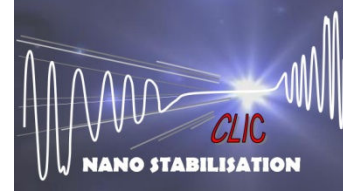


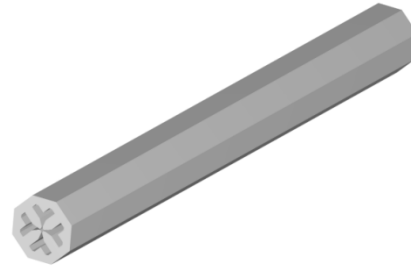
# CLIC Main Beam Quadrupoles Stabilization

C. Collette, K. Artoos, M. Guinchard, A.  
Kuzmin, M. Sylte, F. Lackner, C. Hauviller...  
CERN/EN

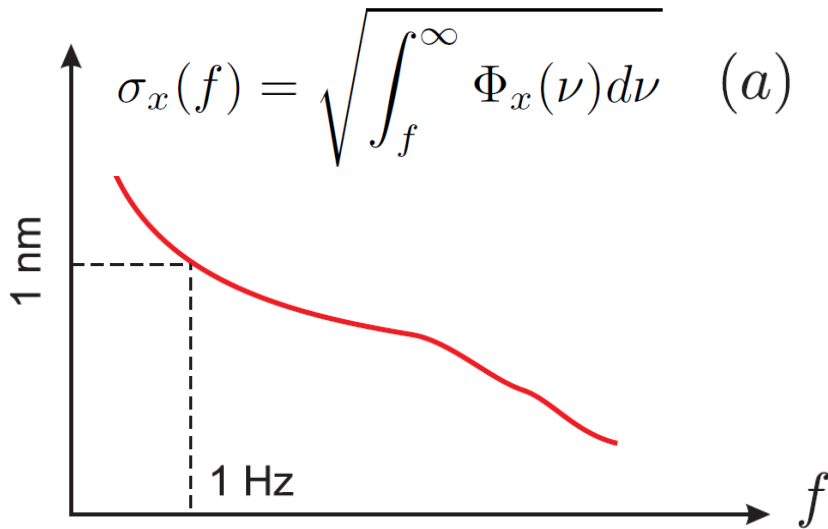


# Requirements

Length: 2m  
 Weight: ~ 400 Kg

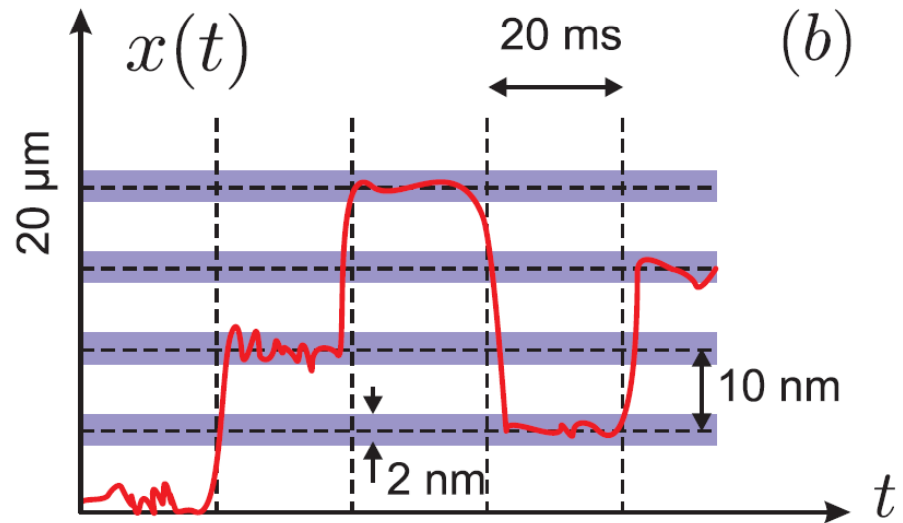


Frequency domain requirements  
 (**stabilization**)



(4 nm in lateral direction)  
 2000 quadrupoles/line

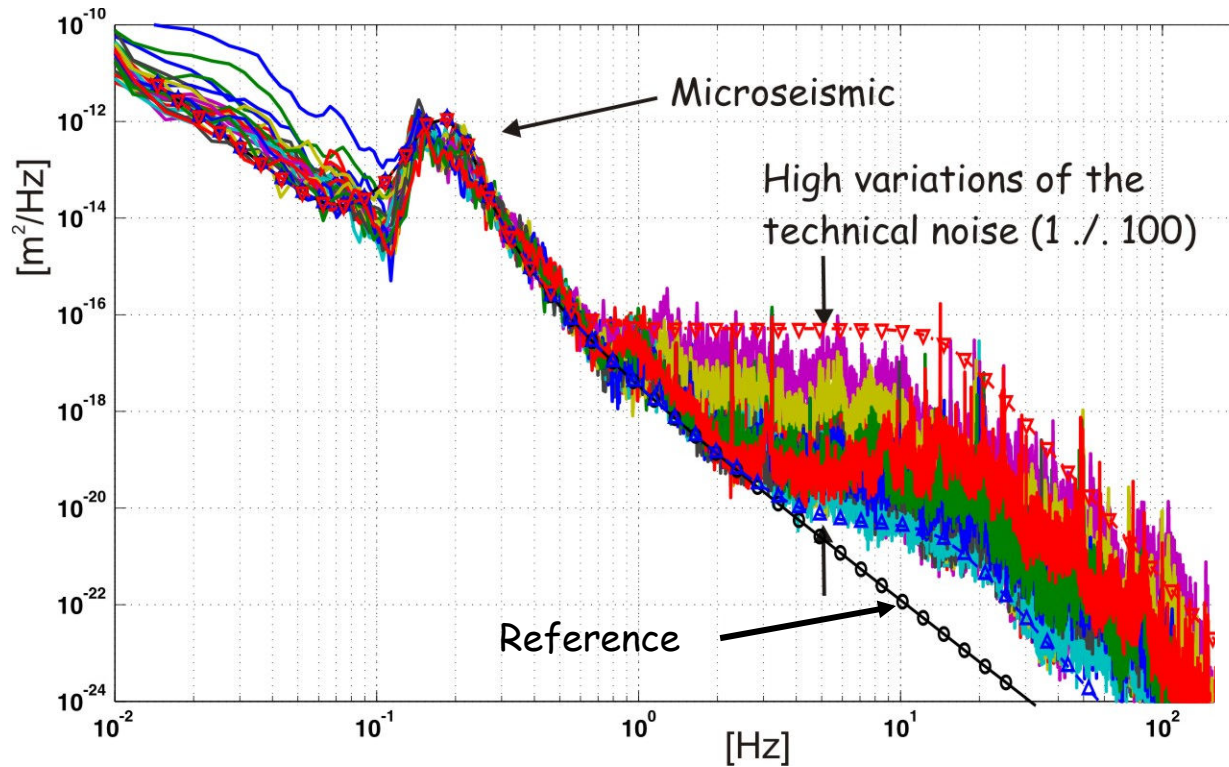
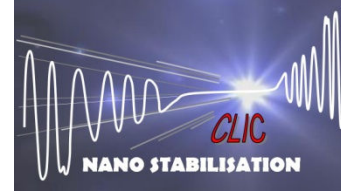
Time domain requirements  
 (**positioning**)



(vertical and lateral)  
 80 quadrupoles/line

# Local excitations

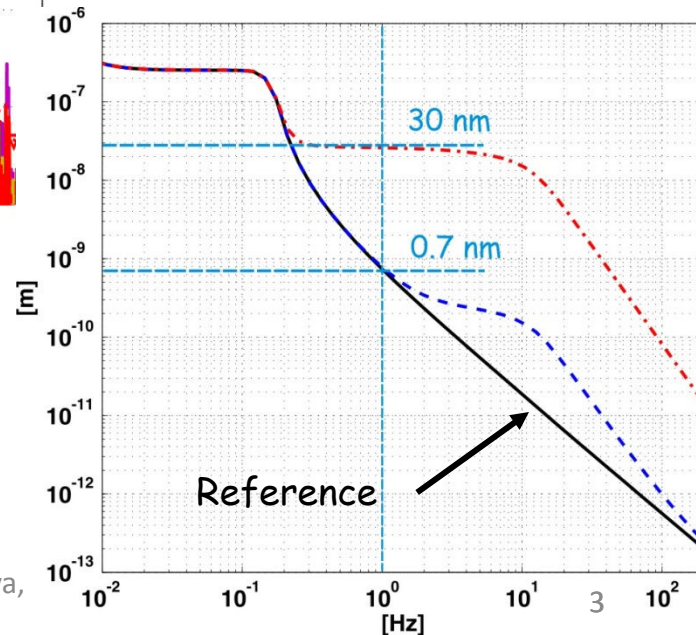
Vertical ground motion



Additional technical noise:

$$N(\omega) = \frac{N_0}{1 + \left(\frac{\omega}{\omega_0}\right)^6}$$

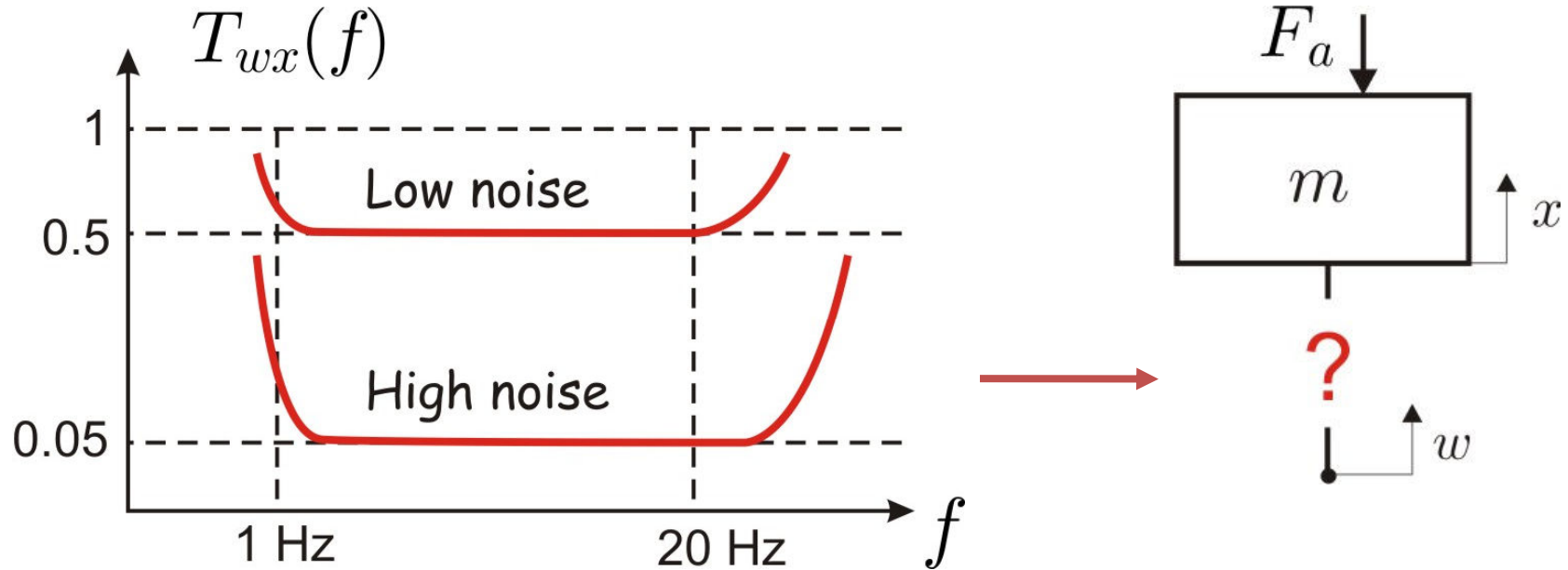
$$f_0 = 2\pi(\text{Hz})$$



Low technical noise:  $N_0 = 5 * 10^{-3} (nm^2/Hz)$

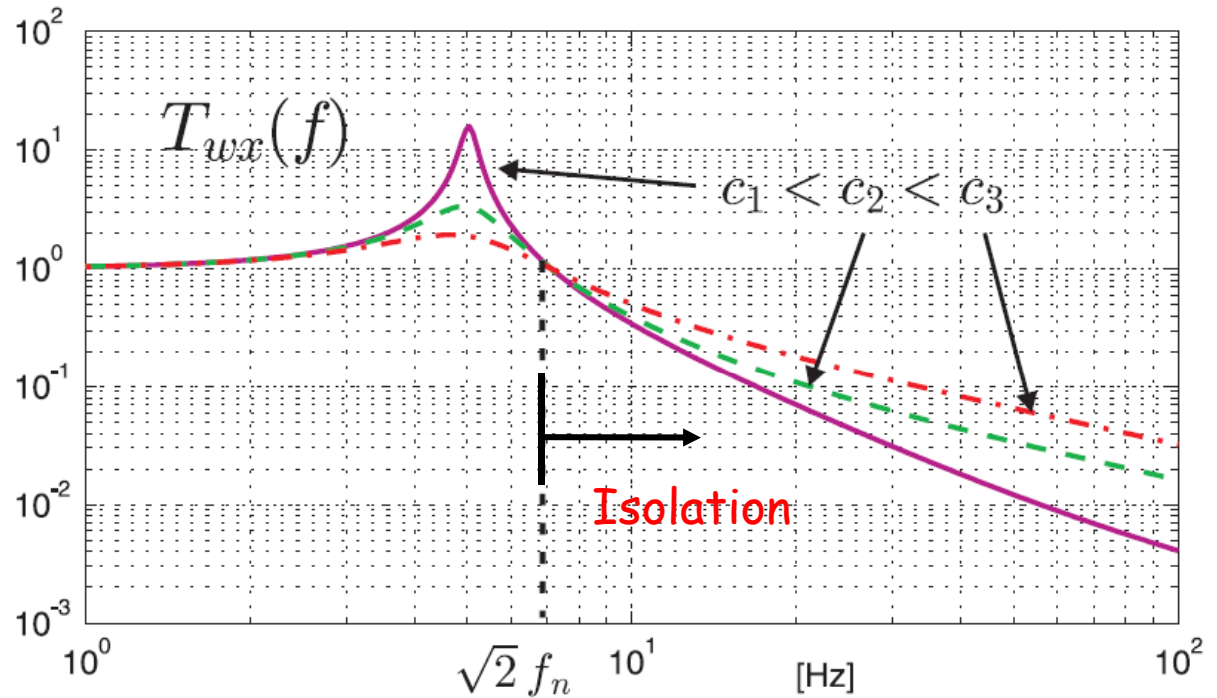
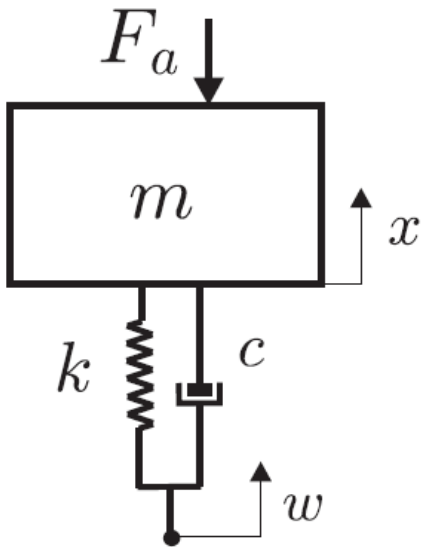
High technical noise:  $N_0 = 50 (nm^2/Hz)$

# How to support the quadrupoles ?



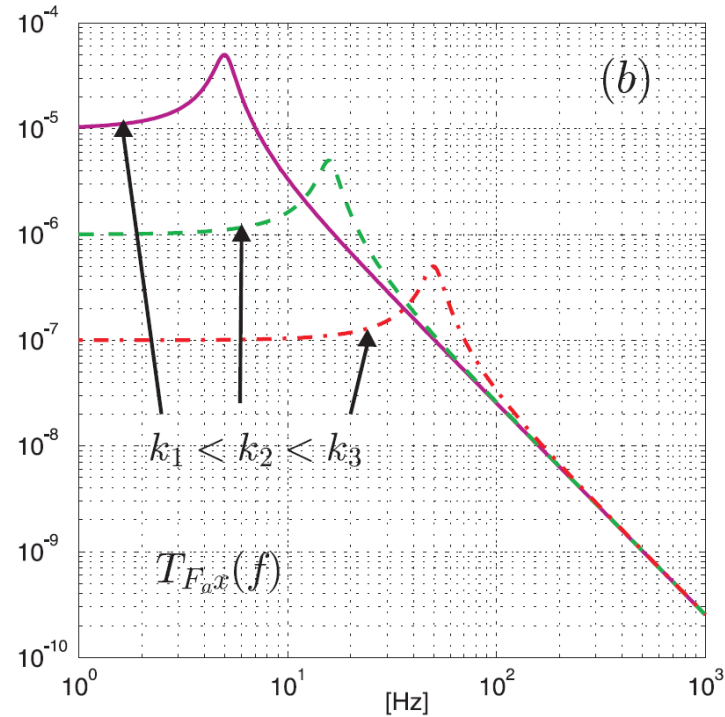
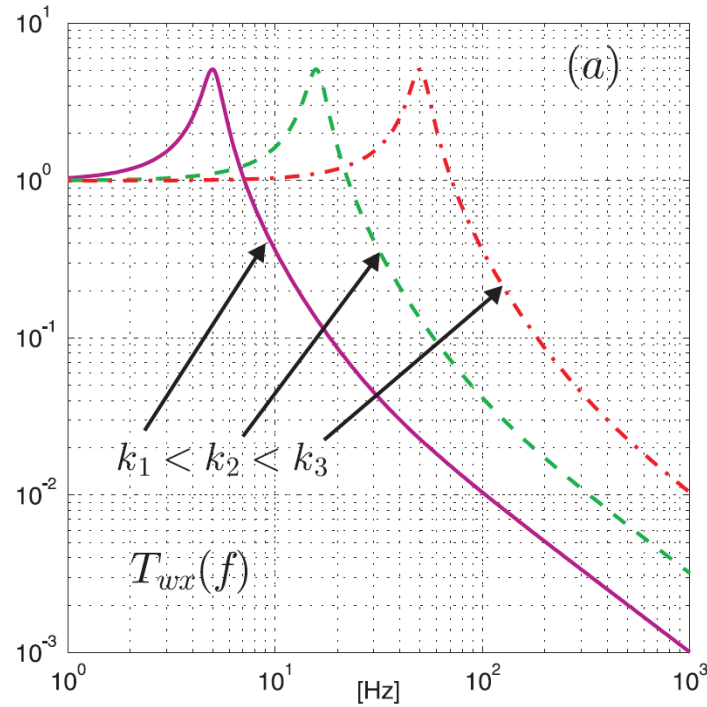
Which type of support can fulfill the requirements ?

# Increase the damping



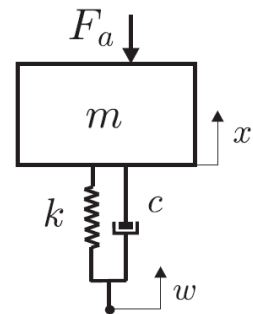
Reduces the overshoot but degrades the isolation at high frequency

# Change the stiffness



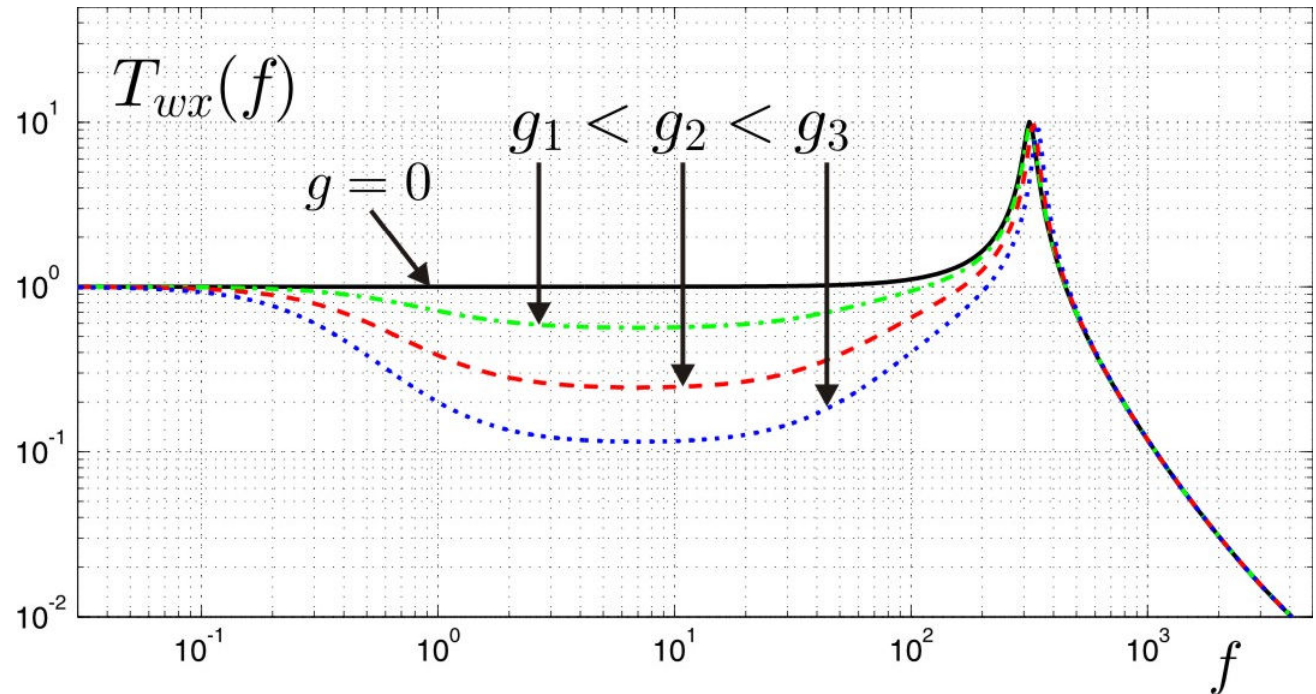
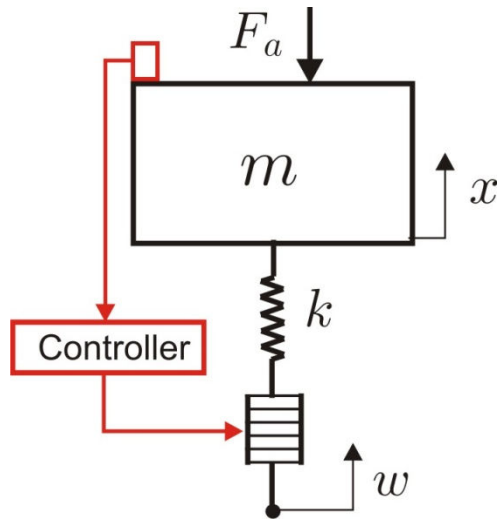
A soft support improves the isolation but :

- (i) Make the quadrupole more sensitive to external forces  $F_a$
- (ii) Cannot be positioned rapidly



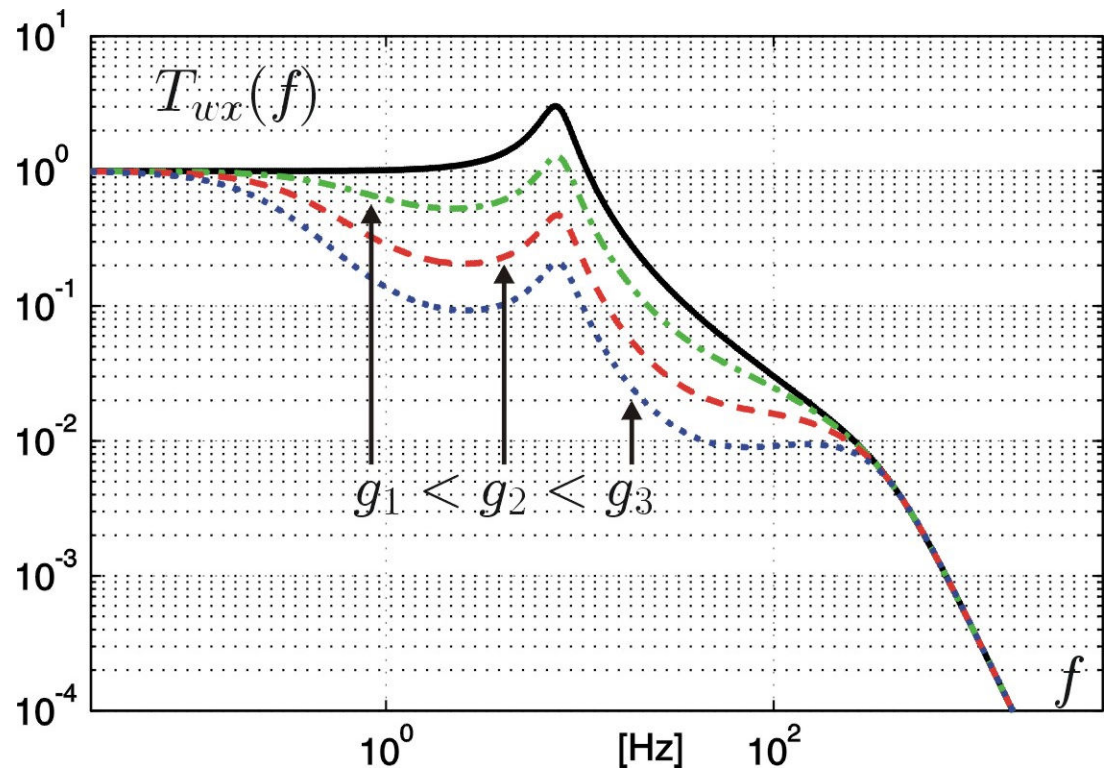
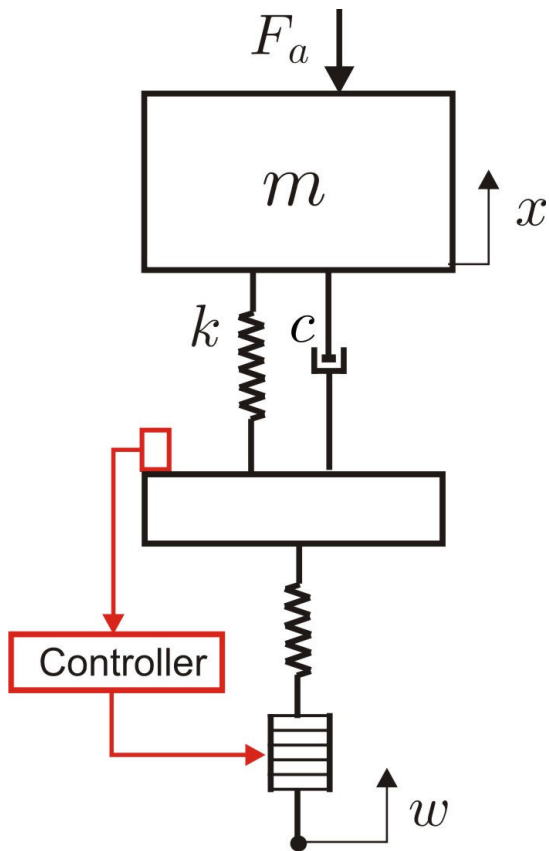
# Control strategy: position feedback

C. Montag (1996, DESY)



# Two stages control

S. Redaelli (CERN, 2004)

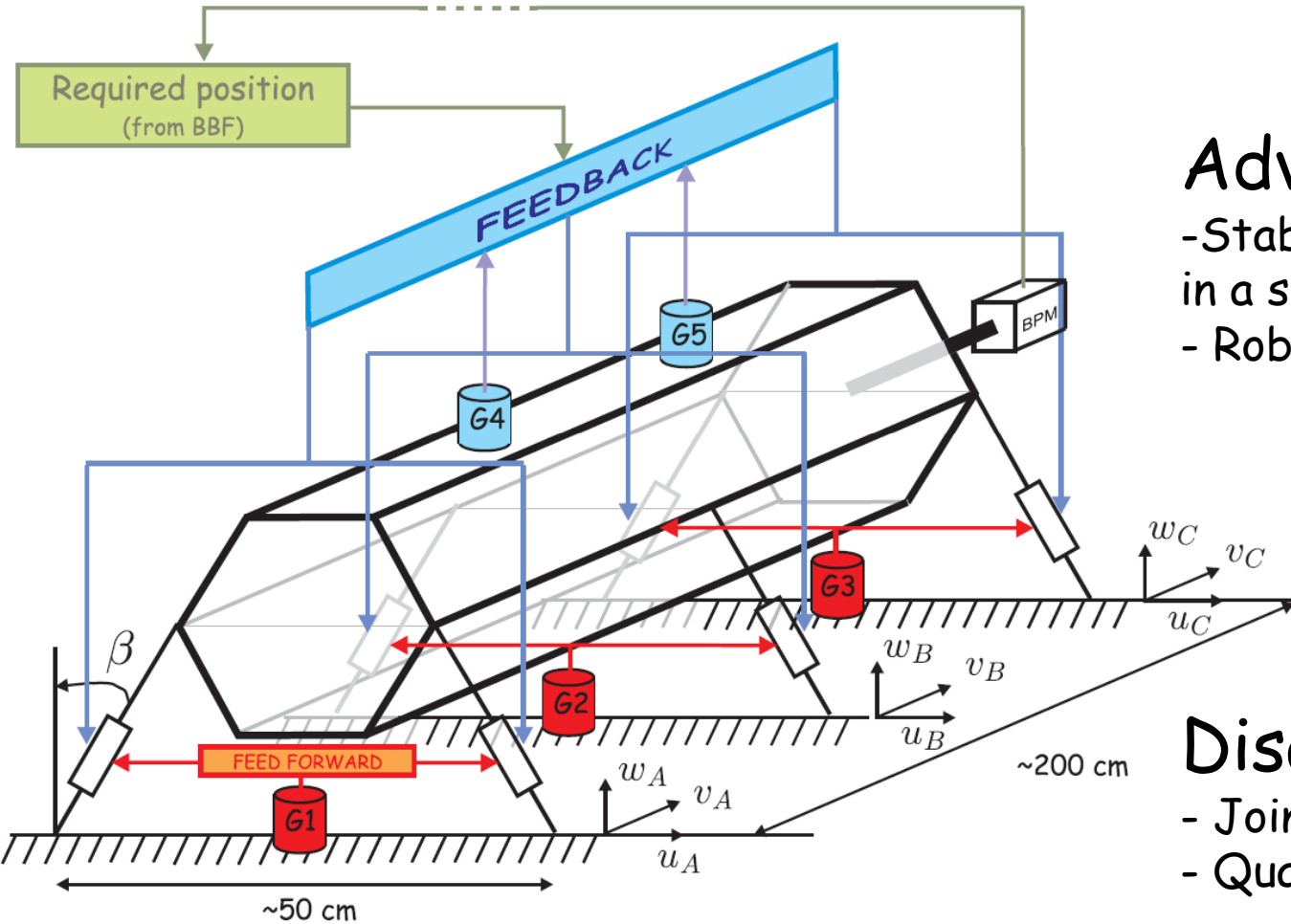




# Comparison

	Stiff support	Soft support
Advantages	<ul style="list-style-type: none"> <li>- Not sensitive to external force</li> <li>- Positioning capabilities</li> <li>- Single stage</li> </ul>	<ul style="list-style-type: none"> <li>- Isolation in a broad frequency range</li> </ul>
Disadvantages	<ul style="list-style-type: none"> <li>- Isolation in a smaller frequency range</li> </ul>	<ul style="list-style-type: none"> <li>- Sensitive to external force</li> <li>- No positioning capabilities</li> <li>- Multi-stage</li> </ul>

# Hexapod concept



## Advantages:

- Stabilization & Positioning in a single stage
- Robust to external forces

## Disadvantages:

- Jointure issues
- Quadrupole flexibility

# System dynamics

Velocity Jacobian  $\dot{\mathbf{q}} = J\dot{\mathbf{x}}$

$$J = \begin{pmatrix} \dots & \dots \\ \mathbf{1}_i^T & -\mathbf{1}_i^T \tilde{\mathbf{p}}_i \\ \dots & \dots \end{pmatrix}$$

Dynamic equations

$$M\ddot{\mathbf{x}} + K\mathbf{x} = B\mathbf{f} + E\mathbf{w}$$

$$\mathbf{f} = (f_1, f_2, \dots, f_6)^T$$

$$K = kBB^T + K_e$$

$$M = \text{diag}(m, m, m, I_\theta, I_\phi, I_\psi)$$

Leg orientations

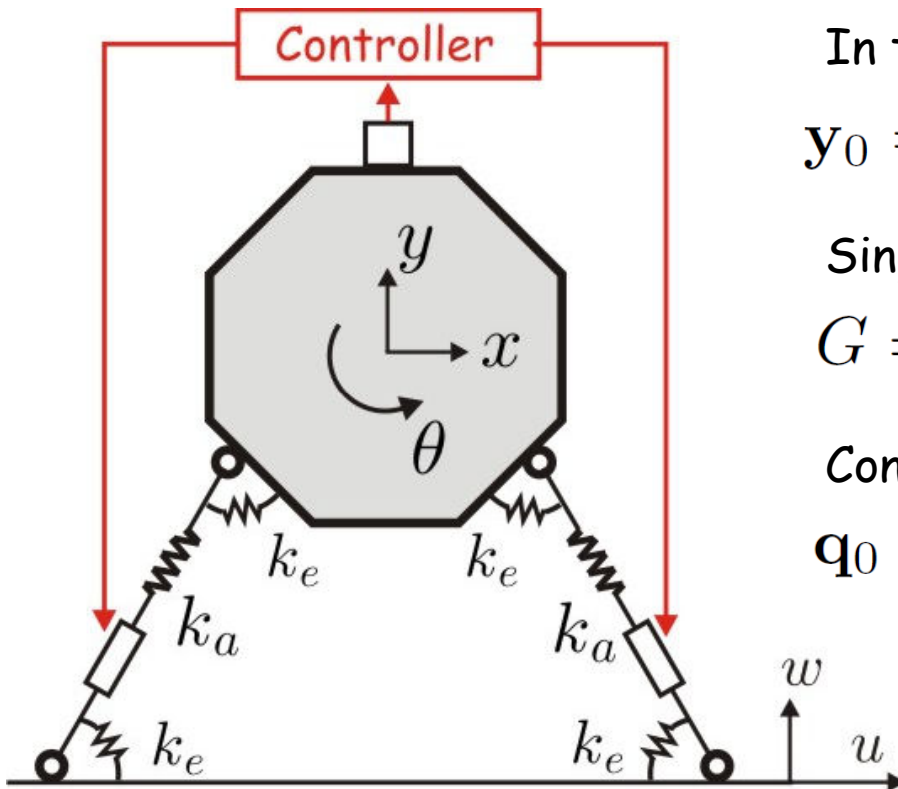
$$Q = \begin{pmatrix} \sin \beta \cos \alpha & \sin \beta \sin \alpha & \cos \beta \\ -\sin \beta \cos \alpha & \sin \beta \sin \alpha & \cos \beta \\ -\sin \beta \sin \alpha & -\sin \beta \cos \alpha & \cos \beta \\ \sin \beta \sin \alpha & \sin \beta \cos \alpha & \cos \beta \\ \sin \beta \cos \alpha & -\sin \beta \sin \alpha & \cos \beta \\ -\sin \beta \cos \alpha & -\sin \beta \sin \alpha & \cos \beta \end{pmatrix}$$

Fixation coordinates

$$P = \begin{pmatrix} -R & R & -R & R & -R & R \\ -L & -L & 0 & 0 & L & L \\ h & h & h & h & h & h \end{pmatrix}$$

Details in ACTIVE CONTROL OF QUADRUPOLE MOTION FOR FUTURE LINEAR PARTICLE COLLIDERS, C. Collette et al., *IASTED International Conference on Intelligent Systems and Control*, Cambridge (2009).

# Two legs



In the observable sub-space:

$$\mathbf{y}_0 = C_0 \mathbf{x}_0 = C_0 J_0^{-1} \mathbf{q}_0 = G \mathbf{q}_0$$

Singular value decomposition:

$$G = U \Sigma V^T \quad \Sigma = \text{diag}(\sigma_1, \dots, \sigma_n)$$

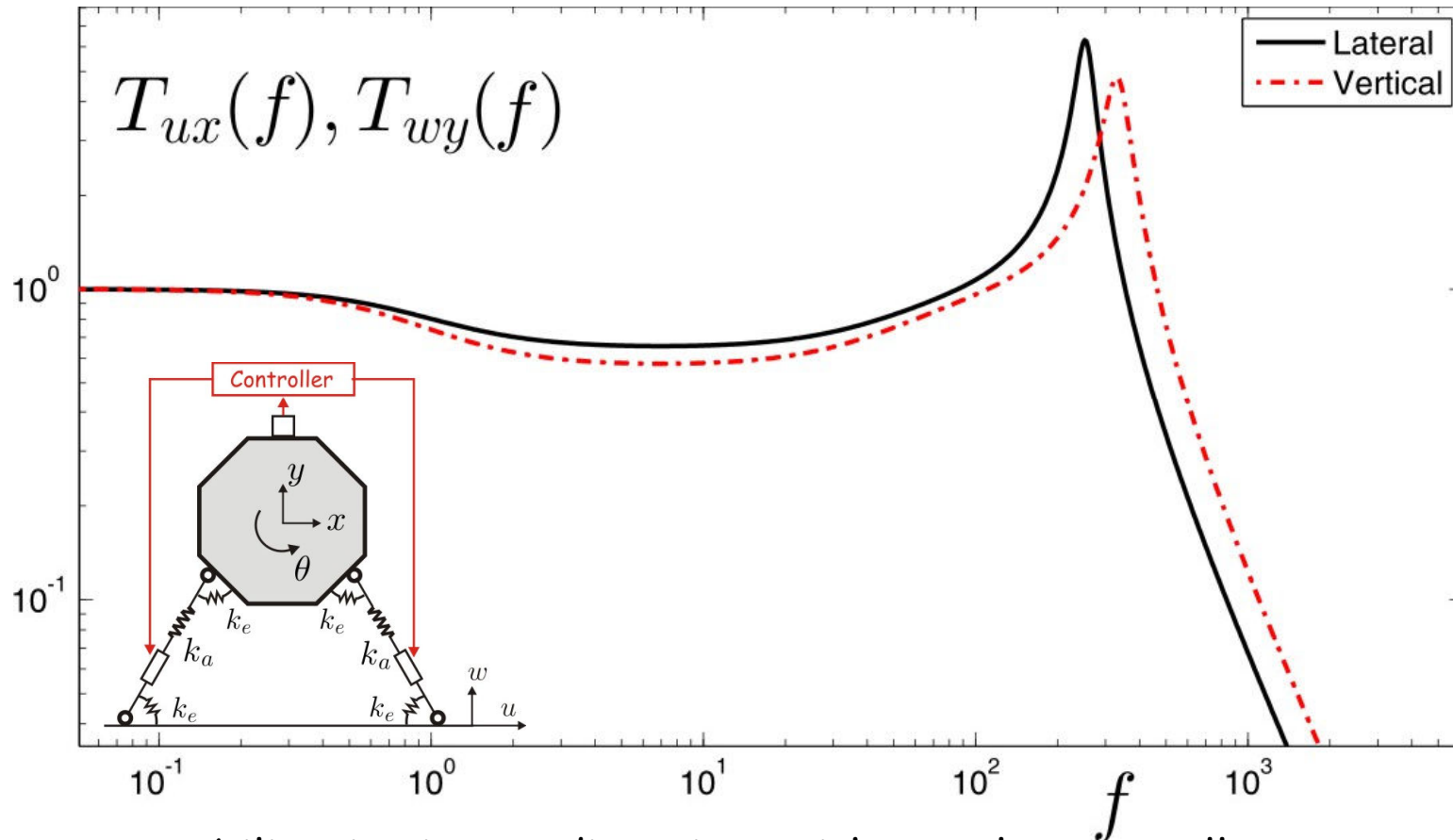
Control strategy:

$$\mathbf{q}_0 = V H(\omega) \Sigma^{-1} U^T \mathbf{y}_0$$

where  $H(\omega) = I h(\omega)$

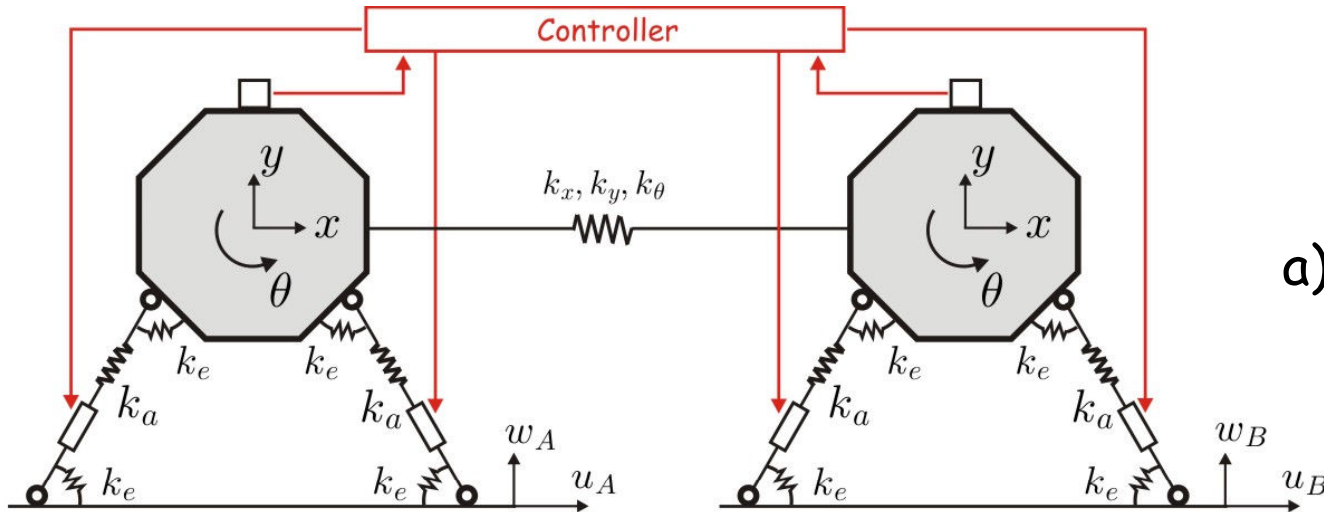
$\sigma_1 / \sigma_n$  is an estimator of the controller performances → Tool for the design

# Two legs

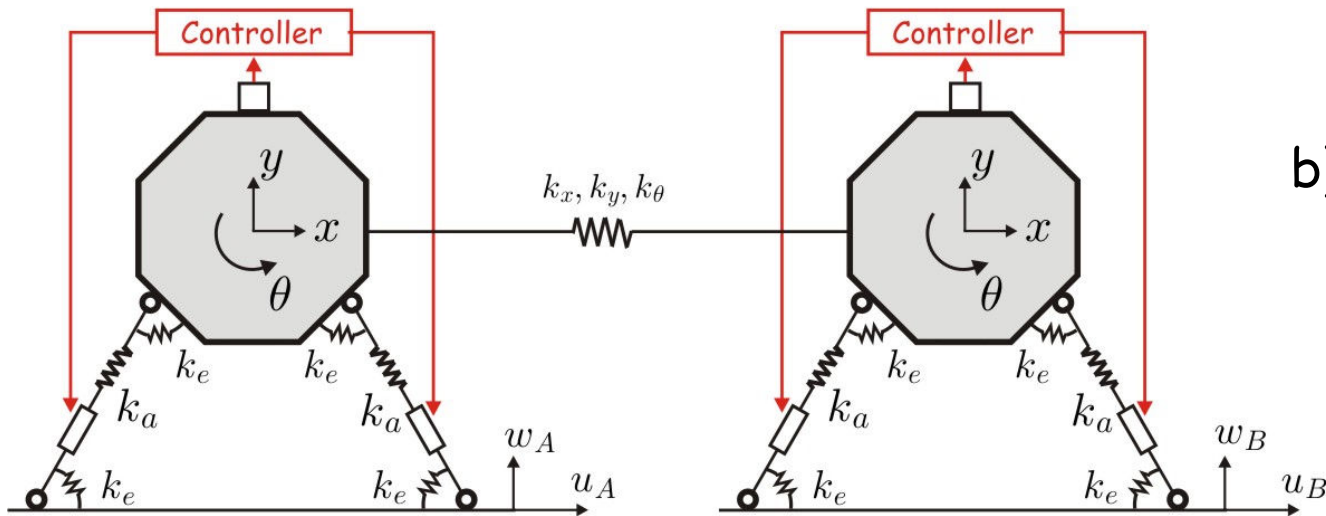


Stabilization in two directions with a scalar controller

# Four legs



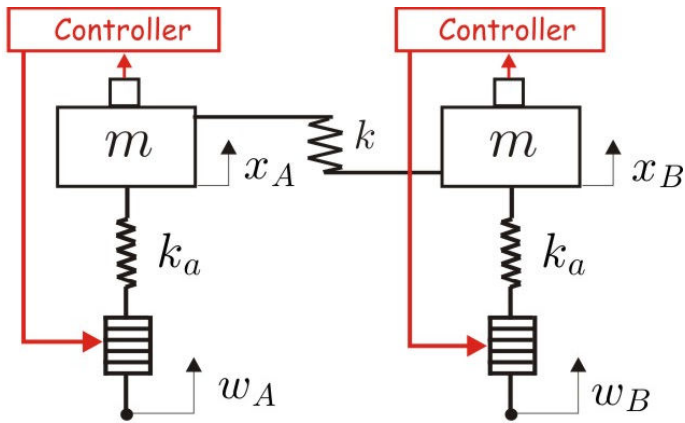
a) Centralized control



b) Decentralized control

# Control architecture

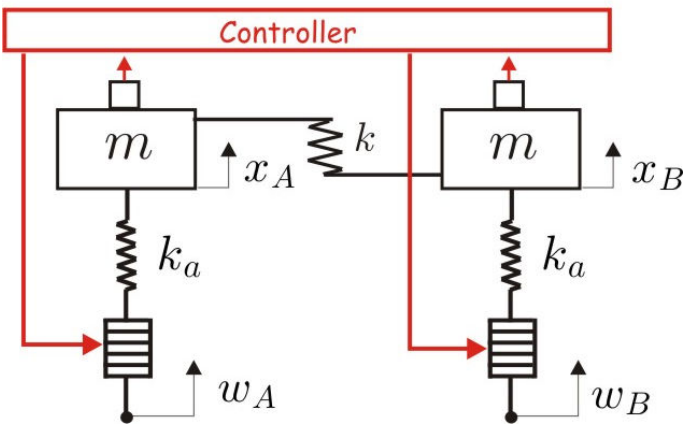
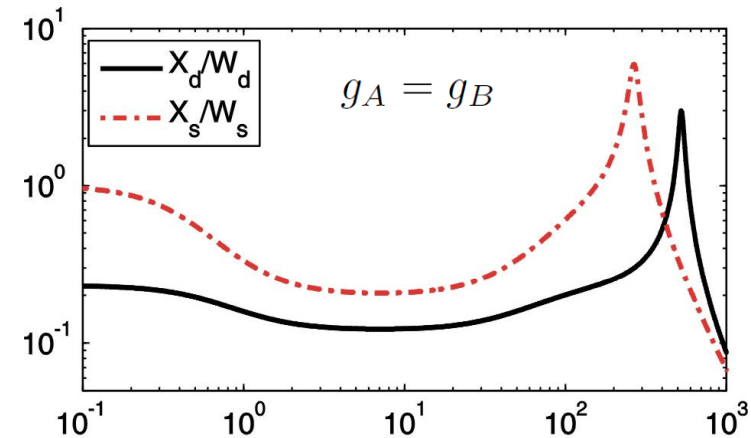
$$X_s = (x_A + x_B)/2; X_d = x_A - x_B; W_s = (w_A + w_B)/2; W_d = w_A - w_B;$$



Decentralized control :

$$\delta_A = g_A x_A$$

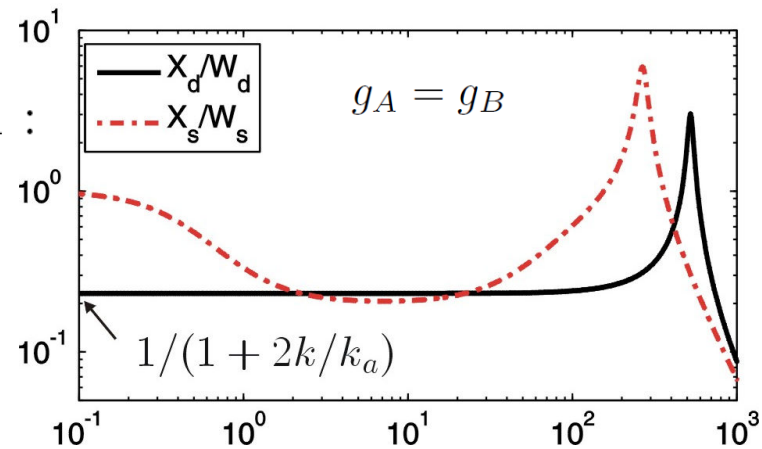
$$\delta_B = g_B x_B$$



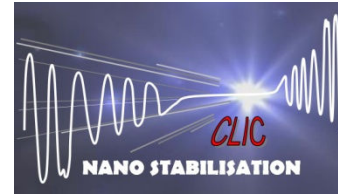
Centralized control :

$$\delta_A = g_A \frac{x_A + x_B}{2}$$

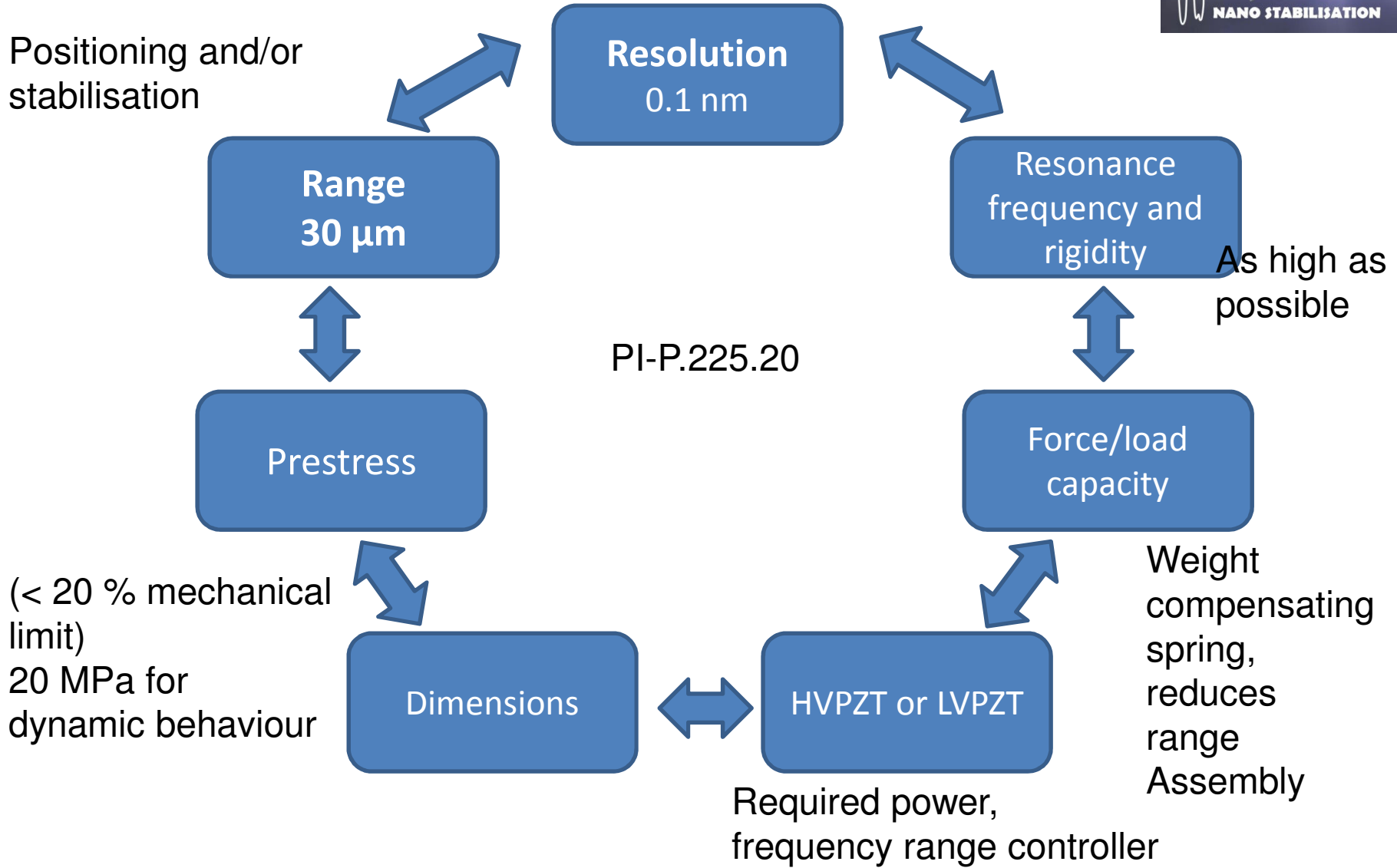
$$\delta_B = g_B \frac{x_A + x_B}{2}$$



# Selection of piezo actuators

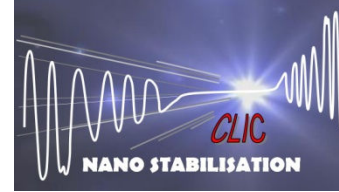


Positioning and/or stabilisation





# Flexible jointure design



## Advantages:

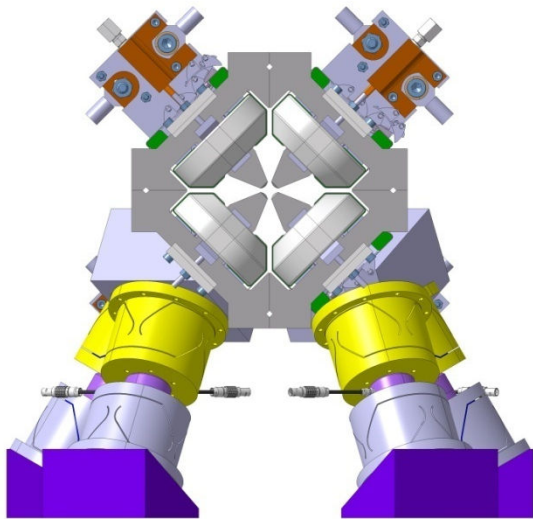
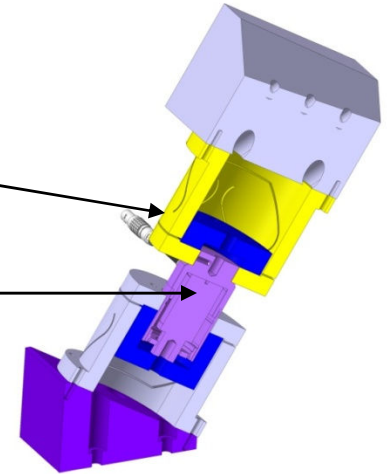
- No friction, no backlash
- Adaptable stiffness

## Disadvantage:

- Requires custom design.

Flexible jointures

Piezoelectric actuator



## Current characteristics:

Rotational rigidity:

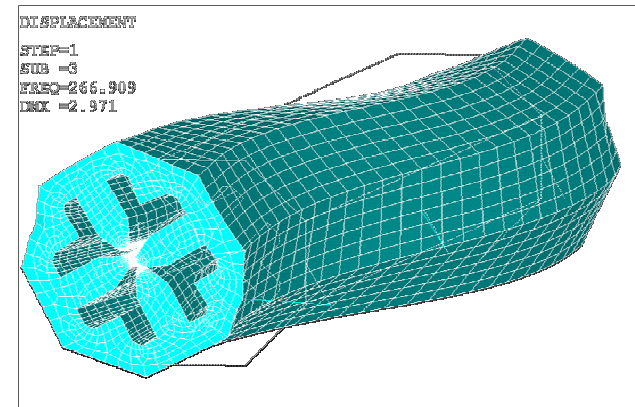
588 Nm/rad

Axial rigidity:

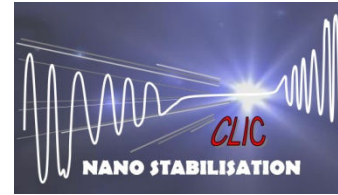
~ 1000 N/ $\mu$ m

Torsional rigidity:

~ 6000 Nm/rad

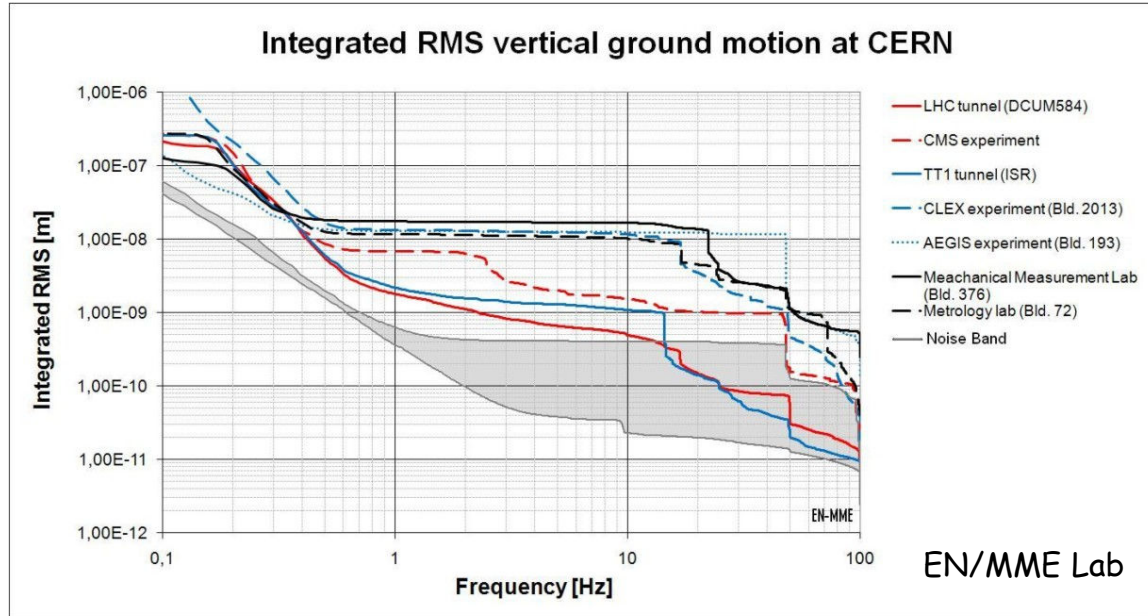
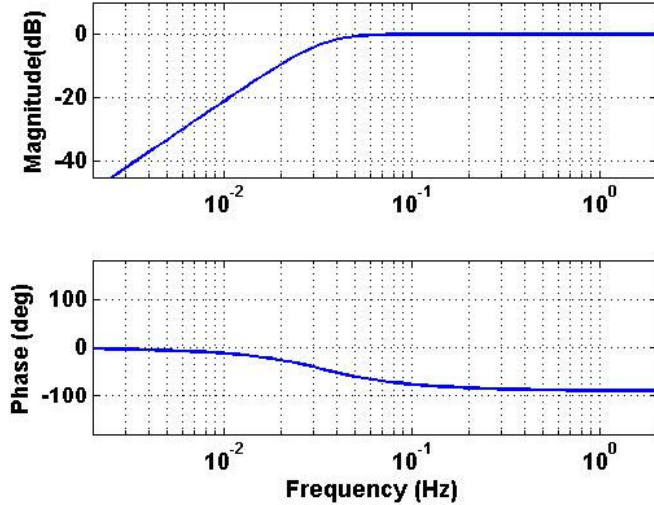


1<sup>st</sup> mode: 266Hz



# Sensor Noise

Sensor GURALP (CMG-6T)

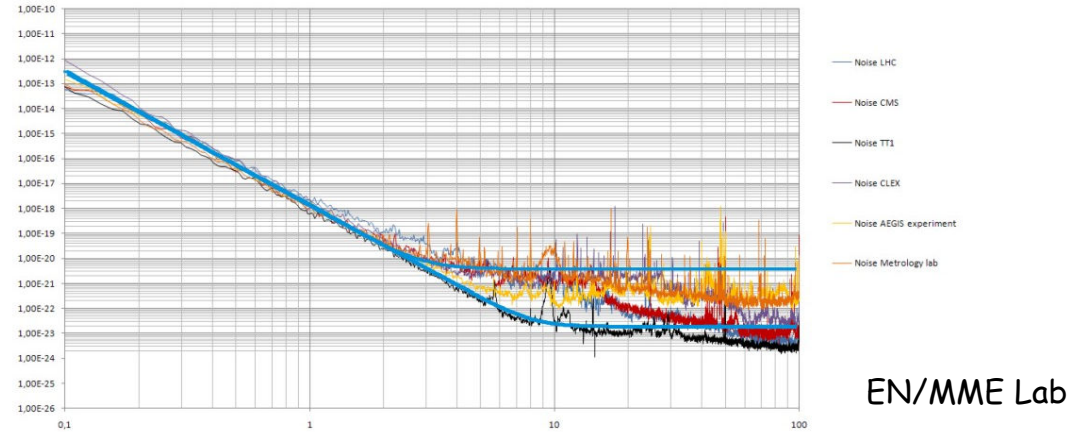


EN/MME Lab

$$\Phi_n(f) = a f^{-5} + b N_0$$

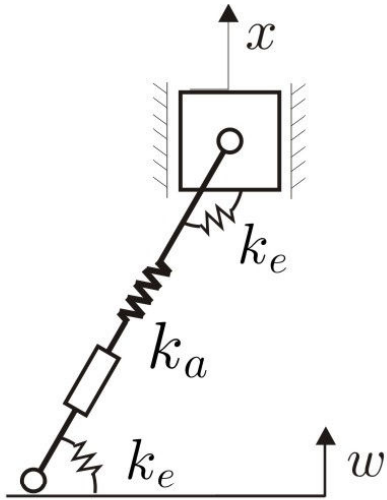
$$a = 10^{-18}; b = 2 * 10^{-4}$$

At high frequency, the sensor noise increases linearly with signal level



EN/MME Lab

# Scaled set up

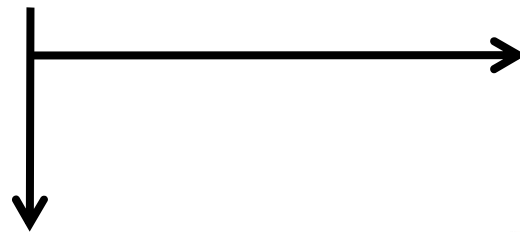


Full scale quadrupole :

- $m = 420/6 = 70 \text{ kg}$
- $k = 250 \text{ MN/m}$

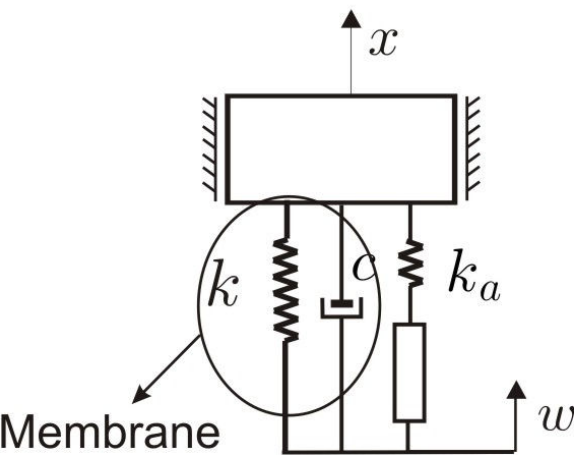
Scaling laws:

- $m = a_m m'$
- $k = a_k k'$
- $\omega = a_\omega \omega'$



Scaled set-up :  $a_\omega \simeq 1$

- $m' = 2.5 \text{ kg} \Rightarrow a_m = 28$
- $k' = 1 \text{ MN/m} \Rightarrow a_k = 25$



# Experimental results

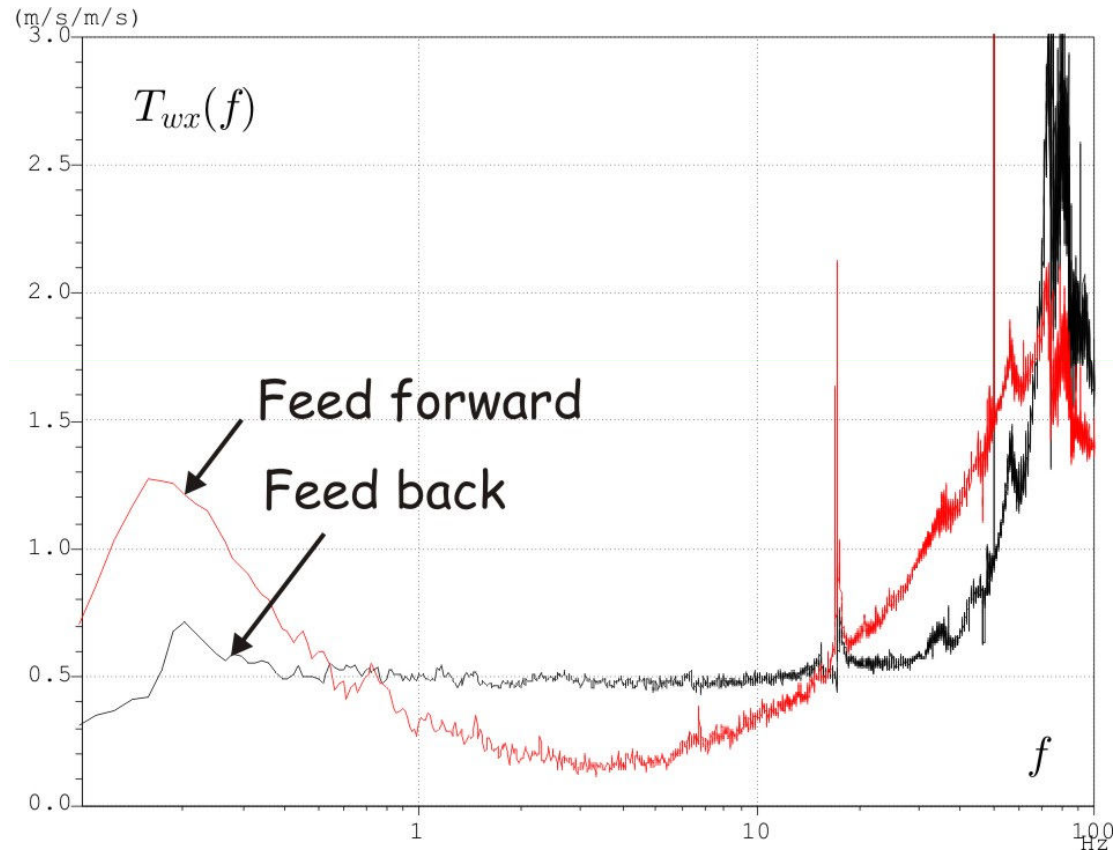
Results obtained in the lab

Feedback :

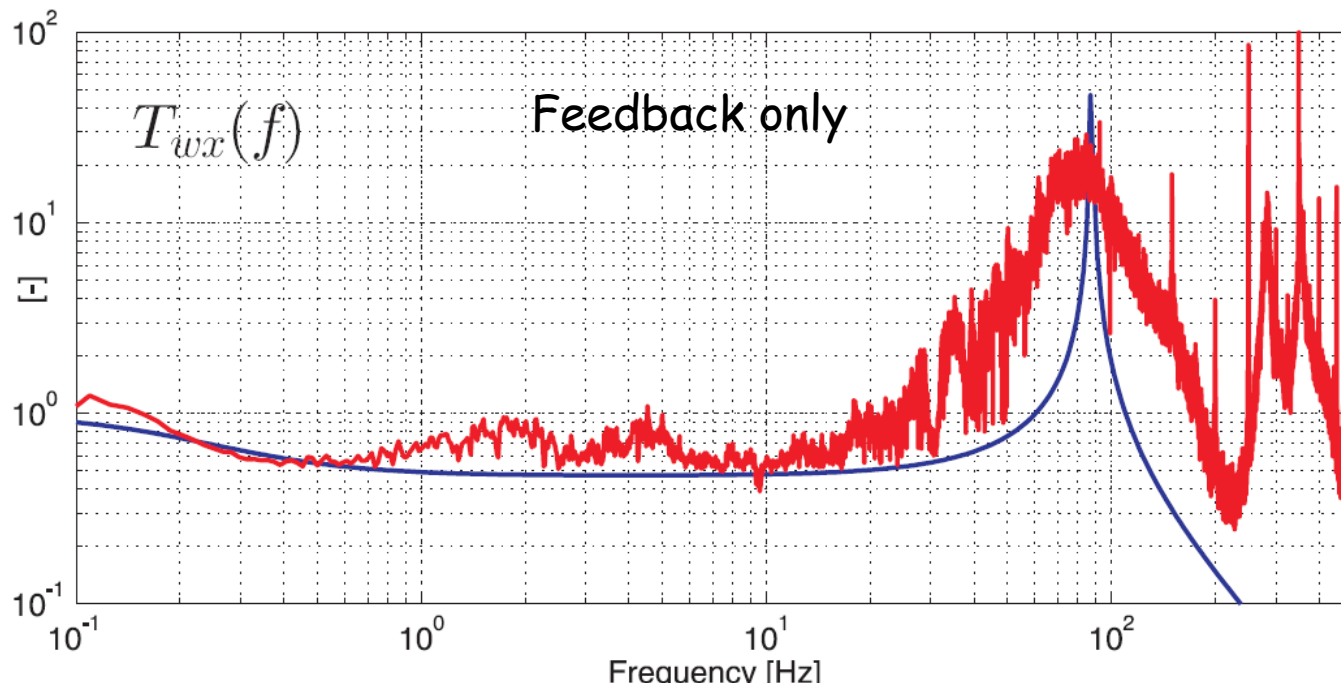
$$F_b = k\delta = K_p^b x$$

Feed forward :

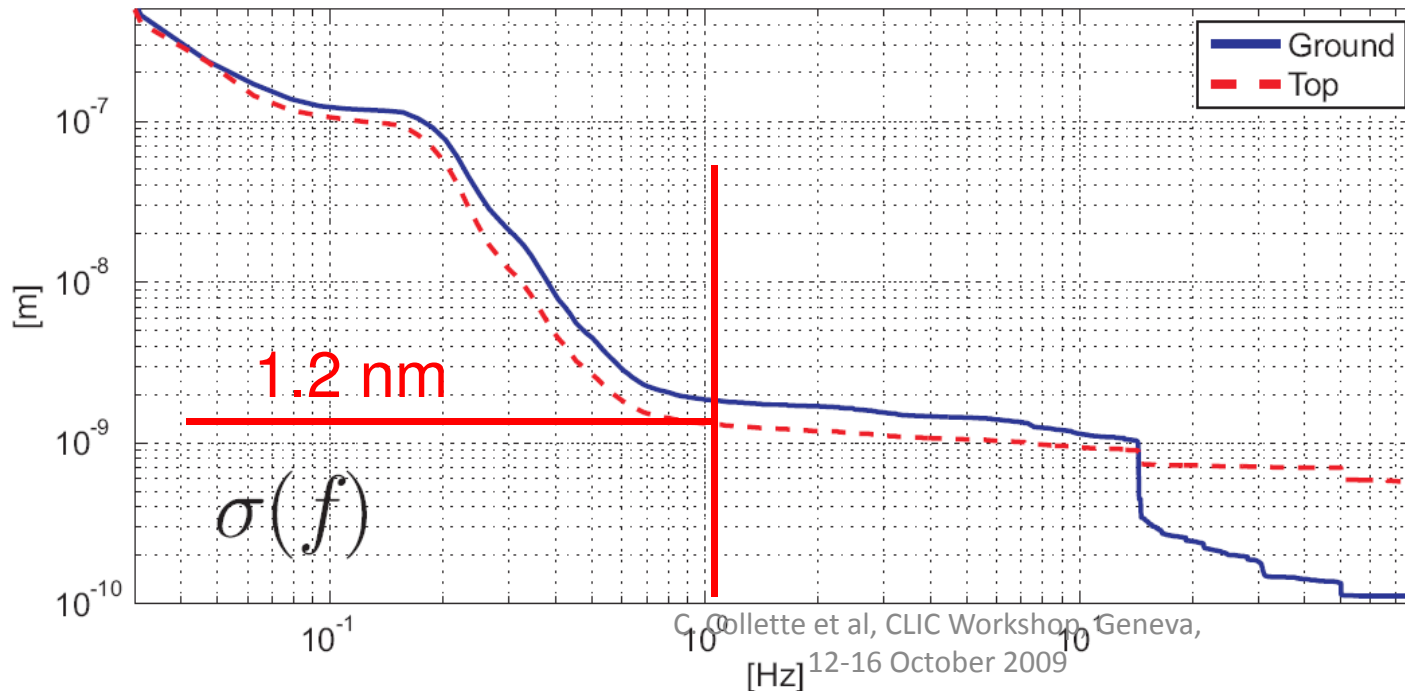
$$F_f = k\delta = K_p^f w$$



Feed forward works better in a narrow frequency range

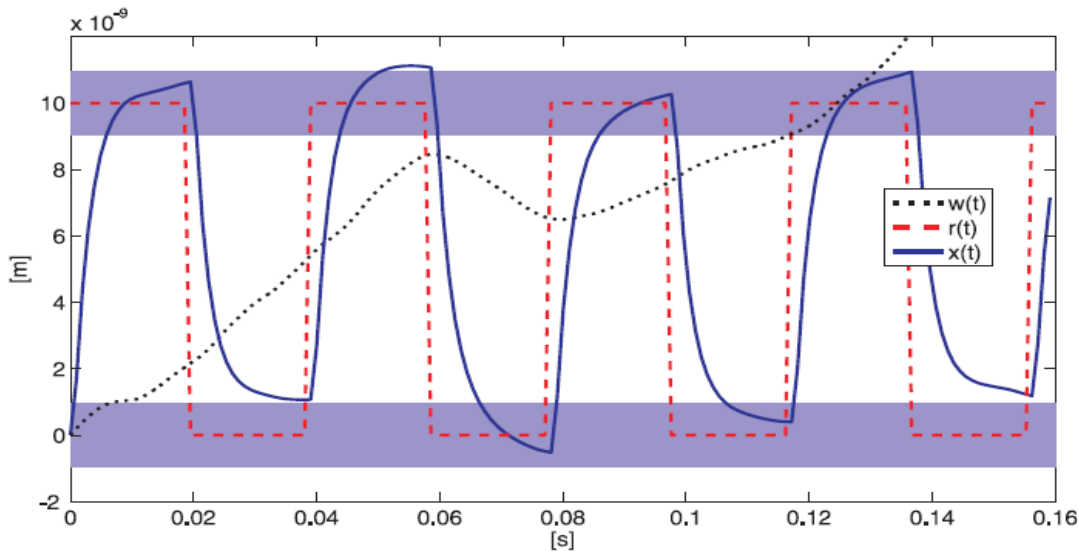
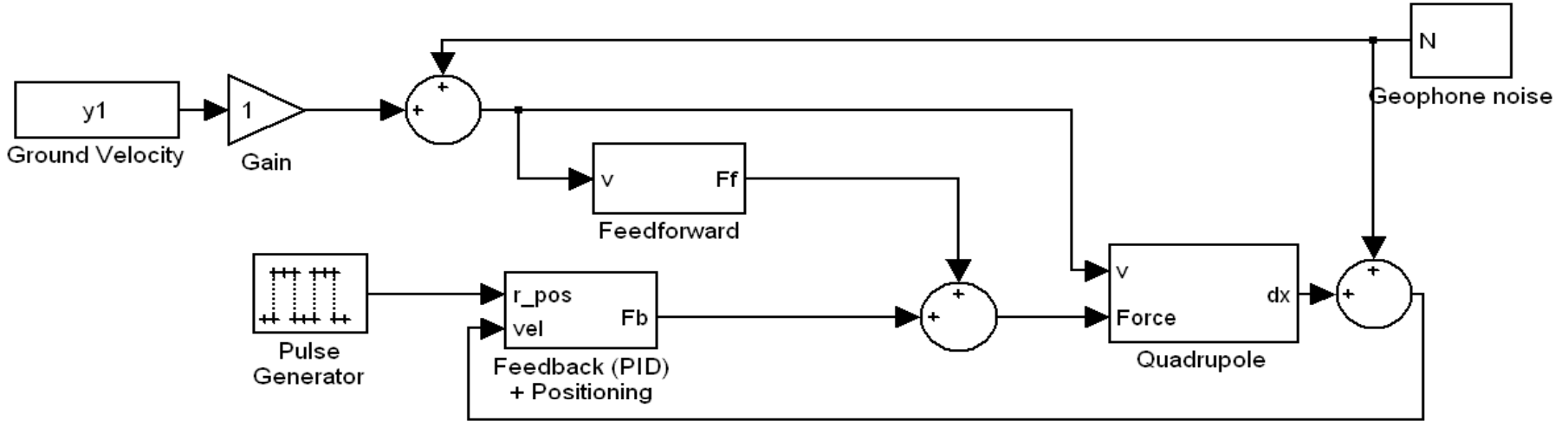


Results  
 obtained in a  
 quiet place  
 (TT1)



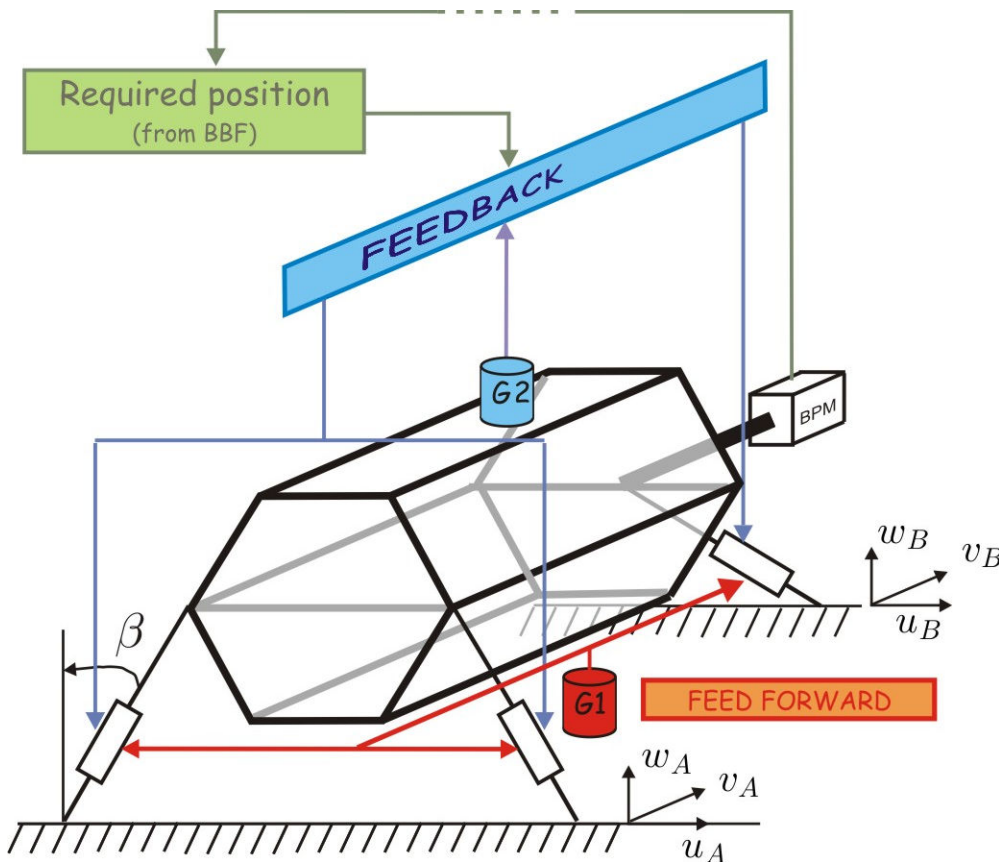
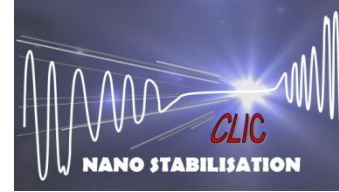
Better results  
 are expected  
 with a more  
 adapted  
 hardware  
 (resolution,  
 noise...)

# Positioning



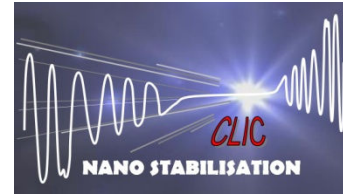
To be tested experimentally on the membrane

# Intermediate experiment: Tripod



Difficulties addressed:

- Heavy load
- Actuators and sensors
- Control law
- Flexible jointure
- Positioning capability



# Conclusions

- Technical noise model
- Hexapod concept and dynamics
- Issues discussed: decentralized controller, jointure design, actuator and sensor choice
- RMS integrated of 1,2 nm with a dedicated scaled bench
- Supports include positioning capabilities