

Searching for heavy neutral lepton and LNV through VBS at muon colliders



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based on [JHEP 09 \(2023\) 131](#)

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高亮度和高精度前沿缪子物理研讨会 北京 2024.4.19—4.22

Outline

- ▶ **Motivation**
- ▶ **Production features**
- ▶ **Heavy neutral lepton and lepton number violation**
- ▶ **Summary**

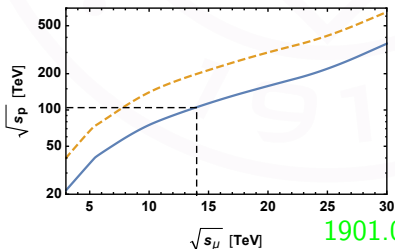
Motivation

Why a muon collider ?

- The past and ongoing particle colliders (LEP, $Spp\bar{p}S$, PETRA, SLC, Tevatron, LHC...) made important measurements for the SM and BSM. So far, we haven't seen any conclusive evidence of BSM physics.
- What kind of collider is an ideal environment to reach higher energy and higher luminosity?

Motivation

- Large muon mass ($m_\mu/m_e \sim 207$) suppresses the synchrotron radiation by a factor of 10^9 , compared with electron beams.
- Compare to a circular electron-positron collider, muon collider with smaller size would have the potential to reach above TeV c.m. energies.
- A 14 TeV muon collider has potential similar to that of a 100 TeV pp collider.
- Higher luminosity
- Lower background



1901.06150

Motivation

- The idea of muon collider introduced in 1980 ' s.

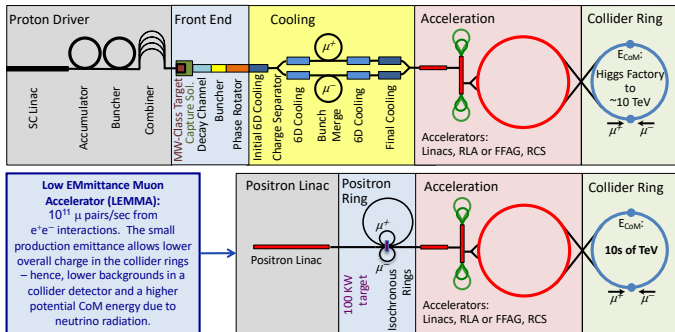
Skrinsky, Parkhomchuk, Sov.J.Part.Nucl.12(1981)223

Neuffer, Part.Accel.14 (1983) 75-90, AIP Conf.Proc.156(1987)201-208

Barger, Berger, Gunion, Han, PRL75(1995)1462-1465, Phys.Rept.286(1997)1-51

- Proton/positron driver scheme.

Muon Accelerator Program (MAP)



Motivation

- Due to the short lifetime ($2\mu\text{s}$) of muon, **cooling** process is the biggest challenge on its construction. **MICE collaboration, Nature 578(2020)53**
 - ▶ Recently, due to the technological development, muon colliders have received much attention in the community.
- Luminosity scaling scheme: $\sigma\mathcal{L} \sim \text{const.}$ and luminosity goals

$$\mathcal{L} \gtrsim \frac{5 \text{ years}}{\text{time}} \left(\frac{\sqrt{s}_\mu}{10 \text{ TeV}} \right)^2 2 \cdot 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$$

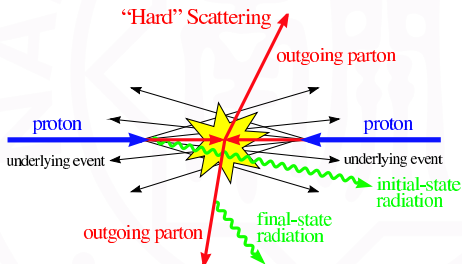
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Production features

- Recall the hadron colliders: $p p$ collision at LHC

Factorization formalism:

PDFs \otimes partonic cross section



$$\sigma(AB \rightarrow X) = \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, Q) f_{b/B}(x_b, Q) \hat{\sigma}(ab \rightarrow X)$$

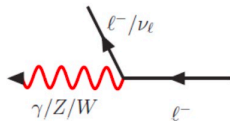
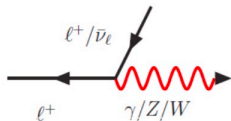
- a, b are the “partons” from the beam particles A, B
- $f_{a/A}(f_{b/B})$ are PDFs, defined as the probabilities of finding partons a (b) from the beam particles A (B) with the momentum fractions $x_a(x_b)$

• EW PDF

- ▶ Ultra-high energy at muon collider $Q > M_Z$: $\frac{v}{E} = \frac{v}{10 \text{ TeV}} \rightarrow 0$
- ▶ The SM gauge symmetry is restored and all EW states are dynamically activated.
- ▶ EW PDF:

“Equivalent photon approximation (EPA)”

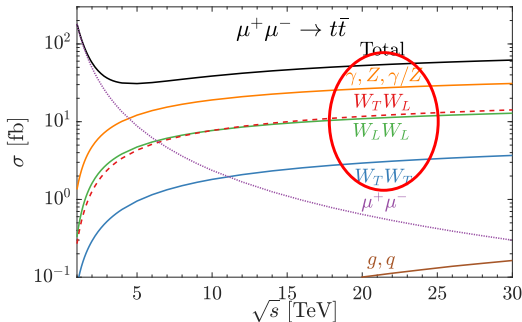
“Effective W Approximation (EWA)”



PLB 148(1984)367
NPB 249(1985)42

- ▶ We should take into account the four EW gauge bosons (B , W^i)

- Inclusive production cross section



2007.14300

- ▶ Sum over all partonic contributions and calculate the inclusive production cross section, e.g. $t \bar{t}$
- ▶ The direct $\mu\mu$ annihilation falls as $1/s$ and vector boson scattering (VBS) takes over it at high energies
- ▶ VBS is important at high energies

Heavy neutral lepton

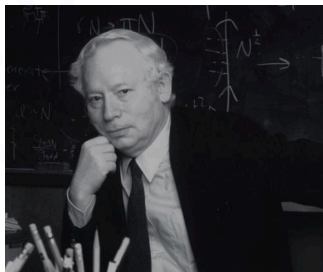


Tom between identities - tau-, electron- or muon-neutrino?

- Since the last century, a large number of neutrino oscillation experiments provide clear evidences that neutrinos have tiny masses. Obviously, it is contrary to the prediction of SM (neutrinos are massless)!!!
- It is well-known that, an economical way to generate neutrino mass in the SM content is through the dim-5 effective operator — “Weinberg operator”

$$\ell_L \ell_L H H$$

Phys.Rev.L.43,1566(1979)



- There are only three ultraviolet (UV) completions of this “Weinberg operator” at tree level:
 - PLB 67,421(1977), Conf.Proc.C 7902131,95(1979)
Conf.Proc.C 790927,315(1979), PRL 44,912(1980)
NATO Sci.Ser.B 61,687(1980), PRD 24,1232(1981)
 - Type-I Seesaw $\rightarrow SU(2)_L$ fermion singlet
 - PLB 70,433(1977)
PRD 22,2227(1980)
PRD 22,2860(1980)
Nucl.Phys.B 181,287(1981)
 - Type-II Seesaw $\rightarrow SU(2)_L$ scalar triplet
 - Type-III Seesaw $\rightarrow SU(2)_L$ fermion triplet
 - Z.Phys.C 44,441(1989)

- The heavy neutral lepton (**HNL**) can be realized in canonical Type I Seesaw mechanism

$$-\mathcal{L}_Y^I = Y_\nu^D \bar{\ell}_L \tilde{H} N_R + \frac{1}{2} \overline{(N^c)}_L M_R N_R + \text{h.c.}$$

- Mixing matrix $V_{\ell N}$: $\nu_\ell = \sum_{m=1}^3 (U_{\text{PMNS}})_{\ell m} \nu_m + \sum_{m'=1} (V_{\ell N})_{\ell m'} N_{m'}^c$

$$\mathcal{L}_{\text{Type-I}} \supset -\frac{g}{\sqrt{2}} W_\mu^- \sum_{\ell=e}^{\tau} \left(\sum_{m=1}^3 \bar{\ell} (U_{\text{PMNS}})_{\ell m} \gamma^\mu P_L \nu_m + \sum_{m'=1} \bar{\ell} (V_{\ell N})_{\ell m'} \gamma^\mu P_L N_{m'}^c \right) + \text{h.c.}$$

$$-\frac{g}{2 \cos \theta_W} Z_\mu \sum_{\ell=e}^{\tau} \left(\sum_{m=1}^3 \bar{\nu}_\ell (U_{\text{PMNS}})_{\ell m} \gamma^\mu P_L \nu_m + \sum_{m'=1} \bar{\nu}_\ell (V_{\ell N})_{\ell m'} \gamma^\mu P_L N_{m'}^c \right) + \text{h.c.}$$

• The search of Majorana neutrino at hadron colliders

PRL 97, 171804 (2006)

PHYSICAL REVIEW LETTERS

week ending
27 OCTOBER 2006

Signatures for Majorana Neutrinos at Hadron Colliders

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²Center for High Energy Physics, Tsinghua University, Beijing 100084, People's Republic of China

³Institute of Theoretical Physics, Academia Sinica, Beijing 100080, People's Republic of China

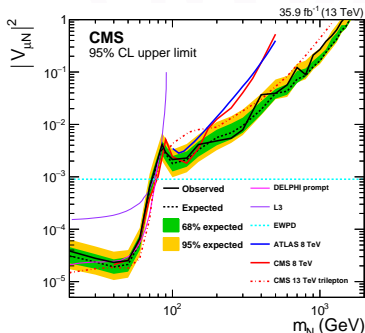
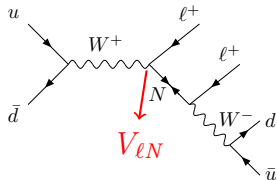
(Received 11 April 2006; published 25 October 2006)

The Majorana nature of neutrinos may only be experimentally verified via lepton-number violating processes involving charged leptons. We explore the $\Delta L = 2$ like-sign dilepton production at hadron colliders to search for signals of Majorana neutrinos. We find significant sensitivity for resonant production of a Majorana neutrino in the mass range of 10–80 GeV at the current run of the Tevatron with 2 fb^{-1} integrated luminosity and in the range of 10–400 GeV at the CERN LHC with 100 fb^{-1} .

DOI: [10.1103/PhysRevLett.97.171804](https://doi.org/10.1103/PhysRevLett.97.171804)

PACS numbers: 14.60.Pq, 13.15.+g, 13.85.Qk, 14.60.St

Lepton number violation (LNV)
signature: $pp \rightarrow \ell^\pm \ell^\pm jj$

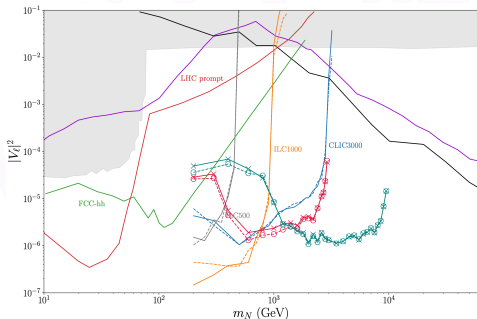
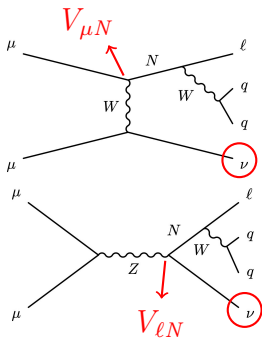


• The search of HNLs at muon colliders 2301.02602

2301.05177

2301.07117

► The signal at $\mu^+\mu^-$ collider: $\mu^+\mu^- \rightarrow N_\ell + \bar{\nu}_\ell$



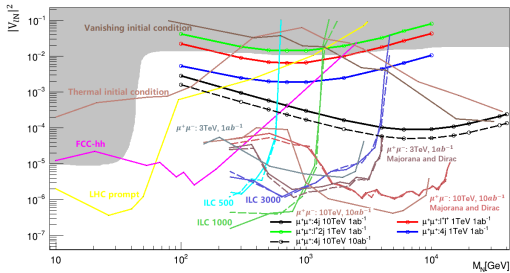
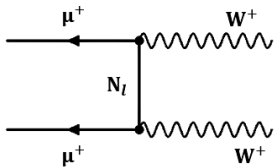
► Features :

- light ν in final states, but Majorana or Dirac type?
- t-channel only sensitive to $V_{\mu N}$
- $V_{\ell N}$ in s-channel

• The search of HNLs at muon colliders 2302.13247

2304.04483

- ▶ The signal at $\mu^+ \mu^+$ collider: $\mu^+ \mu^+ \rightarrow W^+ W^+$

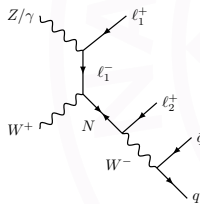
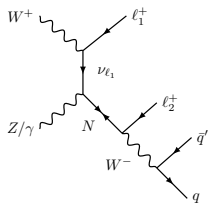


- ▶ Features :

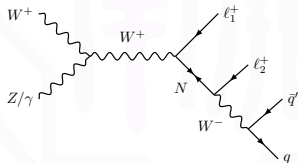
- it can probe HNLs with heavier mass
- only sensitive to $V_{\mu N}$, but $\sigma \propto |V_{\nu N}|^4$ is weaker than $\mu^+ \mu^-$
- LNV through W^+ 's hadronic decays, but it be suppressed by $\text{BR}(W \rightarrow qq')^2 \sim 40\%$

- **Our proposal: LNV through vector boson scattering (VBS)**

► The signal at $\mu^+\mu^-$ collider: $V_i V_j \rightarrow \ell_1^\pm N \rightarrow \underline{\ell_1^\pm \ell_2^\pm q \bar{q}}$



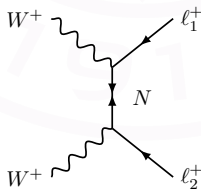
clear LNV signature



► The signal at $\mu^+\mu^+$ collider:

$$W^+ W^+ \rightarrow \underline{\ell^+ \ell^+}$$

clear LNV signature



HNLs

- We simulate to investigate HNLs at muon collider, by using the MadGraph, Madspin, Pythia and Delphes ...



MadGraph5_aMC@NLO

JHEP 07(2014)079

generate parton-level events

parton-shower



PYTHIA 8.3

Comput.Phys.Commun.191(2015)

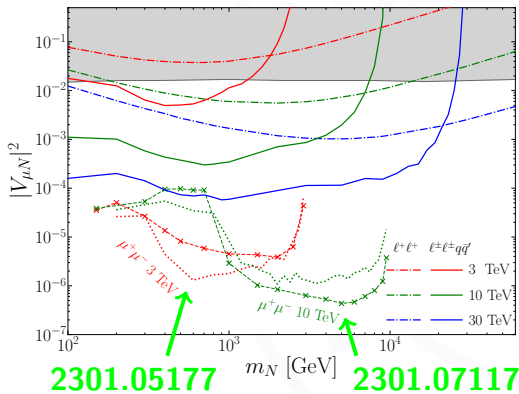
simulate the detector of collider



DELPHES
fast simulation

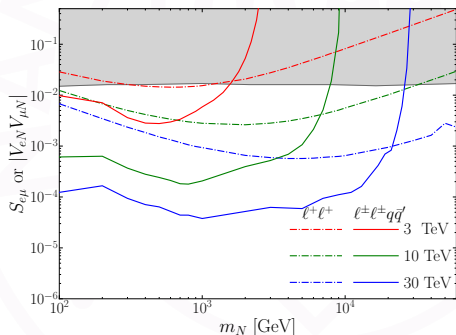
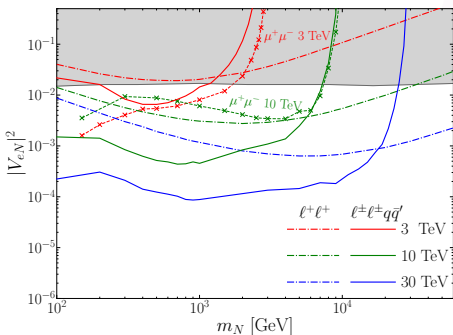
JHEP02(2014)057

- 2σ exclusion limits for $|V_{\mu N}|^2$



- ▶ The probing potential of $|V_{\mu N}|^2$ is worse than that from other annihilation channels.
- ▶ But we provide smoking-gun LNV signatures as a complement by the VBS process.

- 2σ exclusion limits for $|V_{eN}|^2$ and $|V_{eN} V_{\mu N}|$



- The probing potential of $|V_{eN}|^2$ is stronger than that from $\mu^+\mu^- \rightarrow N \nu$ channel with $\sqrt{s} = 10$ TeV or above.
- It can probe lepton flavor combination

Summary

- High-energy muon colliders are potentially ideal machines in both energy and precision frontiers.
- We propose a clear LNV signature through VBS process to search for the heavy neutral lepton at both $\mu^+\mu^-$ and $\mu^+\mu^+$ colliders.

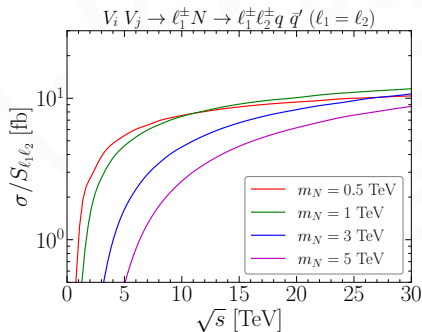
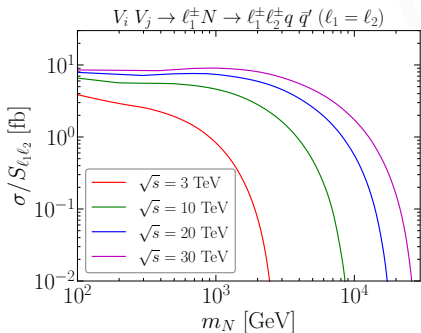
The background features a large, faint watermark of the Tsinghua University logo. The logo is circular and contains the university's name in English, "TSINGHUA UNIVERSITY", around the top edge and the year "1911" at the bottom. In the center is a shield-shaped emblem with the Chinese characters "清華" (Qinghua) written vertically.

Thank you!

backup

- **The LNV signature:** $W^\pm Z/\gamma \rightarrow \ell_1^\pm N \rightarrow \ell_1^\pm \ell_2^\pm W^\mp \rightarrow \ell_1^\pm \ell_2^\pm q\bar{q}'$
 - ▶ The parameter-independent cross section

$$\begin{aligned}\sigma(V_i V_j \rightarrow \ell_1^\pm \ell_2^\pm q\bar{q}') &\approx \sigma(V_i V_j \rightarrow \ell_1^\pm N) \times \text{BR}(N \rightarrow \ell_2^\pm q\bar{q}') \times (2 - \delta_{\ell_1 \ell_2}) \\ &\equiv \frac{|V_{\ell_1 N} V_{\ell_2 N}|^2}{\sum_{\ell=e,\mu,\tau} |V_{\ell N}|^2} \times \sigma_0 \times (2 - \delta_{\ell_1 \ell_2}),\end{aligned}$$



backup

- ▶ The benchmark choices of the collider energies and the corresponding integrated luminosities are

\sqrt{s}	3 TeV	10 TeV	30 TeV
\mathcal{L}	1 ab ⁻¹	10 ab ⁻¹	90 ab ⁻¹

- ▶ The SM backgrounds we are considering

$$B_1: V V \rightarrow W^\pm W^\pm W^\mp \rightarrow \ell^\pm \ell^\pm \bar{\nu}_\ell^{(-)} \nu_\ell^{(-)} q \bar{q}',$$

$$B_2: V V \rightarrow t \bar{t} W^\pm \rightarrow b W^+ \bar{b} W^- W^\pm \rightarrow b \bar{b} \ell^\pm \ell^\pm \bar{\nu}_\ell^{(-)} \nu_\ell^{(-)} + X,$$

where X denotes the decay products of the opposite-sign W boson in B_2 background, i.e., $X = \ell^\mp \bar{\nu}_\ell^{(-)}$ or $q \bar{q}'$.

backup

- ▶ Based on the difference between distributions of signal and backgrounds, we employ some cuts for the final states to suppress the background

- identify final states

$$N_\mu \geq 2, N_J \geq 1,$$
$$65 \leq m_J \leq 95 \text{ GeV}$$

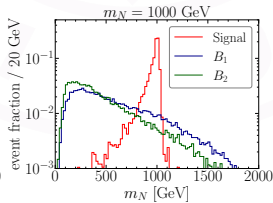
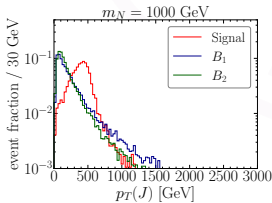
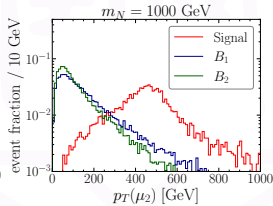
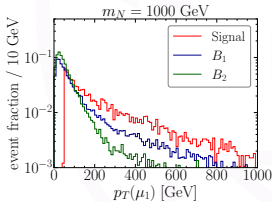
- some basic cuts

$$p_T(\mu), |\eta(\mu)|, \Delta R_{\mu\mu} \dots$$

- kinematic cuts

$$p_T(\mu, J) > m_N/4$$

$$0.8 m_N < m_{\mu_2 J} < 1.1 m_N$$



backup

- ▶ We use the following formula to evaluate the significance

$$\mathcal{S} = \frac{N_S}{\sqrt{N_S + N_B}},$$

$$N_S = \sigma_0 S_{l_1 l_2} \times \epsilon_S \times \mathcal{L}$$

$$N_{B_i} = \sigma_{B_i} \times \epsilon_{B_i} \times \mathcal{L}, \quad i = 1, 2$$

- ▶ 2σ exclusion limits for $|V_{\mu N}|^2$

The probing potential of $|V_{\mu N}|^2$ is worse than that from other annihilation channels.

But we provide smoking-gun LNV signatures as a complement by the VBS process.

