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# ACE3P time-domain codes applied to CLIC

*Arno Candel,*

*Andreas Kabel, Lie-Quan Lee, Zenghai Li, Cho Ng,  
Vineet Rawat, Greg Schussman and Kwok Ko*

***SLAC National Accelerator Laboratory***

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# SciDAC Finite Element Electromagnetics

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## **SLAC Researchers**

### **Accelerator Physicists:**

*Arno Candel, Andreas Kabel, Kwok Ko, Zenghai Li, Cho Ng, Liling Xiao*

### **Computational Scientists:**

*Lixin Ge, Rich Lee, Vineet Rawat, Greg Schussman*

## **Accelerator Collaborators**

*H. Wang, F. Marhauser, C. Reece, R. Rimmer (TJNAF), D. Li (LBNL),  
I. Ben-Zvi, R. Palmer, J. Kewisch, D. Naik (BNL), E. Chojnacki (Cornell),  
A. Grudiev, I. Syratchev, W. Wuensch (CERN)*

## **Computational Science Collaborators**

*E. Ng, X. Li, I. Yamazaki, C. Yang (TOPS/LBNL), L. Dianchin (ITAPS/LLNL), K. Devine,  
E. Boman, (ITAPS/CSCAPES/SNL), D. Keyes (TOPS/Columbia), X. Luo, M. Shephard  
(ITAPS/RPI), W. Gropp (CScADS/UIUC), O. Ghattas (TOPS/UT Austin), Z. Bai (UC Davis),  
K. Ma (ISUV/UC Davis), A. Pothen (CSCAPES/Purdue), T. Tautges (ITAPS/ANL)*



# Parallel Finite Element EM code suite ACE3P

SLAC has developed the conformal, higher-order, C++/MPI-based parallel EM code suite ACE3P for high-fidelity modeling of large, complex accelerator structures.

## ACE3P: Parallel Finite Element EM Code Suite (Advanced Computational Electromagnetics, 3D, Parallel)

### ACE3P Modules – Accelerator Physics Application

<u>Frequency Domain:</u>	Omega3P	– Eigensolver (nonlinear, damping)
	S3P	– S-Parameter
<u>Time Domain:</u>	T3P	– <u>Transients &amp; Wakefields</u>
	Pic3P	– <u>EM Particle-In-Cell (self-consistent)</u>
<u>Particle Tracking:</u>	Track3P	– Dark Current and Multipacting
	Gun3P	– <u>Space-Charge Beam Optics</u>
<u>Multi-Physics:</u>	TEM3P	– <u>EM-Thermal-Mechanical</u>

Visualization: ParaView – Meshes, Fields and Particles

Funded by SciDAC1 (2001-2006) and continuing under SciDAC2 (in black)

Under development for ComPASS (2007-2011) (in blue)



# ACE3P Finite Element EM Time-Domain

## Combine Ampere's and Faraday's laws

$$\nabla \times \nabla \times \vec{E} + \mu \epsilon \frac{\partial^2 \vec{E}}{\partial t^2} + \mu \sigma_{\text{eff}} \frac{\partial \vec{E}}{\partial t} = -\mu \frac{\partial \vec{J}}{\partial t}$$
$$\sigma_{\text{eff}} = \omega \epsilon_0 \epsilon_i$$

## T3P and Pic3P: full-wave EM from first principles

## Unconditionally stable time integration\*

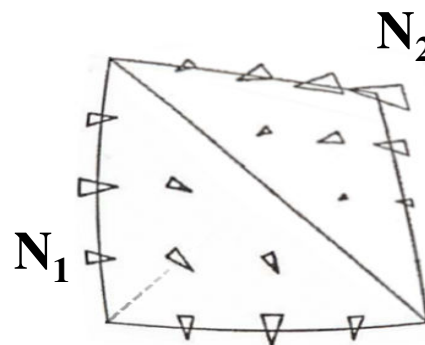
Solve linear system at every time step:

$$Ax=b$$

## ACE3P Finite Element Method:

Curved tetrahedral finite elements with higher-order vector basis functions  $\mathbf{N}_i$ :

$$\mathbf{E}(\mathbf{x}, t) = \sum_i e_i(t) \cdot \mathbf{N}_i(\mathbf{x})$$



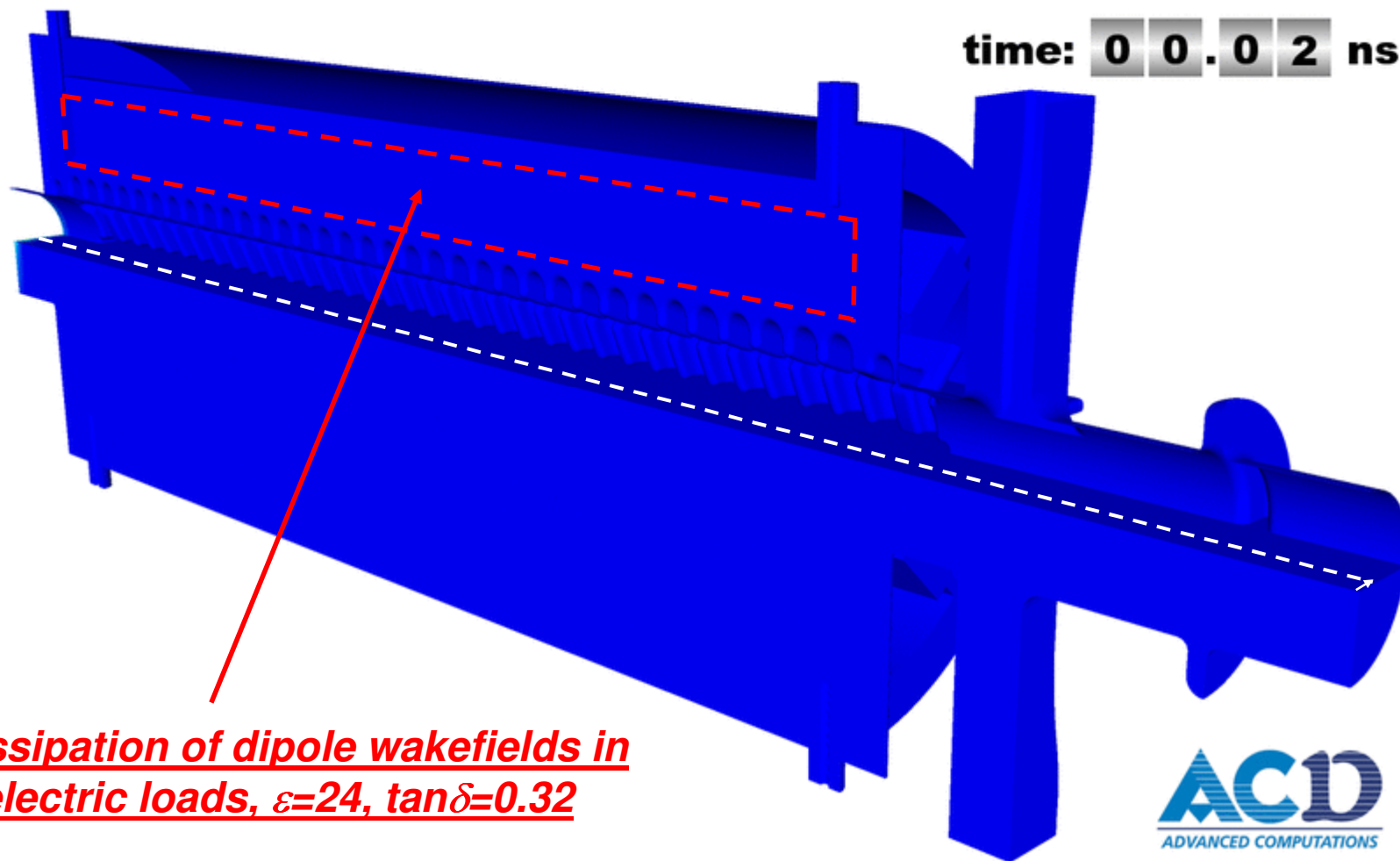
For order  $p=2$ : 20 different  $\mathbf{N}_i$ 's  
For order  $p=6$ : 216 different  $\mathbf{N}_i$ 's

\*Navsariwala & Gedney, *An unconditionally stable parallel finite element time domain algorithm*, Antennas and Propagation, 1996

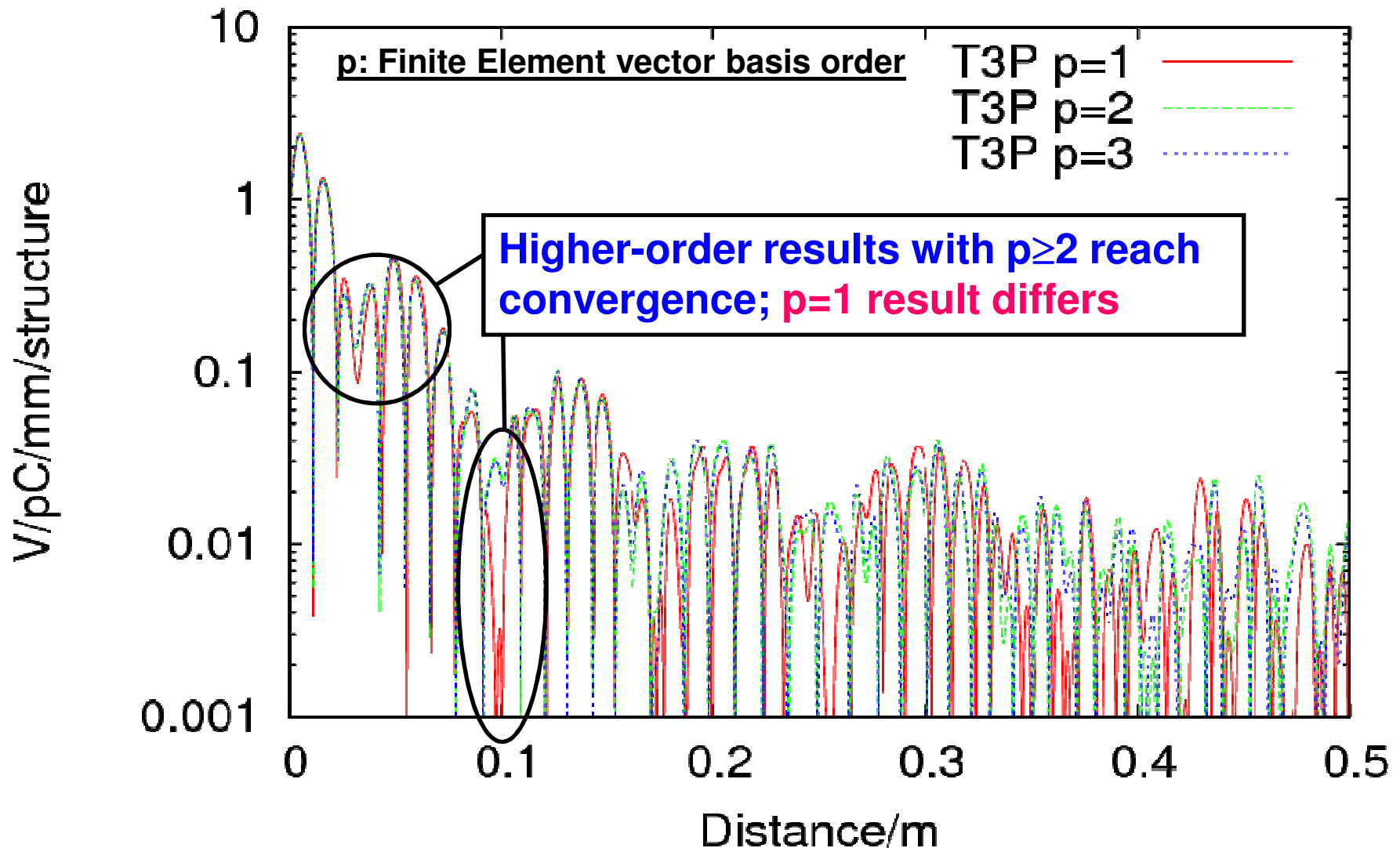


# Previous work: PETS wakefield damping...

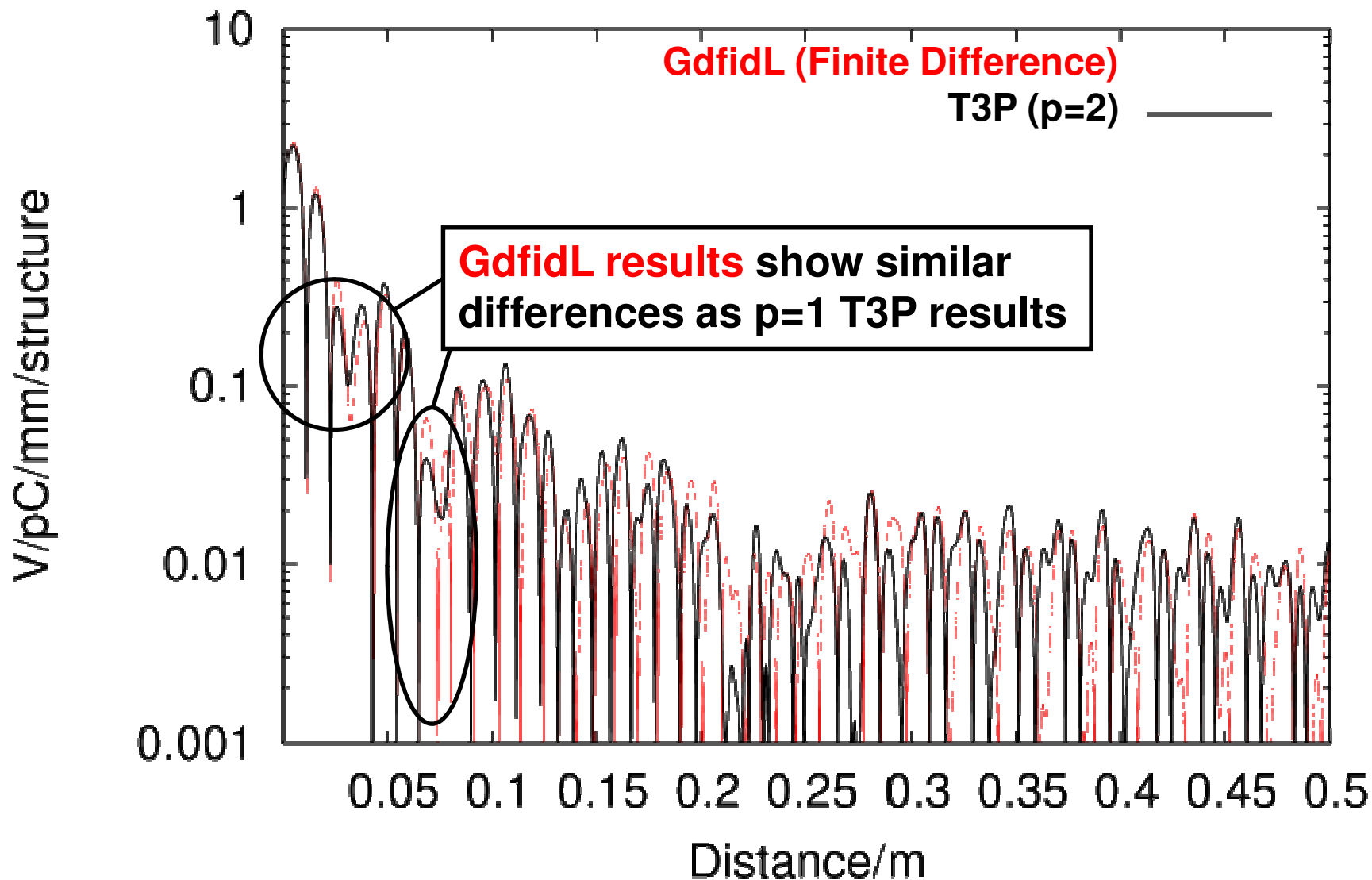
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# ... PETS wakefield convergence ...

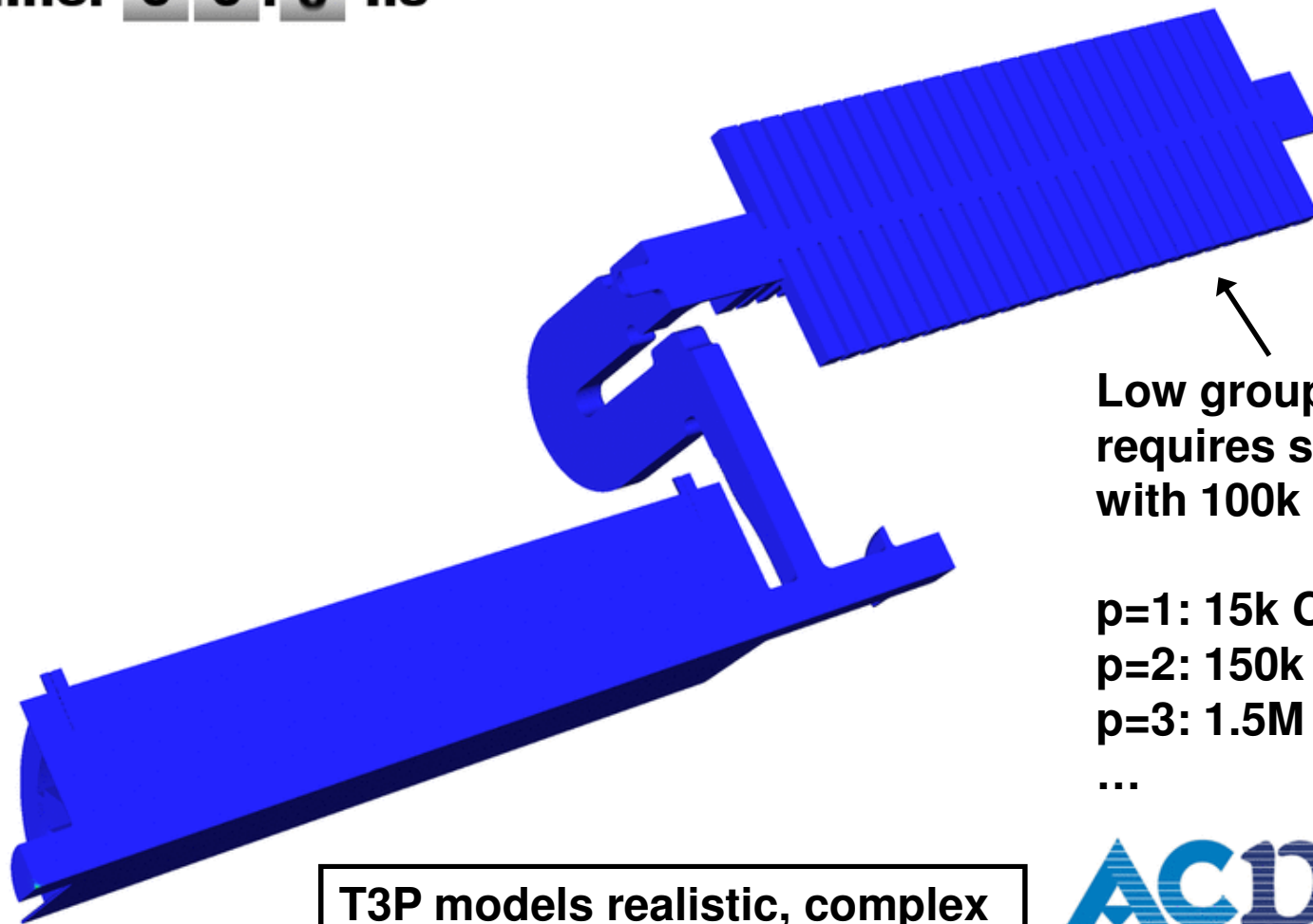


# ... Benchmarking: T3P vs. GdfidL ...



# ... and Simulation of RF power transfer

time: 0 0 . 0 ns



Low group velocity  
requires simulations  
with 100k time steps

p=1: 15k CPU hours  
p=2: 150k CPU hours  
p=3: 1.5M CPU hours

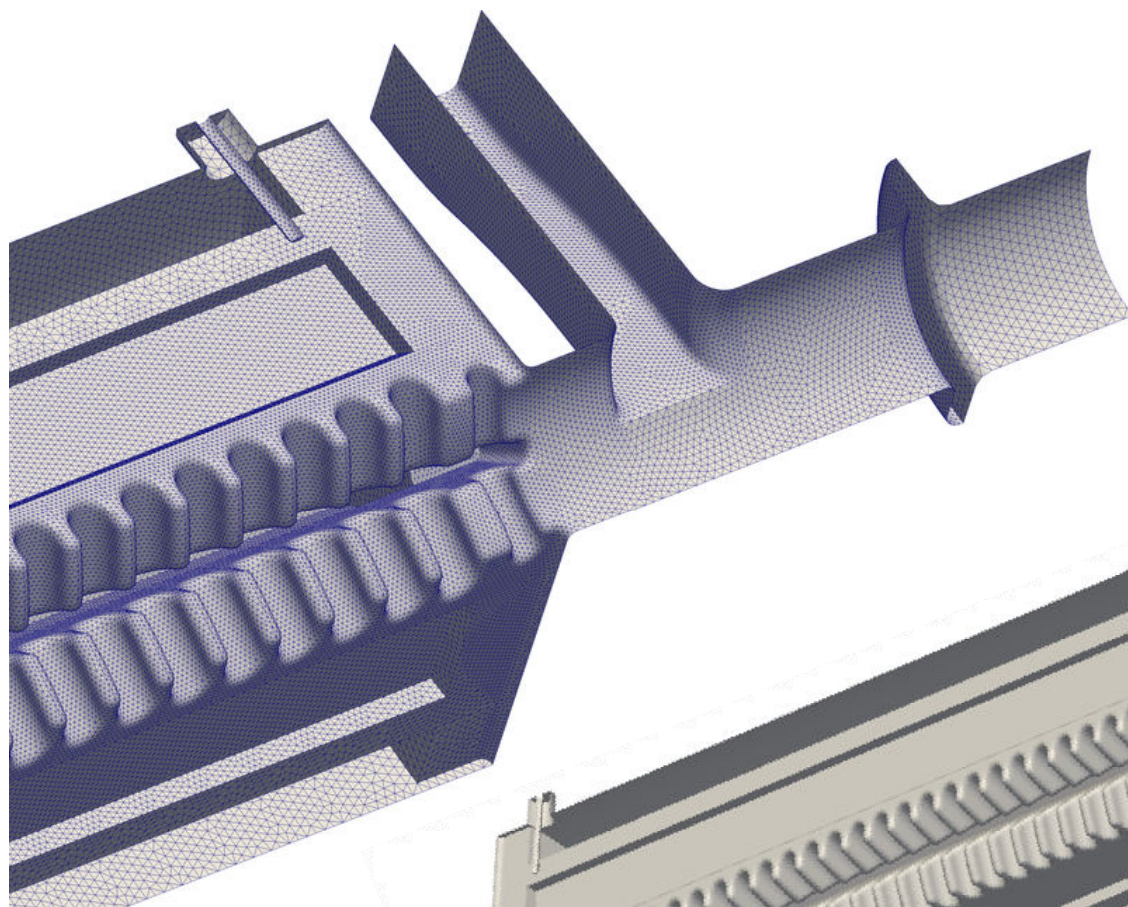
...

T3P models realistic, complex  
accelerator structures with  
unprecedented accuracy



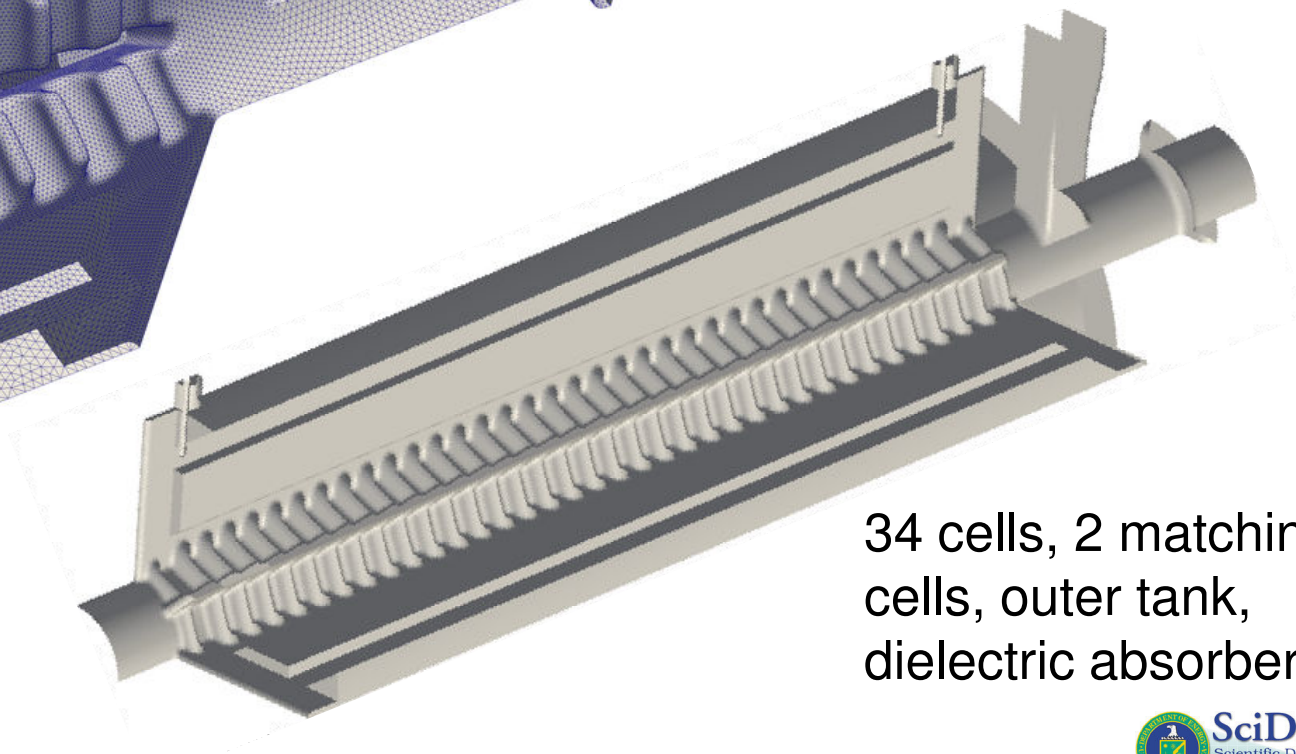


# Now... PETS power extraction study

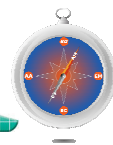


Unstructured conformal (curved) mesh model of a quarter structure, 0.5 mm mesh size on iris:

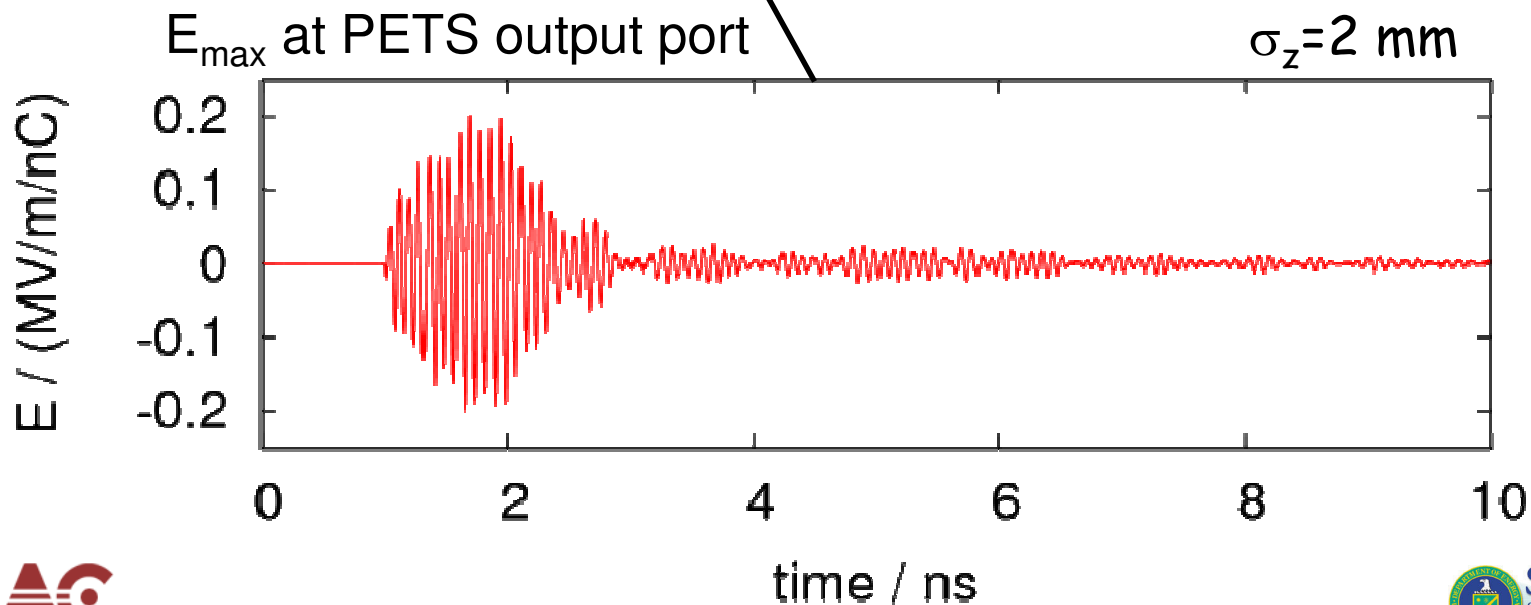
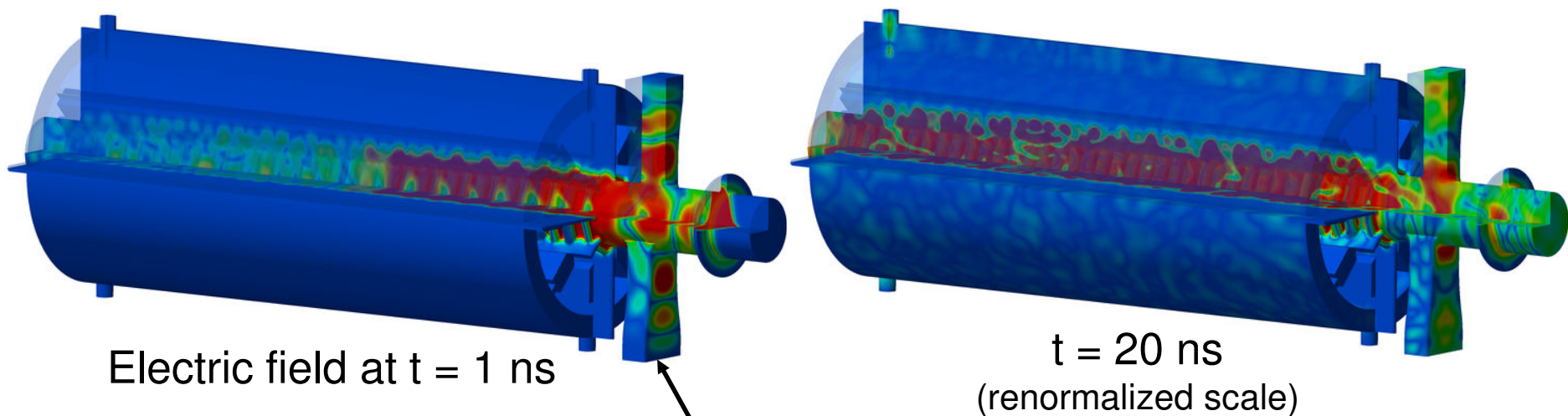
3.7M tetrahedral elements



34 cells, 2 matching cells, outer tank, dielectric absorbers

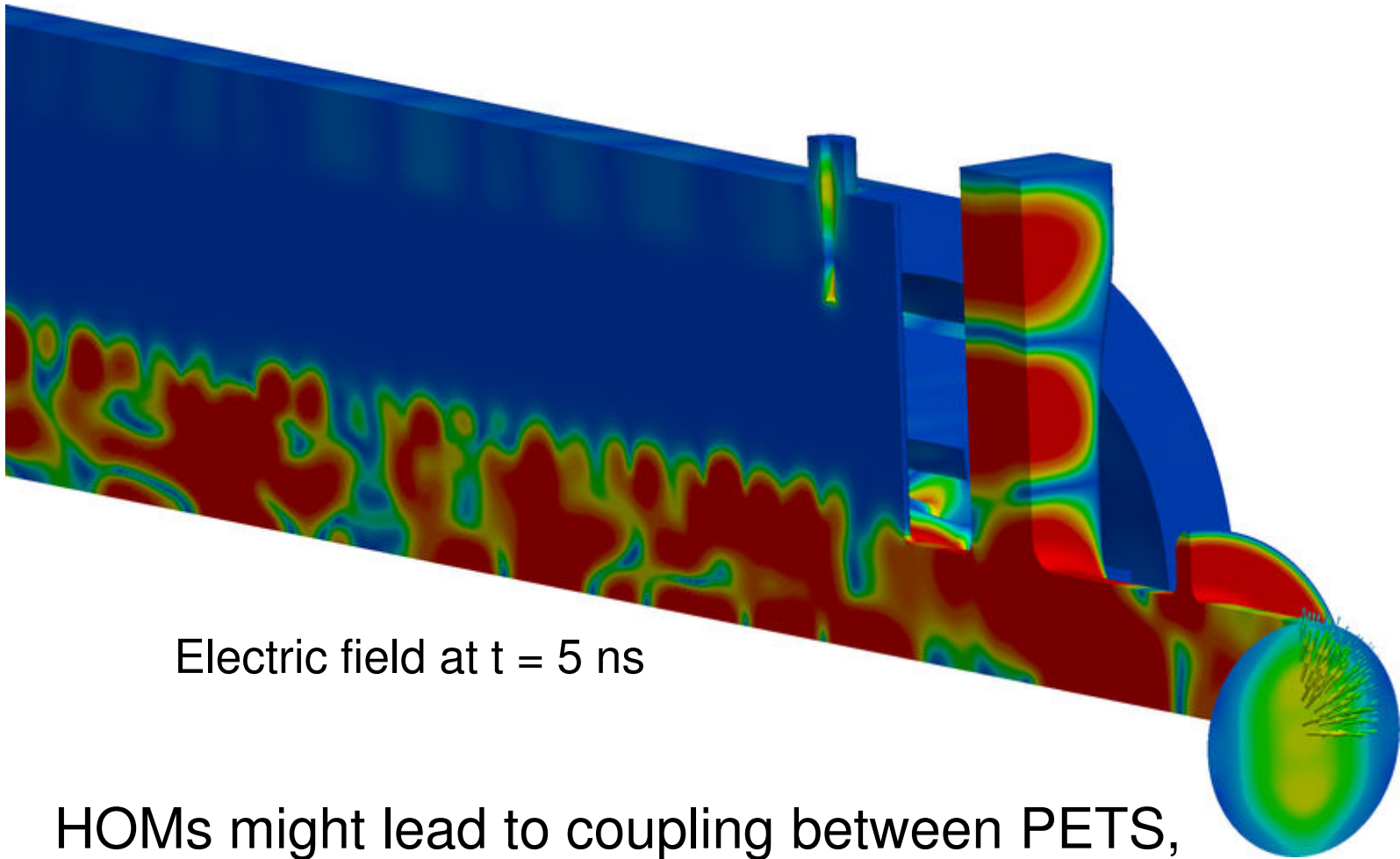


# T3P - Single drive bunch in PETS



# T3P - HOMs in PETS (single drive bunch)

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Electric field at  $t = 5$  ns

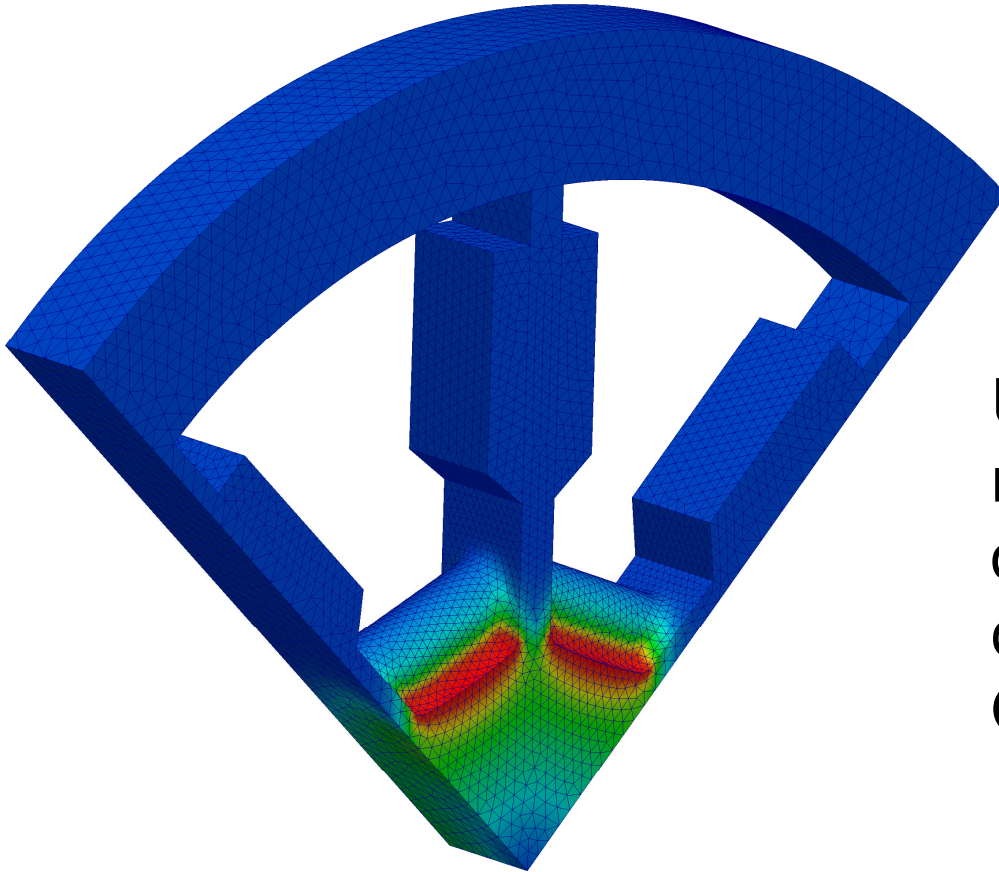
HOMs might lead to coupling between PETS,  
requires further study.



# PETS single cell RF frequency calculation

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To model multiple drive bunches, need to know proper bunch spacing, given by RF frequency.



100k elements, p=2

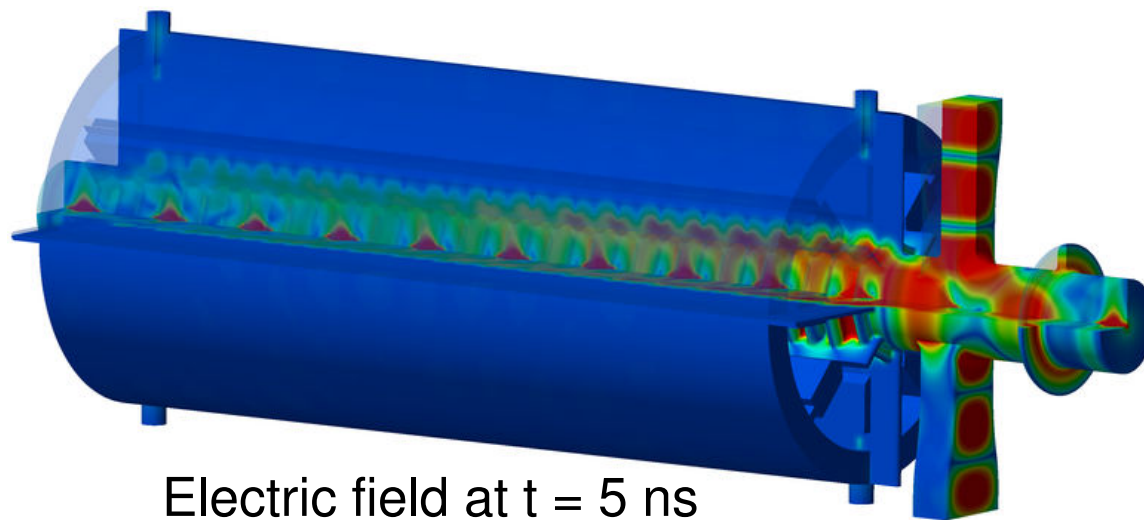
Using the same mesh model as for T3P time-domain calculations, obtain RF frequency with **Omega3P**:

$$\underline{f = 11.9822(2) \text{ GHz}}$$

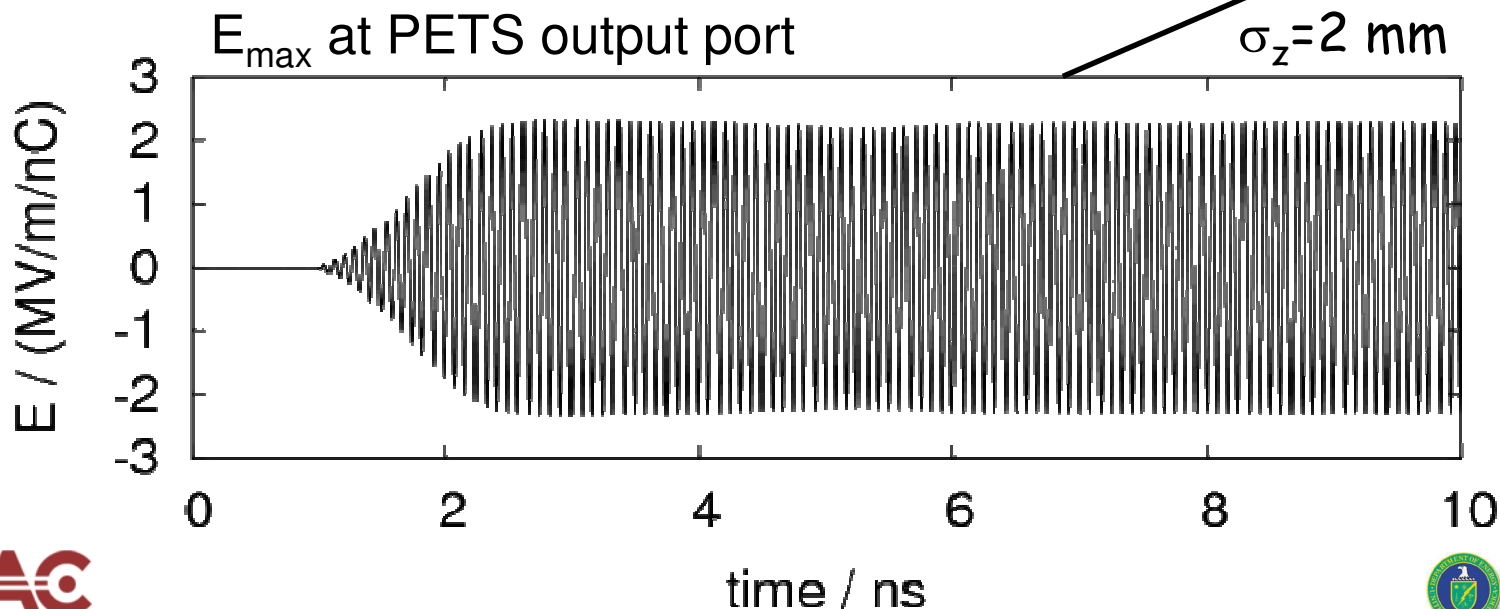


# T3P - Multiple drive bunches in PETS

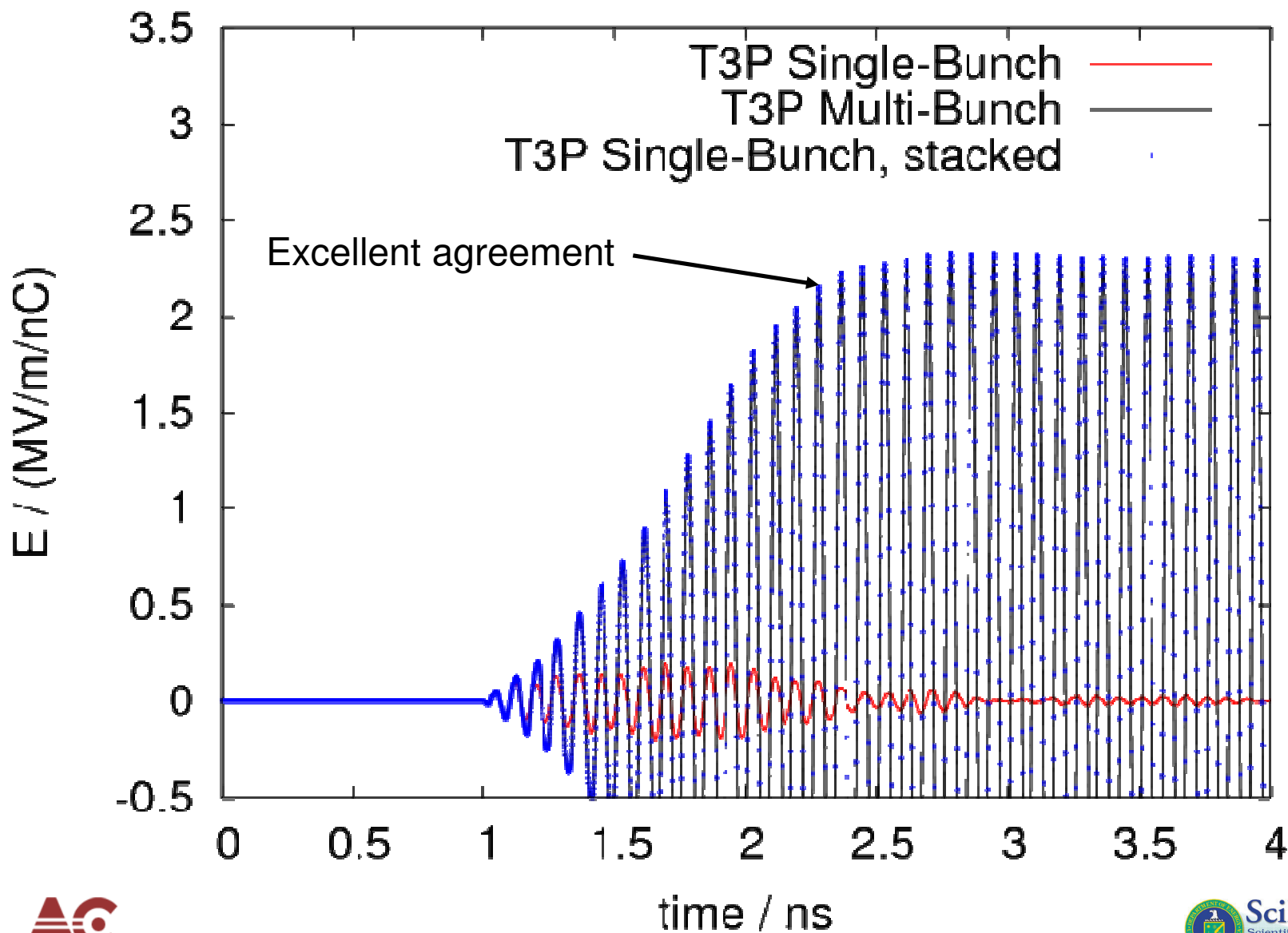
T3P simulation  
using one bunch  
per RF bucket:



Electric field at  $t = 5$  ns



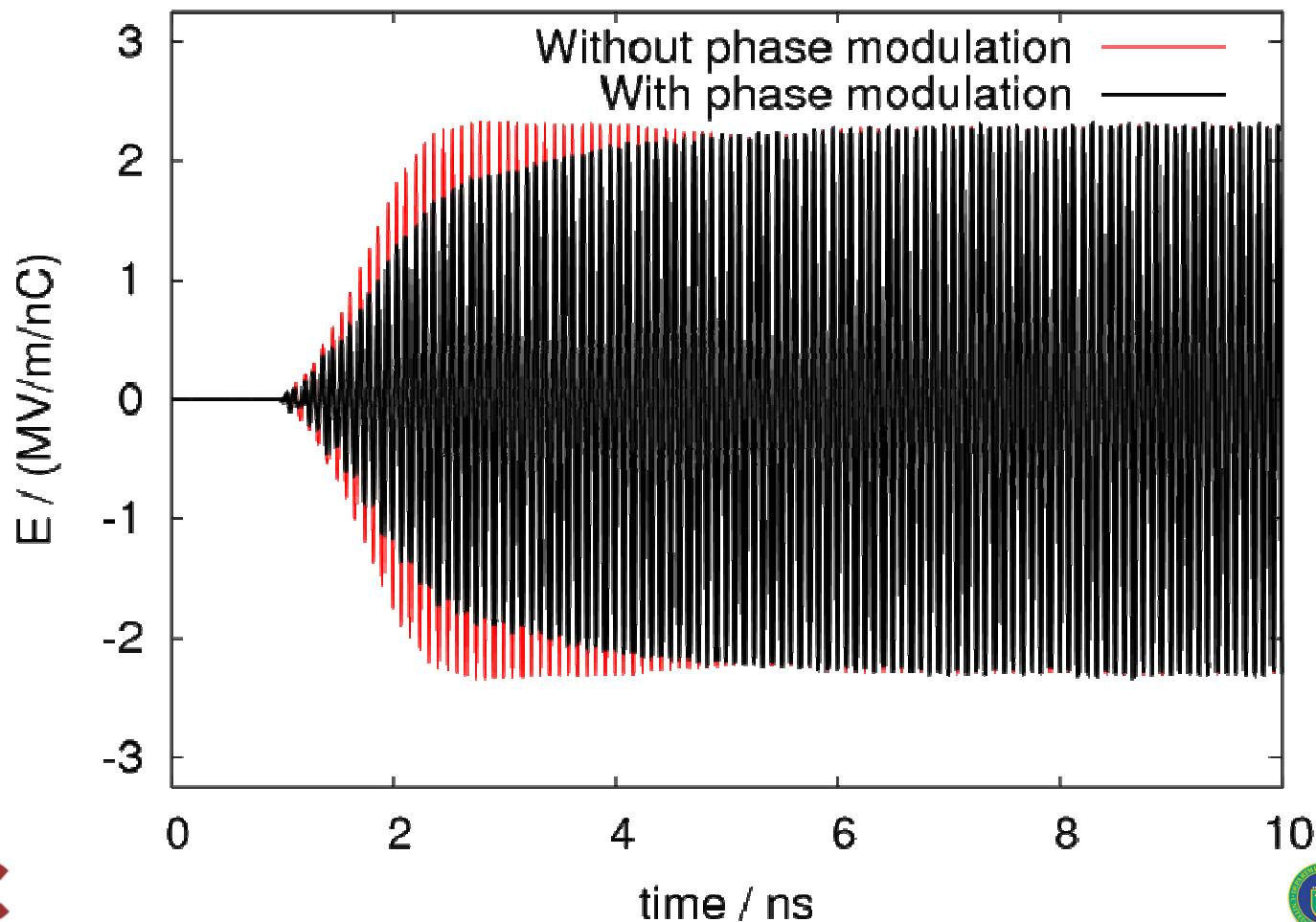
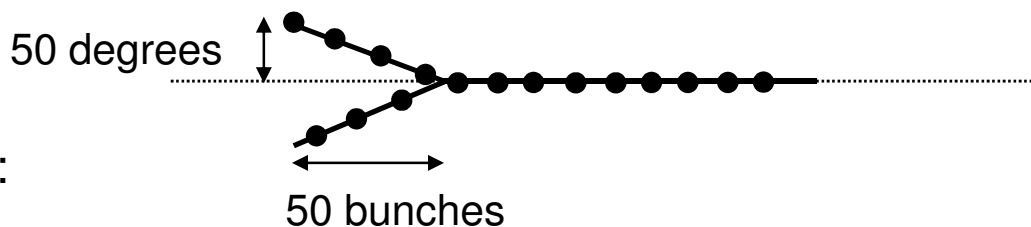
# Multi-bunch simulation vs. stacking



# RF pulse formation

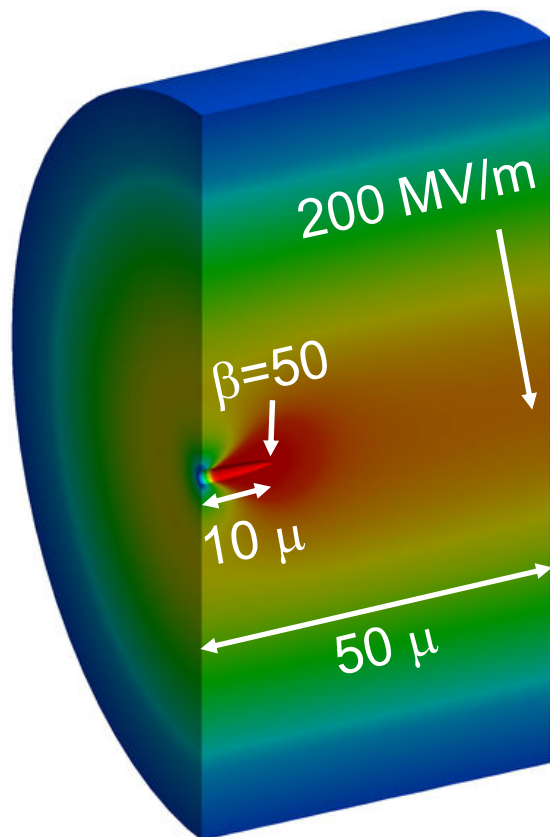
## Phase modulation:

Ramping of drive bunch injection phase offsets, e.g.:



# Pic3P: Dark current field emitter modeling

**Aim:** Use PIC code Pic3P to self-consistently model field emission process to help understand dark current emission and heating.



Enhanced surface RF fields calculated with **Omega3P**

## Simulation parameters and assumptions:

- Ellipsoidal copper tip, half-axes  $10\mu \times 1\mu \times 1\mu$  ( $\beta=50$ )
- Surface fields obtained from eigenmode calculation
- Emission from tip surface, depends on local field strength (RF + space charge)

Fowler-Nordheim predicts emission of  $Q=0.67$  pC from such a tip during one RF cycle, without space-charge effects. A PIC simulation is used to estimate the actually emitted charge.

- 1) Push (macro-)particles  $\frac{d\mathbf{p}}{dt} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$
- 2) Deposit charges  $\mathbf{J}(\mathbf{x}, t) = \sum_i q_i \cdot \delta(\mathbf{x} - \mathbf{x}_i(t)) \cdot \mathbf{v}_i(t)$
- 3) Calculate EM space-charge fields
- 4) Emit particles using **Fowler-Nordheim field emission in RF and space charge fields**





# Pic3P: Self-consistent field emission

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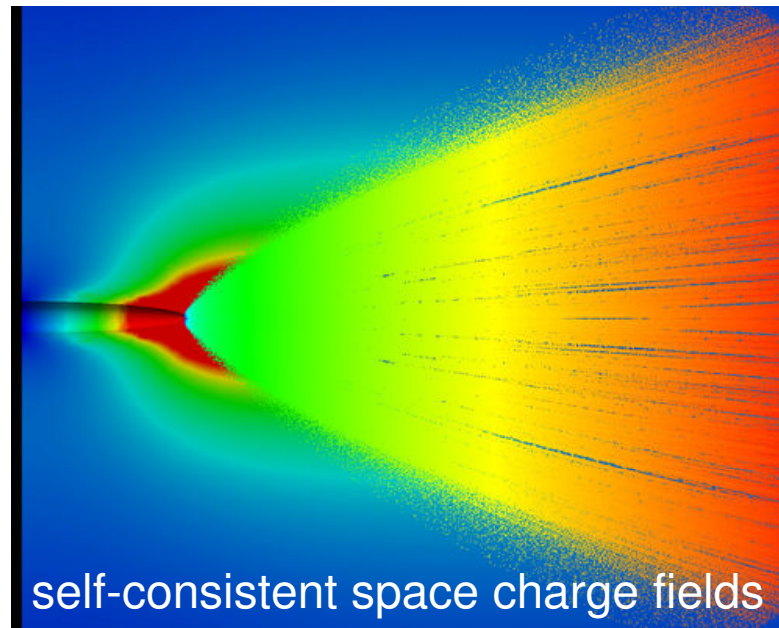
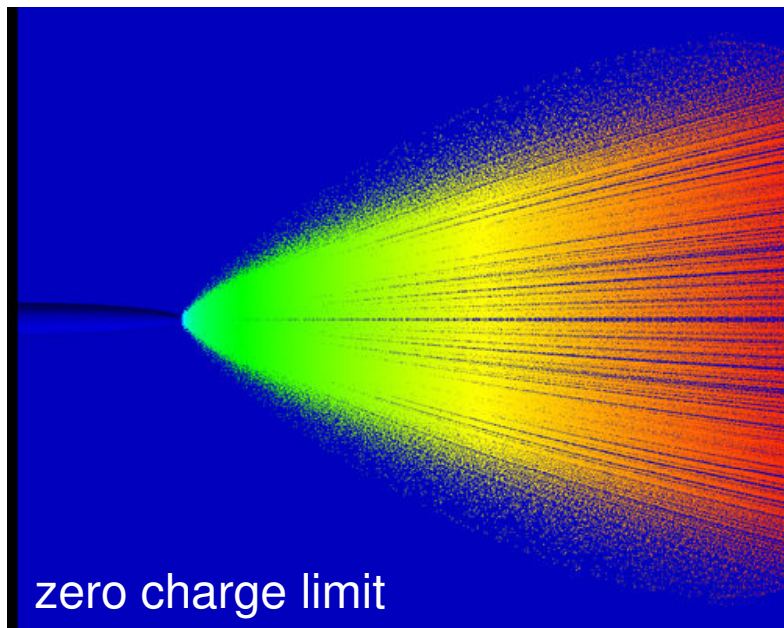


Pic3P simulation of field emission, including space-charge effects.  
Parameters indicated on previous slide.  
Particles colored by momentum, only space-charge fields shown.



# Pic3P: Space-charge effect in field emission

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For the simulated 10-degree window around the RF peak, Fowler-Nordheim without space-charge predicts  $Q=0.14$  pC, but PIC simulation shows only  $Q=0.06$  pC emitted charge.

**Observed space-charge limitation of emission by a factor of  $\sim 2$ .**  
**Estimated emitted average current for full RF cycle from this tip:  $\sim 5$  mA**

*work in progress*



# Summary and Outlook

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- **SLAC's Advanced Computations Department** has developed the **parallel Finite Element ACE3P code suite** for high-fidelity electromagnetic modeling of complex accelerator structures, using conformal unstructured meshes and higher-order field representation.
- **T3P** was applied to model the RF power generation in the PETS.
- **Pic3P** was applied to model self-consistent dark current field emission.

**Future work may include** (we welcome suggestions!):

- Pulse formation and dispersive effects in accelerating structure
- Wakefield damping in accelerating structure
- Coupling between PETS and accelerating structure
- Calculation of trapped modes between PETS
- Further dark current field emission and heating studies

***We acknowledge our SciDAC and CERN collaborators***

