

# *Electro-optic Longitudinal Profile Diagnostics*

*current status & future directions*

**S P Jamison**

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## **Collaborators:**

**W.A. Gillespie** *University of Dundee*

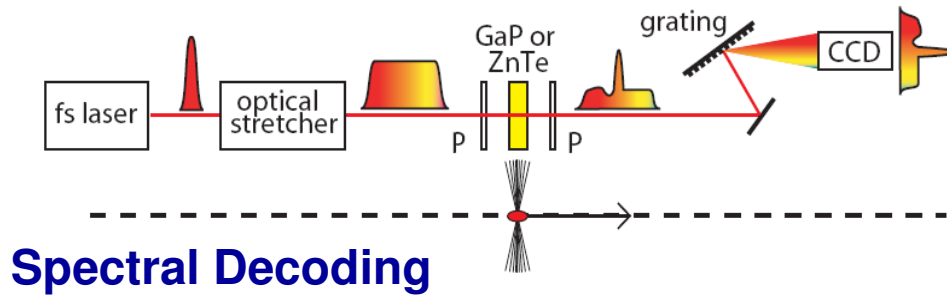
**A.M. MacLeod**, *University of Abertay Dundee*

**G. Berden, B. Redlich, A.F.G. van der Meer** (*FELIX*)

**B. Steffen, E.-A. Knabbe, H. Schlarb, B. Schmidt, P. Schmüser** (*DESY*)

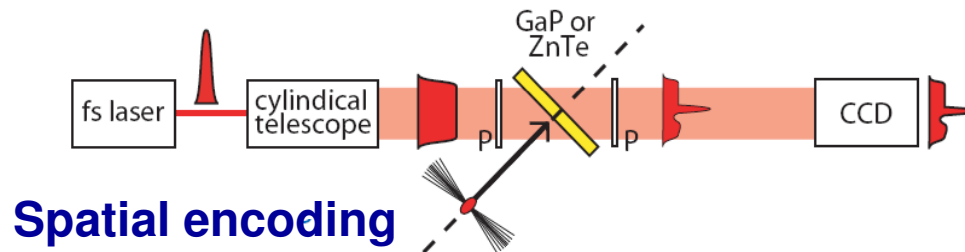
# Electro-optic techniques...

complexity

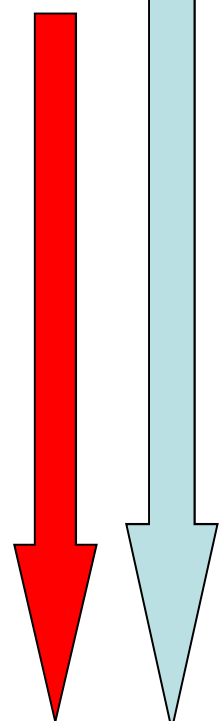
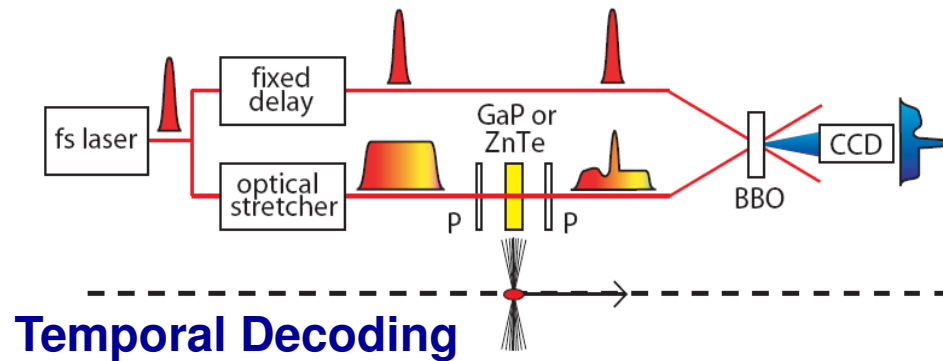


FELIX  
DESY  
BNL  
...

*demonstrated*  
time resolution



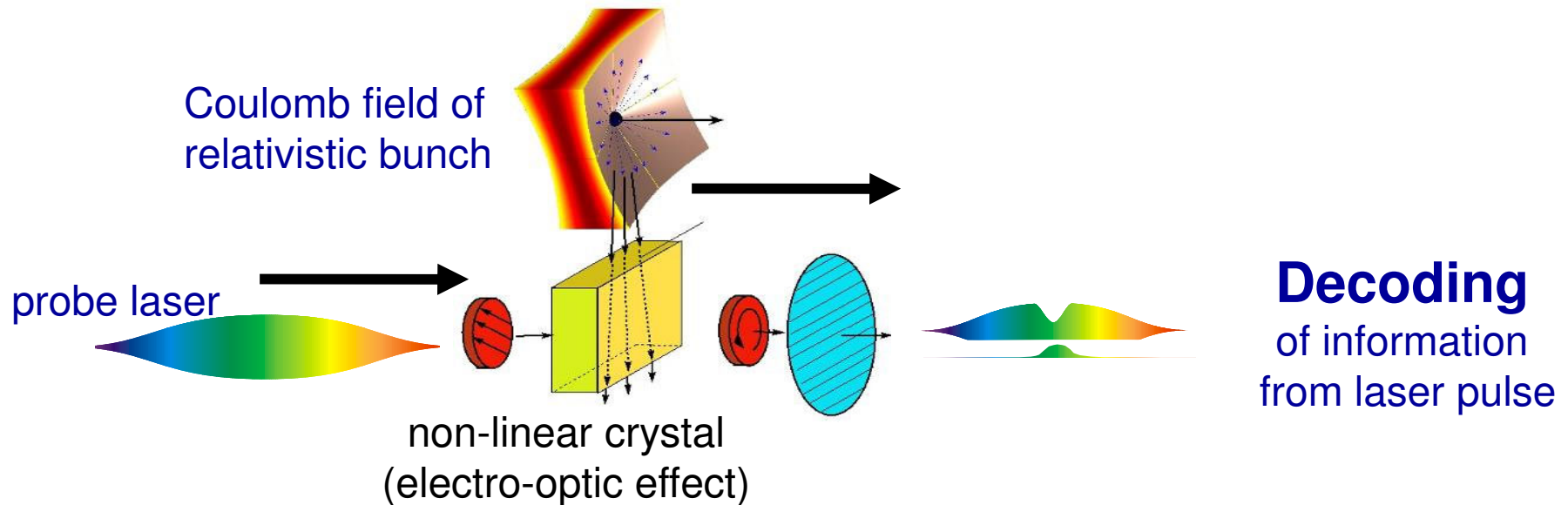
SLAC  
DESY



FELIX  
DESY  
RAL(CLF)  
MPQ  
Jena

# Concept of electro optic profile diagnostic

*all-optical intra-beamline pickup of bunch Coulomb field*



## Encoding

- same for all techniques
- limiting factor for high time resolution techniques

## Decoding

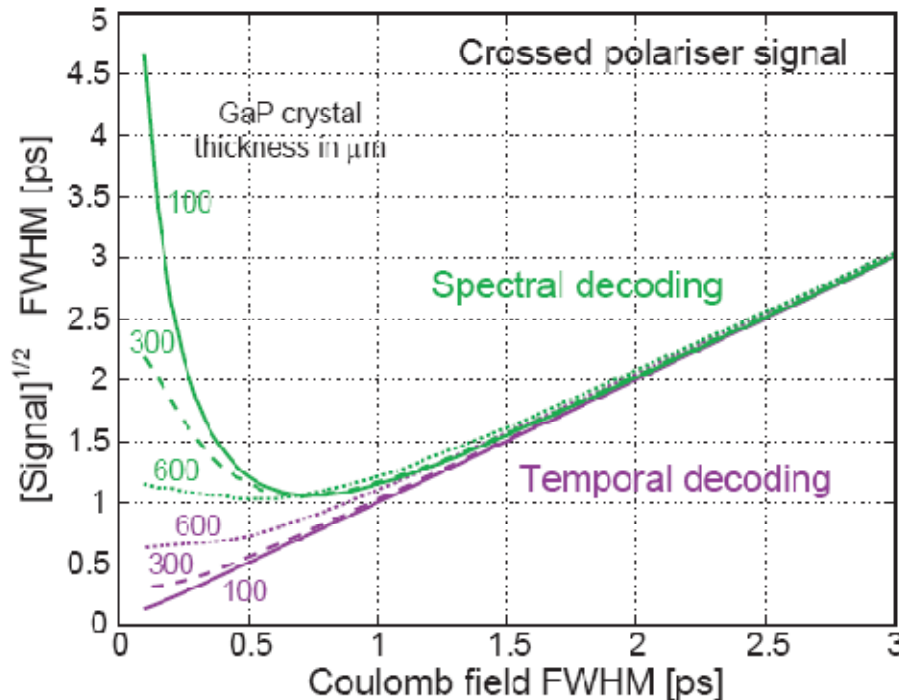
- choices for complexity
- limiting factor for spectral decoding

# Spectral decoding temporal resolution limits...

In general spectral decoding limited by chirp  $\tau_{\text{lim}} = \sqrt{12\pi\beta}$

For specific laser profiles, can relate to FWHM durations...

$$\tau_{\text{lim}} = 2.61\sqrt{T_0T_c} \quad ; \text{ for a Gaussian pulse}$$



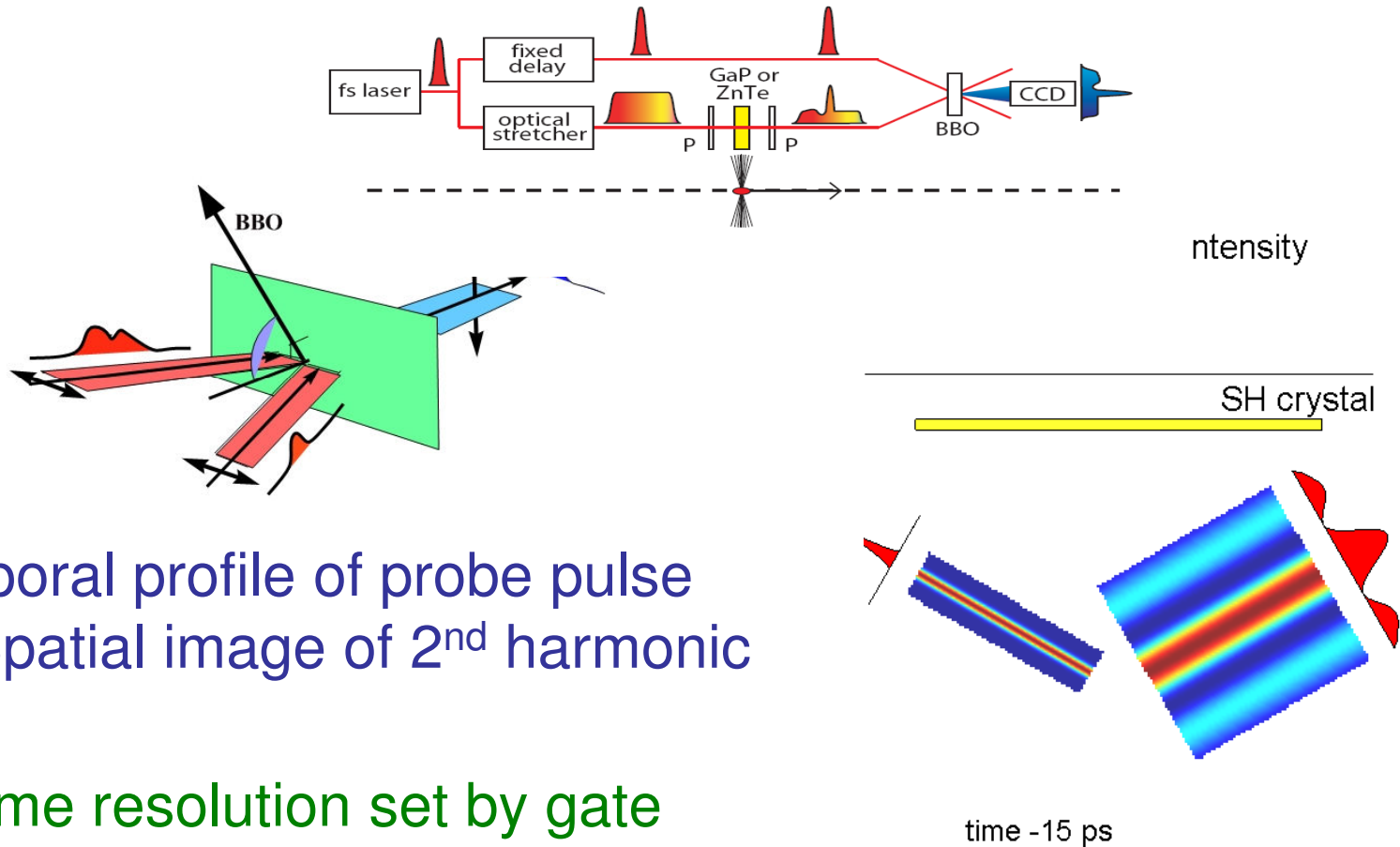
Unlikely to get better than 1.0 ps (FWHM) with spectral decoding

However, still attractive as simplest technique.

Routinely used for finding signal for higher time resolution techniques

# Temporal decoding...

temporal-spatial mapping in 2<sup>nd</sup> Harmonic Generation

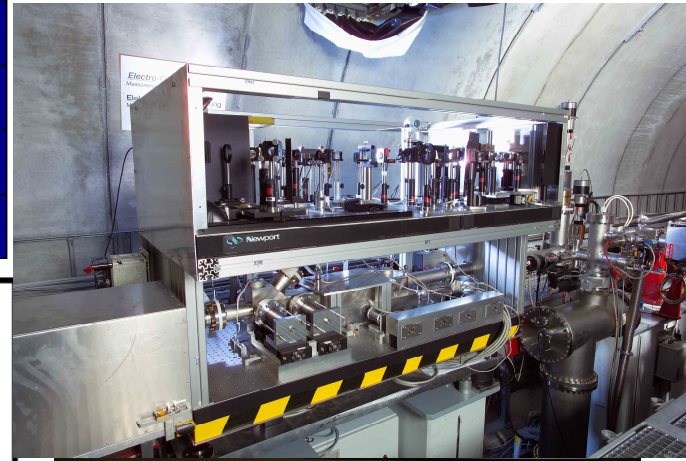
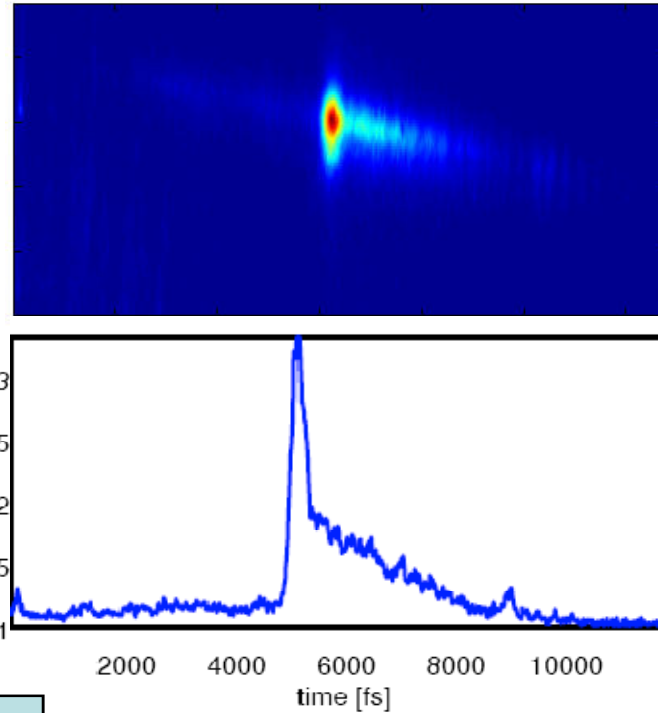
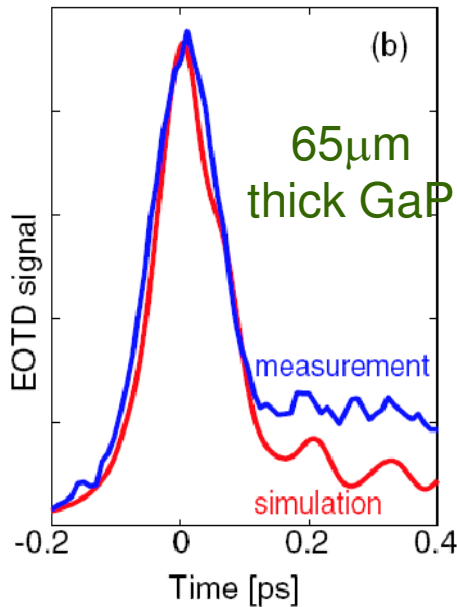


Temporal profile of probe pulse  
⇒ Spatial image of 2<sup>nd</sup> harmonic

Time resolution set by gate  
pulse duration (typically <50fs)

# High Time Resolution...

currently the highest time-resolution  
non-destructive diagnostic demonstrated



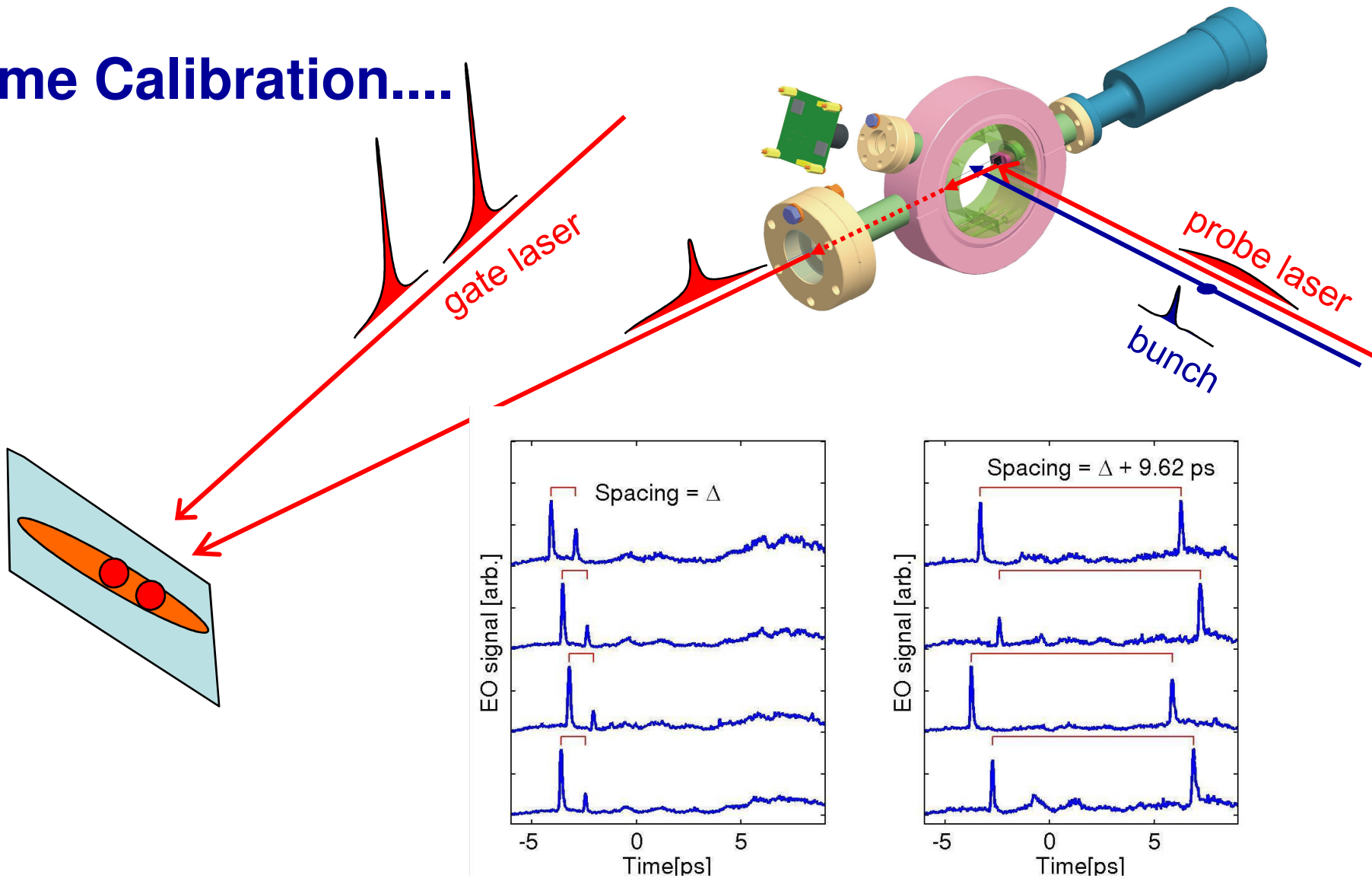
“Time resolution”

$$\sigma_z \sim 90\text{fs (rms)}$$

$$\sigma_z^{\text{actual}} \sim 30\text{fs} \Rightarrow \sigma_z^{\text{measured}} \sim 55\text{fs}$$

$$\sigma_z^{\text{actual}} \sim 90\text{fs} \Rightarrow \sigma_z^{\text{measured}} \sim 90\text{fs}$$

# Time Calibration....

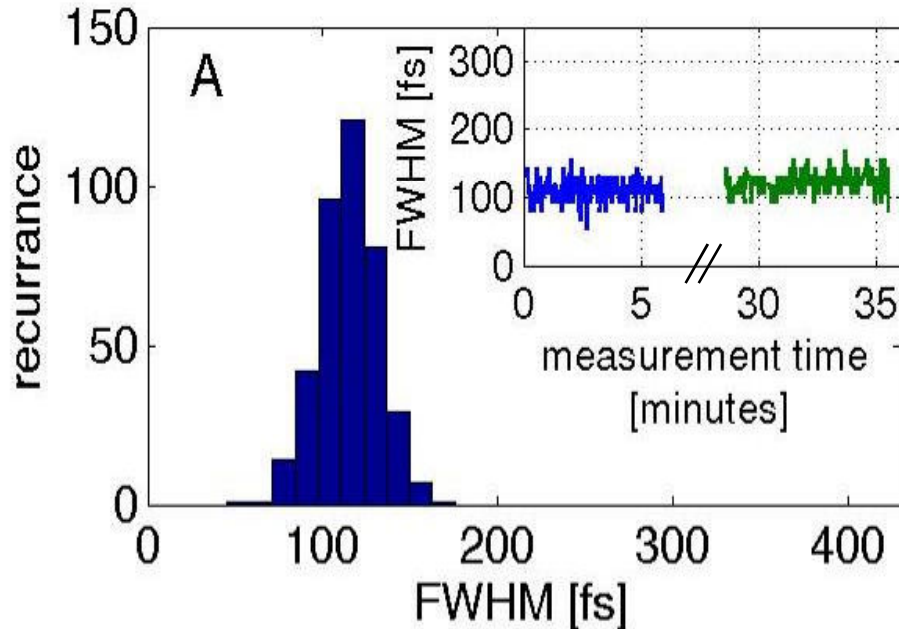


***Concept could be used for checking CLIC/CTF3 bunch stacking?***

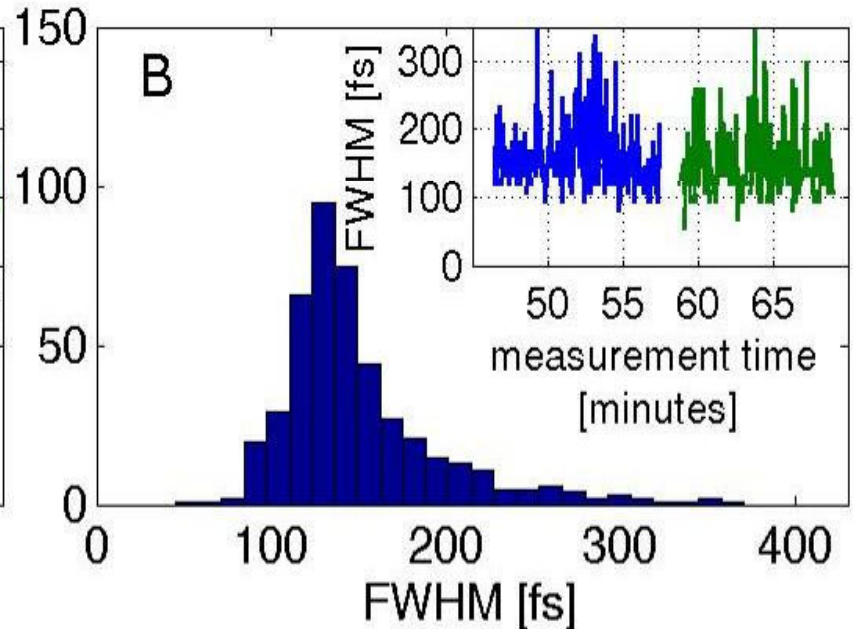
# EO confirmation of CDR feedback systems

single shot capability reveals stabilising effect of slow feedback

CDR feedback on



CDR feedback off

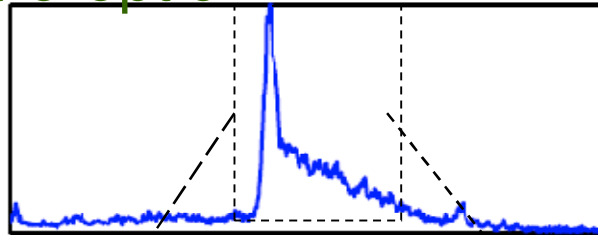
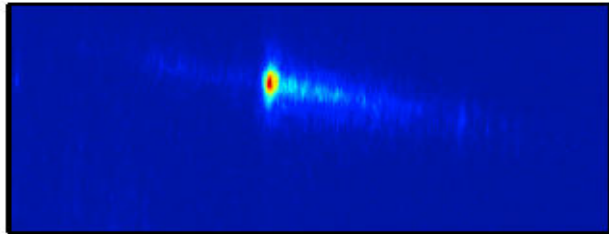




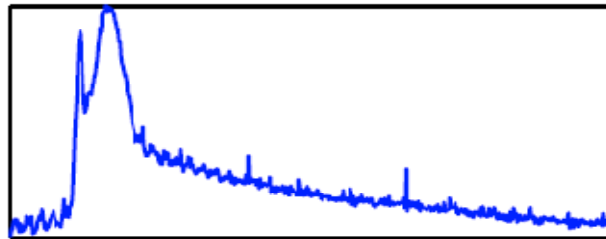
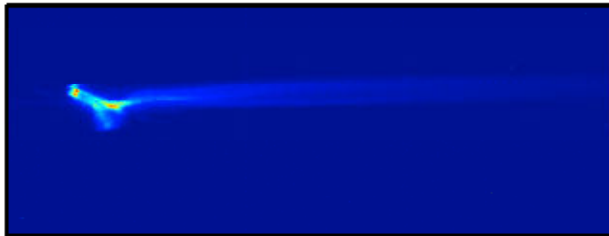
# Benchmarking of EO diagnostics

## comparison with transverse deflecting cavity

Electro-optic

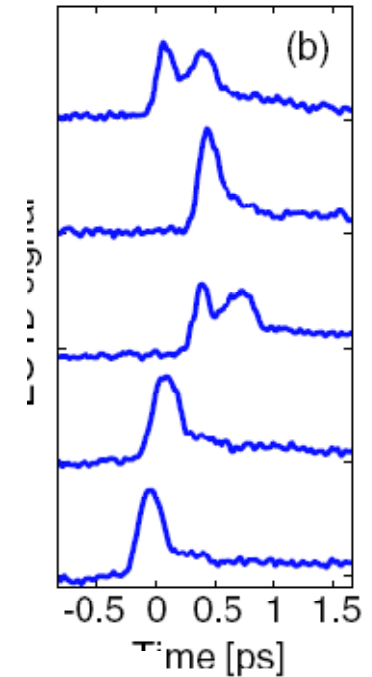


Transverse Deflecting Cavity



500 1000 1500 2000 2500 3000 3500 4000  
time [fs]

*shot-shot variations*



PRL **99**, 164801 (2007)

PHYSICAL REVIEW LETTERS

week ending  
19 OCTOBER 2007

### Benchmarking of Electro-Optic Monitors for Femtosecond Electron Bunches

G. Berden,<sup>1</sup> W. A. Gillespie,<sup>2</sup> S. P. Jamison,<sup>3</sup> E.-A. Knabbe,<sup>4</sup> A. M. MacLeod,<sup>5</sup> A. F. G. van der Meer,<sup>1</sup> P. J. Phillips,<sup>2</sup>  
H. Schlarb,<sup>4</sup> B. Schmidt,<sup>4</sup> P. Schmüser,<sup>4</sup> and B. Steffen<sup>4</sup>

*plus Phys. Rev. ST, 2009*

# So are all problems solved...?

## *Low time resolution (>1ps structure)*

- *spectral decoding offers explicit temporal characterisation*
- *relatively robust laser systems available*
- *diagnostic rep rate only limited by optical cameras*

## *High time resolution (>60 fs rms structure)*

- *proven capability*
- *significant issues with laser complexity /robustness*

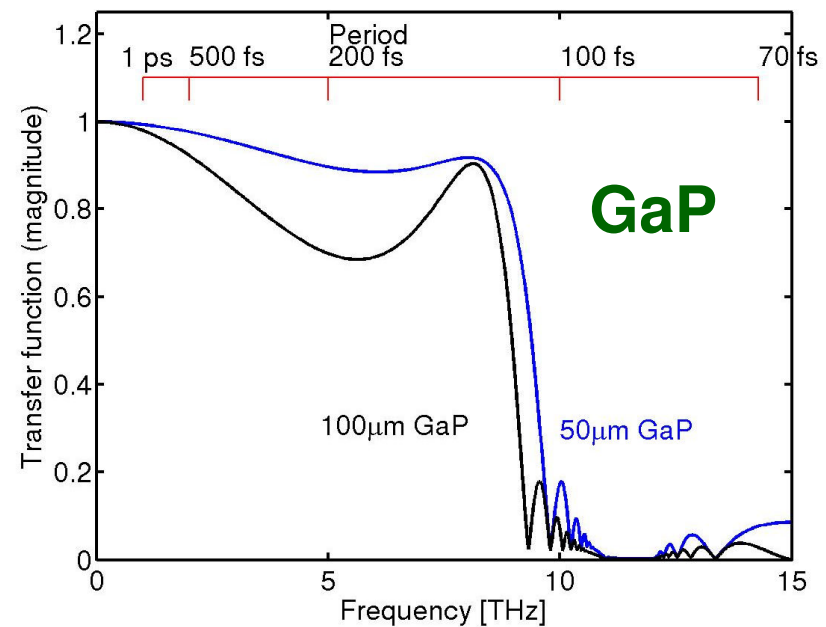
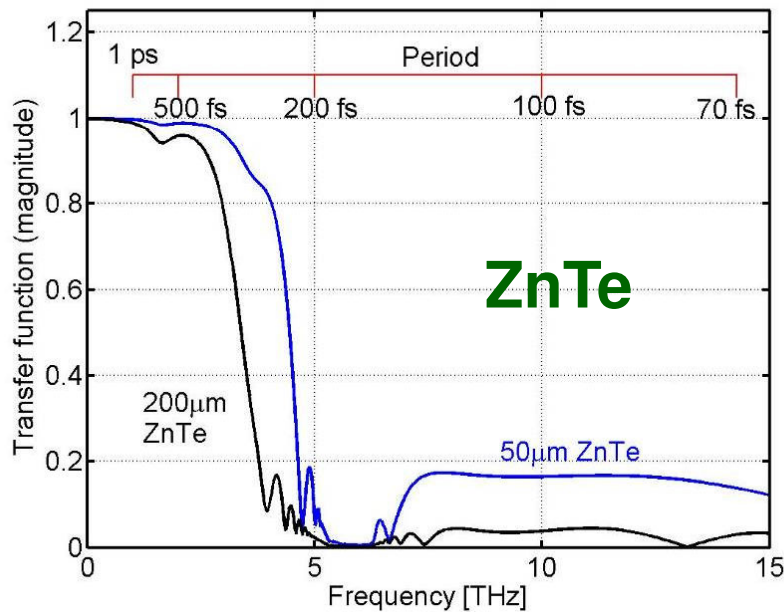
## *Very higher time resolution (<60 fs rms structure)*

- *limited by EO material properties (& laser)*

# Encoding Time Resolution...

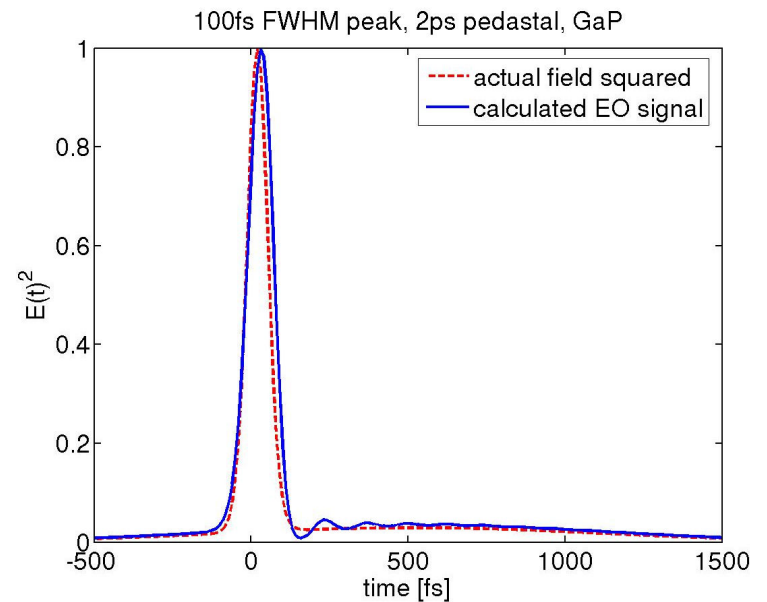
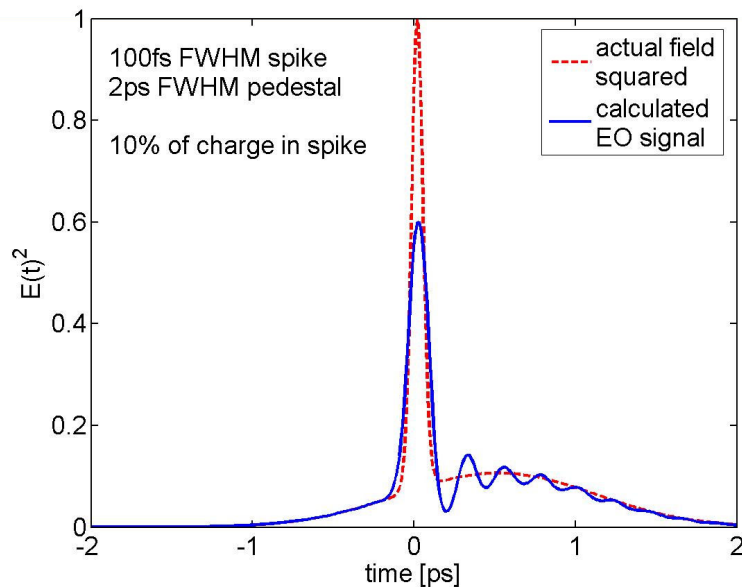
material response,  $R(\omega)$

- velocity mismatch of Coulomb field and probe laser
- frequency mixing efficiency,  $\chi^{(2)}(\omega)$



# Time resolution from frequency response

- Encoding “time resolution” not a RMS measure...
  - Better described as “temporal limitation”
- 
- *structure on longer time scale recorded faithfully*
  - *short time scale structure not observed, PLUS ringing artefacts*



# Can we achieve even better resolution ...?

## *Encoding*

Detector Material:

- GaP
- Move to new material? ( phase matching,  $\chi^{(2)}$  considerations )
- Could use GaSe, DAST, MBANP ..... or poled organic polymers?
- use multiple crystals, **and reconstruction process**

## *Decoding*

Gate pulse width  $\sim 50$  fs

- Introduce shorter pulse
- Use spectral interferometry
- Use FROG Measurement (initially attempted at FELIX, 2004)

## *or Alternative techniques: spectral upconversion*

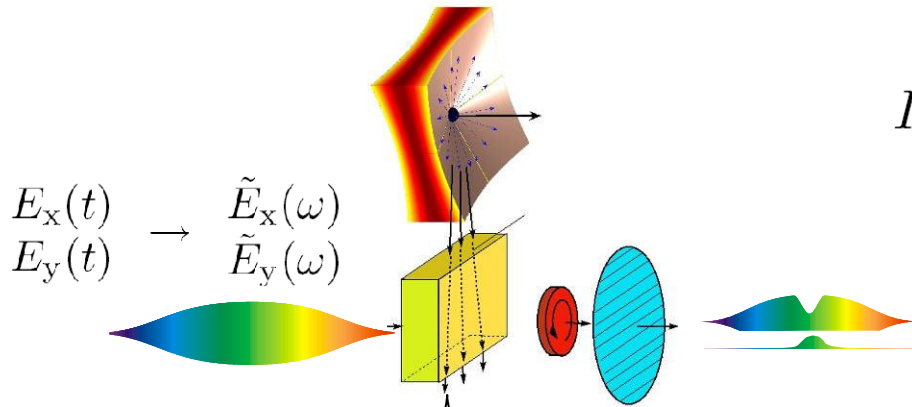
If drop requirement explicit time information at high frequencies,  
other options also become available

# Spectral upconversion diagnostic

Physics of EO encoding...

OR

- shifting Coulomb spectrum to optical region
- creating an optical “replica” of Coulomb field



$$I(t) \propto E_{\text{Coul}}(t)$$

$$[ \text{ or } \propto E_{\text{Coul}}^2(t) ]$$

$$\tilde{E}_{\text{out}}^{\text{opt}}(\omega) = \tilde{E}_{\text{in}}^{\text{opt}}(\omega) + i\omega a \tilde{E}_{\text{in}}^{\text{opt}}(\omega) * \left[ \tilde{E}^{\text{Coul}}(\omega) \tilde{R}(\omega) \right]$$

Coulomb spectrum shifted to optical region

$$E_{\text{out}}^{\text{opt}}(t) = E_{\text{in}}^{\text{opt}}(t) + a \left[ E^{\text{Coul}}(t) * R(t) \right] \frac{d}{dt} E_{\text{in}}^{\text{opt}}(t)$$

Coulomb pulse replicated in optical pulse



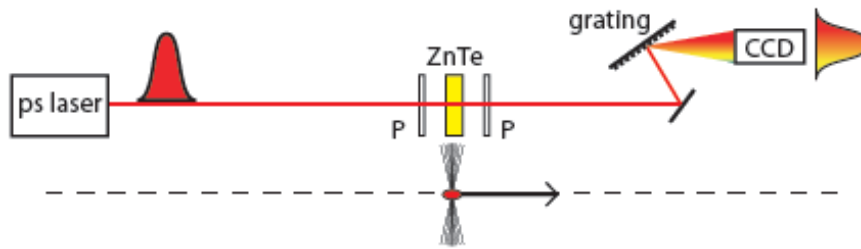
envelope



optical field

# Spectral upconversion diagnostic

Aim to measure the bunch Fourier spectrum...



- ... accepting loss of phase information & explicit temporal information
- ... gaining potential for determining information on even shorter structure
- ... gaining measurement simplicity

***use long pulse, narrow band, probe laser***

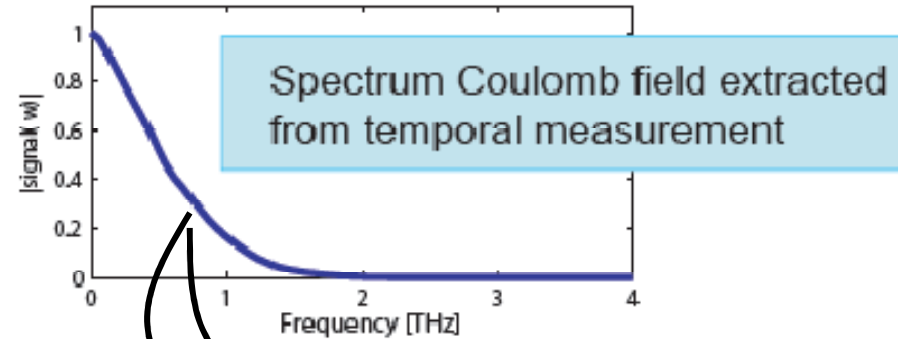
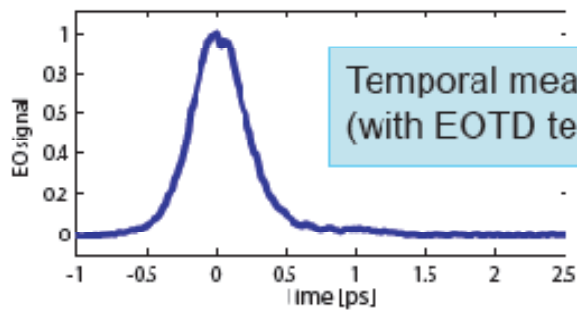
$$\tilde{E}_{\text{out}}^{\text{opt}}(\omega) = \underbrace{\tilde{E}_{\text{in}}^{\text{opt}}(\omega)}_{\rightarrow \delta\text{-function}} + i\omega a \underbrace{\tilde{E}_{\text{in}}^{\text{opt}}(\omega)}_{\rightarrow \delta\text{-function}} * \left[ \tilde{E}^{\text{Coul}}(\omega) \tilde{R}(\omega) \right]$$

- ***laser complexity reduced, reliability increased***
- ***laser transport becomes trivial (fibre)***
- ***problematic artifacts of spectral decoding become solution***

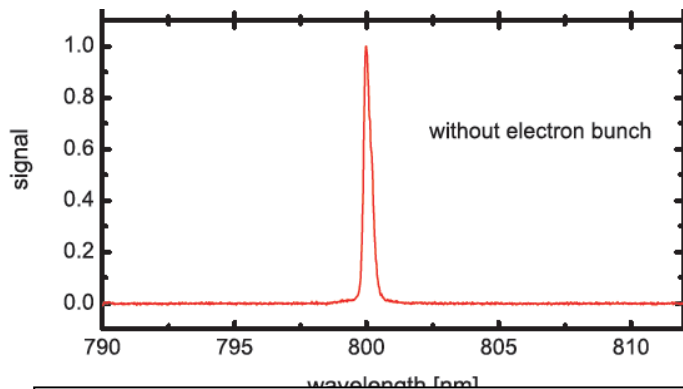
**NOTE: the long probe is still converted to optical replica**

# Spectral upconversion diagnostic

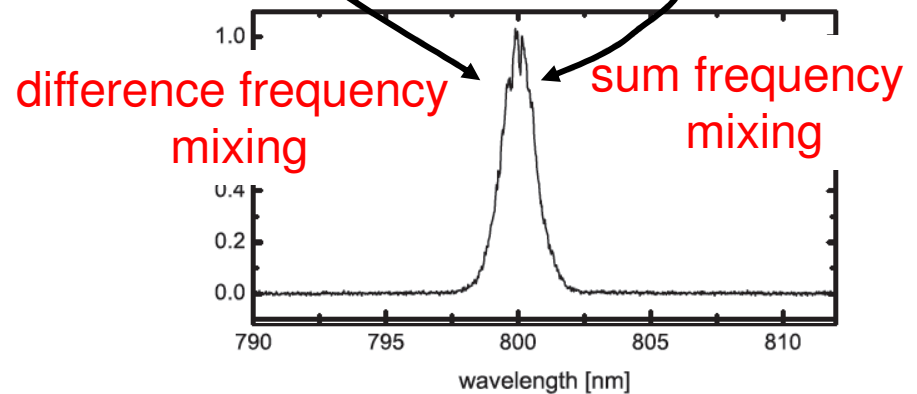
Results from experiments at FELIX (Feb 2009)



## spectral upconversion



Input narrow band optical probe

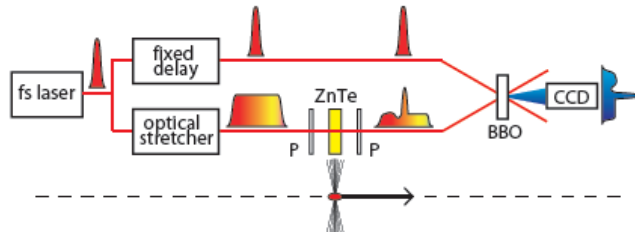
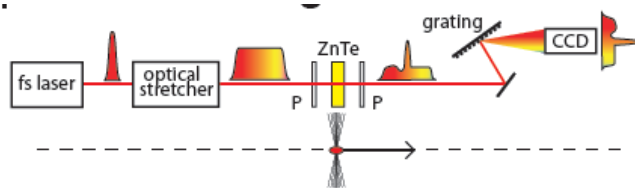


with electron interaction

*and optical replica present if choose to measure it*



# What's different...?



## Spectral decoding & Temporal decoding

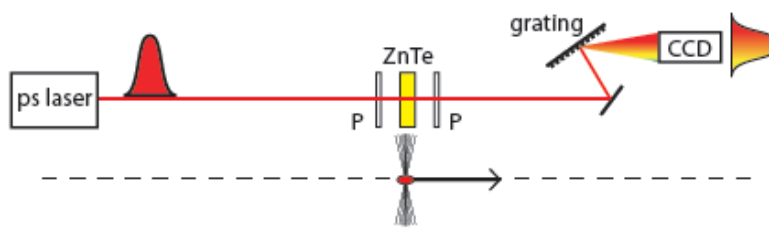
laser bandwidth  $\gg$  bunch spectral extent

issues of

- laser transport
- laser complexity/expense/reliability
- material effects (e.g. group velocity dispersion)

## Spectral upconversion

laser bandwidth  $\ll$  bunch spectral extent



**Important:** can measure non-propagating long wavelength components not accessible to radiative techniques (CSR/CTR/SP)

low power, 'simple' lasers OK  
 fibre transport now an option  
 simple – linear – spectral detection  
*without artefacts of spectral decoding*

# In Summary ...

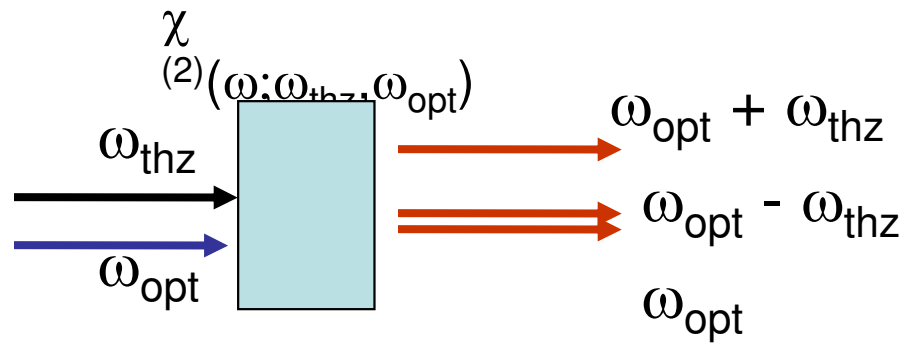
- Proven capability for explicit temporal characterisation up to  $\sim 100$  fs RMS electron bunch structure
- high time resolution techniques have problems with reliability & necessary infrastructure...
- ...*but* avenues available for improving time resolution & robustness (dependent on beam diagnostic requirements)
- For high time resolution, both alternative materials & spectral upconversion under investigation



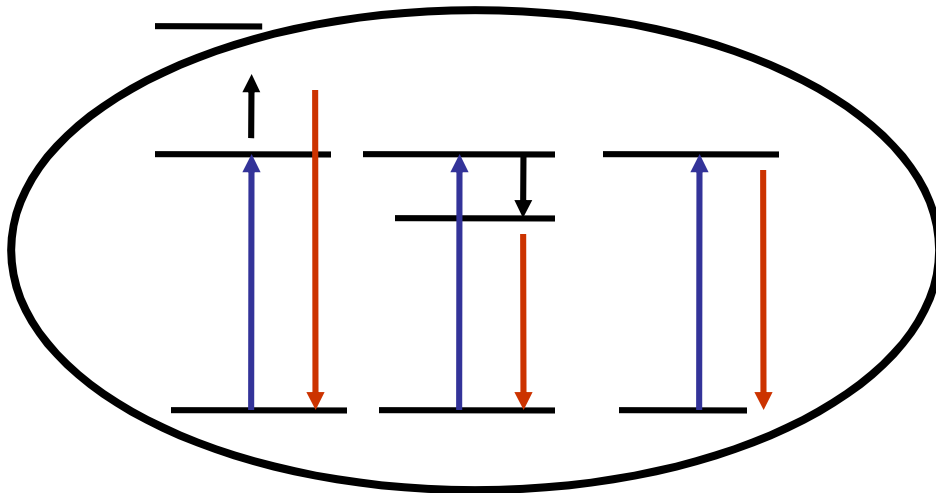


# ***EO Formalism:***

Electro-optic effect as  
sum- and difference-frequency mixing



frequency domain  
description  
of EO detection...

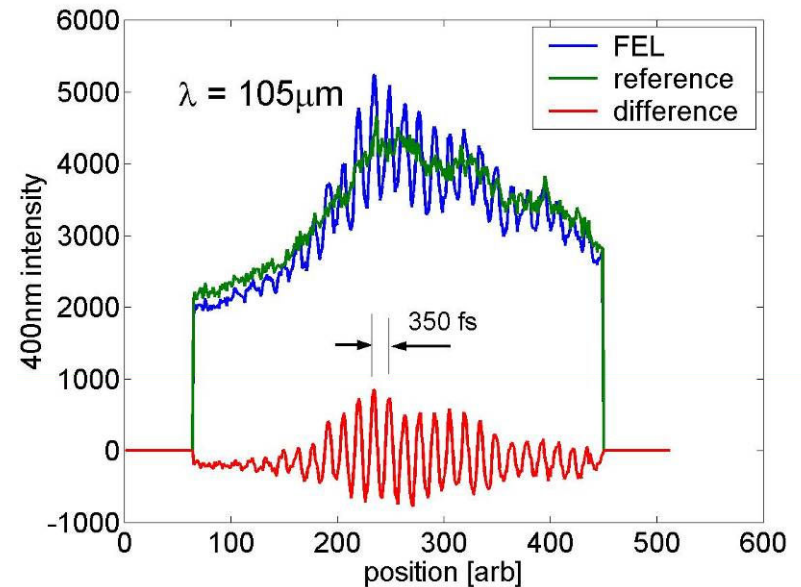
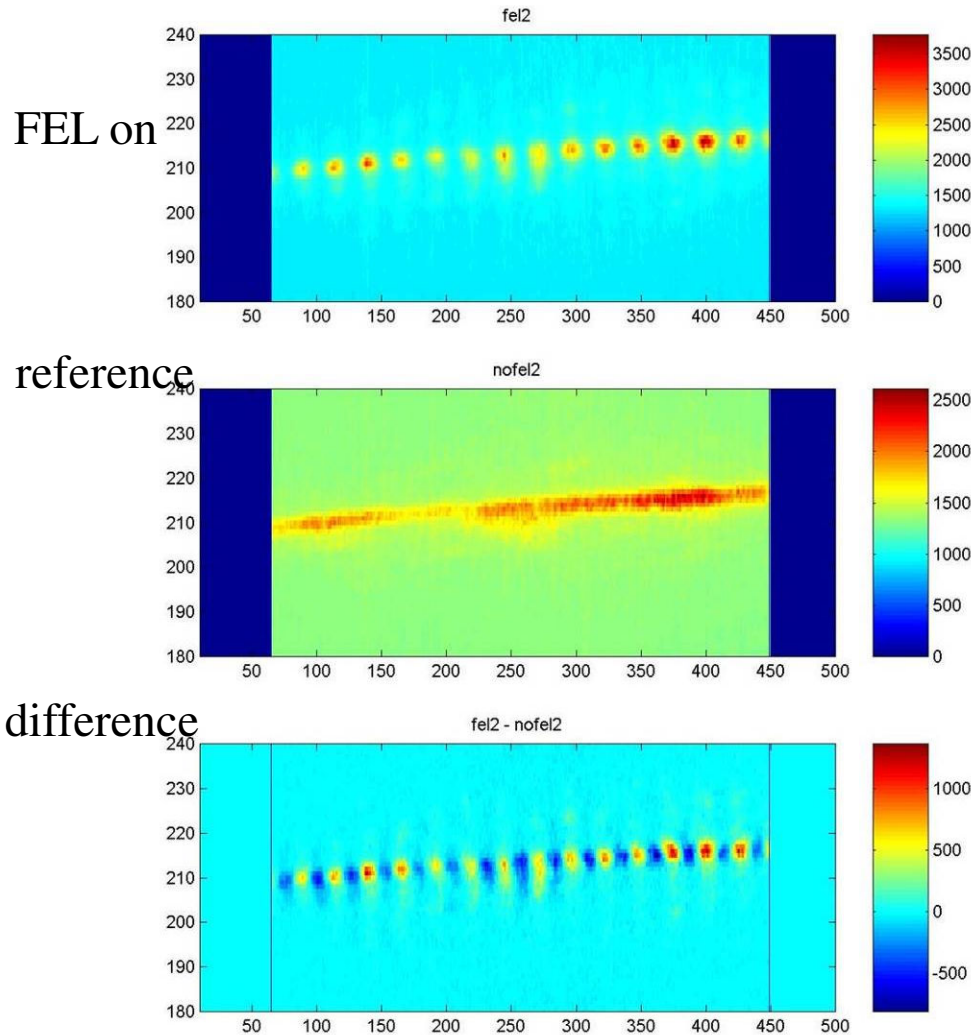


convolved over all  
combinations of optical  
and Coulomb frequencies



# Electro-optic measurements of FEL radiation

## single-shot measurement of THz electric field oscillations

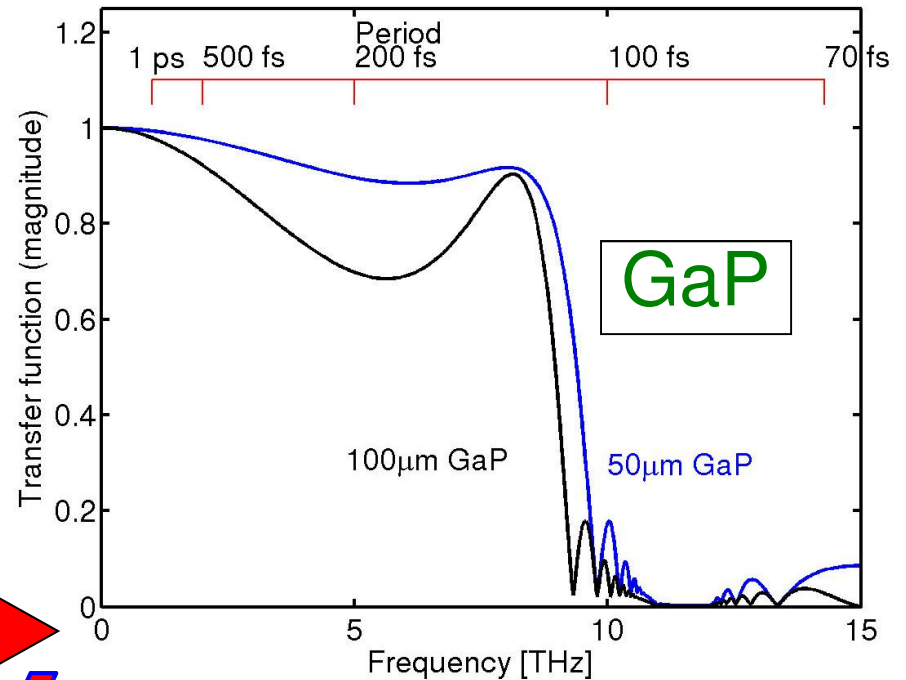
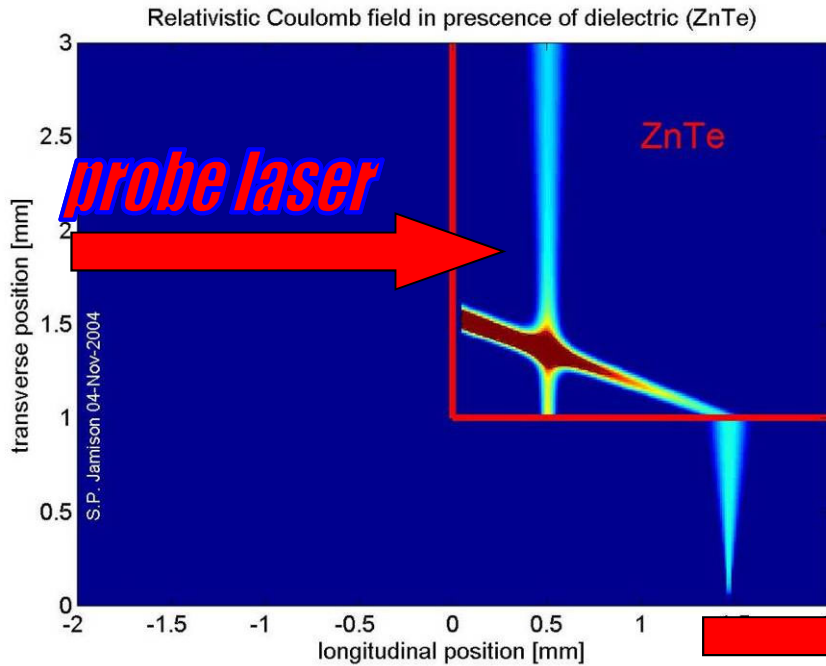


observed down to  $\lambda \sim 60\mu\text{m}$

opens possibility for  
time domain THz spectroscopy  
on light accelerator sources.

# Encoping Time Resolution...

material response,  $R(\omega)$



Uniform response  $< 8\text{THz}$  ( $\lambda > 40\ \mu\text{m}$ )

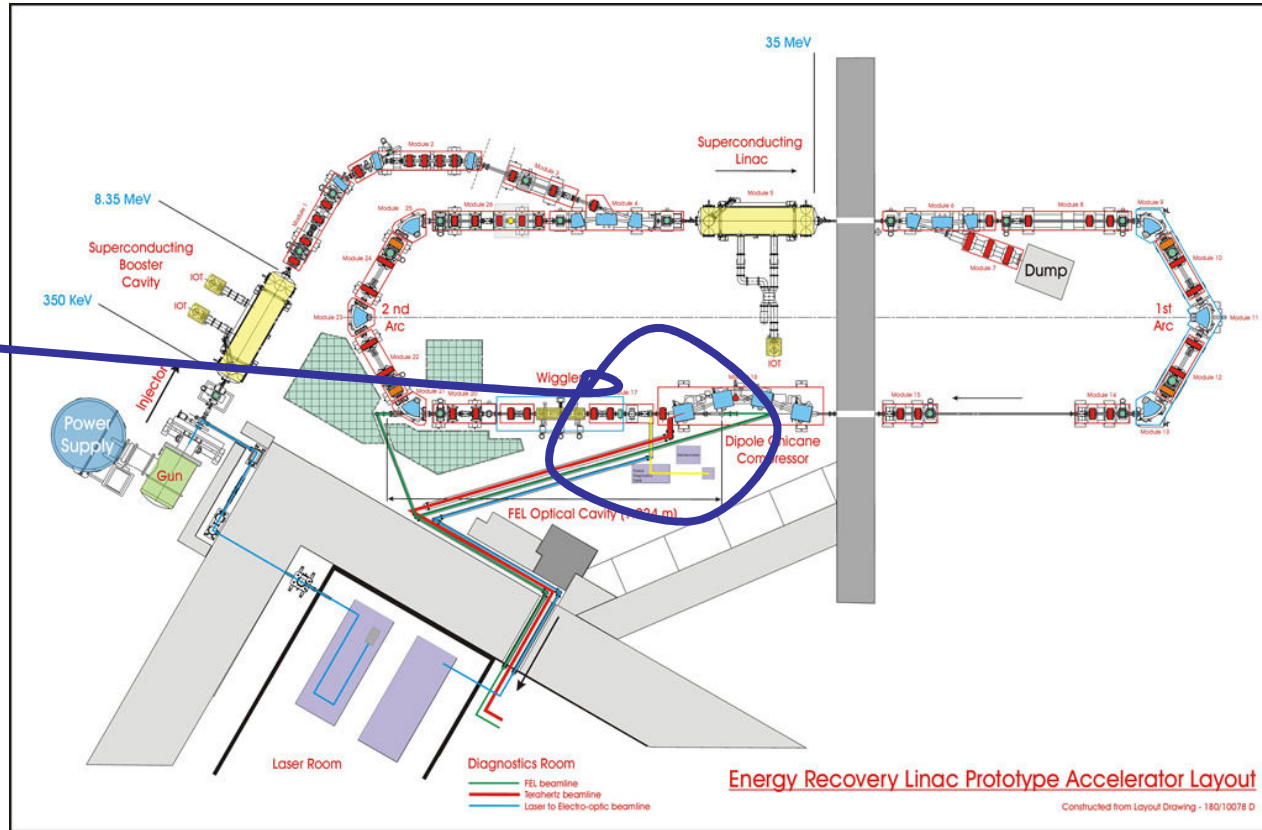
$\Rightarrow$  Faithful reproduction of  $> 150\ \text{fs}$  (FWHM) bunches



# ALICE.... (formerly ERLP)

## Accelerator and Lasers in Combined Experiments

Electro-optic diagnostic test-station



Recent progress (last Thursday):

First beam acceleration through the superconducting booster

- expect rapid commissioning of accelerator to follow..
- aiming for EO station up and running in December

# High field effects...

“Standard” theory of EO measurement does not apply for very strong fields

## Standard description...

Coulomb field induces refractive index change

$$\eta_x(t) = \eta_0(t) + \alpha_x E_{\text{Coul}}(t)$$
$$E_x(t) \sim E_x(t) \exp(i\omega t - i\eta\omega z/c)$$

phase retardation

## Our “standard” description

Frequency mixing of coulomb field

$$\tilde{A}(\omega, z) = \tilde{A}_0(\omega) e^{-z\beta_{\text{opt}}} + \frac{i}{2c\eta} e^{-z\beta_{\text{opt}}} \omega \int d\omega' \tilde{A}_{\text{eff}}^{\text{THz}}(\omega - \omega') \tilde{A}(\omega')$$

new optical field

Both descriptions include assumption of small-signal limit...

(does the “new optical field” itself undergo an EO interaction..?)

# High field effects...

Extension to high field considered necessary for ILC...

$$E_{\text{Coul}} \approx \frac{Q}{\sqrt{2\pi} \epsilon_0 r \sigma_z} \sim 100 \text{ MV.m}^{-1}$$

fields of this magnitude imply significant retardation .... potentially  $> \pi$   
retardation treatment becomes liable to breakdown

SPPS (SLAC):  
expect “over-rotation”  
but not observed

PRL **94**, 114801 (2005) week ending  
25 MARCH 2005  
PHYSICAL REVIEW LETTERS

**Clocking Femtosecond X Rays**

A. L. Cavalieri,<sup>1</sup> D. M. Fritz,<sup>1</sup> S. H. Lee,<sup>1</sup> P. H. Bucksbaum,<sup>1</sup> D. A. Reis,<sup>1</sup> J. Rudati,<sup>2</sup> D. M. Mills,<sup>2</sup> P. H. Fuoss,<sup>3</sup>  
G. B. Stephenson,<sup>3</sup> C. C. Kao,<sup>4</sup> D. P. Siddons,<sup>4</sup> D. P. Lowney,<sup>5</sup> A. G. MacPhee,<sup>5</sup> D. Weinstein,<sup>5</sup> R. W. Falcone,<sup>5</sup> R. Pahl.<sup>6</sup>

EO breakdown  
observed with  
intense CTR pulses

PRL **99**, 043901 (2007) week ending  
27 JULY 2007  
PHYSICAL REVIEW LETTERS

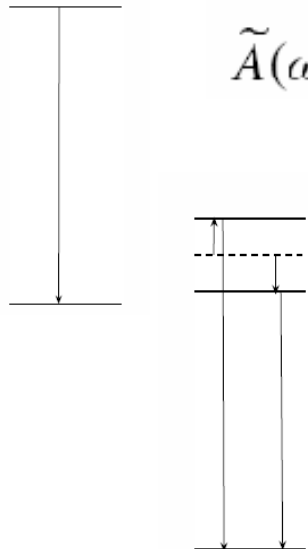
**Nonlinear Cross-Phase Modulation with Intense Single-Cycle Terahertz Pulses**

Y. Shen,<sup>1</sup> T. Watanabe,<sup>1</sup> D. A. Arena,<sup>1</sup> C.-C. Kao,<sup>1</sup> J. B. Murphy,<sup>1</sup> T. Y. Tsang,<sup>2</sup> X. J. Wang,<sup>1</sup> and G. L. Carr<sup>1</sup>  
<sup>1</sup>National Synchrotron Light Source, Brookhaven National Laboratory, Upton, New York 11973-5000, USA  
<sup>2</sup>Instrumentation Division, Brookhaven National Laboratory, Upton, New York 11973-5000, USA  
(Received 27 December 2006; published 23 July 2007)

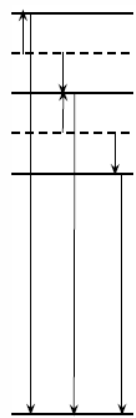
# Development of high-field/large-signal EO theory

starting point... wave equation with co-propagating non-linear source

$$\tilde{A}(\omega, z) = \tilde{A}_0(\omega)e^{-z\beta_{\text{opt}}} + \frac{i}{2c\eta}e^{-z\beta_{\text{opt}}}\omega \int d\omega' \tilde{A}_{\text{eff}}^{\text{THz}}(\omega - \omega')\tilde{A}(\omega'),$$

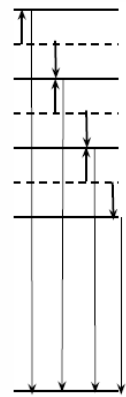


optical “sidebands” in small signal theory



“sidebands” on sidebands

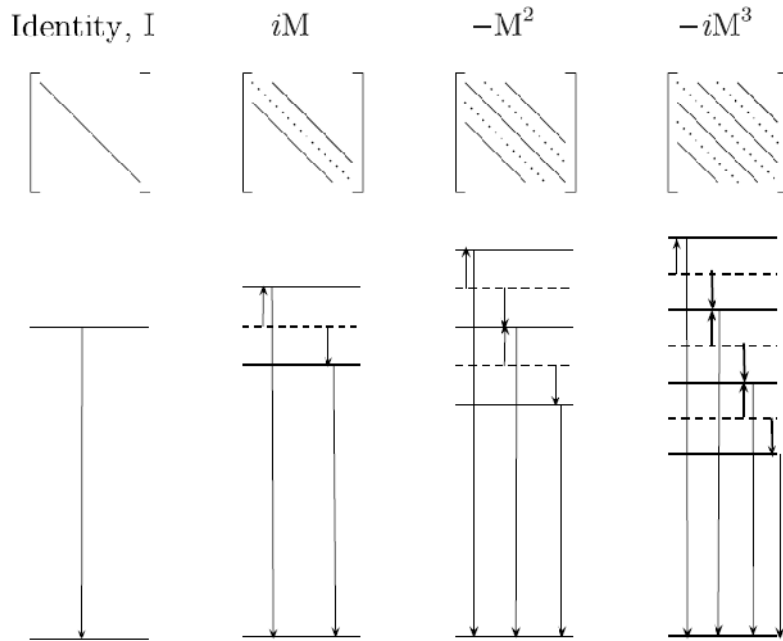
describes probe depletion



...on sidebands

.....

# ...high-field/large-signal EO theory



can associate EO interaction with matrix operation on input probe spectrum

$$\underline{\mathbf{A}}(z) = \exp \left[ -z \underline{\underline{\beta}}^{\text{opt}} + \frac{i}{2c\eta} \underline{\underline{\mathbf{T}}}(z) \right] \underline{\mathbf{A}}_0,$$

where

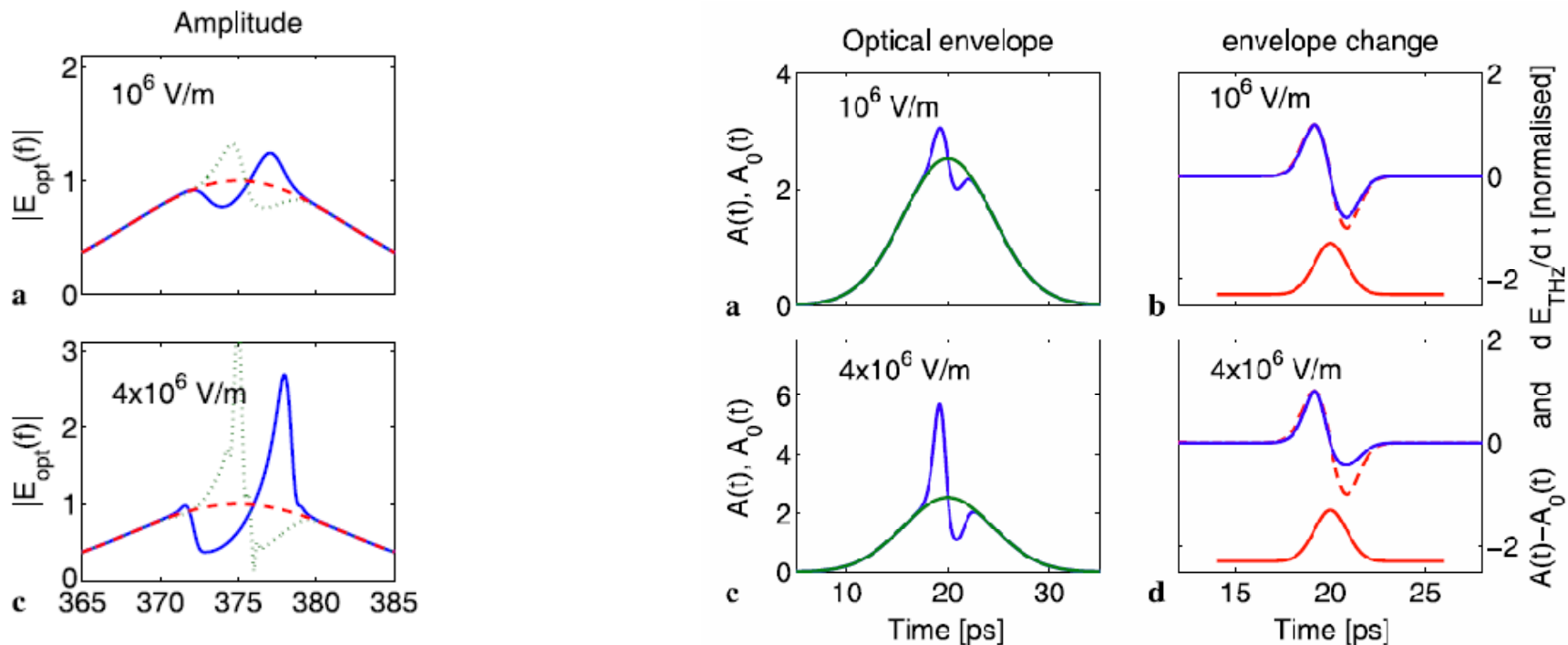
$$\begin{aligned} \underline{\underline{\mathbf{T}}}(z) = \{T_{mn}\} &\equiv \left\{ M_{mn}^{(0)} \left[ \frac{\exp(i\Delta\tilde{k}_{(m-n),m}z) - 1}{i\Delta\tilde{k}_{(m-n),m}} \right] \right\} \\ &= \left\{ \delta\omega_m \chi_{m-n}^{(2)} A_{m-n}^{\text{THz}} \left[ \frac{\exp(i\Delta\tilde{k}_{(m-n),m}z) - 1}{i\Delta\tilde{k}_{(m-n),m}} \right] \right\}. \end{aligned}$$

End result....

- “simple” matrix exponential solution to probe spectrum
- Fourier transform to get time domain solution

S.P. Jamison. Appl. Phys. B **91**, 241-247, (2008)

# Example of high field short-pulse simulation...

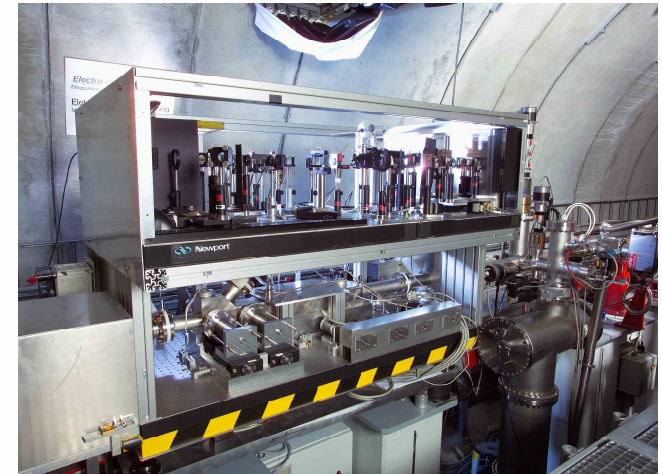
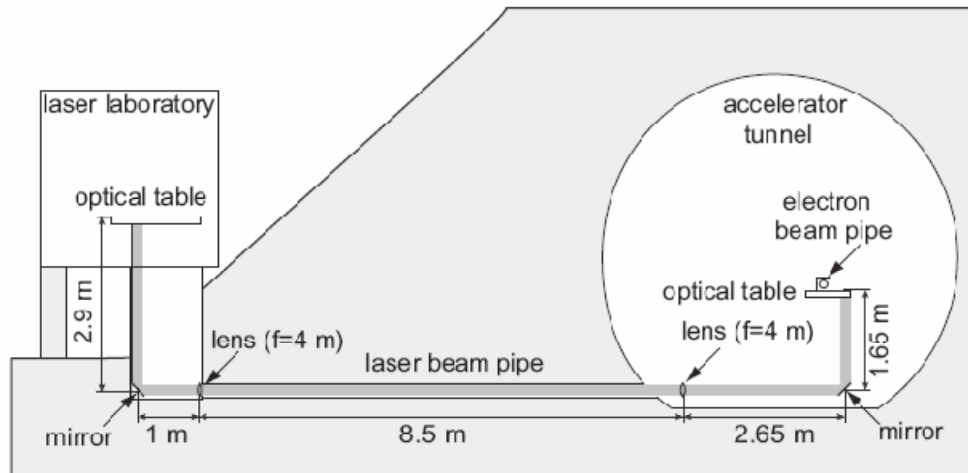


“simple” matrix exponential solution...

care needed for e.g. 4000x4000 matrix as in above simulation

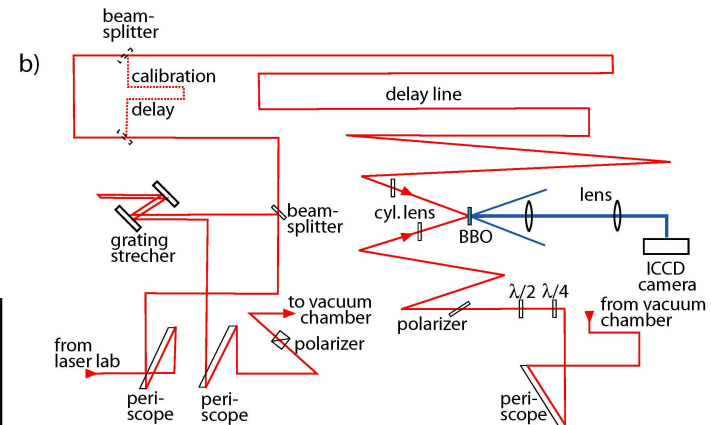
# Laser transport... in FLASH experiments

## EO Temporal decoding setup



More complicated setup  
Less access to setup in accelerator

- Vacuum laser transport from laser "hut" to tunnel.
- Some relay lenses in transport
- Remote adjustments on many mirrors



## ***Selected References:***

Free-electron laser pulse shape measurements with 100fs temporal resolution using a 10fs Ti:sapphire laser and differential optical gating

X. Yan, A.M. MacLeod, W.A. Gillespie et al.

*Nucl. Instr. Meths. Phys. Res. Vol A429 (1999) 7- 9*

Sub-picosecond electro-optic measurement of relativistic electron pulses

X. Yan, A.M. MacLeod, W.A. Gillespie, G.M.H. Knippels, D. Oepts, A.F.G. van der Meer.

*Physical Review Letters 85 (2000) 3404-7*

Single-shot electron bunch length measurements

I. Wilke, A.M. MacLeod, W.A. Gillespie, G. Berden, G.M.H. Knippels, A.F.G. van der Meer

*Phys. Rev. Lett. 88 No 12 (2002) 124801/1-4*

Real-time, non-destructive, single-shot electron bunch-length measurements

G. Berden, S.P. Jamison, A.M. MacLeod, W.A. Gillespie, B. Redlich and A.F.G. van der Meer

*Physical Review Letters 93 (2004) 114802*

Temporally resolved electro-optic effect

S.P. Jamison, A.M. Macleod, G. Berden, D.A. Jaroszynski and W.A. Gillespie

*Optics Letters 31, 11 (2006) 1753-55*

Benchmarking of Electro-Optic monitors for Femtosecond electron bunches

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