta, \varepsilon, c$   
in cumulative region

Location of CP



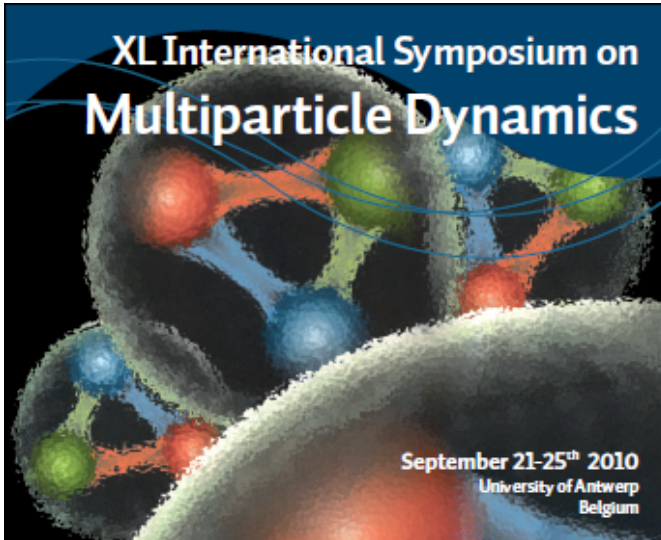
# Conclusions

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- Results of analysis of energy scanned spectra of charged hadrons produced in **AuAu** collisions at  $s^{1/2} = 200, 130, 62.4, 9.2$  GeV in the **z**-scaling approach were presented.
- We argue that **z**-scaling reflects the self-similarity, locality, and fractality of hadron interactions at a constituent level.
- Microscopic scenarios of hadron production were suggested.
- The constituent energy loss in **AuAu** collisions in terms of the momentum fractions were estimated. Its dependence on collision energy, centrality, and momentum of produced hadron was studied.
- Discontinuity of **c,  $\delta$ ,  $\epsilon$**  as a signature of phase transition was suggested.

The obtained results may be of interest in searching for a **Critical Point** and signatures of phase transition in hadron matter at **SPS, RHIC, Tevatron**, and **LHC** in present, and at **FAIR (GSI) & NICA (JINR)** in future.





**XL International Symposium on Multiparticle Dynamics**

September 21-25<sup>th</sup> 2010  
University of Antwerp  
Belgium

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- Soft Interactions
- Multiparticle correlations
- High pT interactions
- Forward Physics and Cosmic Rays
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- Techniques in Experiment and Theory
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**ABSTRACT SUBMISSION DEADLINE** - June 30<sup>th</sup> 2010

**INFORMATION AND REGISTRATION**  
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*Thank You For Attention !*



M. Tokarev (*JINR, Dubna*) & I. Zborovský (*NPI, Řež*)

## Charged hadrons in pp collisions at low $p_T$

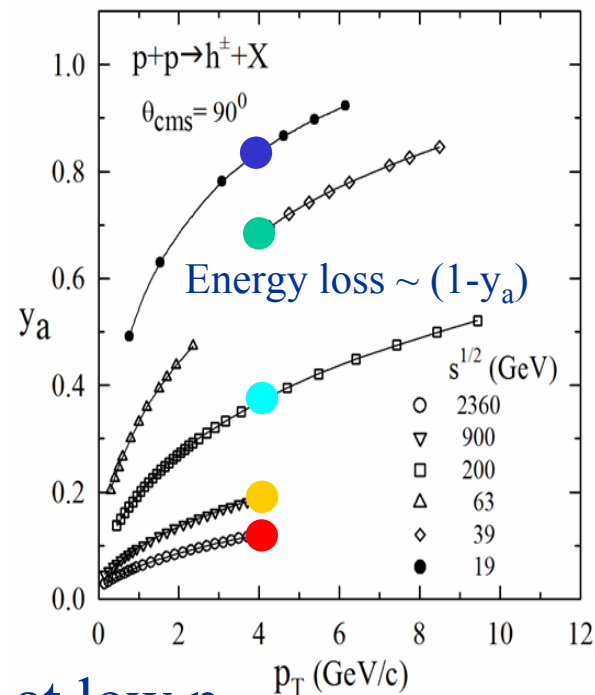
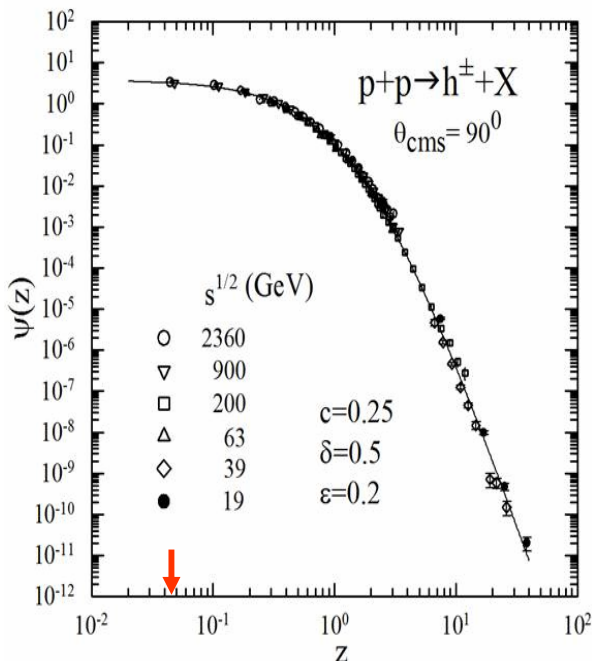
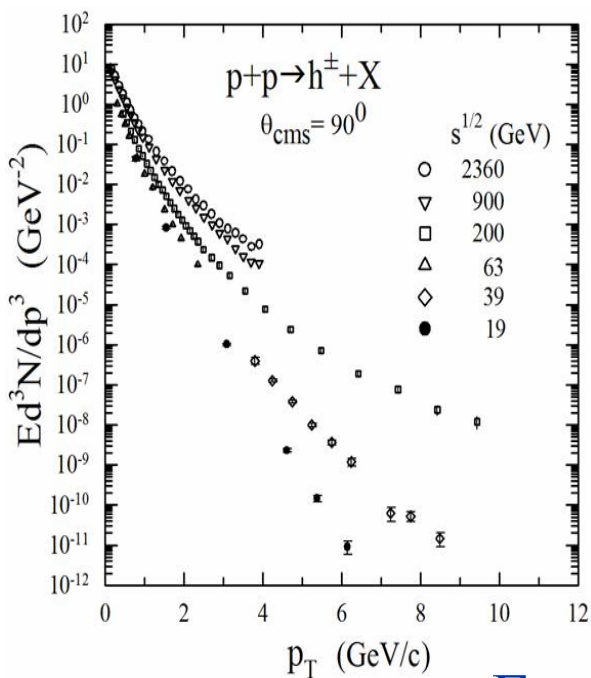
LHC: CMS Coll.  
JHEP 02 (2010) 041

RHIC: STAR Coll.  
PRL 91 (2003) 172302

ISR: BS Coll.  
NPB 100 (2007) 237

FNAL (fixed target)  
PRD 19 (1979) 764  
PRD 40 (1989) 2777

M.T. & I.Zborovský  
J.Phys.G: Nucl.Part.Phys.  
37,085008(2010)



Energy independence of  $\Psi(z)$  at low  $p_T$

Saturation of  $\Psi(z)$  at low  $z$  is confirmed at LHC