

# Colour-dipole cascades involving initial-state partons

[MCnet meeting in Lund]

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Jan Winter <sup>a</sup>

PPD/Theory, Fermilab



- Extension of the Colour Dipole Model (CDM): final–initial and initial–initial dipole radiation pattern.
- Survey of first dipole-shower results.

..... based on *arXiv:0712.3913*.

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<sup>a</sup> SHERPA authors: T. Gleisberg, S. Höche, F. Krauss, M. Schönherr, F. Siegert, S. Schumann, J. W.

<http://www.sherpa-mc.de/>

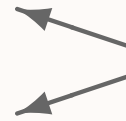
# Parton showers ... recent developments.

- New physics challenges (LHC), rewrites of PYTHIA/HERWIG codes **plus**
- enormous progress in the techniques of combining (N)LO calculations with parton showers led to an **intensive overhaul of existing formulations.**
- Efforts aim at ...
  - *achieving better analytic control.*
  - *gaining better understanding of systematic uncertainties.*
  - *providing (easier/more consistent) merging/matching with LO/NLO calculations.*
  - *going beyond common approximations (LL, large  $N_C$ , include small- $x$ )?*
- New **1 → 2 splittings** showers, for PYTHIA and HERWIG, and new shower formulation based on Catani–Seymour dipole factorization.
- Still other ways to identify/pick leading logs of multiple QCD emissions?  
**Yes. 2 → 3 splittings. → VINCIA.** And, of course, the successful Lund CDM as implemented in **ARIADNE.**

# The Colour Dipole Model (CDM)

Alternative to conventional Altarelli–Paris parton showers // same principles.

- soft gluons intrinsically correct
- colour coherent emission



Exponentiation of soft gluon limit

- QCD antenna pattern

$$d\sigma = \frac{8\alpha_s}{3\pi} \frac{d\omega_g}{\omega_g} dy_g = \frac{4\alpha_s}{3\pi} \frac{dx_1 dx_3}{(1-x_1)(1-x_3)}$$

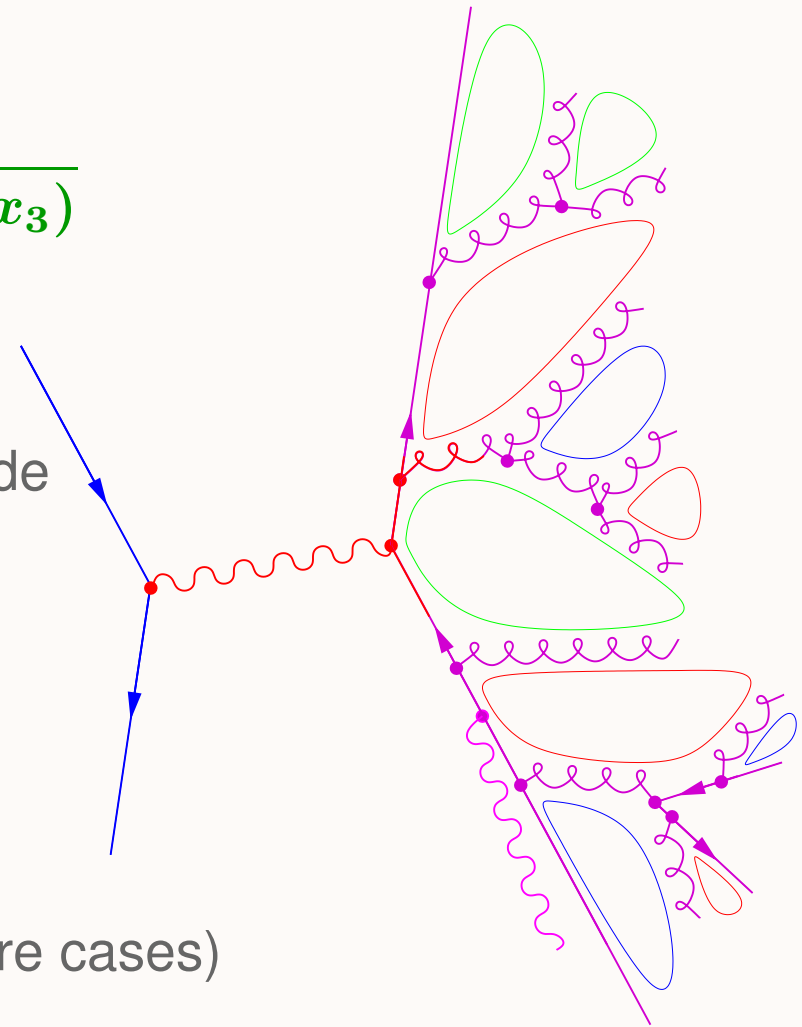
corrigible for hard bremsstrahlung (spin!)  
recall PS: ME corr. + conar conditions

- semiclassical probabilistic picture for dipole cascade

$q\bar{q}$  emits  $g$ , in turn  $q'g\bar{q}'$  may emit softer  $g'$   
 $q'\bar{q}'$  contribution neglected ( $1/N_C^2$  supp.)

- onshell kinematics; no momentum reshuffling
- emitters almost independent of rest of tree

- $2 \rightarrow 3$  splittings somewhat more complicated (more cases)
- gluon splitting not naturally, easily included



# CDM for timelike evolution

**Pioneering works:** Azimov, Dokshitzer, Khoze, Troyan / Gustafson, Pettersson, Andersson, Lönnblad

● Splitting functions ( $g$  emit):  $x_i$  inv  $E$ -fracs; AP limit!  $\frac{d\sigma_{2\rightarrow 3}}{dx_1 dx_3} = \frac{2\alpha_s}{3\pi} \left[ 1 + \frac{1}{8}\Theta(g_{1,3}) \right] \frac{x_1^{2+\Theta(g_1)} + x_3^{2+\Theta(g_3)}}{(1-x_1)(1-x_3)}$

● Evolution variables

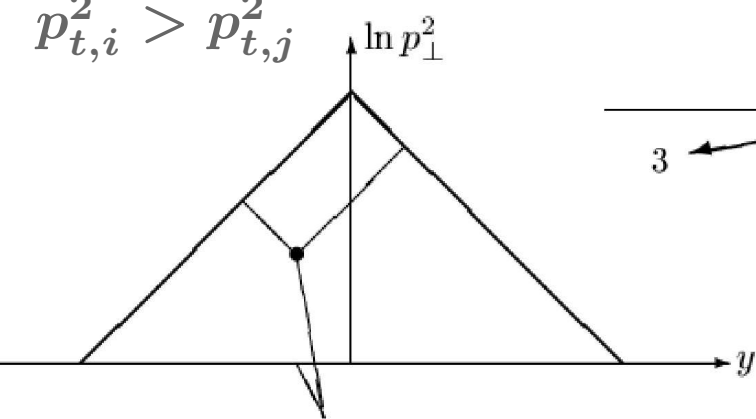
$$p_t^2 = M^2(1-x_1)(1-x_3), \quad y = \frac{1}{2} \ln \frac{1-x_1}{1-x_3} \quad \rightarrow \quad \boxed{d\sigma_{2\rightarrow 3} \propto \alpha_s \frac{dp_t^2}{p_t^2} dy}$$

● Sudakov exponentiation

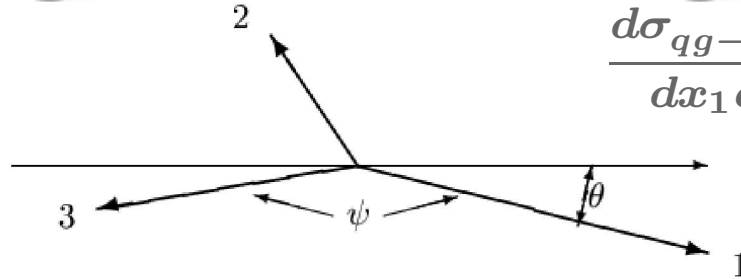
$$\frac{dP}{dp_t^2 dy} = \frac{d\sigma_{2\rightarrow 3}}{dp_t^2 dy} \exp \left( - \int_{p_t^2}^{p_{t,\max}^2} dk_t^2 \int_{y_{\min}(k_t^2)}^{y_{\max}(k_t^2)} dy' \frac{d\sigma_{2\rightarrow 3}}{dk_t^2 dy'} \right)$$

● Ordering

$$p_{t,i}^2 > p_{t,j}^2$$



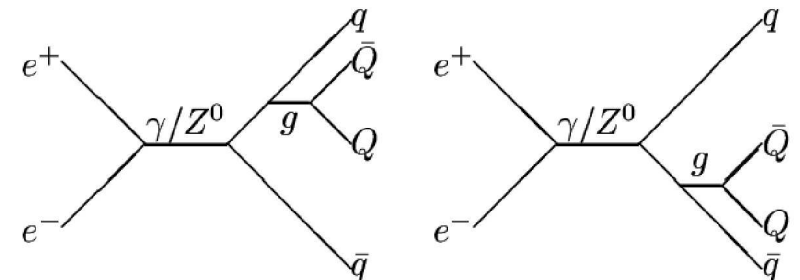
● Recoils



$q\bar{q}$  Kleiss  
 $qg, gg$  minimize  $p_{\perp}$ 's

● Gluon splitting (competition)

$$\frac{d\sigma_{qg \rightarrow qQ\bar{Q}}}{dx_1 dx_3} = \frac{N_F \alpha_s}{8\pi} \frac{(1-x_2)^2 + (1-x_3)^2}{1-x_1}$$

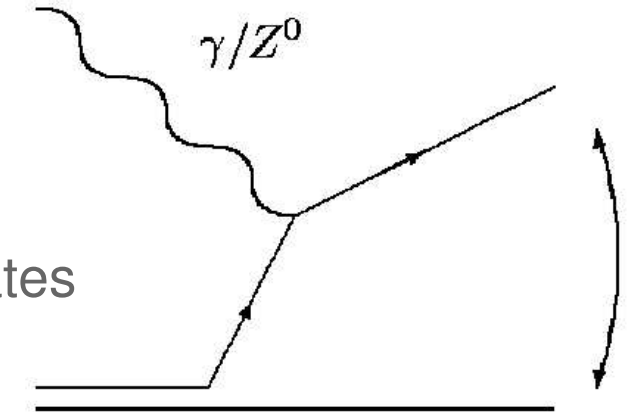


# Lund CDM for DIS & hadron-hadron collisions

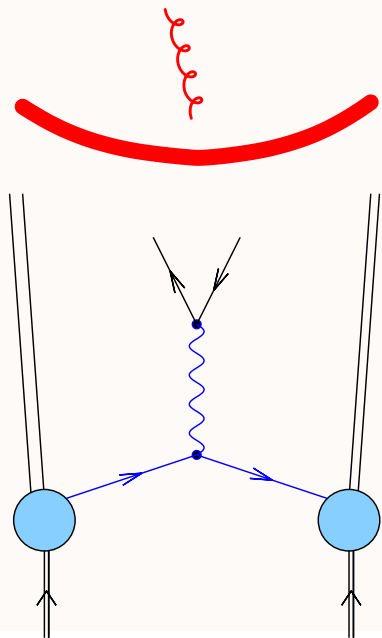
Bo Andersson et al. Z. Phys. C 43 (1989) 625.

QCD cascade is **not** divided in IS and FS.

- Struck **quark** pointlike. Hadron **remnant** extended.
- Suppression of the emission of small wavelengths from extended antennae.
- Only a fraction of remnant's light-cone momentum participates in emission of  $p_{\perp}$  (extra tunable parameter).

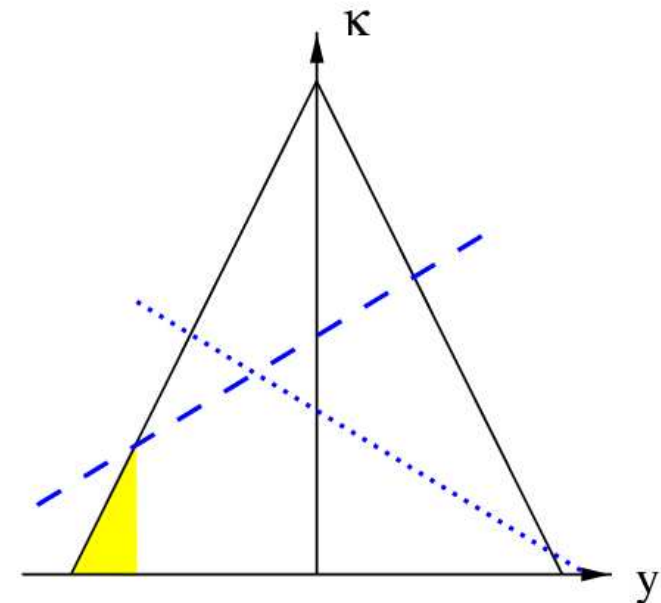


## Leif Lönnblad: Small-x effects in $W + \text{jets}$ at the Tevatron (CERN-TH/95-212)



Jan Winter

- Boson not intrinsically coupled.
- Boson's transverse momentum through recoil transfer according to a phase-space measure.
- 1st emission also ME corrected.



# Gluon emission from colour dipoles

→ Differential cross section for a  $\tilde{k}\tilde{\ell} \rightarrow kgl$  dipole splitting:

$$d\mathcal{P}_{\tilde{k}\tilde{\ell} \rightarrow kgl} \equiv \frac{d\sigma_{0 \rightarrow kgl}}{d\sigma_{0 \rightarrow \tilde{k}\tilde{\ell}}} = \frac{\alpha_s(\mu_R)}{2\pi} D_{\tilde{k}\tilde{\ell} \rightarrow kgl}(p_\perp, y) \frac{dp_\perp^2}{p_\perp^2} dy$$

→ Studying the pure final-state case:  $\tilde{k} = k = f, \quad \tilde{\ell} = \ell = \bar{f}', \quad f = q, g$

$$d\Gamma_{0 \rightarrow fg\bar{f}'} \simeq d\Gamma_{0 \rightarrow f\bar{f}'} \frac{C\alpha_s}{2\pi} \hat{D}_{f\bar{f}' \rightarrow fg\bar{f}'}(p_\perp, y, \varphi) dp_\perp^2 dy \frac{d\varphi}{2\pi}$$

using dipole phase-space and matrix-element factorization:

$$d\Phi_{0 \rightarrow fg\bar{f}'}(p_0; p_f, p_g, p_{\bar{f}'}) = d\Phi_{0 \rightarrow f\bar{f}'}(\tilde{p}_0 = p_0; \tilde{p}_f, \tilde{p}_{\bar{f}'}) \frac{ds_{fg} ds_{g\bar{f}'}}{16\pi^2 M^2} \frac{d\varphi}{2\pi}$$

$$|\mathcal{M}_{0 \rightarrow fg\bar{f}'}|^2 \simeq 8\pi\alpha_s C \hat{D}_{f\bar{f}' \rightarrow fg\bar{f}'} |\mathcal{M}_{0 \rightarrow f\bar{f}'}|^2 \quad \rightarrow D_{f\bar{f}' \rightarrow fg\bar{f}'}(p_\perp, y)$$

→ Instead of redefining ISR in terms of FSR,

$$= \xi C p_\perp^2 \hat{D}_{f\bar{f}' \rightarrow fg\bar{f}'}(p_\perp, y)$$

$$\tilde{k}\tilde{\ell} \rightarrow \begin{cases} \tilde{k} g_f \tilde{\ell} & : \text{ gluon emission,} \\ q g_i \tilde{\ell} & : \text{ quark emission, provided that } \tilde{k} = \bar{q}_i, \\ \tilde{k} g_i \bar{q} & : \text{ antiquark emission, provided that } \tilde{\ell} = q_i. \end{cases}$$

# Gluon emission from colour dipoles

## → Generalizing the kinematic framework:

- momentum balances,  $\varsigma_0 = \pm 1$  (+ for // dipoles),  $\tilde{\varsigma}_m, \varsigma_m = \pm 1$  (+ outgoing, - incoming),

$$-\varsigma_0 \tilde{p}_0 = \tilde{\varsigma}_k \tilde{p}_k + \tilde{\varsigma}_\ell \tilde{p}_\ell, \quad -\varsigma_0 p_0 = \varsigma_k p_k + \varsigma_g p_g + \varsigma_\ell p_\ell$$

- dipole invariant masses,

$$\tilde{p}_0^2 = p_0^2 = M^2 = s_{kg} + s_{gl} + s_{kl} = s_{kgl} = -Q^2$$

- invariant energy fractions and parton-system invariant masses,

$$x_m = \frac{2 p_m p_0}{p_0^2}, \quad s_{mn} = (\varsigma_m p_m + \varsigma_n p_n)^2, \quad s_{mnr} = (\varsigma_m p_m + \varsigma_n p_n + \varsigma_r p_r)^2$$

## → Lorentz invariant evolution variables:

$$p_\perp^2 = \left| \frac{s_{kg} s_{gl}}{s_{kgl}} \right|, \quad y = \frac{1}{2} \ln \left| \frac{s_{gl}}{s_{kg}} \right|; \quad |s_{kg}| = |M| p_\perp e^{-y}, \quad |s_{gl}| = |M| p_\perp e^{+y}$$

# Gluon emission from colour dipoles

→ Similarly apply to II dipoles:

$$d\sigma_{\bar{v}'i(gi)\rightarrow 0g(0q)} \simeq d\sigma_{\bar{v}'i(\bar{q}i)\rightarrow 0} \left( \frac{dy_{\text{cm}}}{d\tilde{y}_{\text{cm}}} \right) \frac{f_{\bar{v}'(g)}(x_{\pm}, \mu_{\text{F}}) f_i(x_{\mp}, \mu_{\text{F}})}{f_{\bar{v}'(\bar{q})}(\tilde{x}_{\pm}, \tilde{\mu}_{\text{F}}) f_i(\tilde{x}_{\mp}, \tilde{\mu}_{\text{F}})} \frac{M^4}{s_{\bar{v}'i(g_i i)}^2(p_{\perp}, y)}$$

$$\times \frac{\xi C\alpha_s}{2\pi} \hat{D}_{\bar{v}'i(\bar{q}_i i)\rightarrow \bar{v}'gi(qg_i i)}(p_{\perp}, y) dp_{\perp}^2 dy$$

- $y_{\text{cm}} = \ln(x_{+}/x_{-})/2, \quad \tilde{y}_{\text{cm}} = \ln(\tilde{x}_{+}/\tilde{x}_{-})/2$

→ And to FI dipoles as well:

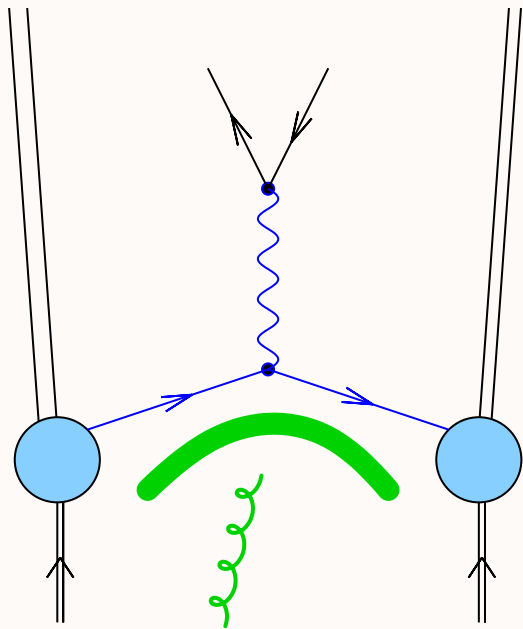
$$d\sigma_{0i(0g)\rightarrow fg(f\bar{q})} \simeq d\sigma_{0i(0q)\rightarrow f} \frac{f_{i(g)}(x_{\pm}, \mu_{\text{F}})}{f_{i(q)}(\tilde{x}_{\pm}, \tilde{\mu}_{\text{F}})} \frac{Q^4}{[s_{fg(f\bar{q})}(p_{\perp}, y) + Q^2]^2}$$

$$\times \frac{\xi C\alpha_s}{2\pi} \hat{D}_{fi(fq_i)\rightarrow fgi(fg_i\bar{q})}(p_{\perp}, y) dp_{\perp}^2 dy$$



# Colour dipole shower for hadronic collisions

- ➔ Formulate IS emission completely perturbatively through colour dipoles (partly) spanned by incoming parton lines.
- ➔ Radiation that is associated to **initial**, **initial-final** and **final** colour lines.
- ➔ Keep beam remnants outside evolution as long as hadronization has not set in.



## Construction principles of perturbative CDM:

- new dipole types:  $\bar{q}_i q_i$ ,  $g_i q_i$ ,  $g_i g_i$  and  $q_f q_i$ ,  $q_f g_i$ ,  $g_f g_i$ .
- radiation pattern in terms of  $2 \rightarrow 3$  splittings.
- generalization of the kinematics setup to the new cases  
➔ *dipole phase-space factorization and invariant evolution variables.*
- *dipole ME factorization* ➔ re-calculate or use crossing symmetry of FF dipole MEs or use antenna functions.
- probabilistic interpretation of Sudakov form factor based on dipole splitting cross sections.
- large  $N_C$  limit, onshell kinematics, for all ISR apply backward evolution.

# Initial-state dipole evolution at a glance: $\bar{v}'i \rightarrow \bar{v}'gi$

→ Invariant **transverse momentum** and **rapidity**

$$p_{\perp}^2 = \left| \frac{s_{\bar{v}'g} s_{gi}}{s_{\bar{v}'gi}} \right| = \frac{\hat{t} \hat{u}}{M^2}, \quad y = \frac{1}{2} \ln \left| \frac{s_{gi}}{s_{\bar{v}'g}} \right| = \frac{1}{2} \ln \frac{\hat{u}}{\hat{t}}$$

→ Phase space,  $a = \hat{s}_{\max}/M^2 \leq S/M^2$

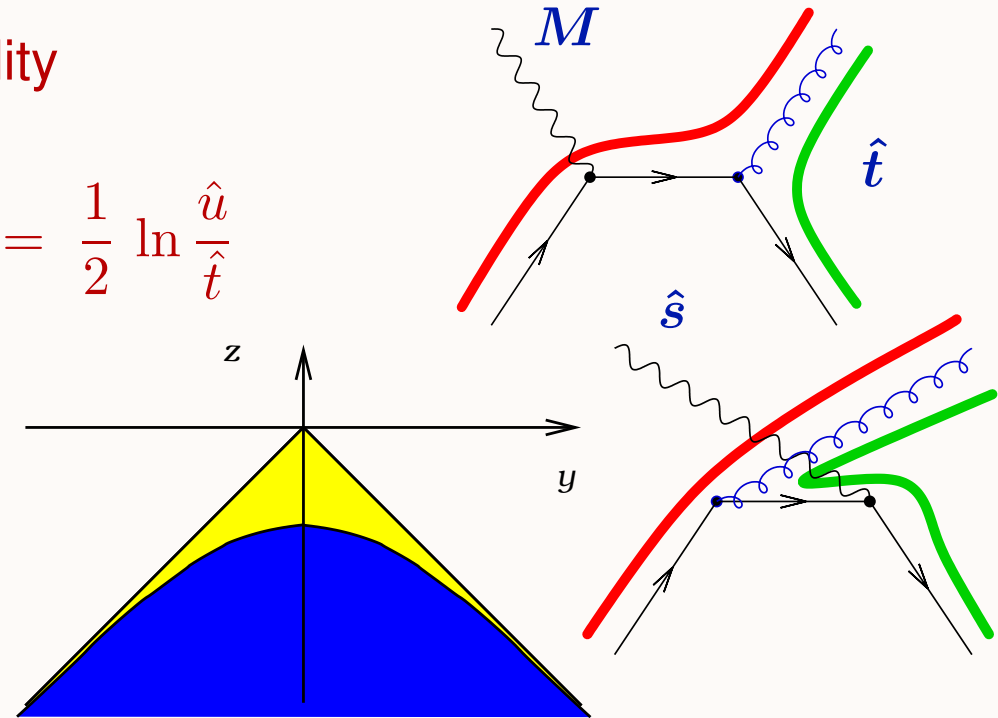
$$|y| \leq \operatorname{arcosh} \frac{(a-1)M}{2p_{\perp}} \leq \ln \frac{(a-1)M}{p_{\perp}} = \ln \frac{1}{z}$$

→ Dipole splitting function for **gluon emission** off II dipoles,  $x_{\bar{v}',i} = 1 + \frac{p_{\perp}}{M} e^{\pm y}$

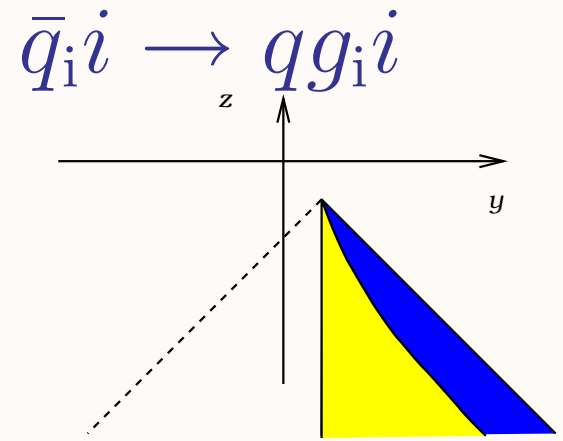
$$D_{\bar{v}'i \rightarrow \bar{v}'gi}(p_{\perp}, y) = \frac{f_{\bar{v}'}(x_{\pm}, \mu_F) f_i(x_{\mp}, \mu_F)}{f_{\bar{v}'}(\tilde{x}_{\pm}, \tilde{\mu}_F) f_i(\tilde{x}_{\mp}, \tilde{\mu}_F)} \xi_{\{A\}^F} C_{\{A\}^F} \frac{x_{\bar{v}'}^{n_{\bar{v}'}}(p_{\perp}, y) + x_i^{n_i}(p_{\perp}, y)}{[x_{\bar{v}'}(p_{\perp}, y) + x_i(p_{\perp}, y) - 1]^2}$$

$$\leq \mathcal{N}_{\text{PDF}} \xi_{\{A\}^F} C_{\{A\}^F} \left\{ \begin{array}{c} 2 \\ a+1 \end{array} \right\} \equiv D_{\bar{v}'i \rightarrow \bar{v}'gi}^{\text{approx}}(p_{\perp}, y)$$

$$n_{q,g} = 2, 3; \quad \left\{ \begin{array}{l} \dots \text{ for quark dipoles} \\ \dots \text{ else} \end{array} \right\}$$



# Initial-state dipole evolution at a glance:

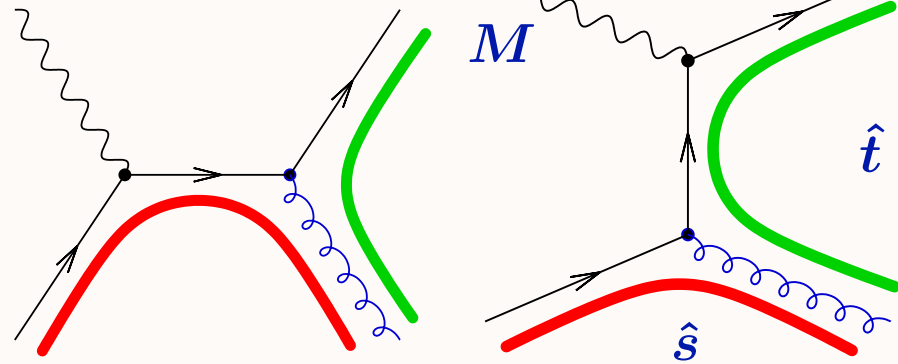


→ Invariant **transverse momentum** and **rapidity**

$$p_{\perp}^2 = \left| \frac{s_{qg_i} s_{g_i i}}{s_{qg_i i}} \right| = -\frac{\hat{t} \hat{s}}{M^2}, \quad y = \frac{1}{2} \ln \left| \frac{s_{g_i i}}{s_{qg_i}} \right| = \frac{1}{2} \ln \frac{\hat{s}}{-\hat{t}}$$

→ Phase space,  $a = \hat{s}_{\max}/M^2 \leq S/M^2$

$$\operatorname{arsinh} \frac{M}{2p_{\perp}} \leq y \leq \ln \frac{aM}{p_{\perp}} = \ln \frac{1}{z}$$



→ Dipole splitting function for **quark emission** off II dipoles,

$$x_{q,i} = \mp 1 + \frac{p_{\perp}}{M} e^{\pm y}$$

$$D_{\bar{q}_i i \rightarrow q g_i i}(p_{\perp}, y) = \frac{f_g(x_{\pm}, \mu_F) f_i(x_{\mp}, \mu_F)}{f_{\bar{q}}(\tilde{x}_{\pm}, \tilde{\mu}_F) f_i(\tilde{x}_{\mp}, \tilde{\mu}_F)} T_R \frac{x_q^2(p_{\perp}, y) + x_i^{n_i}(p_{\perp}, y)}{[1 + x_q(p_{\perp}, y)]^2}$$

$$\leq \mathcal{N}_{\text{PDF}} T_R \left\{ \begin{matrix} 2 \\ a+1 \end{matrix} \right\} \equiv D_{\bar{q}_i i \rightarrow q g_i i}^{\text{approx}}(p_{\perp}, y)$$

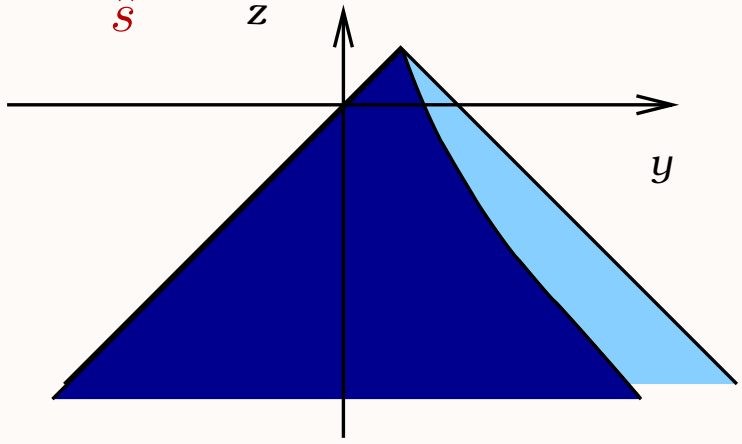
$$n_{q,g} = 2, 3;$$

$\left\{ \begin{matrix} \dots & \text{for quark dipoles} \\ \dots & \text{else} \end{matrix} \right\}$

# Final–initial dipole evolution at a glance: $fi \rightarrow fgi$

→ Invariant **transverse momentum** and **rapidity**

$$p_{\perp}^2 = \left| \frac{s_{fg} s_{gi}}{s_{fgi}} \right| = \frac{\hat{s} \hat{t}}{-Q^2}, \quad y = \frac{1}{2} \ln \left| \frac{s_{gi}}{s_{fg}} \right| = \frac{1}{2} \ln \frac{-\hat{t}}{\hat{s}}$$



→ Phase space,  $a = \hat{s}_{\max}/Q^2 \leq x_B^{-1} - 1$

$$\ln z = -\ln \frac{aQ}{p_{\perp}} \leq y \leq \operatorname{arsinh} \frac{Q}{2p_{\perp}}$$

→ Dipole splitting function for **gluon emission** off FI dipoles,  $x_{f,i} = \pm 1 - \frac{p_{\perp}}{Q} e^{\pm y}$

$$D_{fi \rightarrow fgi}(p_{\perp}, y) = \frac{f_i(-x_i x_B, \mu_F)}{f_i(x_B, \tilde{\mu}_F)} \xi_{\{A\}^F} C_{\{A\}^F} \frac{|x_f(p_{\perp}, y)|^{n_f} + |x_i(p_{\perp}, y)|^{n_i}}{x_i^2(p_{\perp}, y)}$$

$$\leq \mathcal{N}_{\text{PDF}} \xi_{\{A\}^F} C_{\{A\}^F} \left\{ \begin{matrix} 2 \\ 2(a+1) \end{matrix} \right\} \equiv D_{fi \rightarrow fgi}^{\text{approx}}(p_{\perp}, y)$$

$n_{q,g} = 2, 3; \quad \left\{ \begin{matrix} \dots & \text{for quark dipoles} \\ \dots & \text{else} \end{matrix} \right\}$

# Final–initial dipole evolution at a glance: $f q_i \rightarrow f g_i \bar{q}$

→ Invariant **transverse momentum** and **rapidity**

$$p_{\perp}^2 = \left| \frac{s_{f g_i} s_{g_i \bar{q}}}{s_{f g_i \bar{q}}} \right| = \frac{\hat{u} \hat{t}}{Q^2}, \quad y = \frac{1}{2} \ln \left| \frac{s_{g_i \bar{q}}}{s_{f g_i}} \right| = \frac{1}{2} \ln \frac{\hat{t}}{\hat{u}}$$

→ Phase space,  $a = \hat{s}_{\max}/Q^2 \leq x_B^{-1} - 1$

$$\operatorname{arcosh} \frac{Q}{2 p_{\perp}} \leq |y| \leq \operatorname{arcosh} \frac{(a+1) Q}{2 p_{\perp}} \leq \ln \frac{(a+1) Q}{p_{\perp}} = \ln \frac{1}{z}$$

→ Dipole splitting function for **antiquark emission** off FI dipoles,

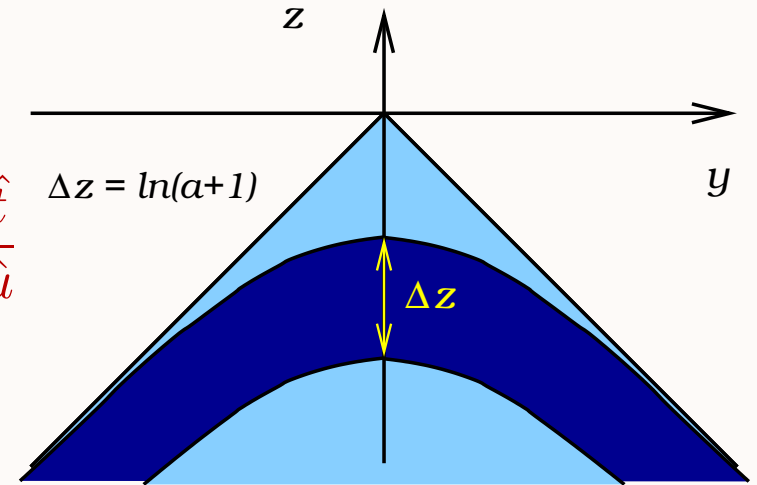
$$n_{q,g} = 2, 3;$$

$$x_{f, \bar{q}} = 1 - \frac{p_{\perp}}{Q} e^{\pm y}, \quad x_{g_i} = -\frac{2 p_{\perp}}{Q} \cosh y$$

{ ... for quark dipoles }  
{ ... else }

$$D_{f q_i \rightarrow f g_i \bar{q}}(p_{\perp}, y) = \frac{f_{g_i}(-x_{g_i} x_B, \mu_F)}{f_{q_i}(x_B, \tilde{\mu}_F)} T_R \frac{|x_f(p_{\perp}, y)|^{n_f} + x_{\bar{q}}^2(p_{\perp}, y)}{x_{g_i}^2(p_{\perp}, y)}$$

$$\leq \mathcal{N}_{\text{PDF}} T_R \left\{ \begin{matrix} 1 \\ \max\{2, a+1\} \end{matrix} \right\} \equiv D_{f q_i \rightarrow f g_i \bar{q}}^{\text{approx}}(p_{\perp}, y)$$



# Sudakov exponentiation, kinematics and showering

→ Rule of thumb: no-branching probability exponentiates

$$\Delta(p_{\perp,\text{stt}}^2, p_{\perp}^2) = \exp \left\{ - \int_{p_{\perp}^2}^{p_{\perp,\text{stt}}^2} \frac{dk_{\perp}^2}{k_{\perp}^2} \mathcal{I}(k_{\perp}^2) \right\},$$

$$\mathcal{I}(k_{\perp}^2) = \frac{\alpha_s[\mu_R(k_{\perp})]}{2\pi} \sum_{\{\tilde{k}\tilde{\ell} \rightarrow kgl\}} \int_{y_-(k_{\perp}, a)}^{y_+(k_{\perp}, a)} dy D_{\tilde{k}\tilde{\ell} \rightarrow kgl}(k_{\perp}, y)$$

→ Differential probability that branching occurs at  $p_{\perp}^2$

$$\frac{dP}{dp_{\perp}^2} = \frac{d\Delta(p_{\perp,\text{stt}}^2, p_{\perp}^2)}{dp_{\perp}^2} = \frac{\mathcal{I}(p_{\perp}^2)}{p_{\perp}^2} \Delta(p_{\perp,\text{stt}}^2, p_{\perp}^2)$$

→ Monte Carlo method (**Veto Algorithm**) yields values for evolution variables.

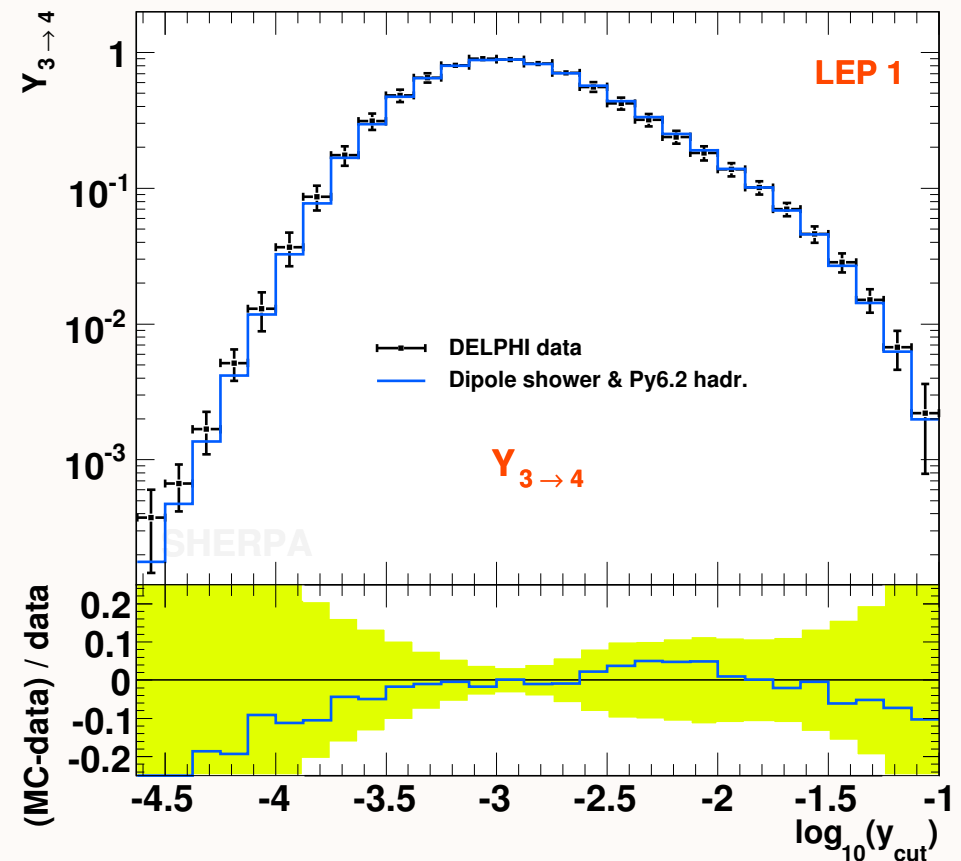
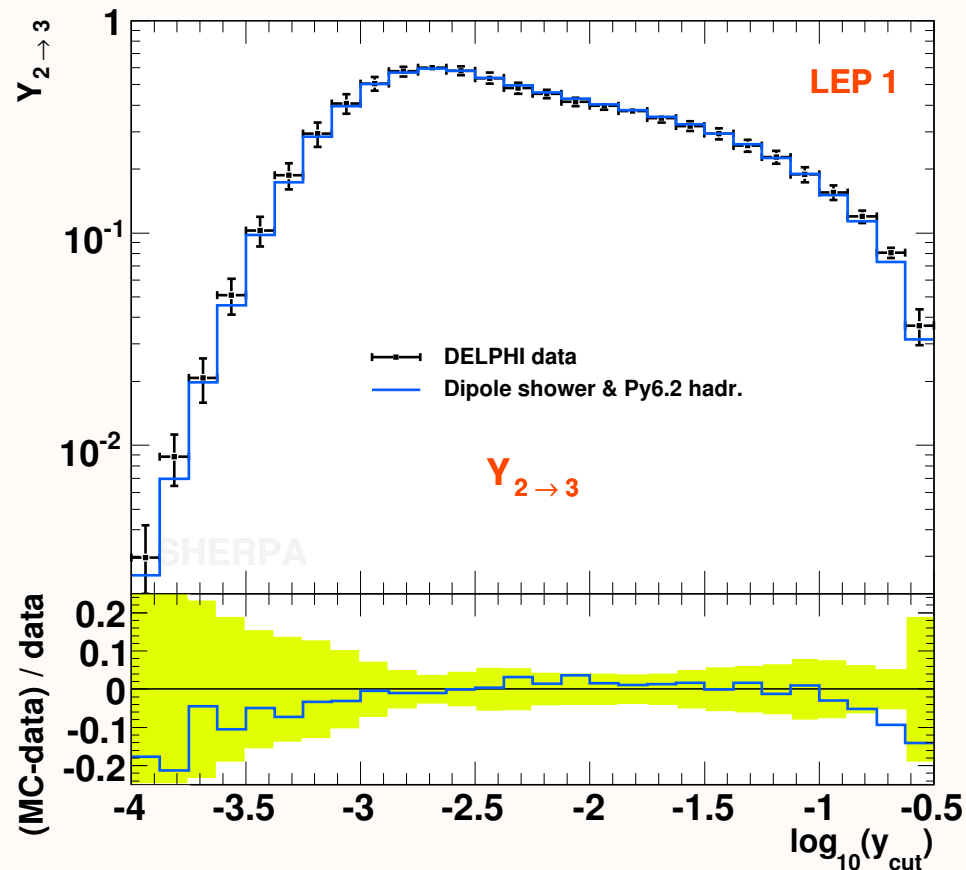
→ Set up kinematics: use light-cone variables and recoil strategies.

→ Shower algorithm fully defined by fixing:

- *renormalization and factorization scale choices.*
- *the initializing scale in dependence on the hard process.*
- *the maximal phase space of a single emission globally.*
- *the iteration procedure to generate the cascade and the cut-off(s).*

# Results for pure final-state cascading

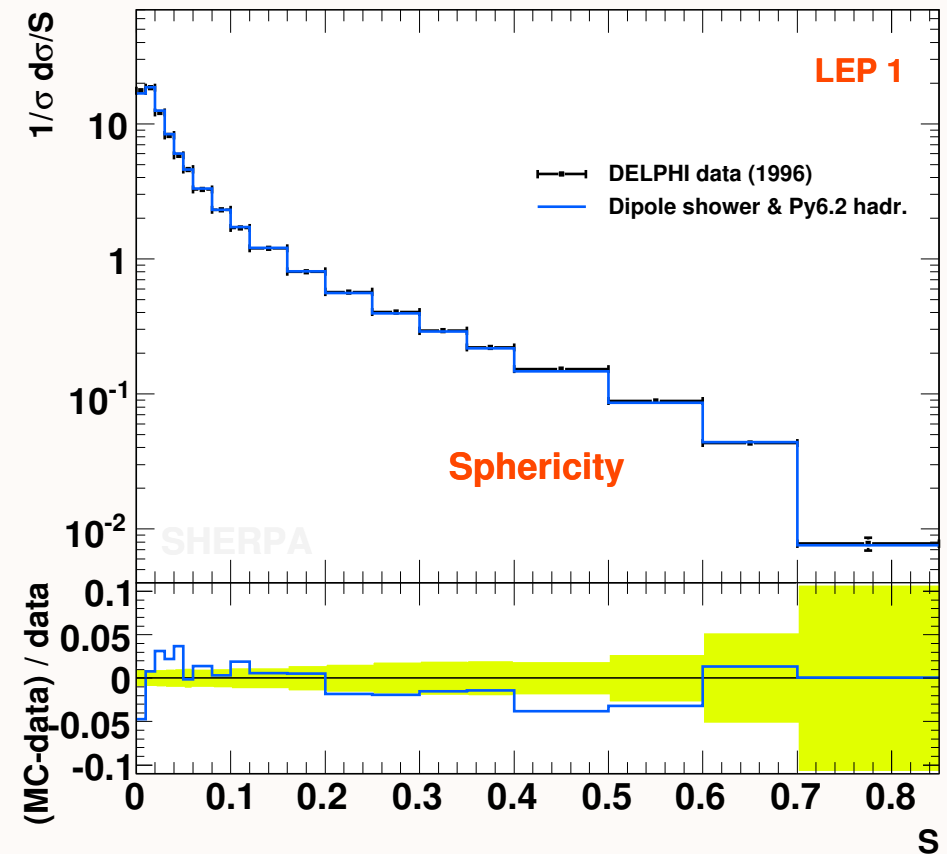
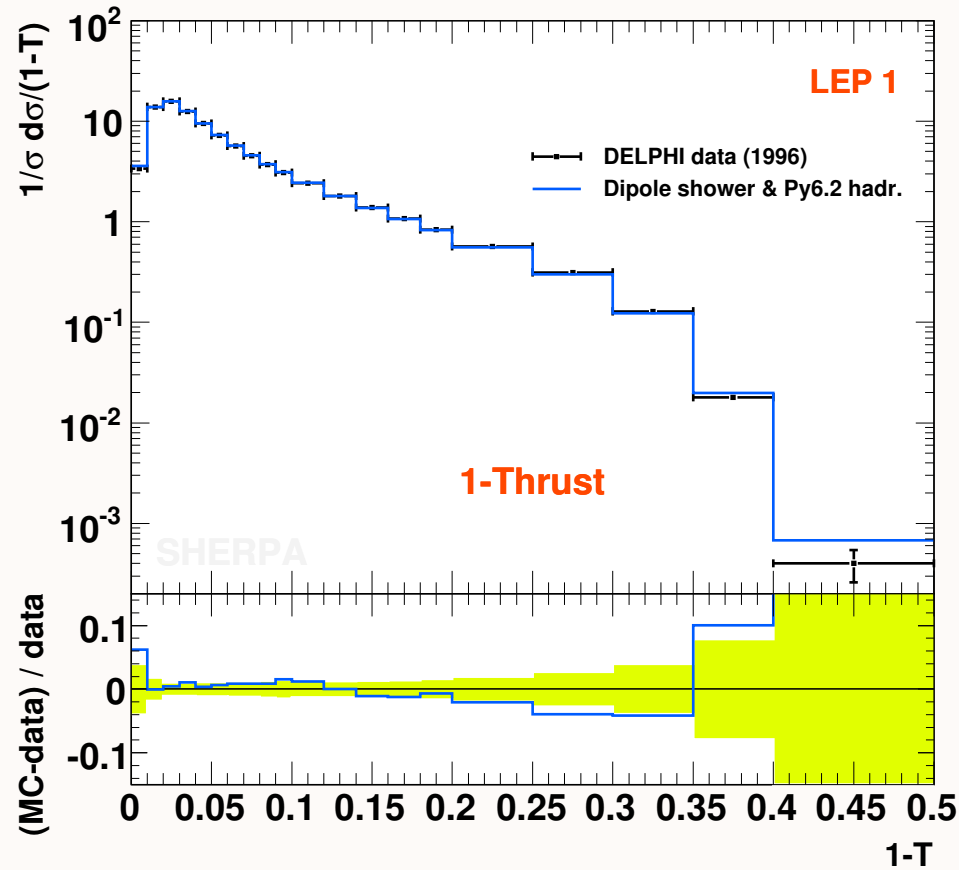
➔ Testbed: hadron production in electron–positron annihilations @ LEP1



- Durham differential jet rates as a function of the jet-resolution parameter  $y_{\text{cut}}$ .
- Data: H. Hoeth, diploma thesis, Bergische Universität Wuppertal.

# Results for pure final-state cascading

➔ Testbed: hadron production in electron–positron annihilations @ LEP1

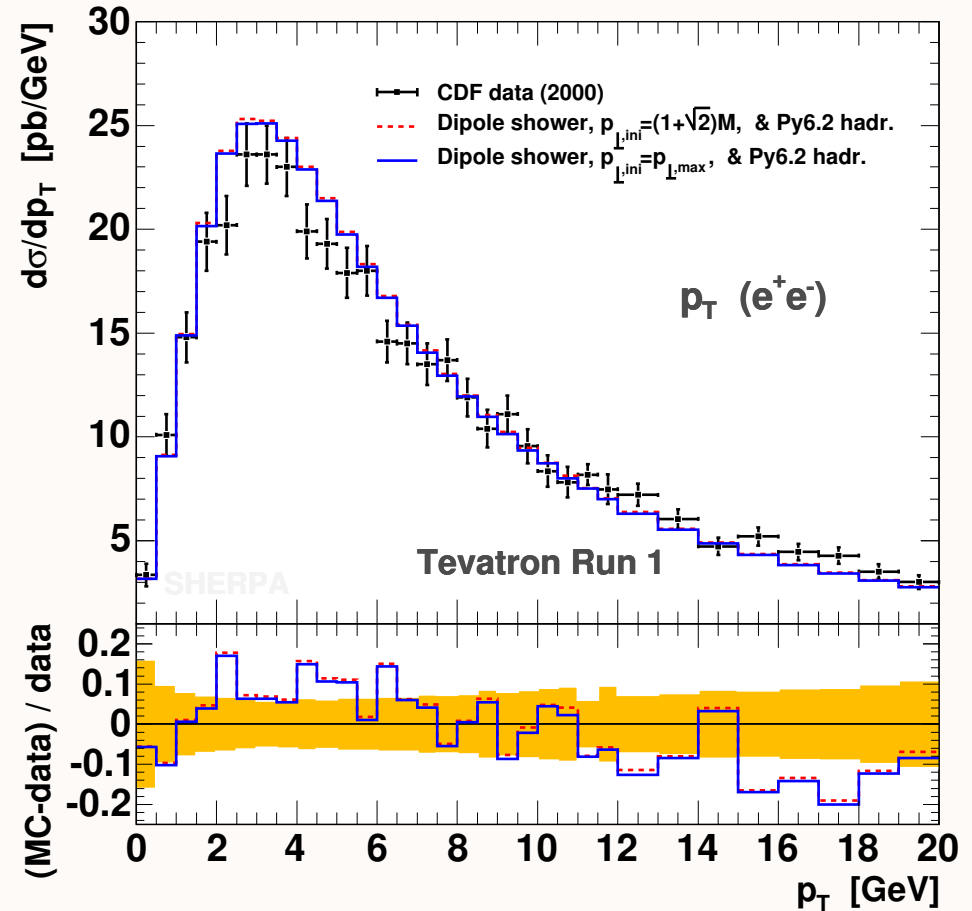
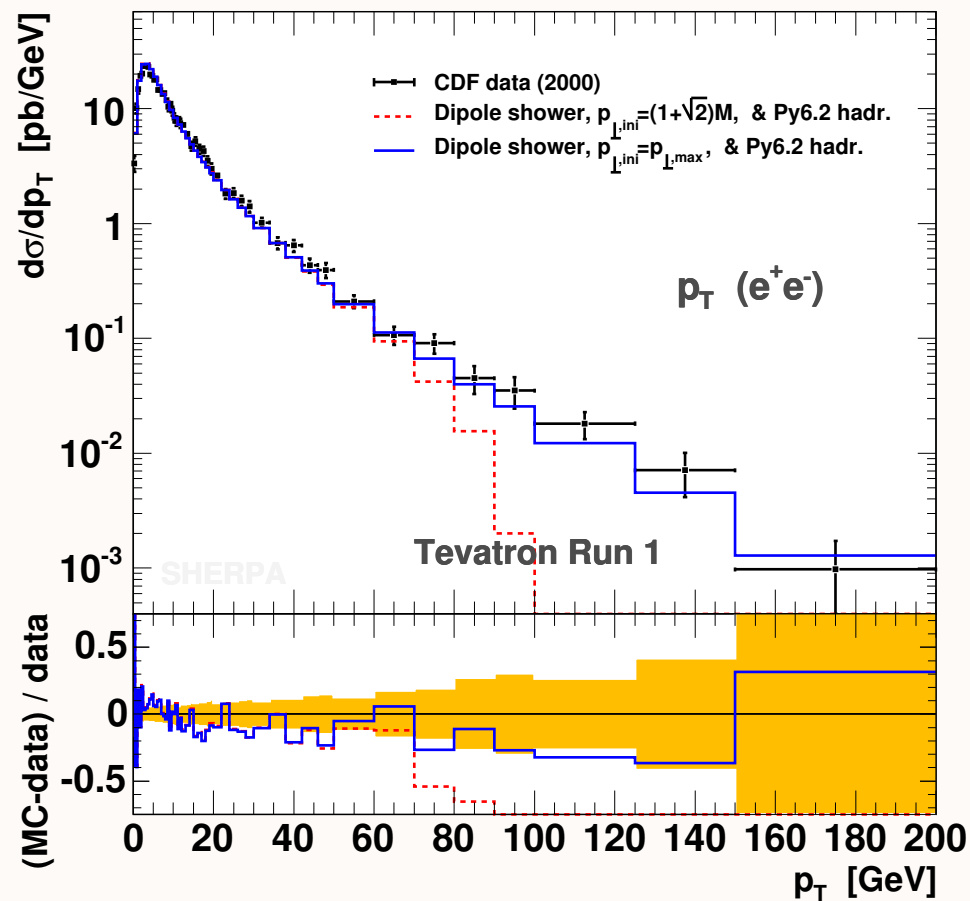


- Examples of event-shape observables: 1-thrust (left panel) and sphericity.
- Data: P. Abreu et. al. Z. Phys. C73 (1996) 11.



# Results for hadronic collisions

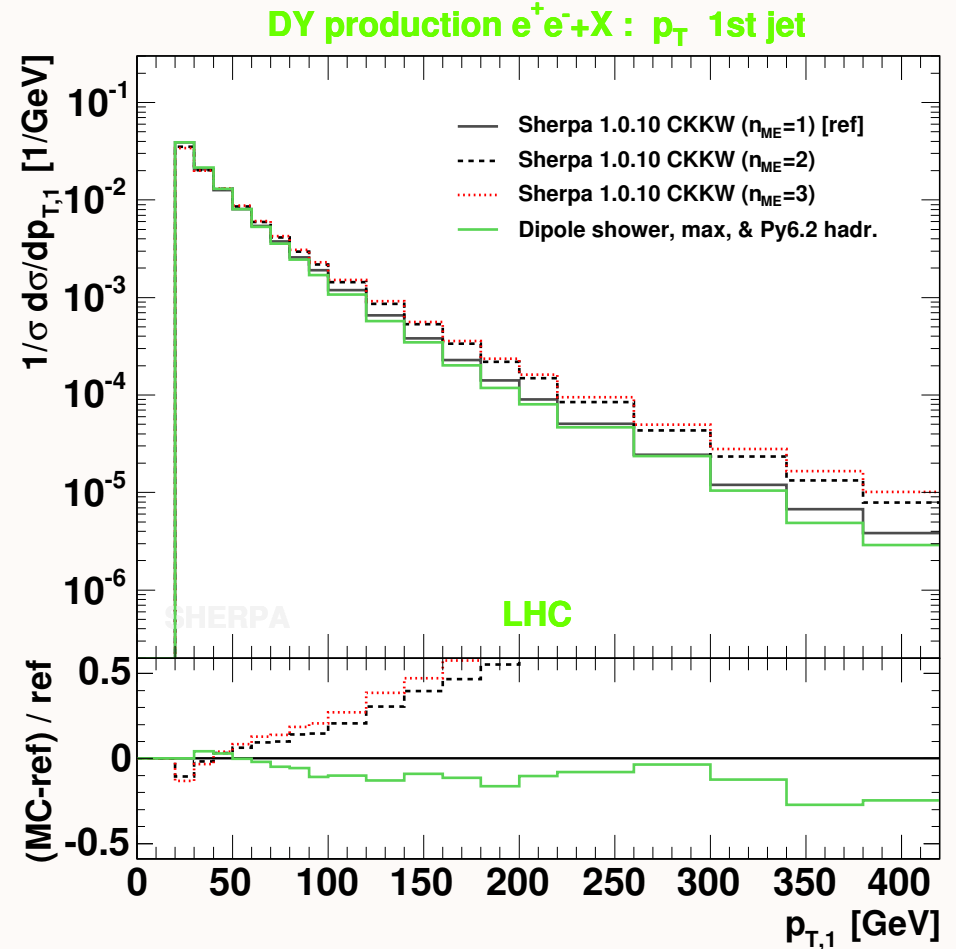
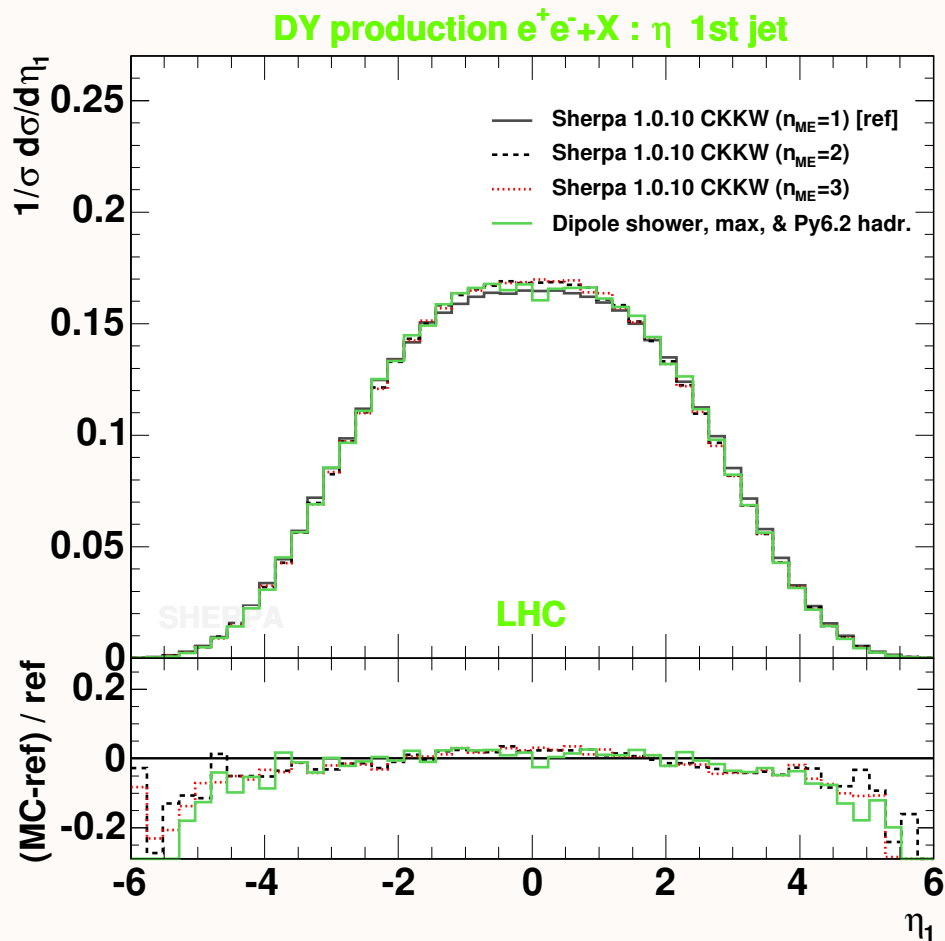
➔ Testbed: inclusive production of Drell–Yan lepton pairs @ Tevatron Run I



- Boson transverse-momentum distribution and its peak region in  $e^+e^- + X$ .
- Data: A. A. Affolder et. al. Phys. Rev. Lett. 84 (2000) 845.

# Results for hadronic collisions

→ Testbed: Drell–Yan pair production @ LHC, compared to SHERPA predictions

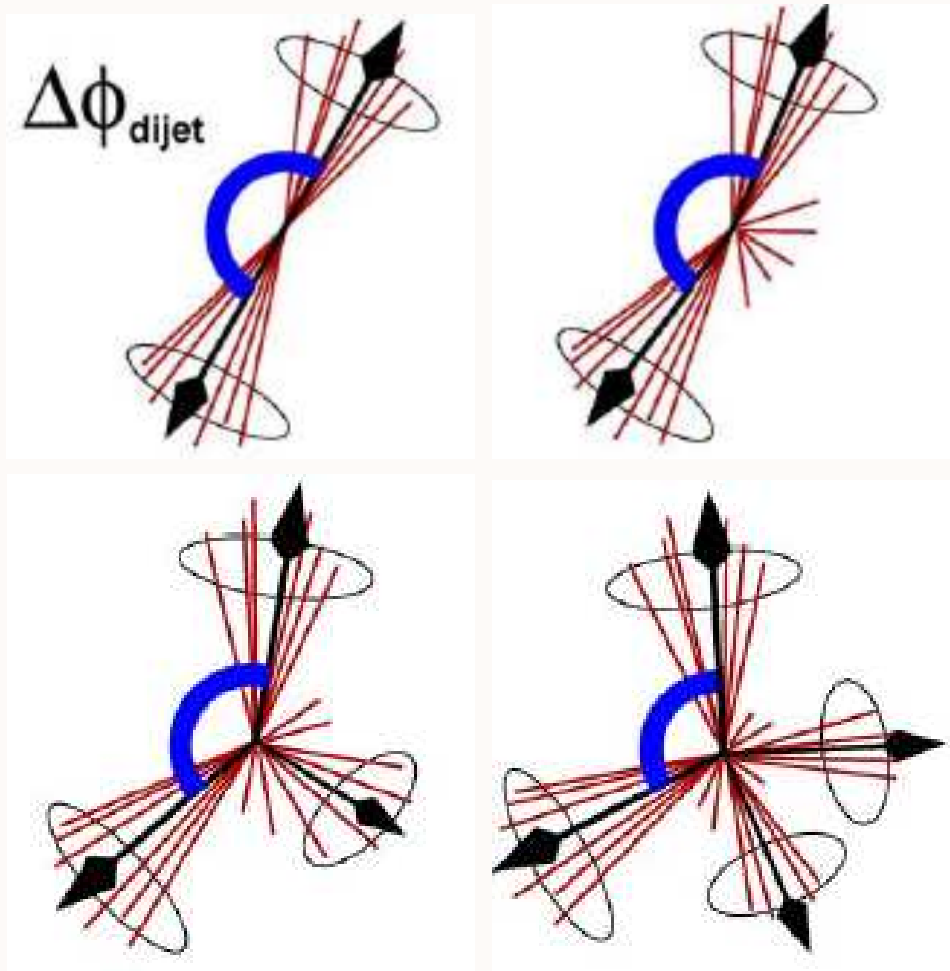


- Pseudo-rapidity (left) and transverse-momentum (right) distribution of the first jet.
- The 1st emission in the dipole shower is ME corrected per construction.

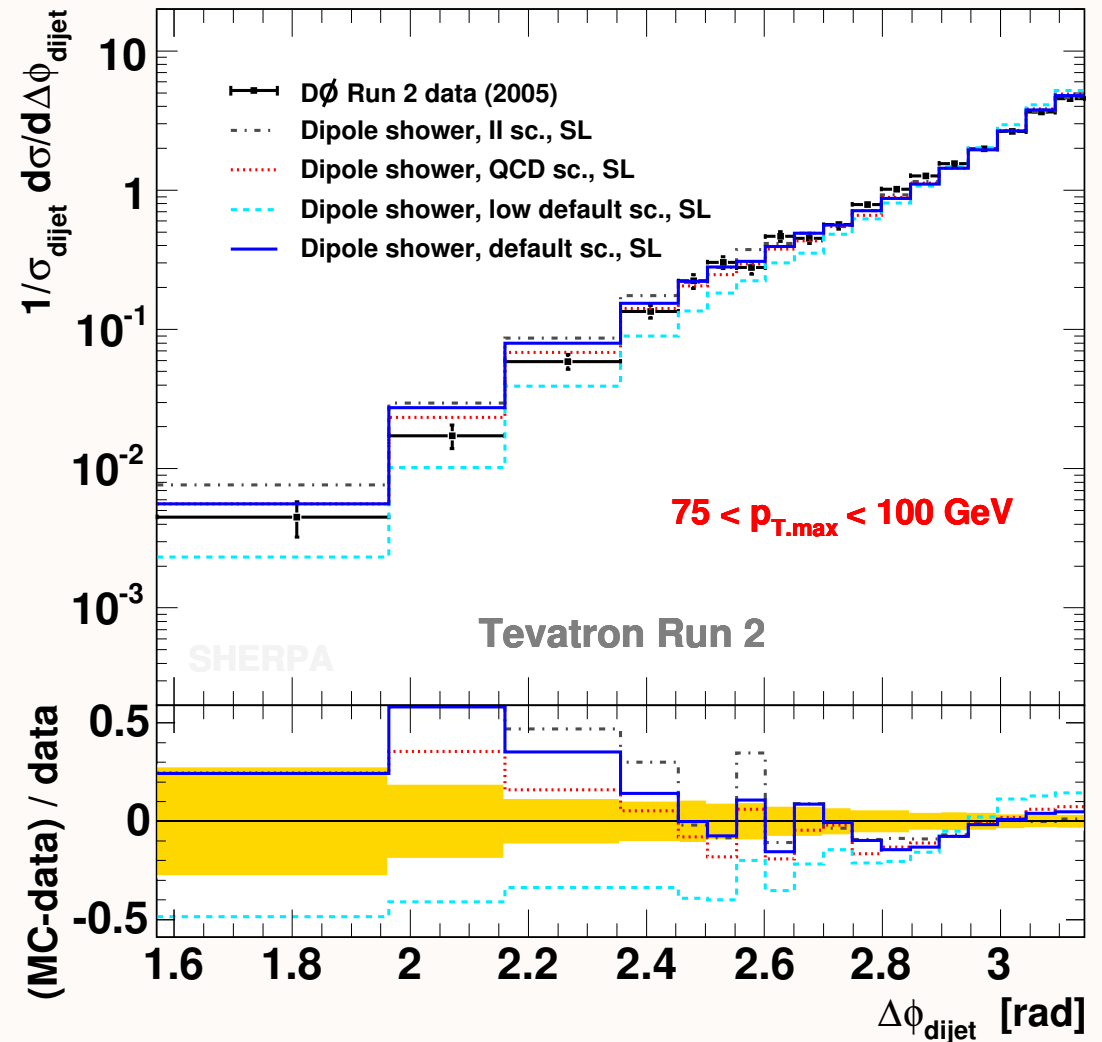
# Correlations ... inclusive jet production @ Tevatron

V.M. Abazov et al., Phys. Rev. Lett. **94** (2005) 221801

- Dijet azimuthal decorrelation measured by  $D\phi$  at Run II.
- Idea: test QCD radiation pattern.



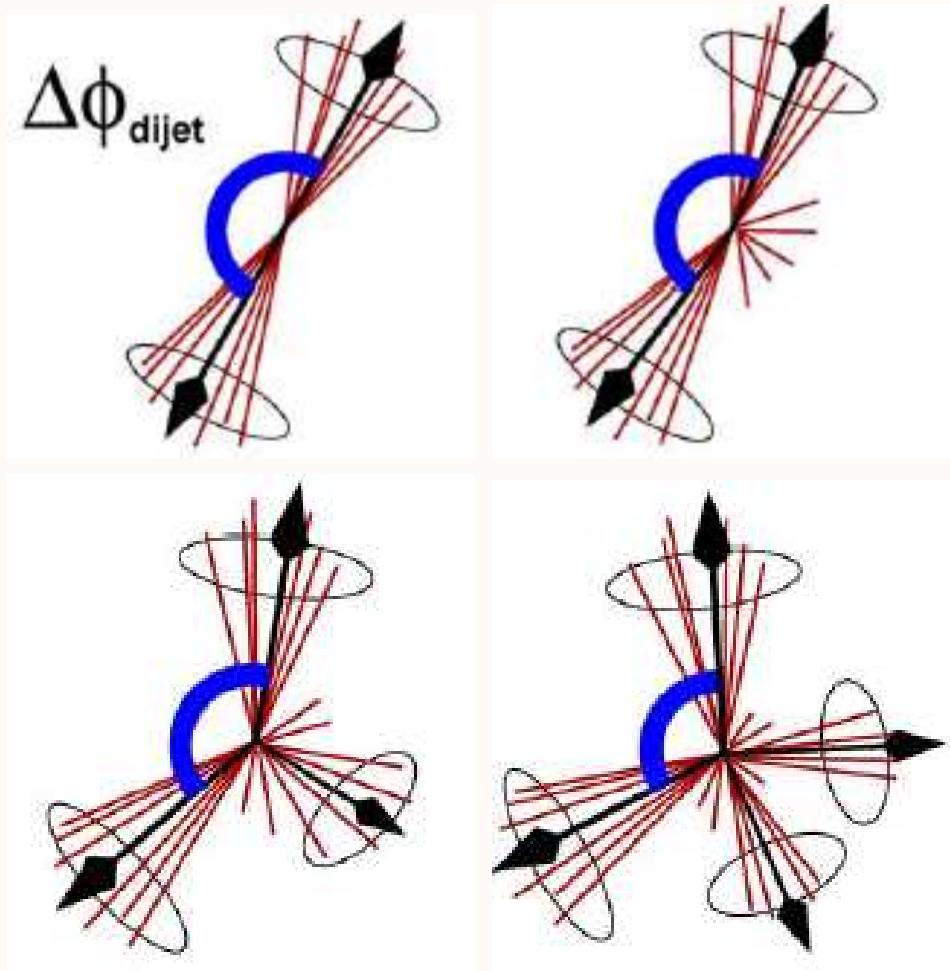
Jet production : Dijet azimuthal decorrelation



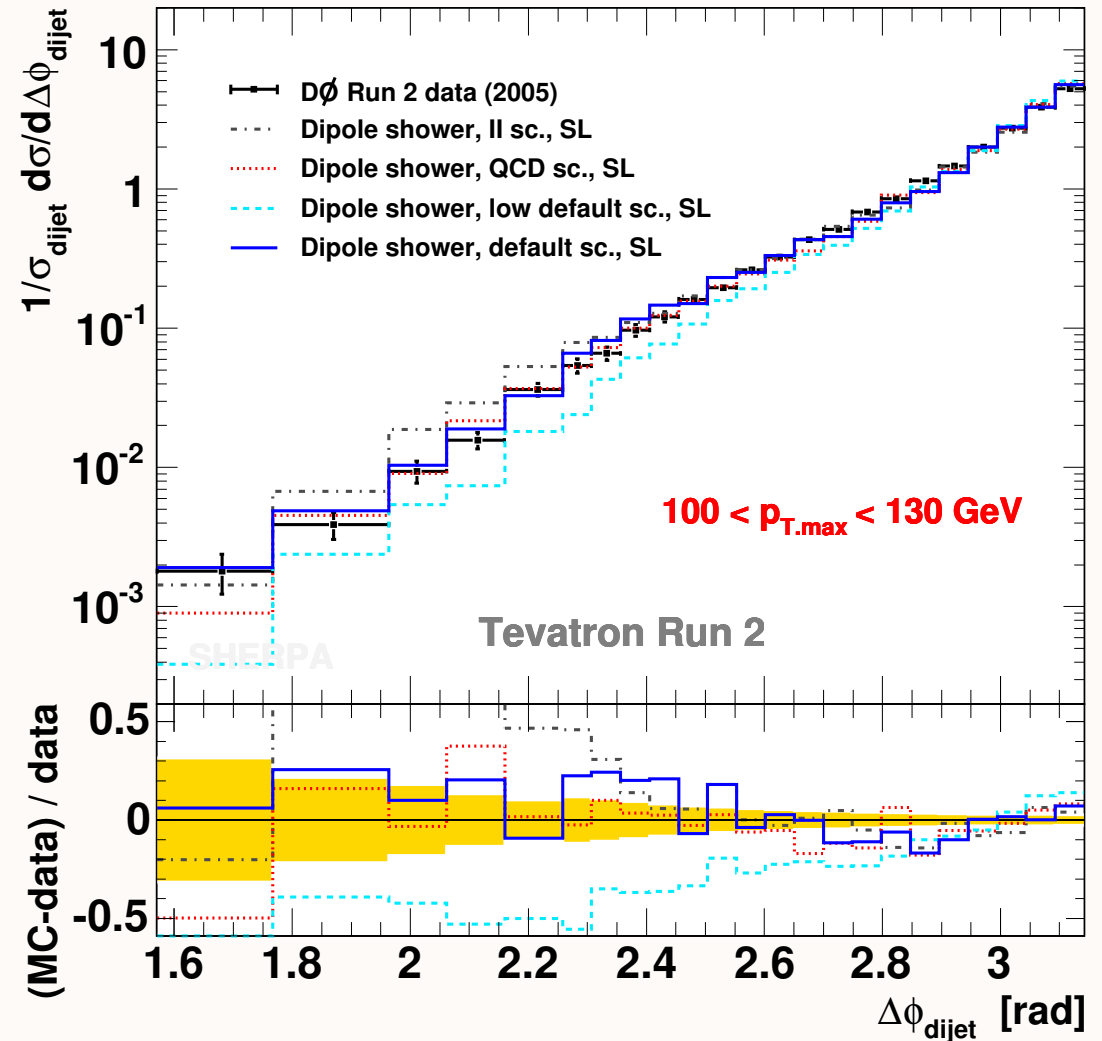
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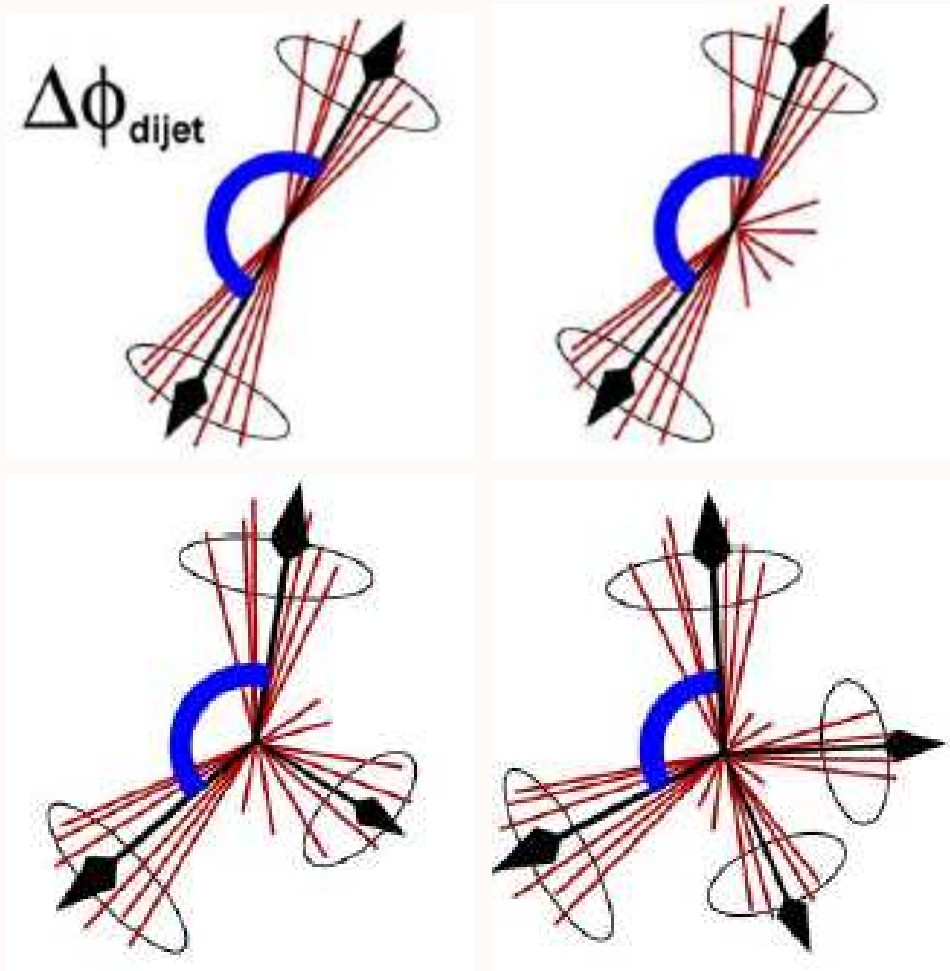
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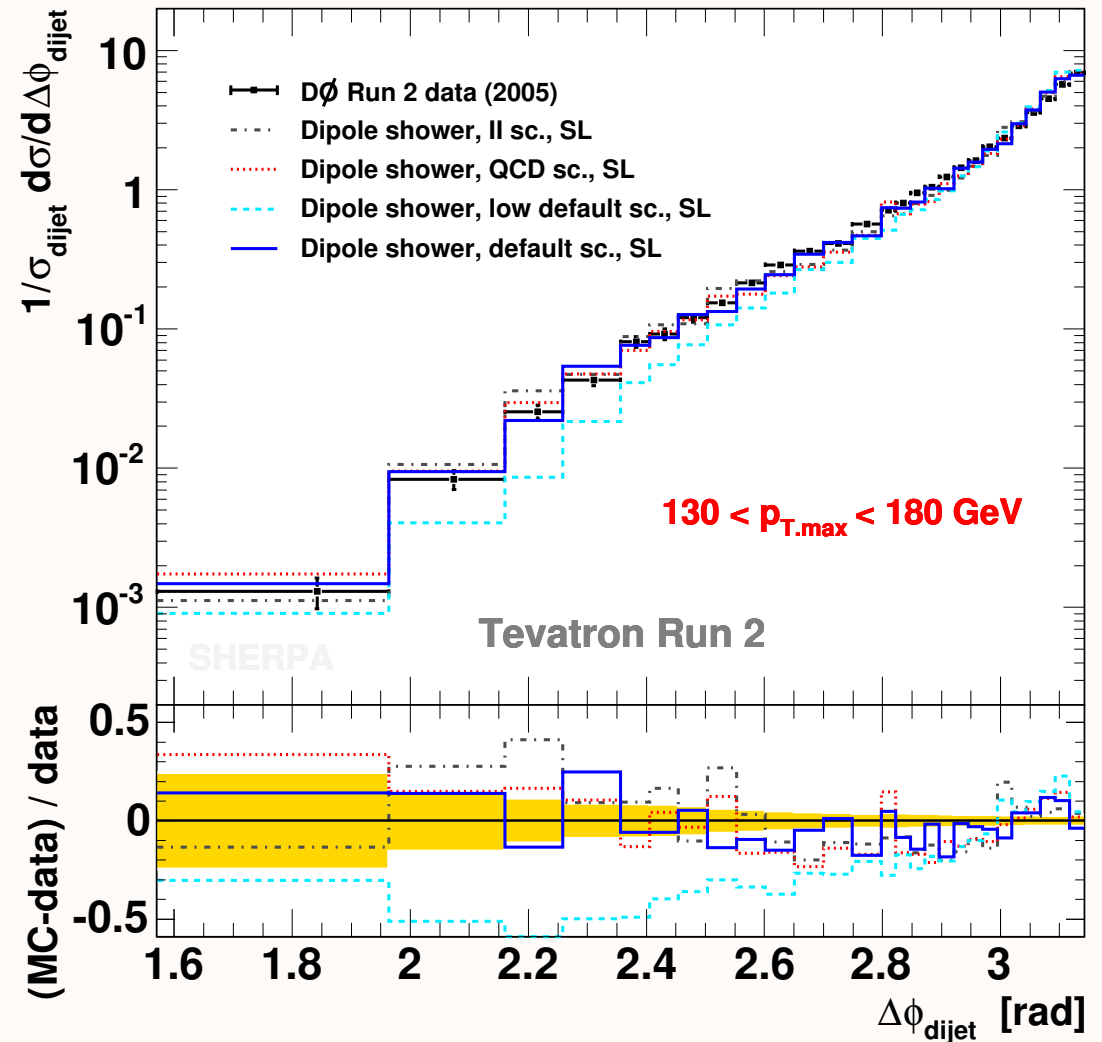
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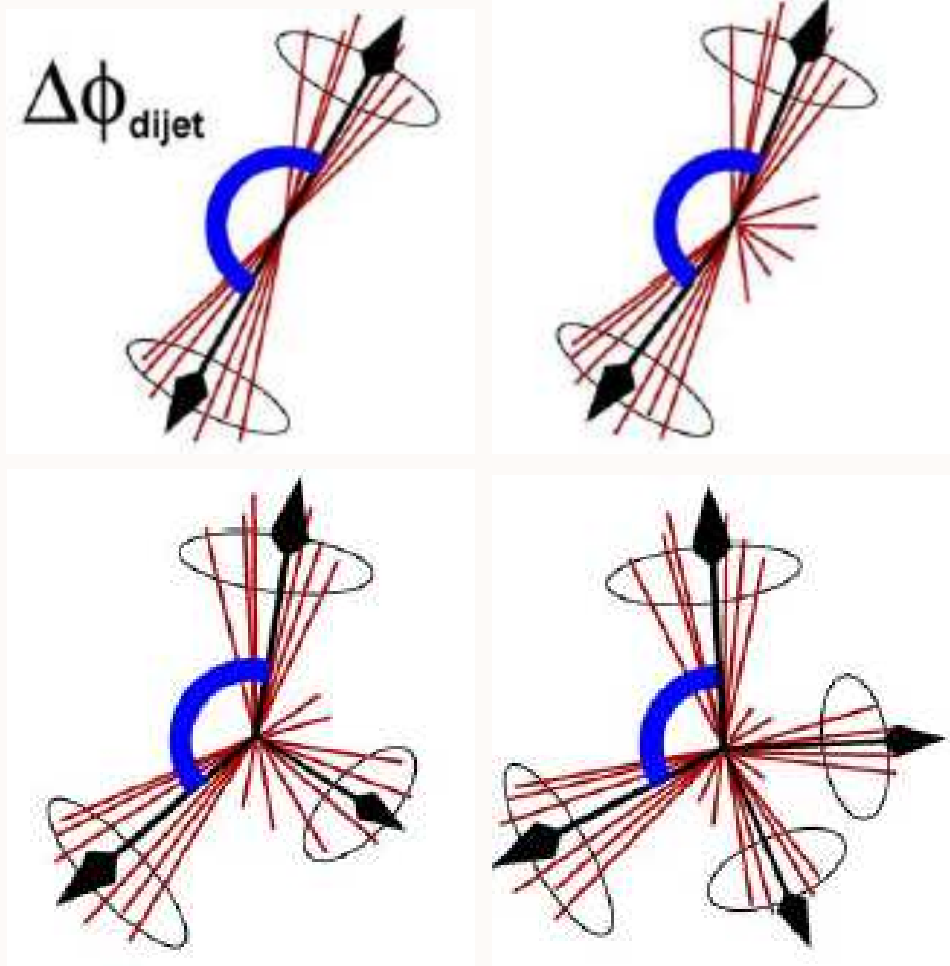
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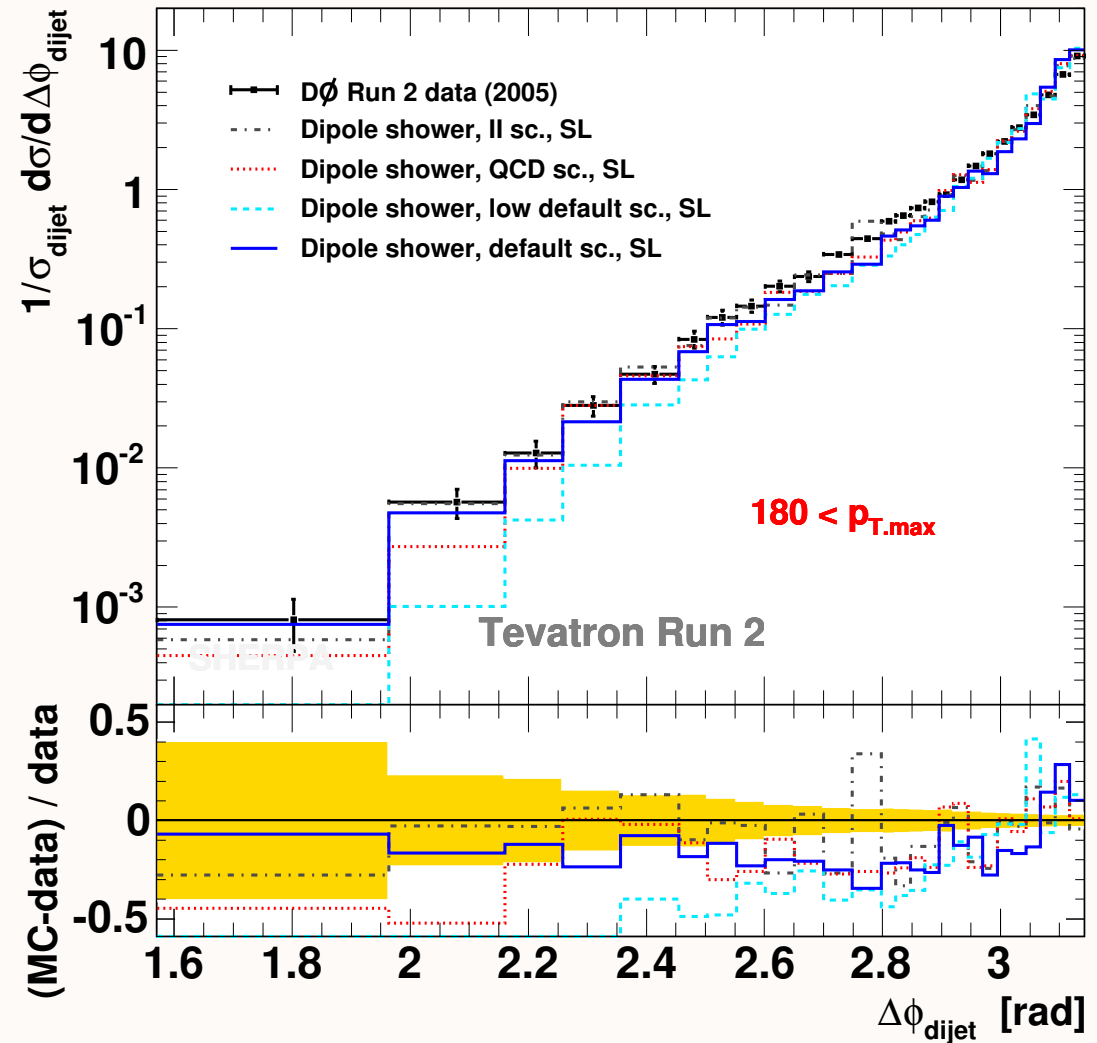
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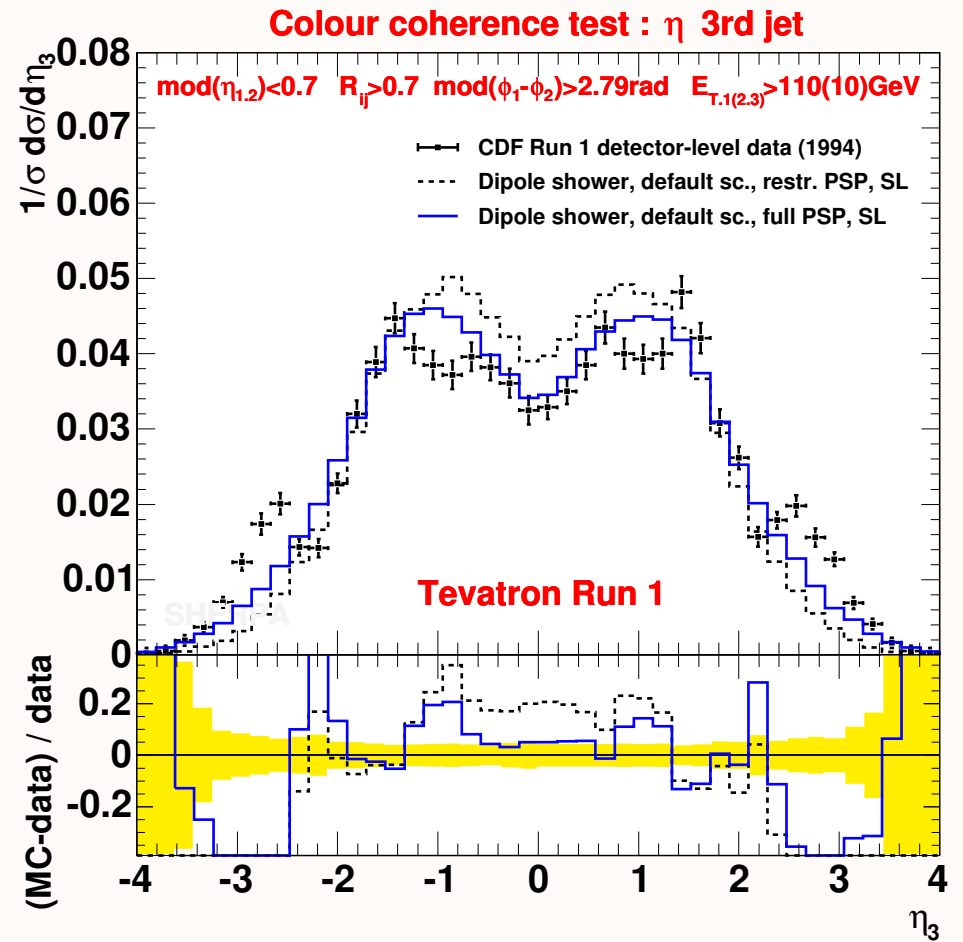
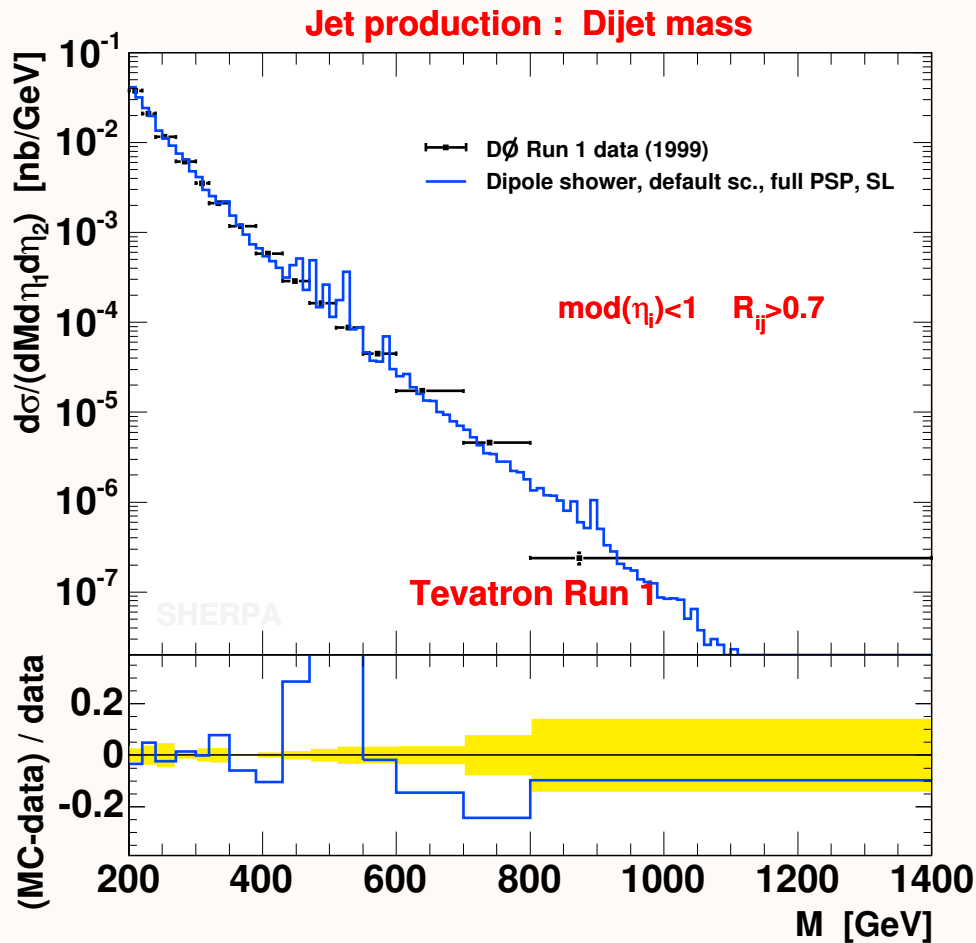


Jet production : Dijet azimuthal decorrelation



# Results for hadronic collisions

→ Testbed: inclusive jet production @ Tevatron Run I

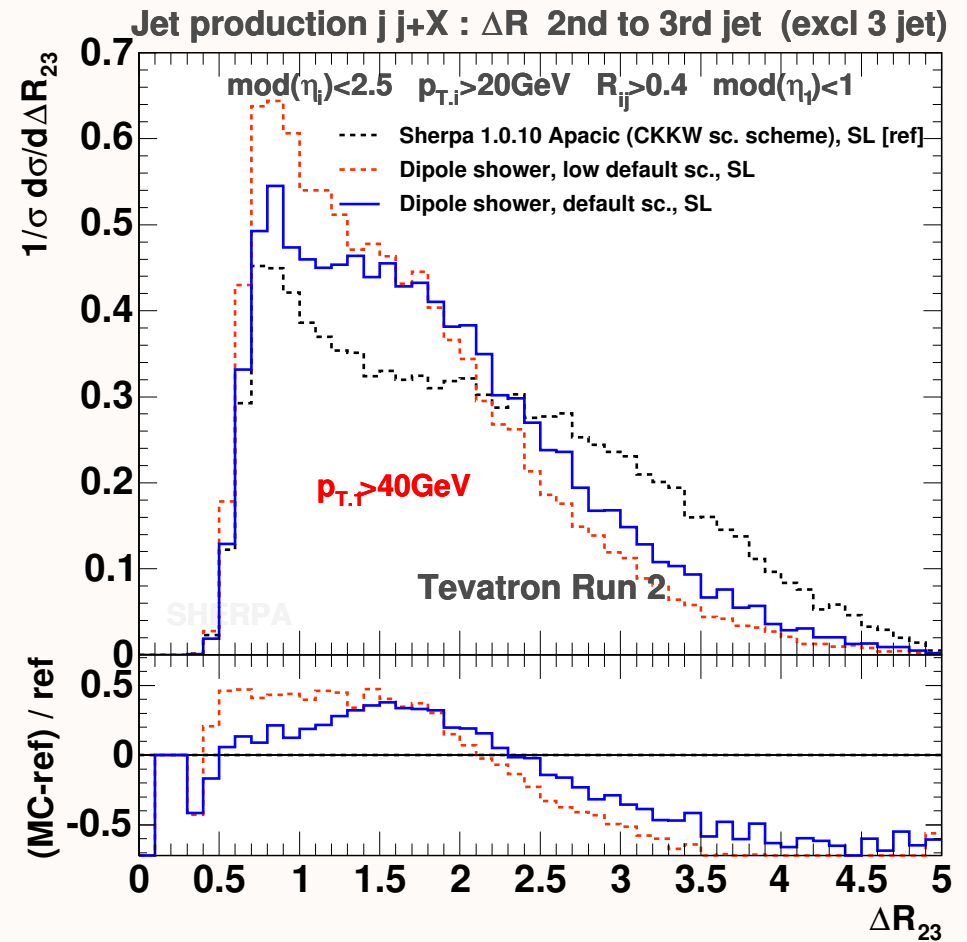
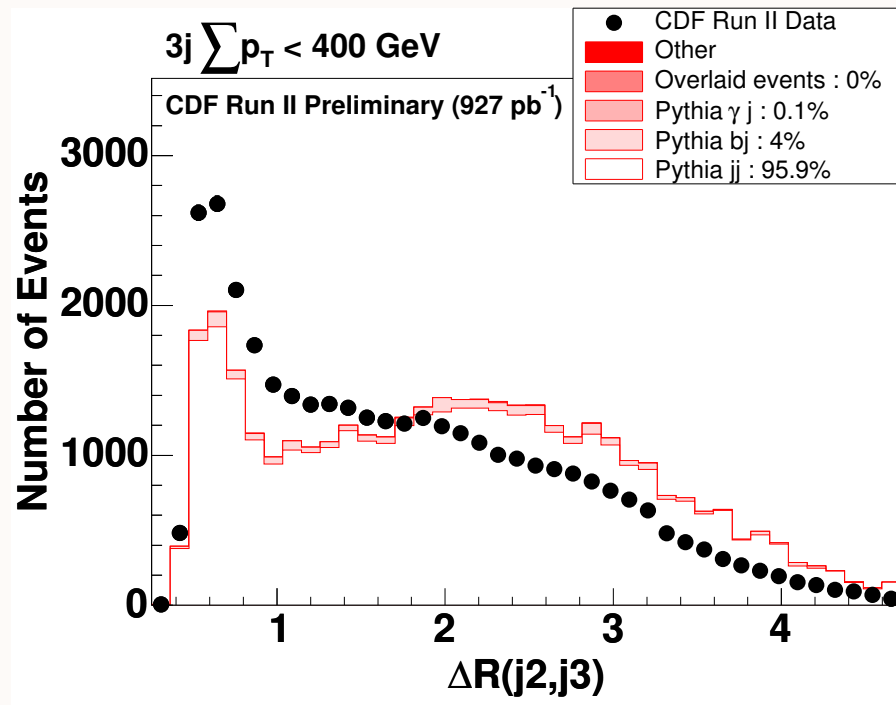


- DØ data: B. Abbott et. al. Phys. Rev. Lett. 82 (1999) 2457.
- CDF data: F. Abe et. al. Phys. Rev. D50 (1994) 5562.



# Results for hadronic collisions

→ Testbed: inclusive jet production @ Tevatron Run II



- Discrepancy between MC and CDF data: arXiv:0710.2372.
- Was interested what the new dipole shower would predict.