

The MUonE Experiment: Understanding Muon $g - 2$ Puzzle via $\mu - e$ Scattering

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on behalf of the MUonE collaboration

MIP 2024



UNIVERSITY OF
LIVERPOOL

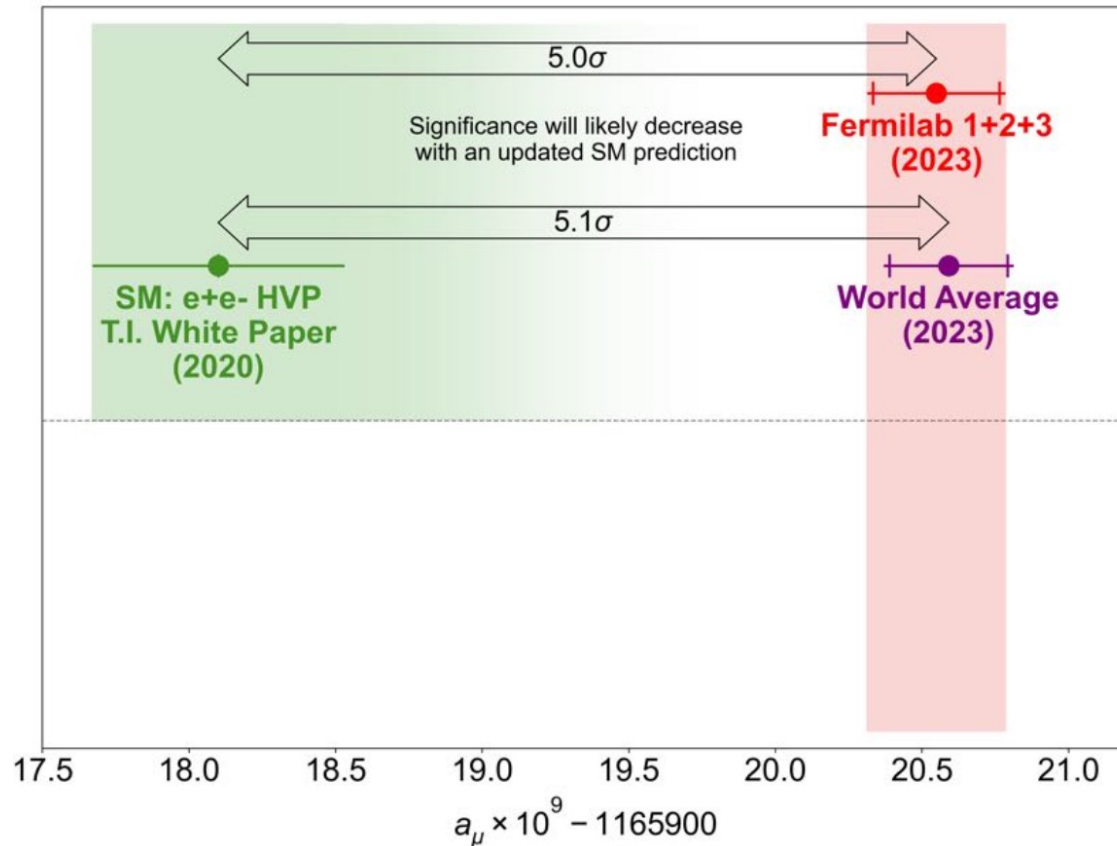
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TRUST

The MUonE Experiment: Understanding Muon $g - 2$ Puzzle via $\mu - e$ Scattering

- ▶ Muon $g - 2$ Puzzle
- ▶ The MUonE Experiment
 - Principle
 - Setups
 - Test runs & first results
 - Timeline
- Summary

Muon $g - 2$ Puzzle

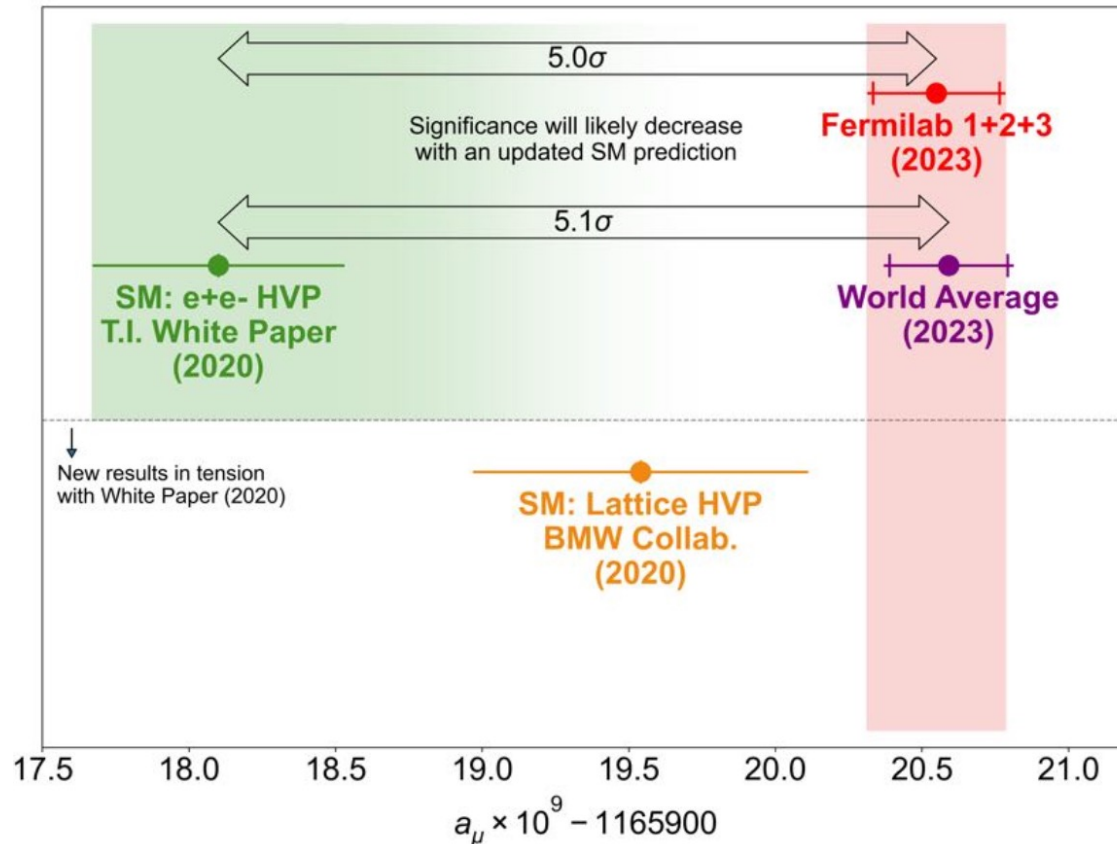
Discrepancy between experiments & theories



- New experimental average with SM prediction (WP-2020) gives $> 5\sigma$

Muon $g - 2$ Puzzle

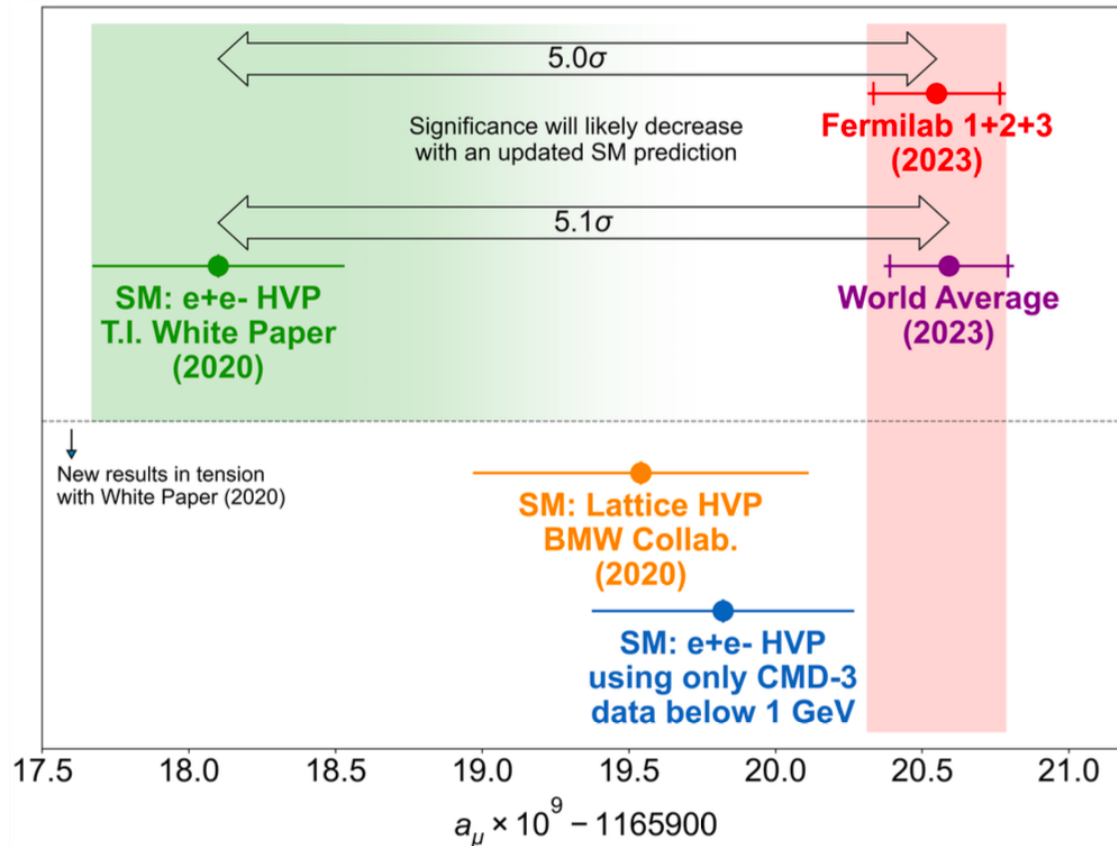
Discrepancy between experiments & theories



- New experimental average with SM prediction (WP-2020) gives $> 5\sigma$
- Since then, two important developments on SM prediction:
 - Lattice QCD from the BMW (2020)

Muon $g - 2$ Puzzle

Discrepancy between experiments & theories



- New experimental average with SM prediction (WP-2020) gives $> 5\sigma$
- Since then, two important developments on SM prediction:
 - Lattice QCD from the BMW (2020)
 - New $e^+e^- \rightarrow \pi^+\pi^-$ cross section from CMD-3 (2023)

➤ Disclaimer:

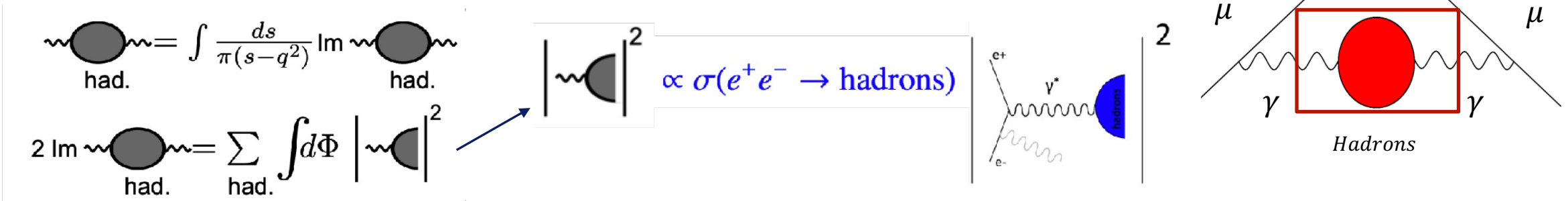
The CMD-3 point is a visual exercise. It is not a fully updated SM prediction!

- T.I. White Paper result has been substituted by CMD-3 only for 0.33 \rightarrow 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes \rightarrow should not be taken as final!

Muon $g - 2$ Puzzle

Standard Model (SM) predictions

- The uncertainty in the SM prediction of a_μ is **entirely limited** by our knowledge of the hadronic leading order contribution a_μ^{HLO} ($a_\mu^{\text{HVP},\text{LO}}$)
- Approaches (at low-E):
 - 1) Lattice QCD Method: Ab-initio calculation on lattice
 - 2) Dispersive Method: using $\sigma(e^+e^- \rightarrow \text{hadrons})$ data

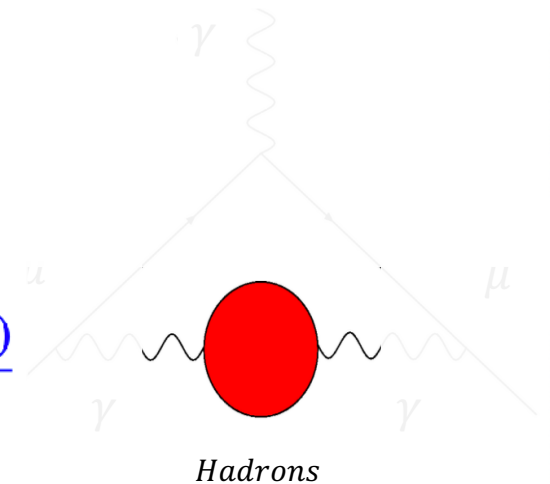


Muon $g - 2$ Puzzle

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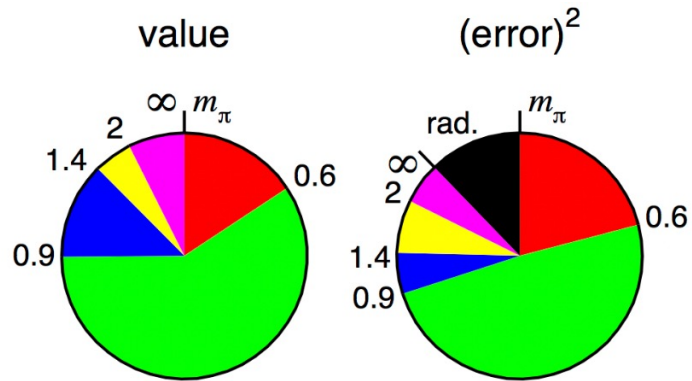
$$a_\mu^{\text{HVP}} = \left(\frac{\alpha m_\mu}{3\pi}\right)^2 \int_{m_{\pi^0}^2}^{\infty} ds \frac{R_{\text{had}}(s) K(s)}{s^2}, \quad R_{\text{had}}(s) = \sigma(e^+e^- \rightarrow \text{hadrons}) \left/ \frac{4\pi\alpha(s)}{(3s)} \right.$$



Muon $g - 2$ Puzzle

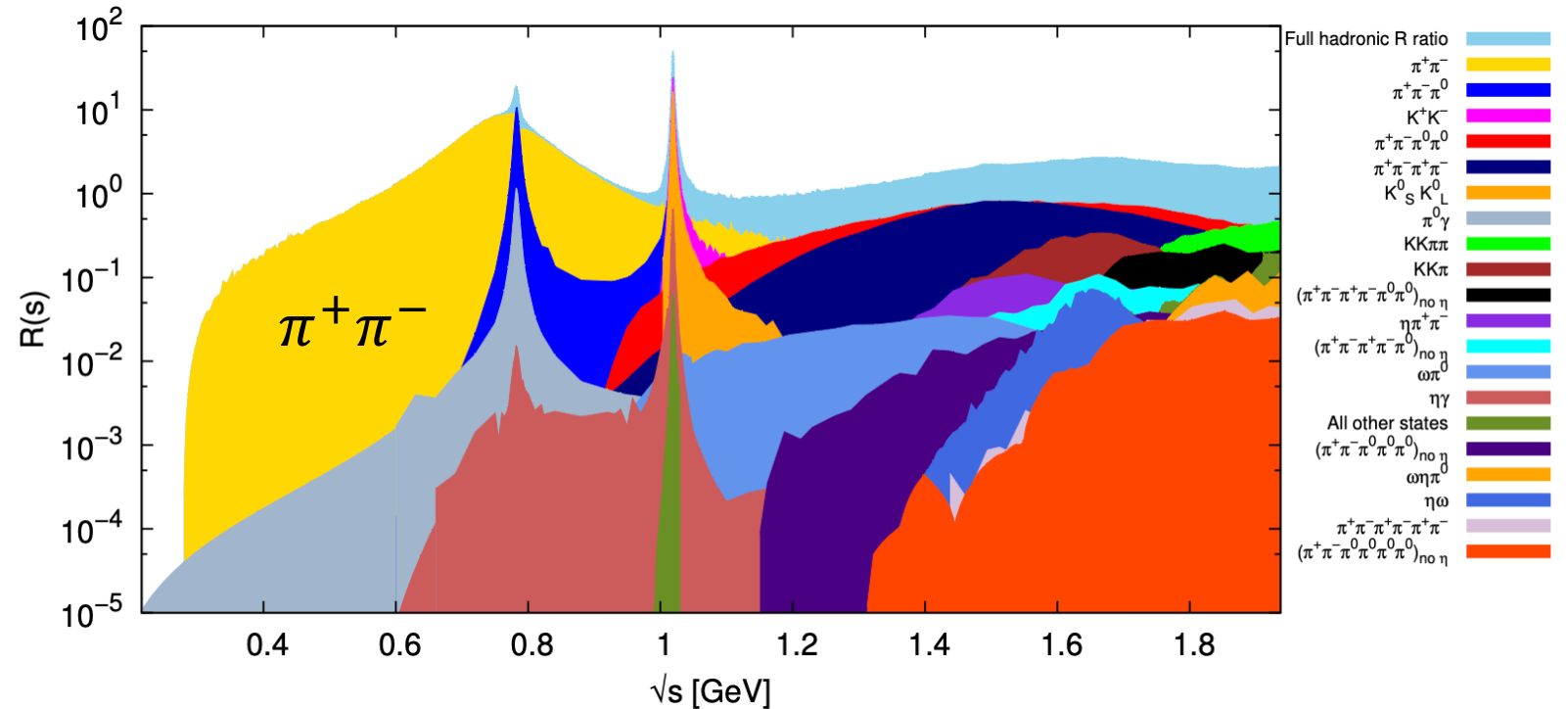
Chaotics in $e^+e^- \rightarrow \pi^+\pi^-$ for a_μ^{HVP}

- $e^+e^- \rightarrow \pi^+\pi^-$ channel is the major source of uncertainty in a_μ^{HVP}



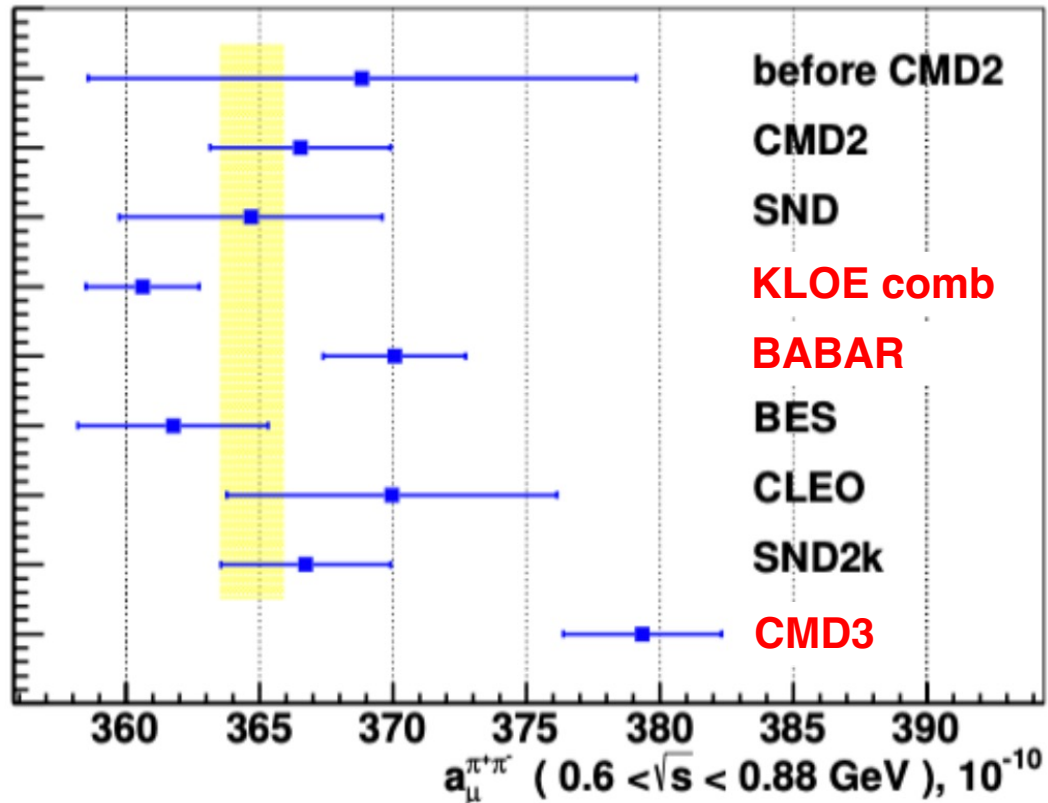
Keshavarzi, Nomura, Teubner 2018

$\sigma(e^+e^- \rightarrow \text{hadrons})$ contribution
in the energy region



Muon $g - 2$ Puzzle

Chaotics in $e^+e^- \rightarrow \pi^+\pi^-$ for a_μ^{HVP}

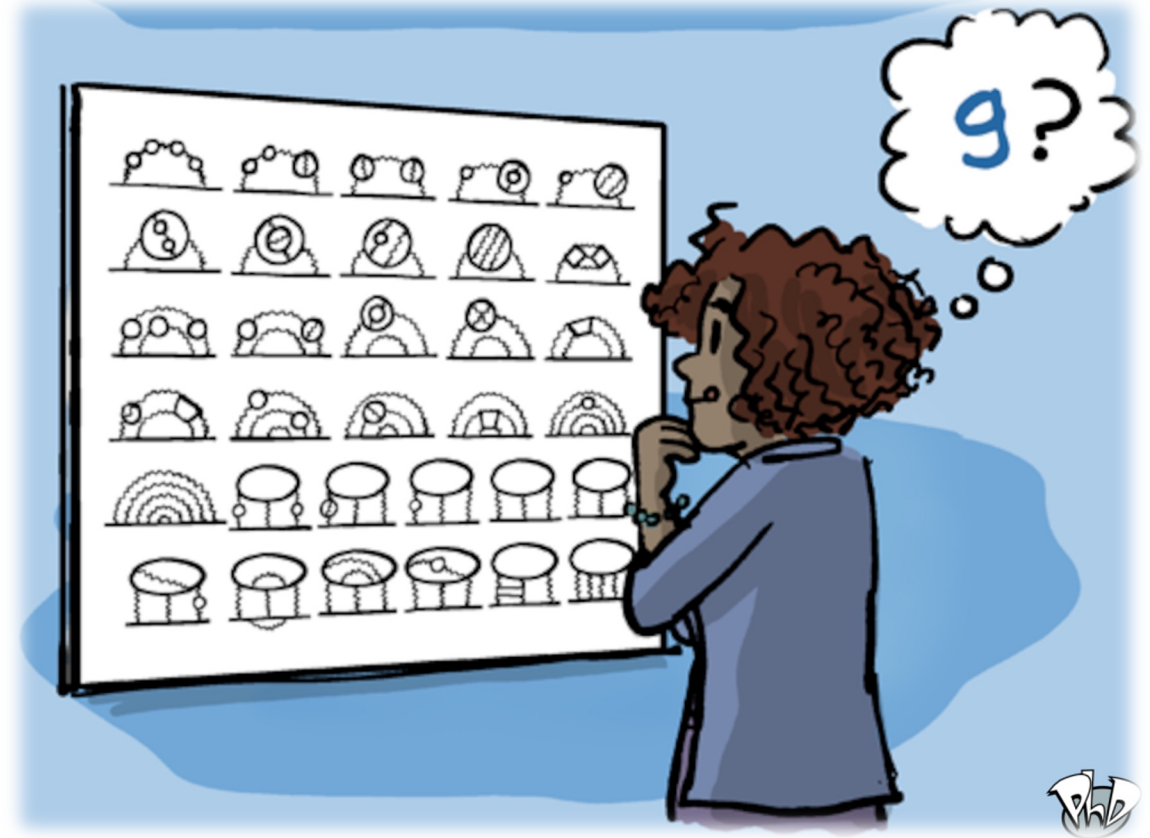


- Discrepancy between **KLOE** and **BABAR** result needs further investigation
- A recently published **CMD-3 result** was different from all the previous data!

Muon $g - 2$ Puzzle

A quick summary on the muon $g-2$ theory puzzle:

- a_{μ}^{HVP} represents a major uncertainty
- e^+e^- data-driven \Leftrightarrow Lattice conflict
- Conflicts in the data-driven method:
 - BABAR \Leftrightarrow KLOE
 - Latest CMD3 \Leftrightarrow all the previous data

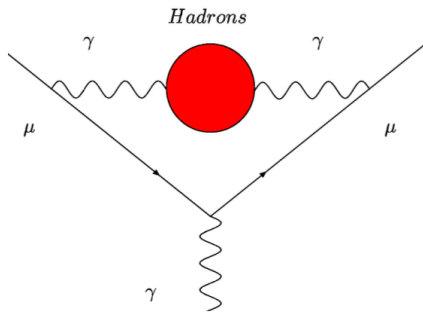


MUonE Experiment



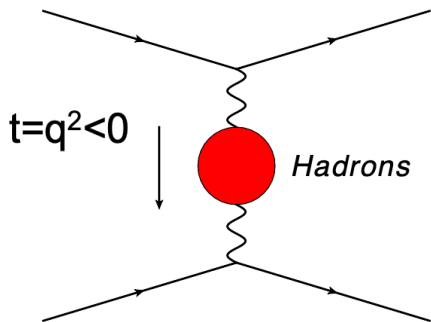
A new approach measuring $\alpha_{\mu}^{\text{HVP}}$ with running of $\Delta\alpha_{\text{had}}$

- The dispersive approach to compute $\alpha_{\mu}^{\text{HVP,LO}}$ is via the **time-like** formula:



$$\alpha_{\mu}^{\text{HVP}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{m_{\pi^0}^2}^{\infty} ds \frac{R_{\text{had}}(s) \mathbf{K}(s)}{s^2}, \quad \mathbf{K}(s) = \int_0^1 dx \frac{x^2(1-x)}{x^2 + (1-x)(s/m_{\mu}^2)}$$

- Alternatively, exchanging the x and s integrations \rightarrow **space-like** formula:



$$\alpha_{\mu}^{\text{HVP}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)], \quad t(x) = \frac{x^2 m_{\mu}^2}{x-1} < 0$$

- $\Delta\alpha_{\text{had}}$ is the hadronic contribution to the **running α** (electromagnetic coupling constant)

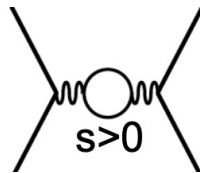
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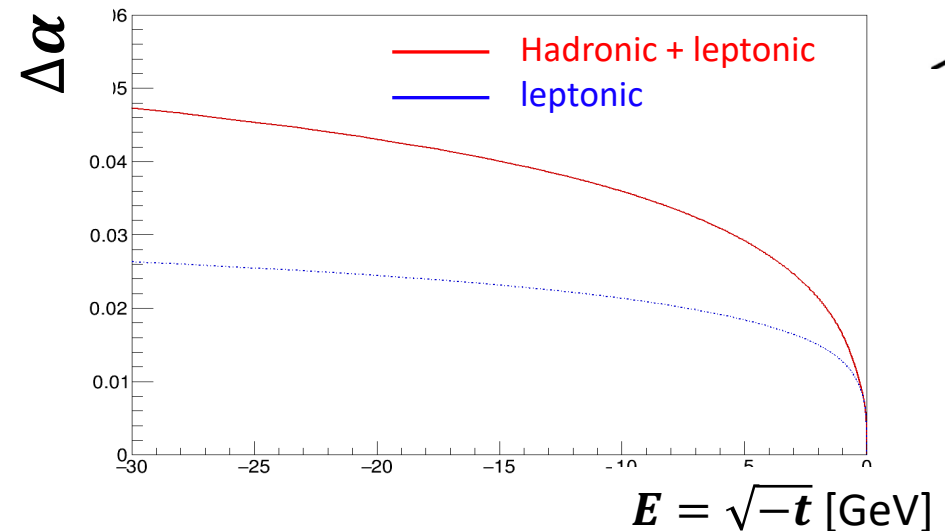
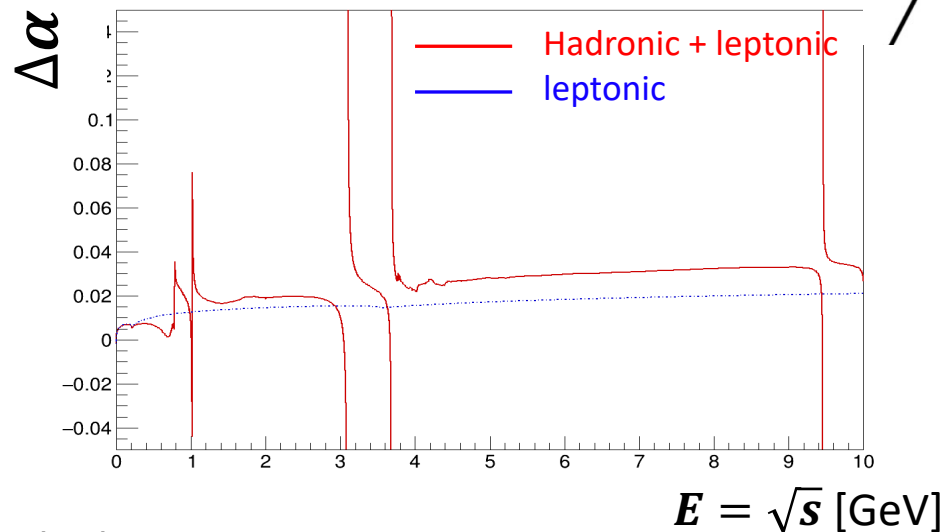
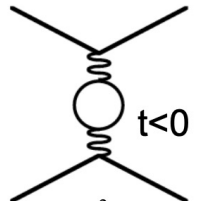
Running of $\Delta\alpha_{had}$: 'Time-like' vs 'Space-like'

$$\Delta\alpha_{had}^{(5)}(q^2) = -\frac{\alpha}{3\pi} q^2 \int_{m_{\pi^0}^2}^{\infty} ds' \frac{R(s')}{s'(s' - q^2)}$$

- Time-like:** characterized by the opening of resonances



- Space-like:** very smooth behaviour

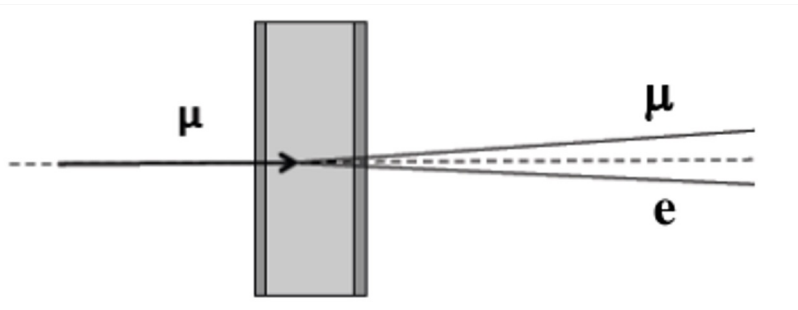


MUonE Experiment

$\Delta\alpha_{\text{had}}$ via Muon-electron scattering



- $\Delta\alpha_{\text{had}}[t(x)]$ can be extracted from the **shape** of the differential cross-section of **muon-electron scattering** $\mu^+ e^- \rightarrow \mu^+ e^-$



$$R_{\text{had}} = \frac{d\sigma_{\text{data}}(\Delta\alpha_{\text{had}})}{d\sigma_{\text{MC}}(\Delta\alpha_{\text{had}} = 0)} \sim 1 + \underline{2\Delta\alpha_{\text{had}}(t)}$$

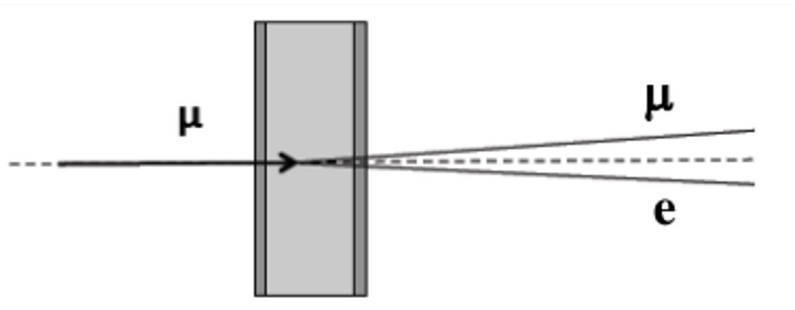
To be determined
in this experiment

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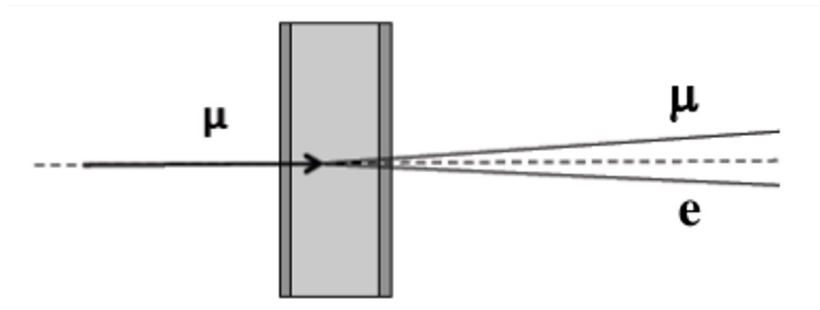
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The NNLO differential cross section from **theoretical calculation**

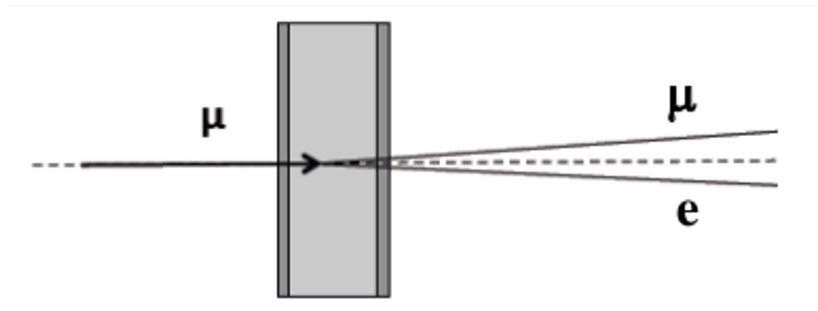
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MUonE Experiment



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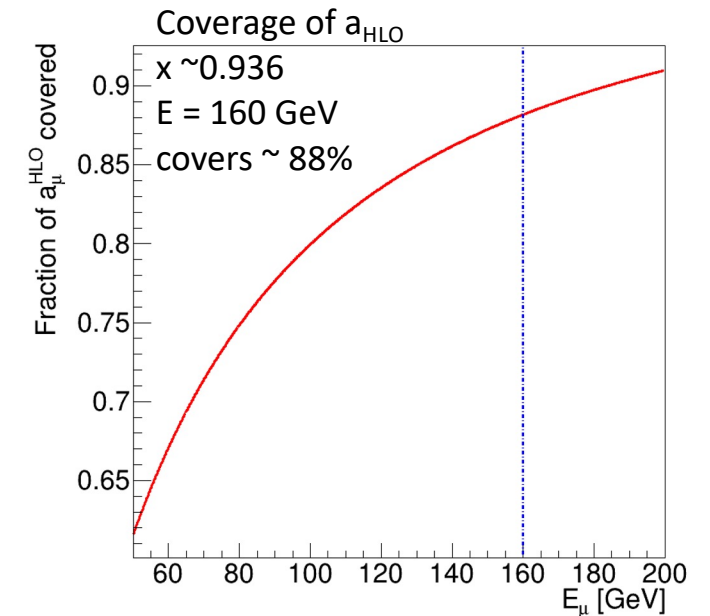
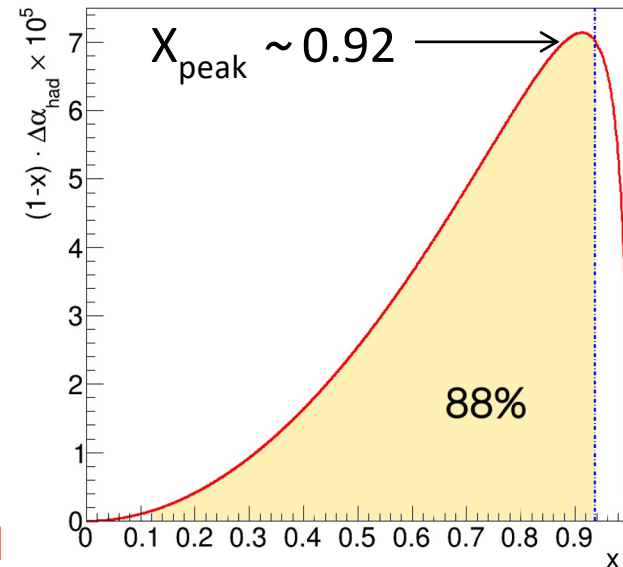


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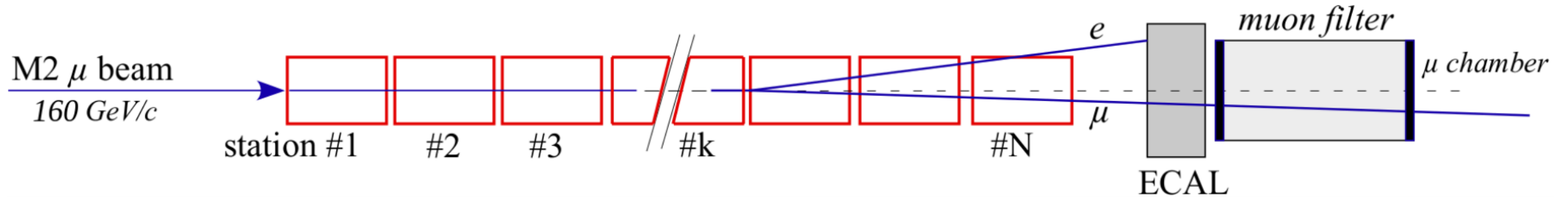
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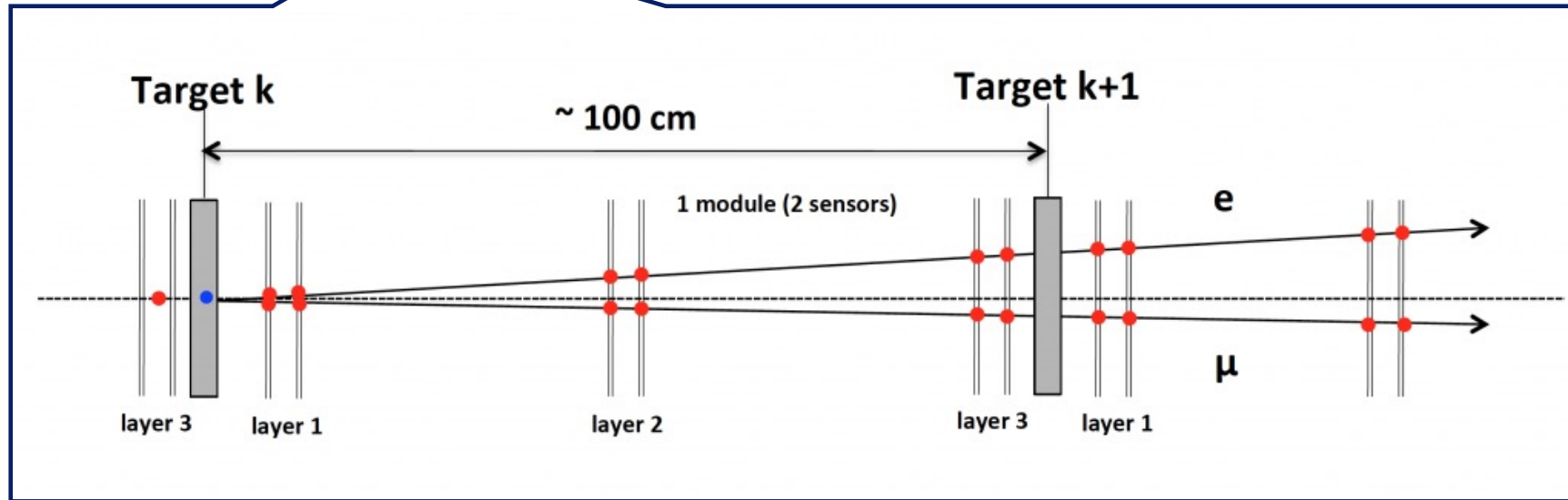
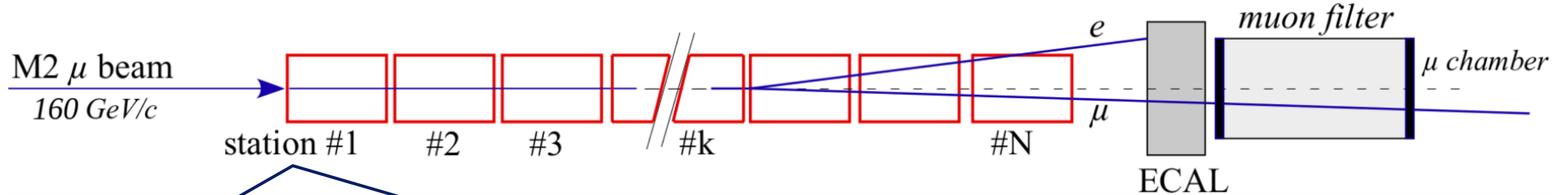
MUonE Experiment

Setup overview



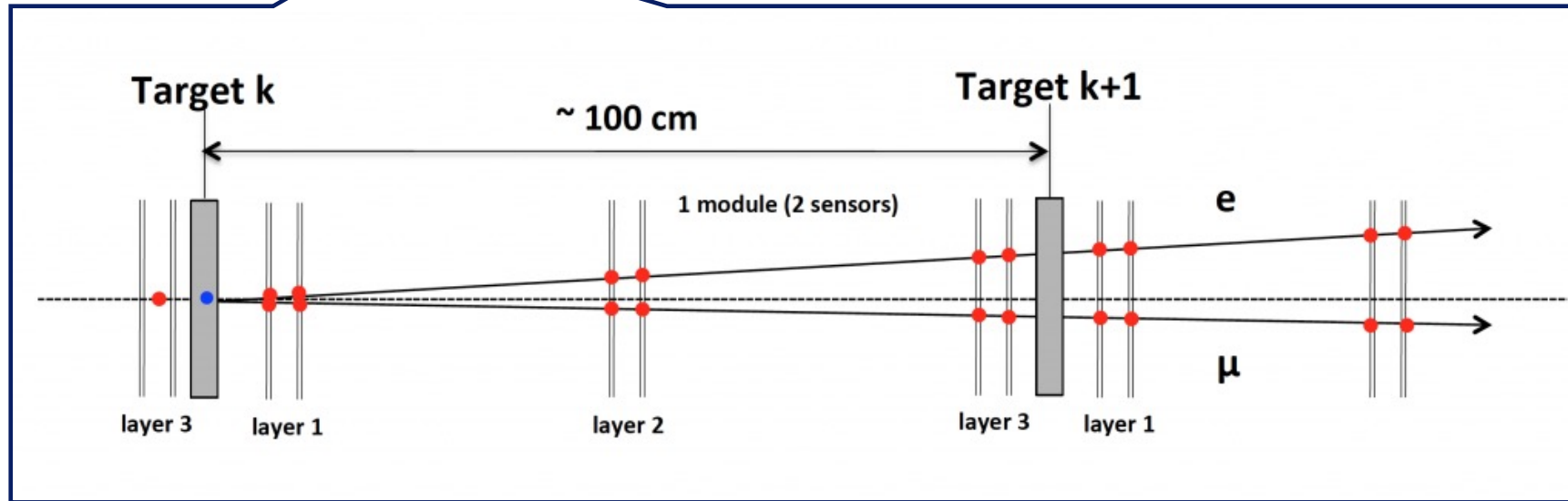
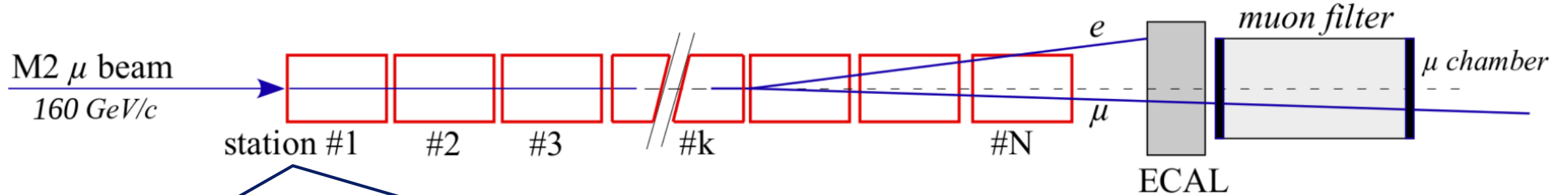
MUonE Experiment

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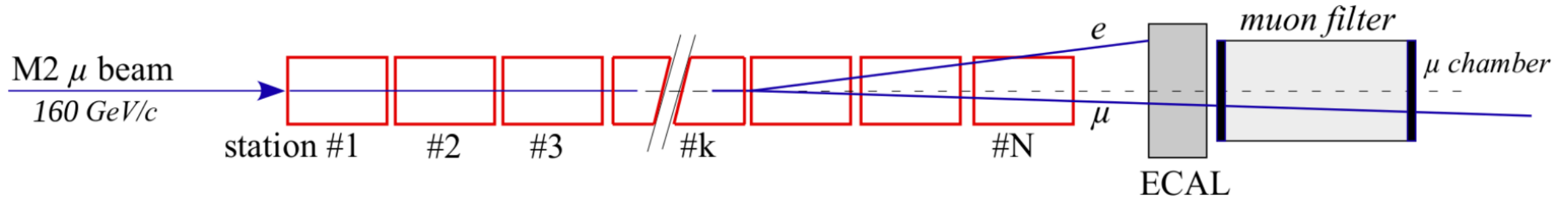
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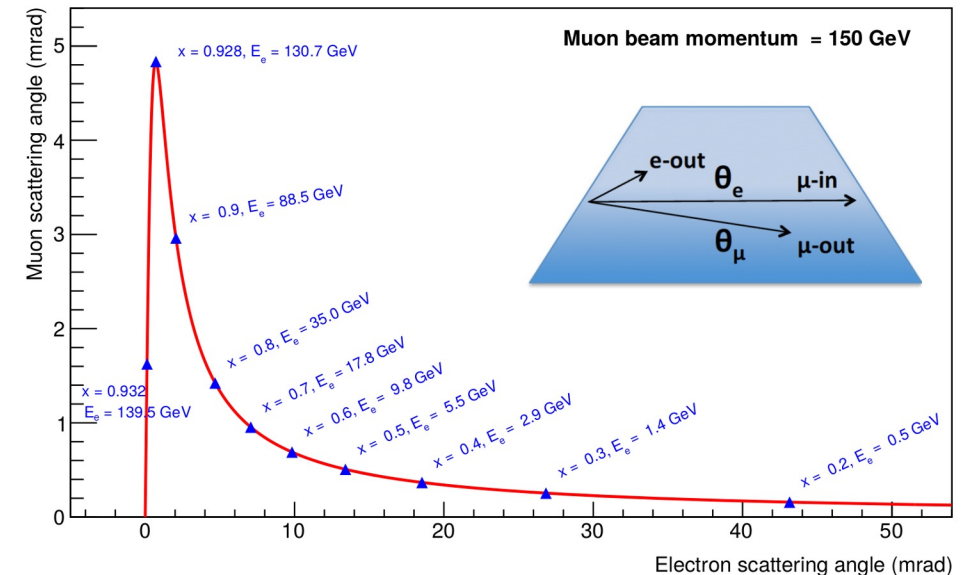
- Be (or C) target divided into 40 slices with a few cm thickness
- Tracking system: 3 pairs of silicon strip detectors
- ECAL: energy and PID

MUonE Experiment

Setup overview

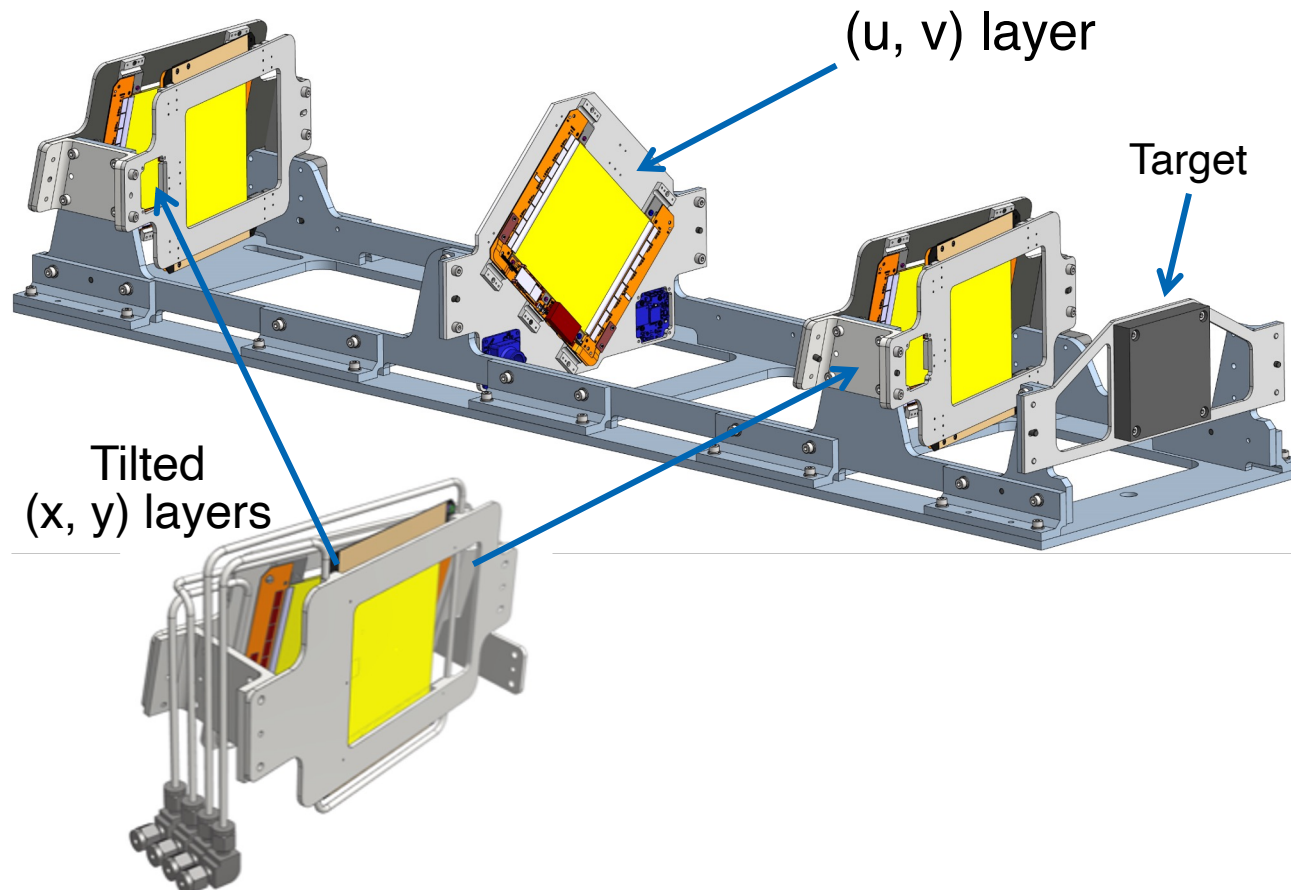


- **Angle correlation** between muon and electron allows to select elastic events and reject background ($\mu N \rightarrow \mu N e^+e^-$).
- Boosted kinematics:
 - Single detector to cover full acceptance
 - $\theta_\mu < 5$ mrad, $\theta_e < 32$ mrad.



MUonE Experiment

Setup: the tracking station



- Two (x, y) layers and (u, v) layer
 - (x, y) layers tilted for better resolution
 - (u, v) layer rotated to solve reconstruction ambiguities.
- Relative position between stations must be stable at **10 μm** → **a super precise experiment!**
 - Low-CTE material (INVAR, carbon)
 - Well-controlled temperature
 - Laser system to monitor stability

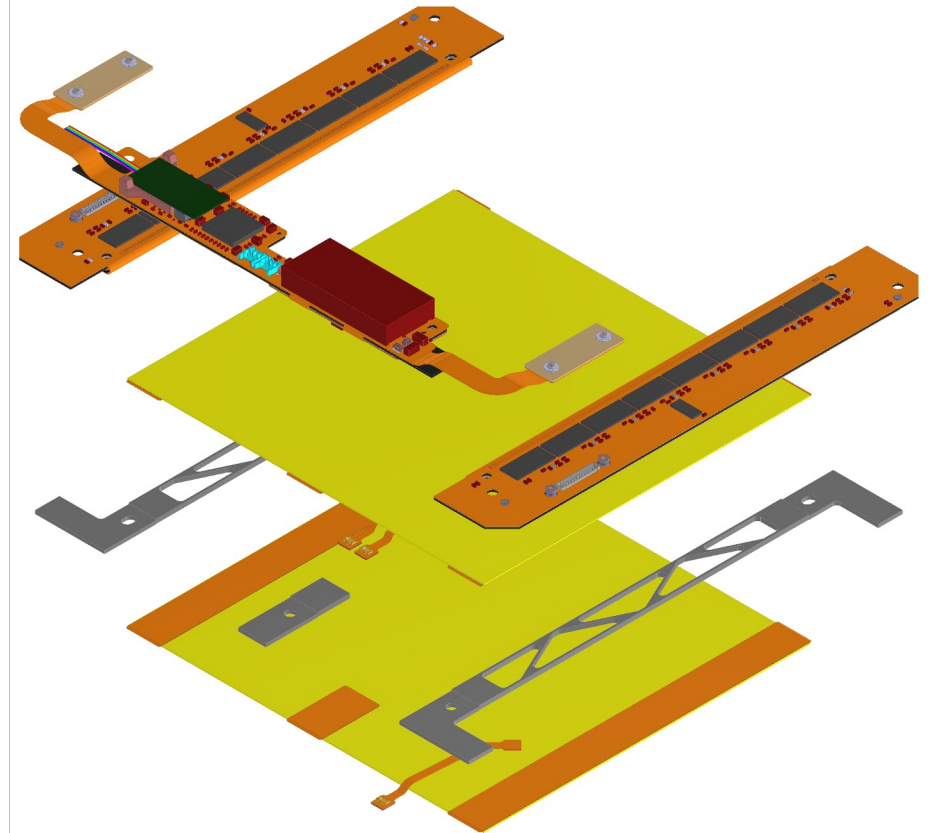
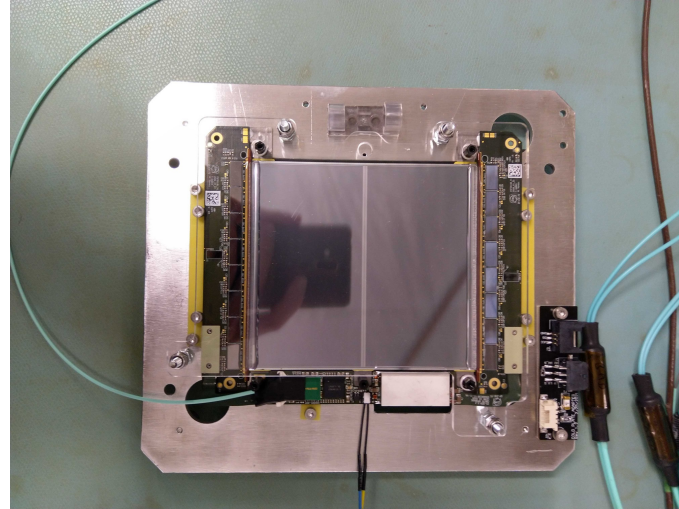
MUonE Experiment

Setup: the tracker (CMS 2S Module)

- Silicon strip sensors currently in production for the CMS-Phase 2 upgrade (HL-LHC).
- Each module is divided in two independent halves.

A single half:

- 1016 strips
- 5 cm long
- Divided in 8 sectors
- Each sector has independent read-out



MUonE Experiment

Setup: calorimeter

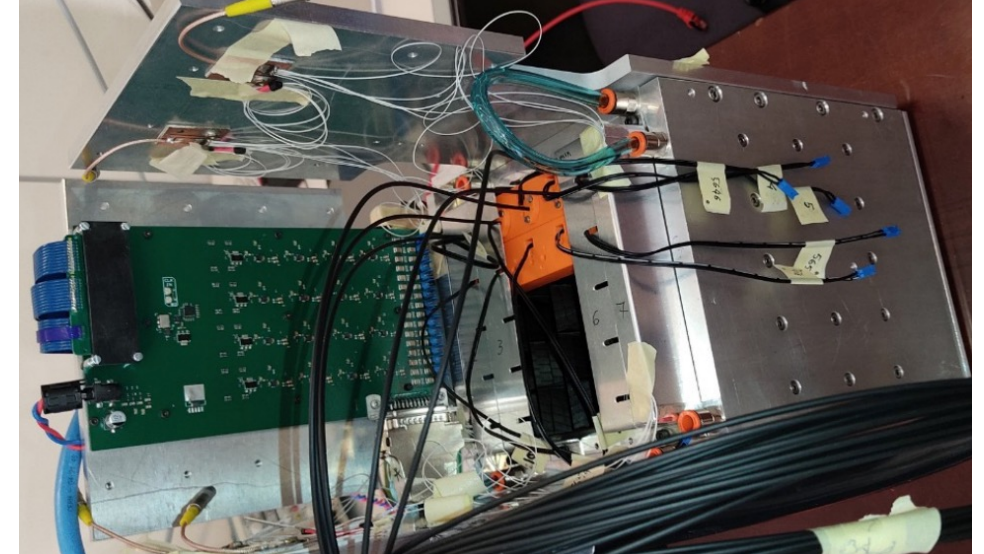


- A forward ECAL covering part of the total scattering acceptance
- Useful for **PID** & systematic study (an independent kinematic measurement)
- Support from FNAN muon g-2 ECAL

Transverse dim: $\sim 1 \times 1 \text{ m}^2$

5x5 PbWO₄ crystals:

- Area: $2.85 \times 2.85 \text{ cm}^2$
- Length: 22 cm ($\sim 25 \text{ X0}$).
- Total area: $\sim 14 \times 14 \text{ cm}^2$.
- Readout: APD sensors.



The experiment location

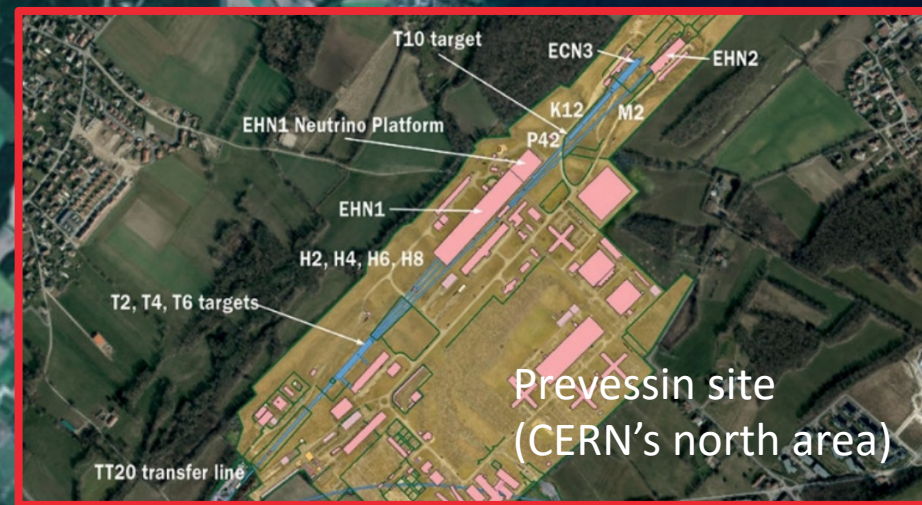
Muon (M2) beam-line at CERN Préveessin site

μ ONE



The experiment location

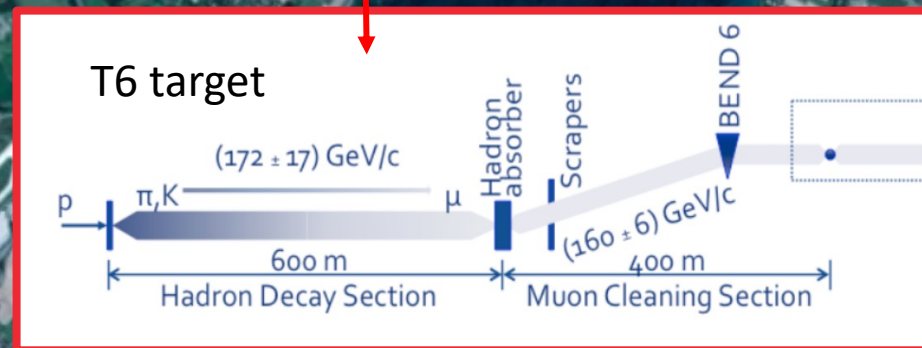
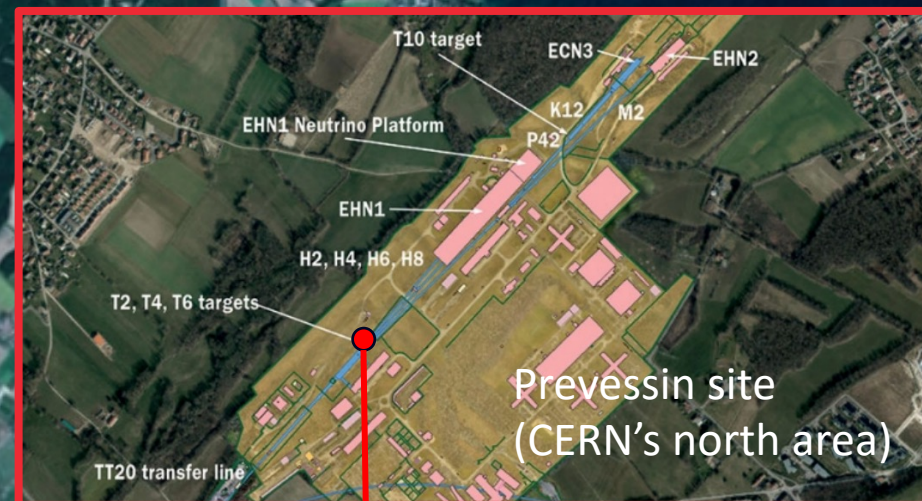
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μ ONE



Test runs

Joint test with CMS tracker group from 2021 to 2023



Oct – Nov 2021

- First test of the 2S module with tracker DAQ system
- Also confirmed thermal stability of the mechanical structure

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July and Oct 2022

- 1 full station (6 modules) + ECAL in the proposed MUonE location
- Beam intensity and profile measured in the real beam conditions

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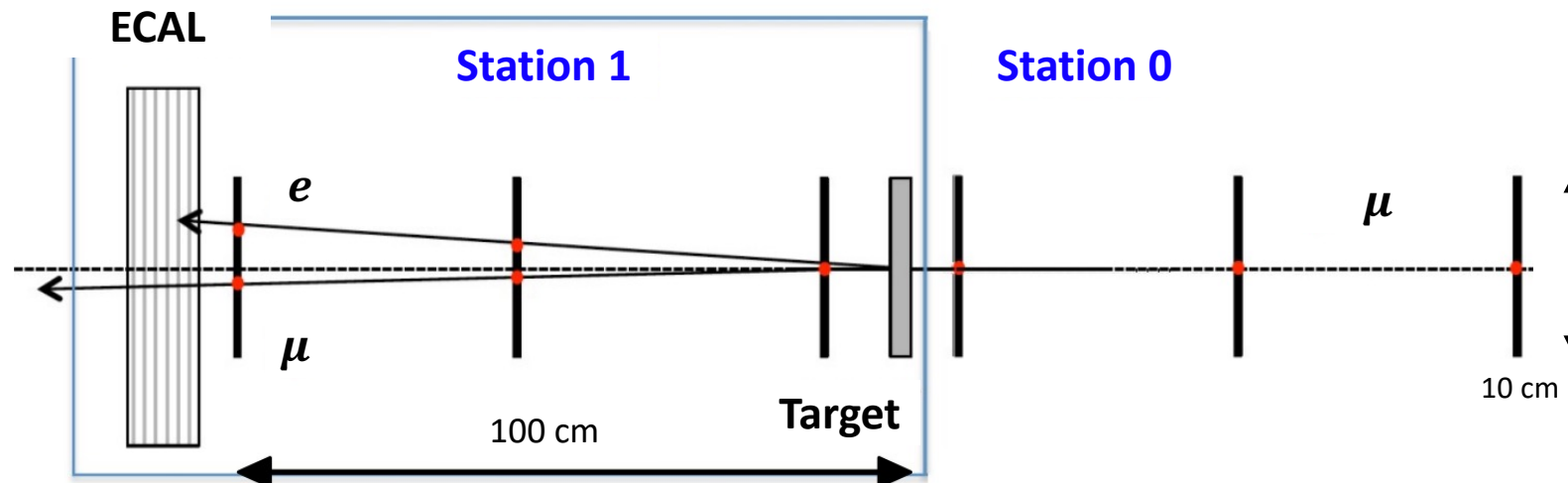
Aug – Sep 2023

- **First physics data taking to for the $\Delta\alpha_{lep}$ measurement**

Test run 2023

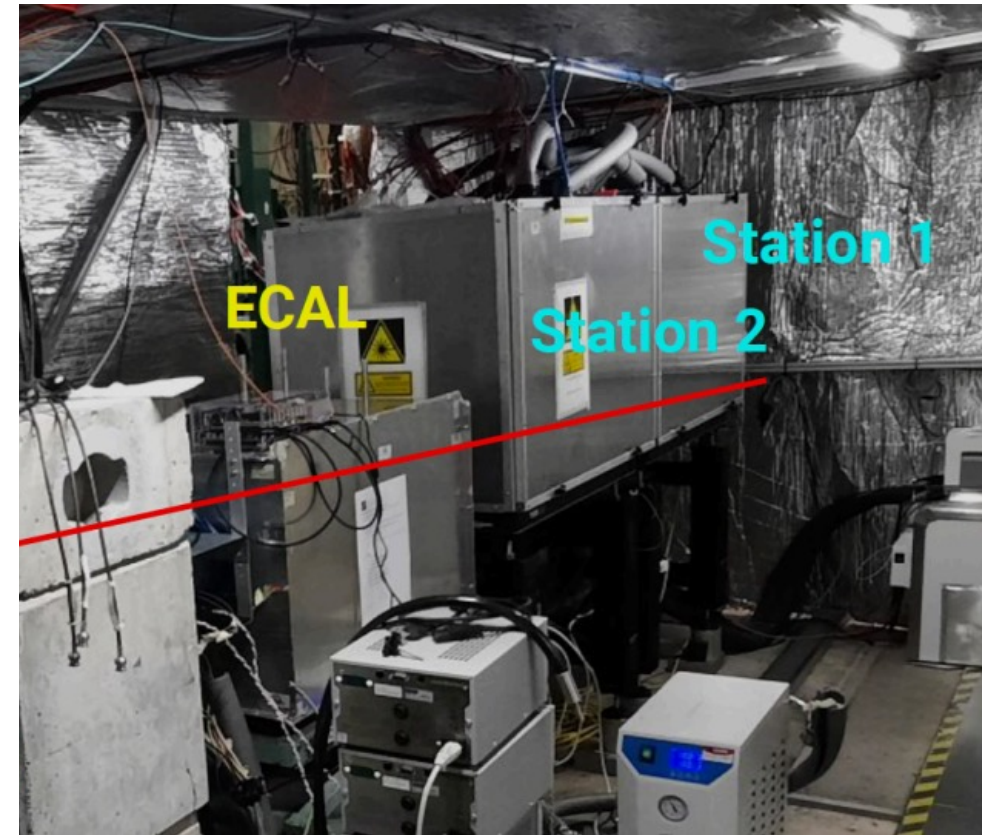
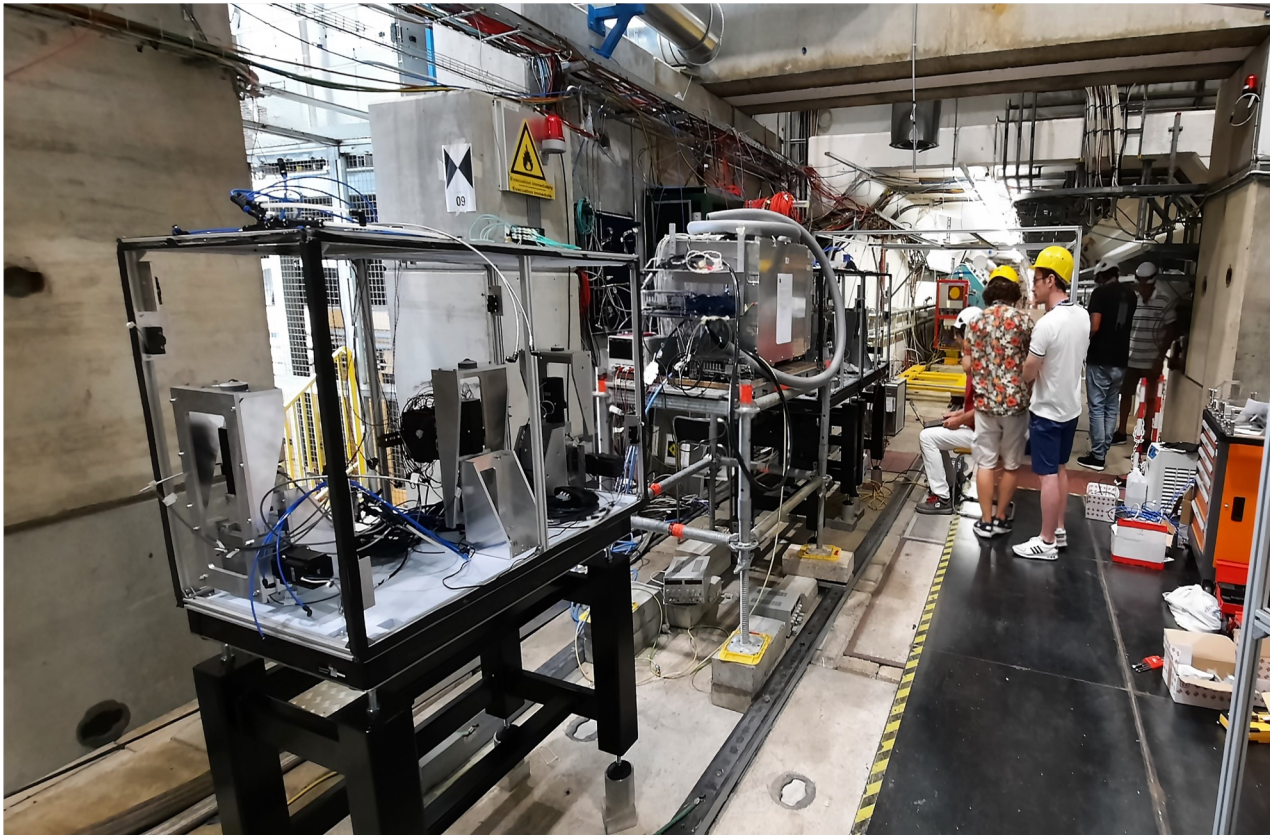
2 stations (pre-tracker + target + tracker) + ECAL

- Expected luminosity: $\sim 1 \text{ pb}^{-1}$
- $\sim 10^{12}$ μ accumulated on target with $\sim 2.5 \times 10^8$ elastic events with $E_e > 1 \text{ GeV}$
- Goal: demonstration measurement of $\Delta\alpha^{\text{LEP}}$ with a few % precision



Test run 2023

2 stations (pre-tracker + target + tracker) + ECAL



Test run 2023

Data sets under various configs



- 160 GeV muons with max asynchronous rate of 50 MHz (2E8/spill)

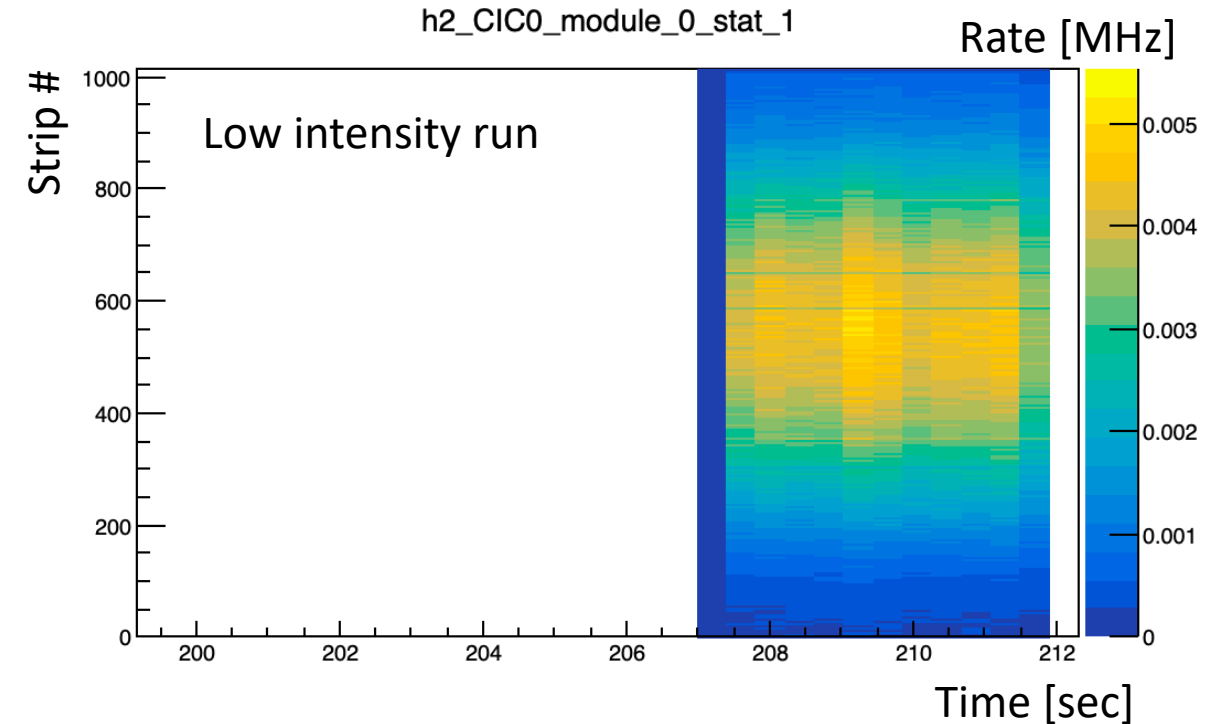
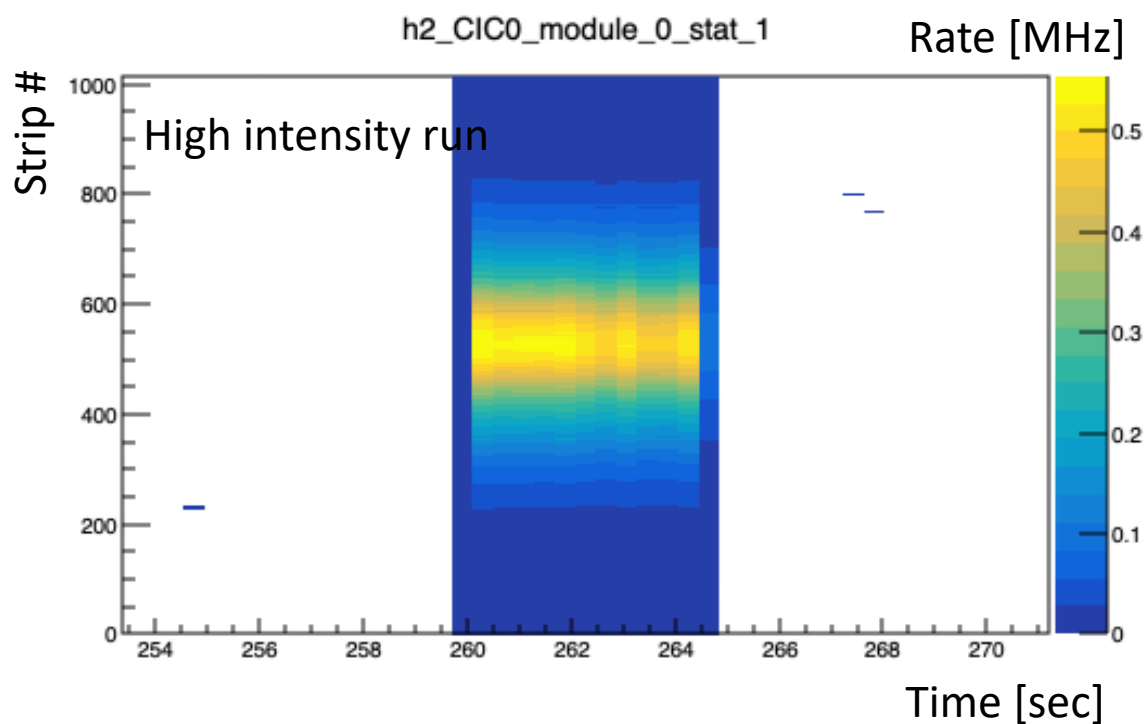
Beam intensity	Particle type	Target thickness	ECAL	Estimated muons
Low	Muon	2 cm	N	~1e9
High	Muon	2 cm	N	>300e9
High	Muon	3 cm	N	under production
High	Muon	2 cm	Y	under production
Low	Electron	2 cm	N	N/A

Test run 2023

Muon beam profile & intensity



- Silicon strip helps us ‘see’ the beam profile at the target position

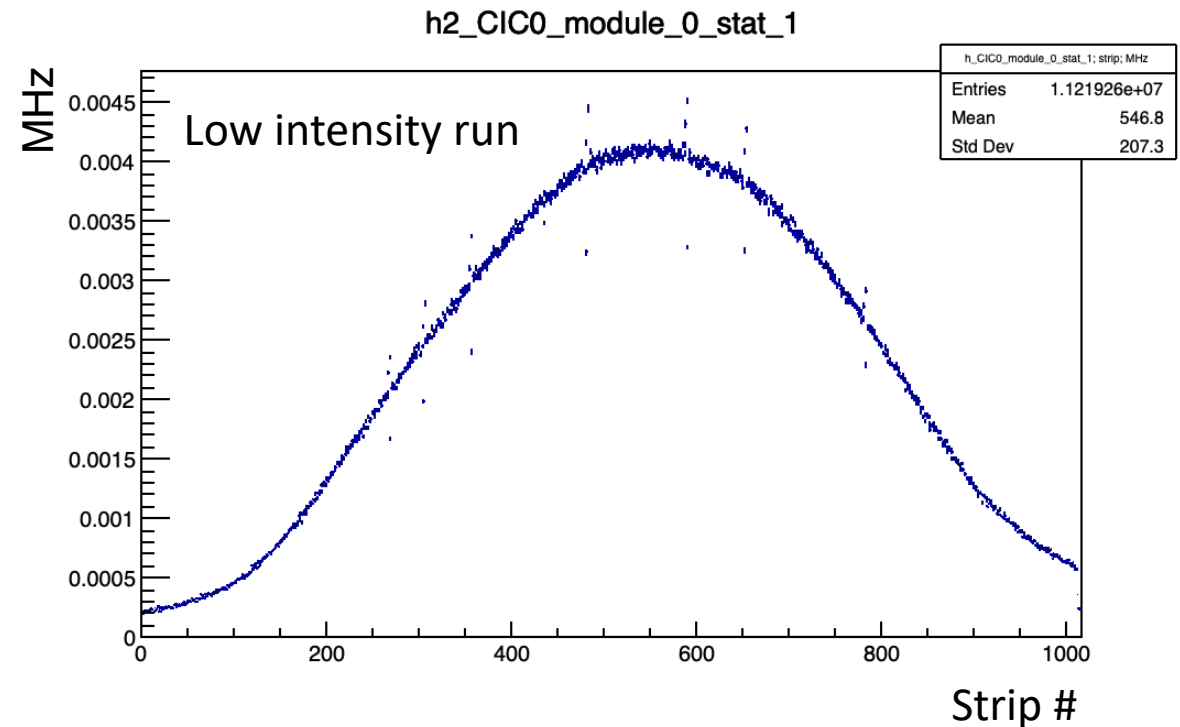
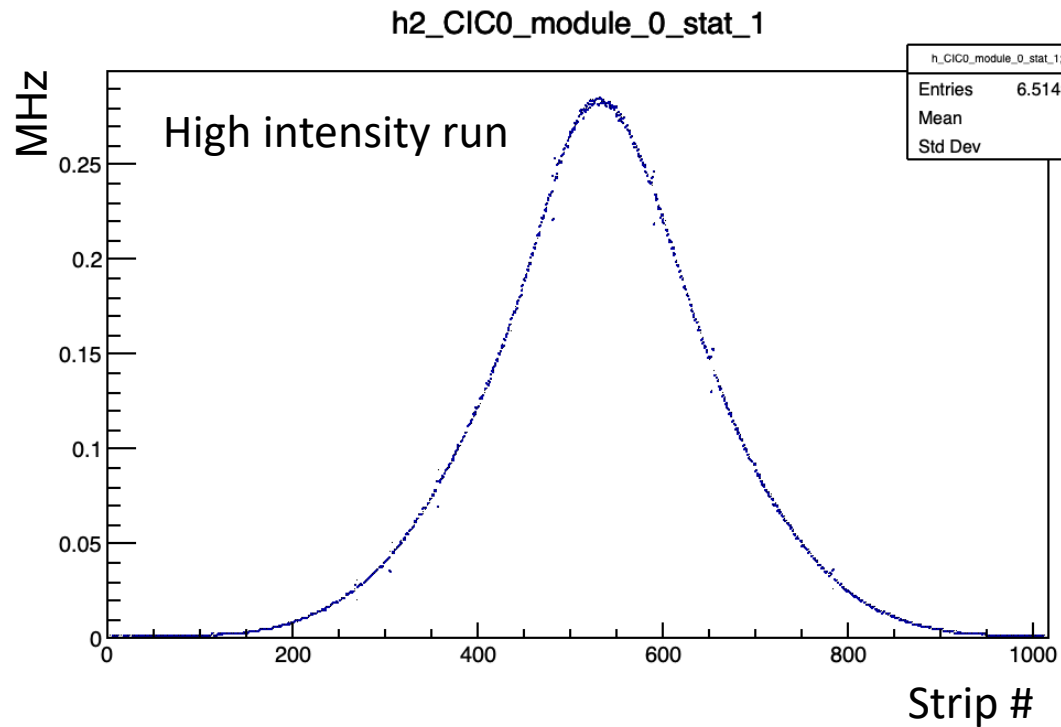


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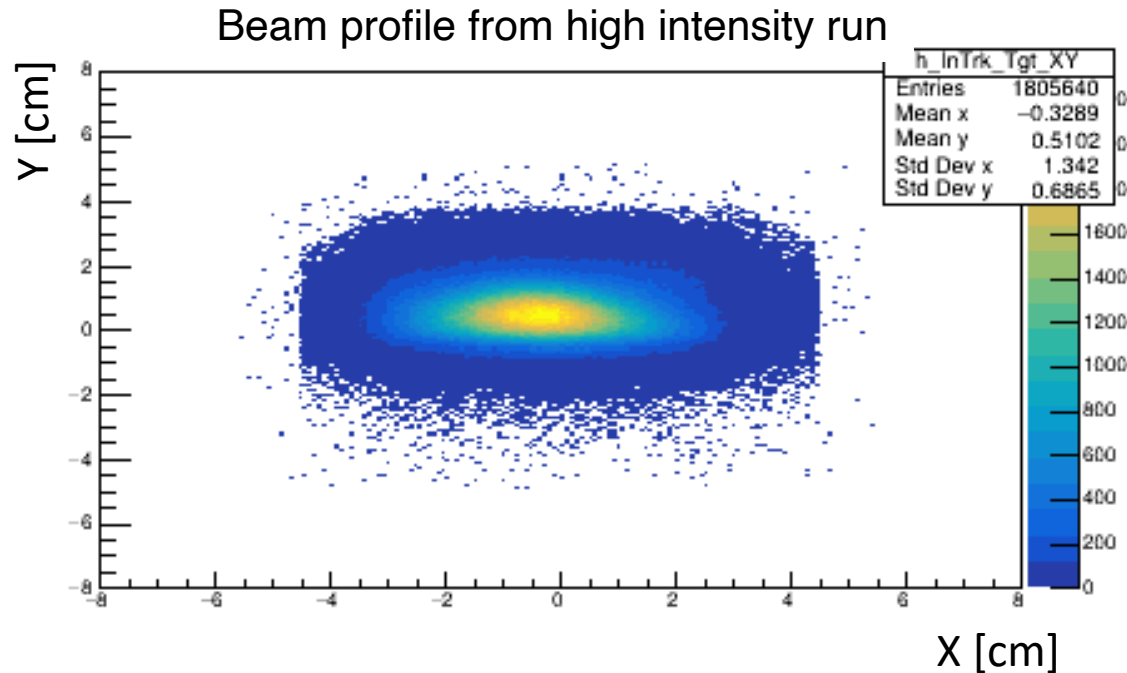


Test run 2023

Muon beam profile & intensity



- Silicon strip helps us ‘see’ the beam profile at the target position



$$\sigma_x = 1.34 \text{ cm}$$

$$\sigma_y = 0.68 \text{ cm}$$

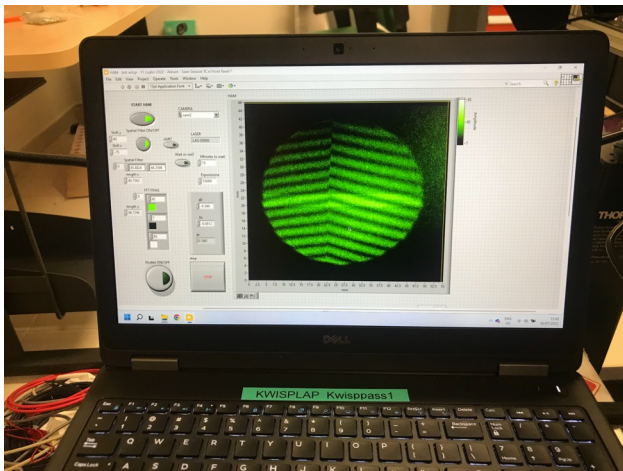
Confirmed the beam profile fits our detector dimensions

Test run 2023

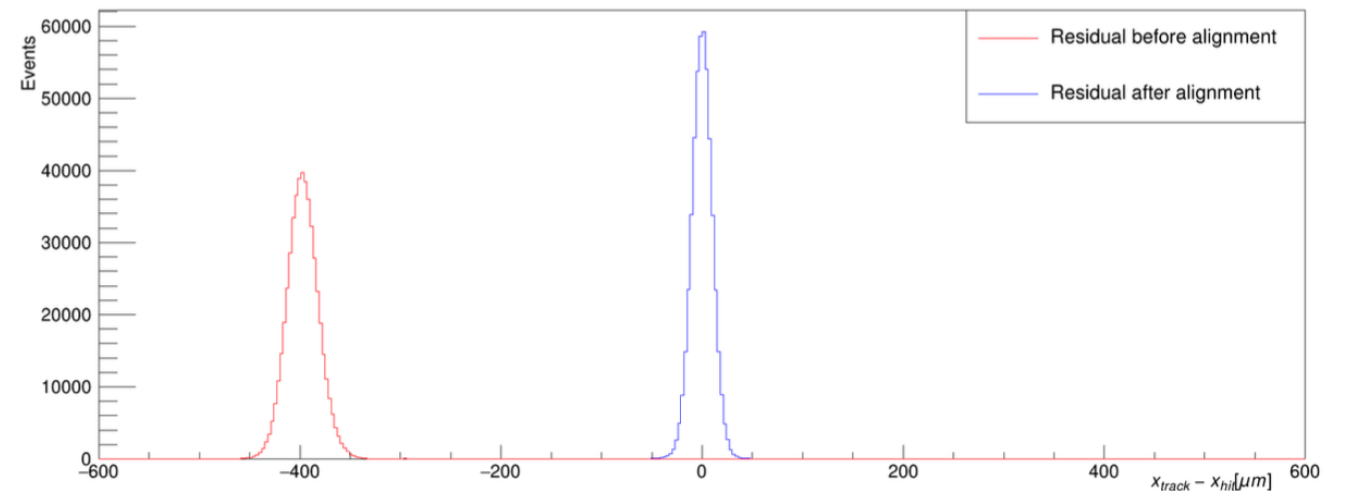
Module alignment, resolution and efficiency



- It is extremely challenging for MUonE to achieve precise alignment of less than **1 μm** transversely and **$\sim 10 \mu\text{m}$** longitudinally for the modules and stations.
 - Hardware level: metrology measurements using **laser survey**
 - Software level: implemented with FairMUonE



a laser
holographic
system
developed at
INFN



Test run 2023

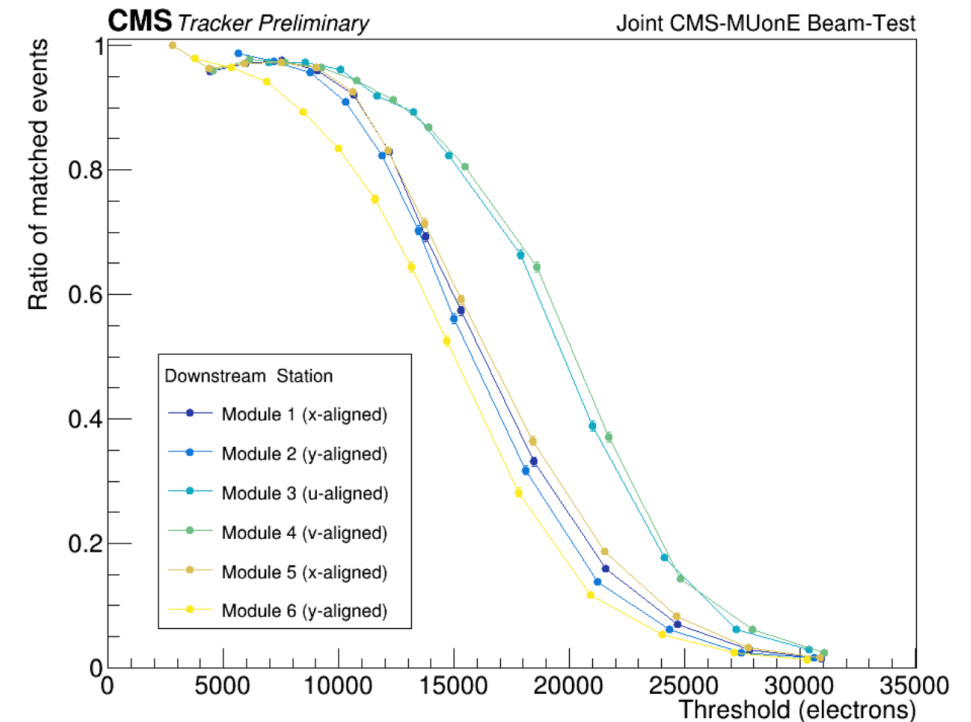
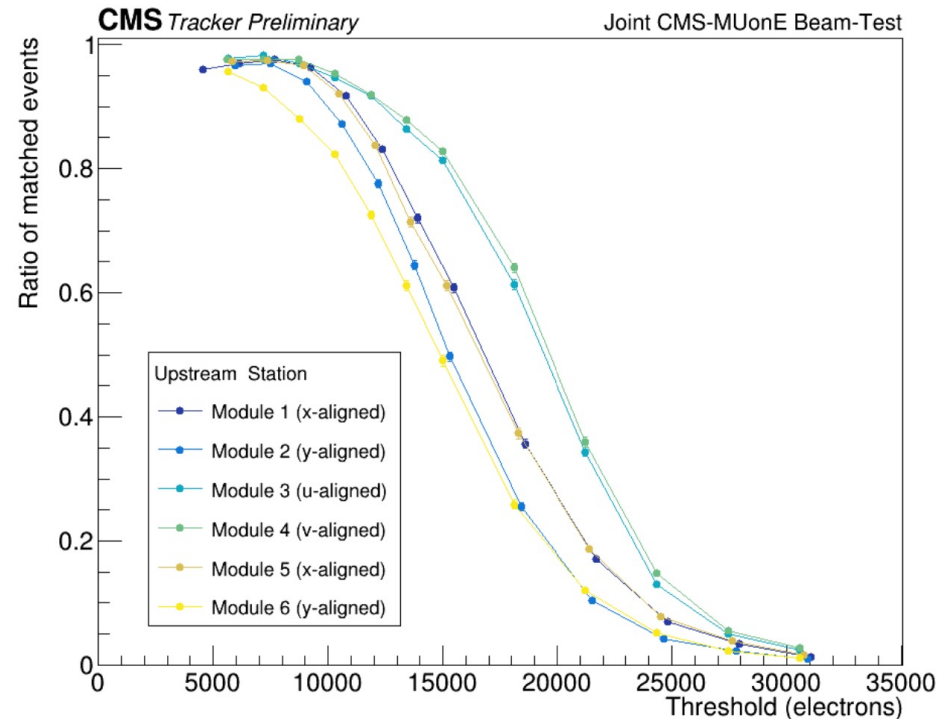
Module alignment, resolution and efficiency



- Module consistency check performed jointly with CMS tracker team

Ratio of events with at least a stub in a given module when all other modules have measured a single stub, as a function of comparator threshold

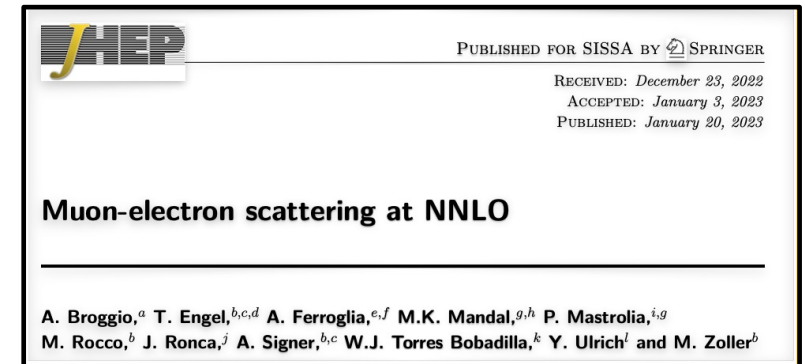
Plots approved by CMS



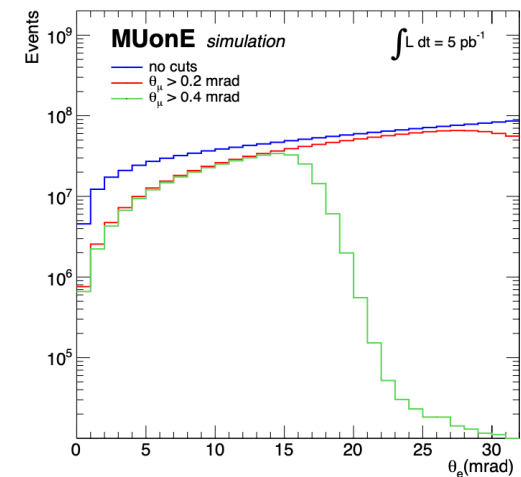
Analysis for test run 2023

Software framework

- **NNLO** Monte Carlo generator: [MESMER](#)
- [‘MuE’](#) fast simulation (Geant4-based)
 - (θ_e, θ_μ) up to the NLO generator
 - Limited detector effects (multiple scattering) included
- [‘FairMUonE’](#) dedicatedly developed for this project
 - **Full detector effects** and **track reconstruction**
 - Event selection & **weighted (θ_e, θ_μ)** for template fits
- [‘Combine’](#) tool for analyzing systematic effects



First NNLO prediction!



Analysis for test run 2023

Event reconstruction & selections



- Some basic criteria

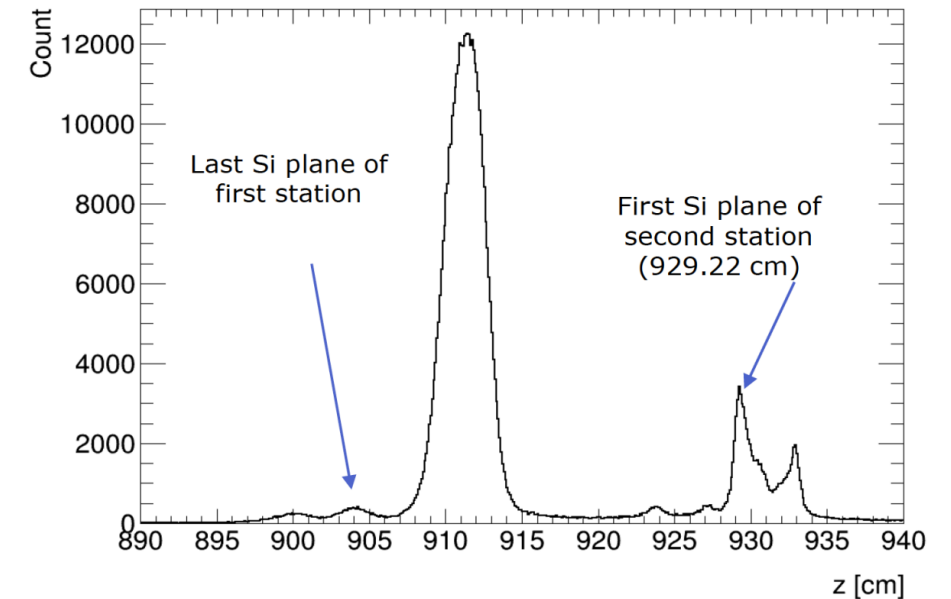
- Track candidate quality (χ^2)
- Vertex position in the target
- Acoplanarity

- Kinematic considerations

- $E_{\mu(\text{beam})}$, θ_{μ} , θ_e :
 - θ_{μ} : tune background of e^+e^- pairs
 - θ_e : tune acceptance
 - $E_{\mu(\text{beam})}$ is in principle described by two angles

- PID: muons can be distinguished from electrons using solely the angular information

Skimming + 2 outgoing tracks + (min, max) angular cuts



Analysis for test run 2023

Event reconstruction & selections



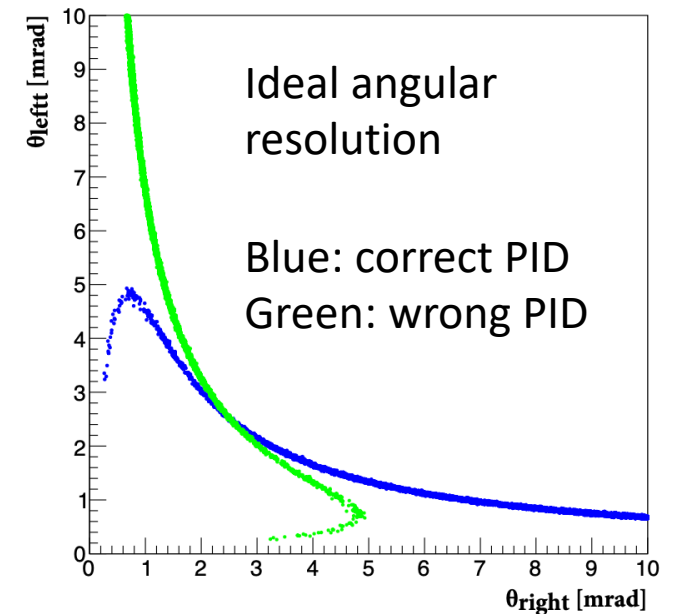
- Some basic criteria

- Track candidate quality (χ^2)
- Vertex position in the target
- Acoplanarity

- Kinematic considerations

- $E_{\mu(\text{beam})}$, θ_{μ} , θ_e :
 - θ_{μ} : tune background of e^+e^- pairs
 - θ_e : tune acceptance
 - $E_{\mu(\text{beam})}$ is in principle described by two angles

- PID: muons can be distinguished from electrons using solely the angular information

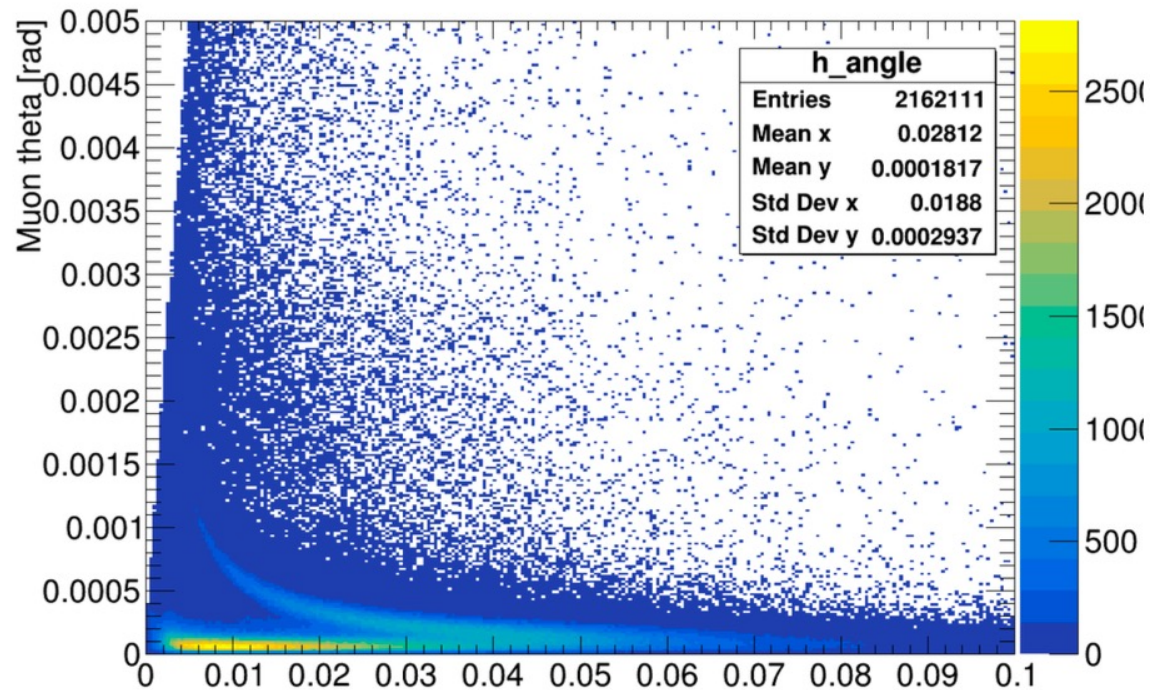


Test run 2023

First elastic scattering results



Angle distribution before selection



Selections:

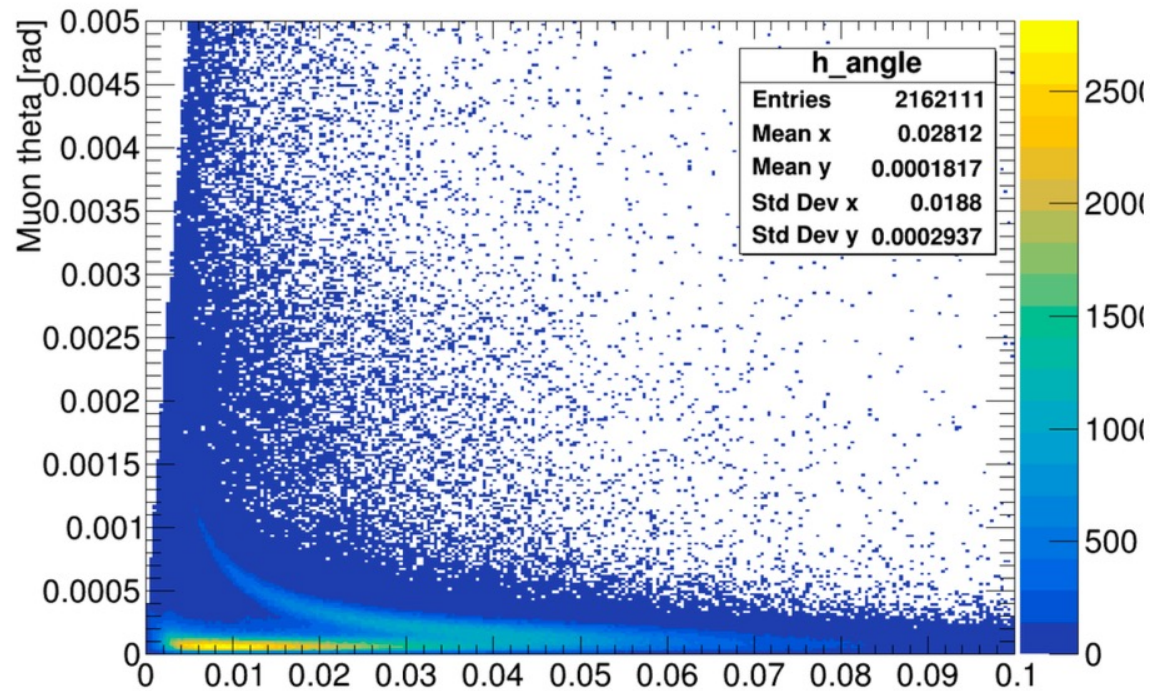
- Angles from the best vertex fit in FairMUonE
- 3 tracks (1 incoming & 2 out)
- Acoplanarity cut (≤ 1)
- Vertex reconstructed ± 1 cm of the target mean position
- **Angles: $\theta_{\mu} > 0.2$ mrad; $\theta_e < 32$ mrad**

Test run 2023

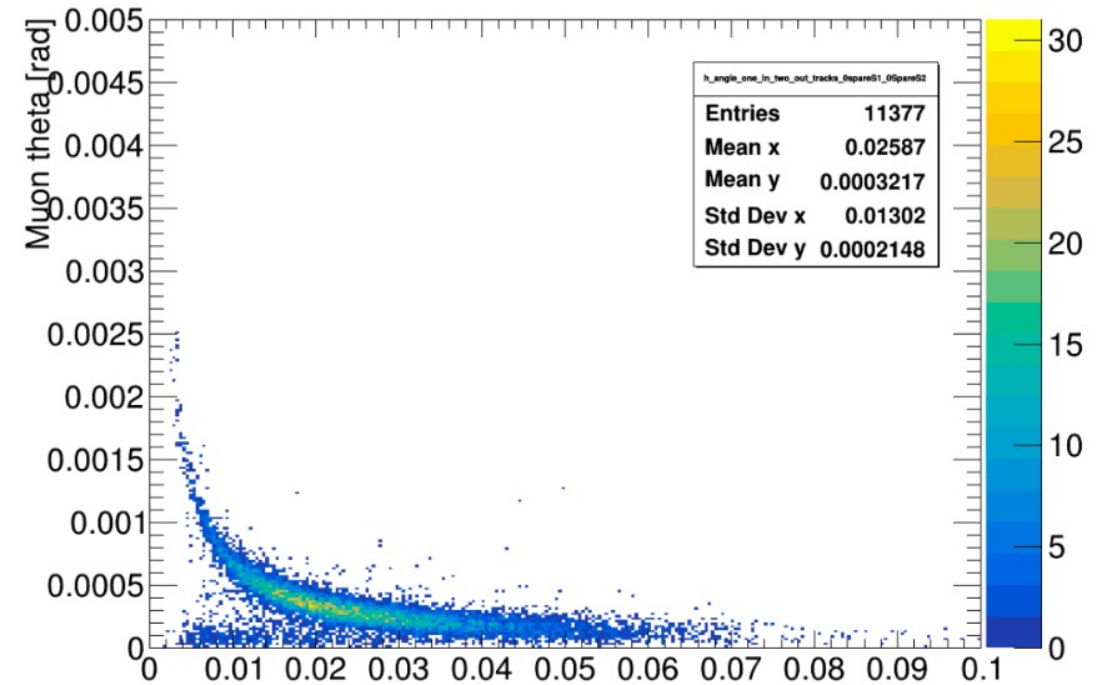
First elastic scattering results



Angle distribution before selection



Angle distribution after selection

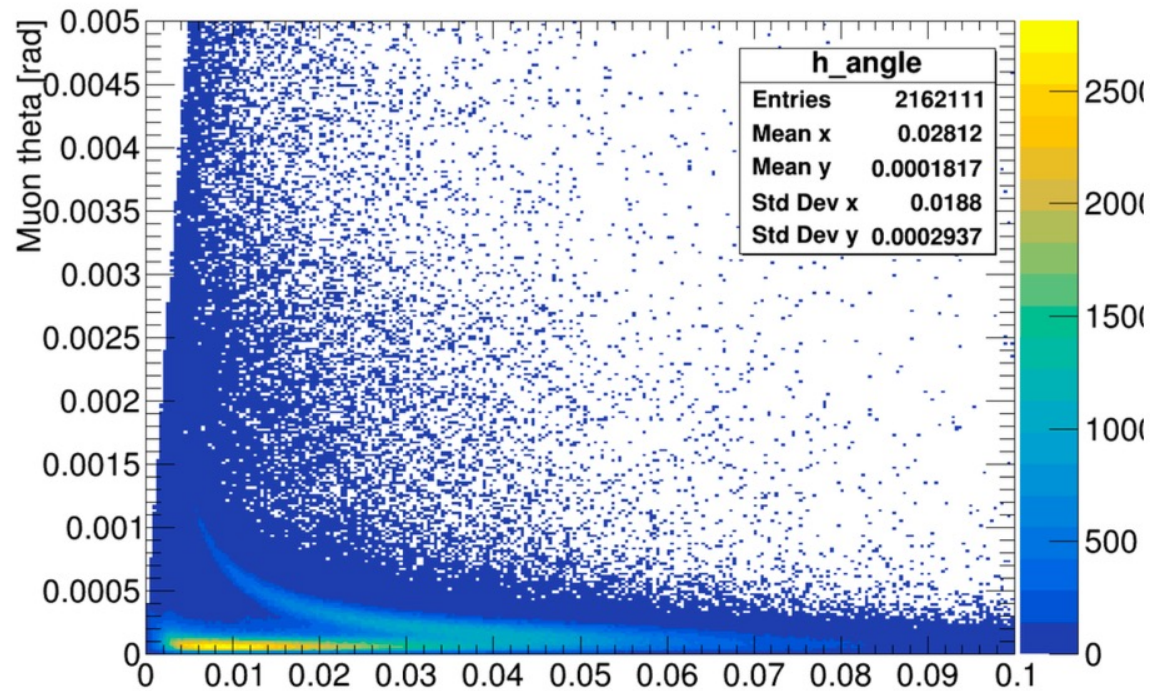


Test run 2023

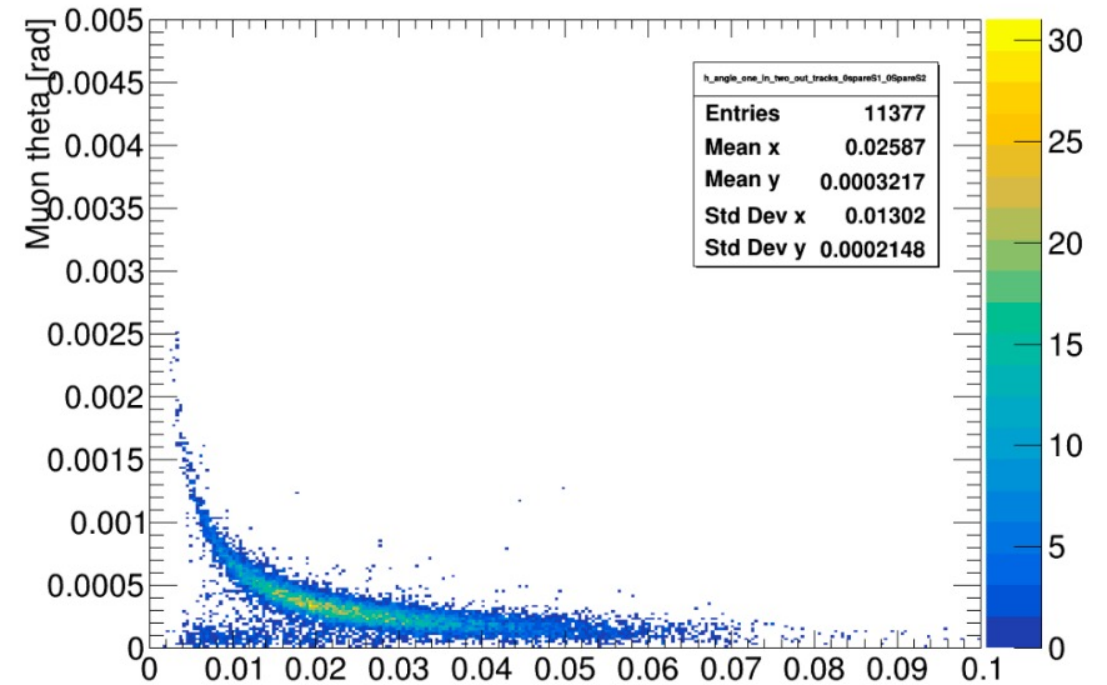
First elastic scattering results



Angle distribution before selection



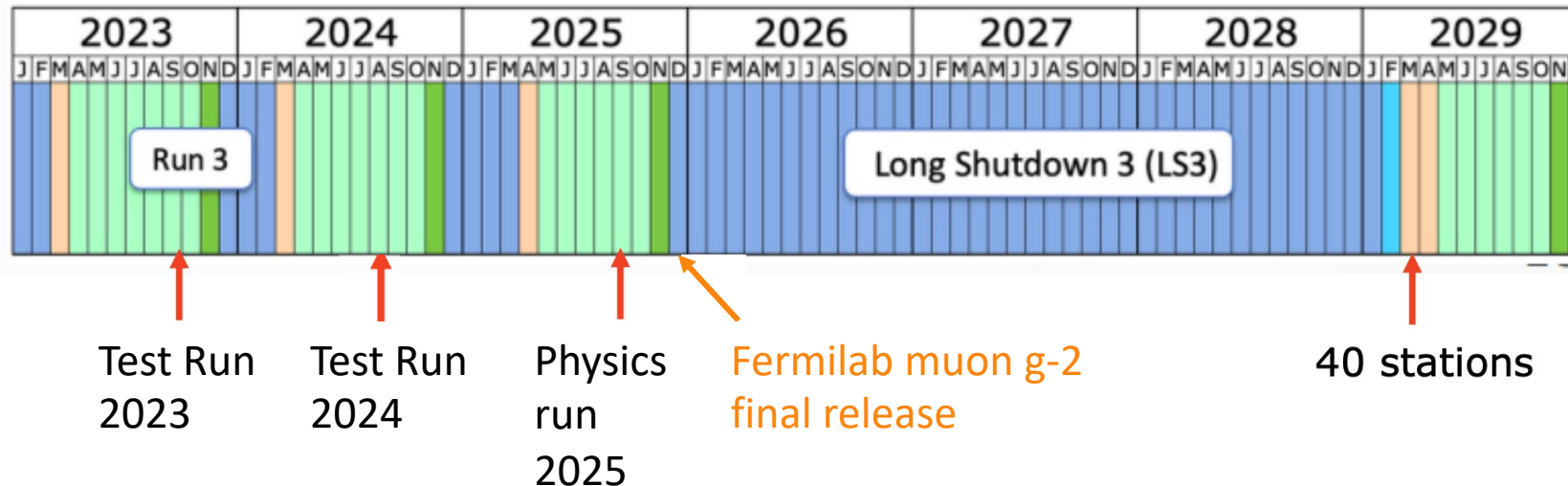
Angle distribution after selection



Timeline



- **Experimental proposal** to be submitted this year! (June 2024)
- **The first physics run in 2025** before LHC *Long Shutdown* (2026 - 2028)
 - 3 stations; 2- 4 months data-taking; **about 20% precision of $\alpha_{\mu}^{\text{HLO}}$**
- **Full run** with 40 stations after LS3 with final goal $\sim 0.3\%$ precision



Summary

- Muon $g - 2$ puzzles:
 - Conflict between **Muon g-2 SM predictions** and experimental measurement
 - $\alpha_{\mu}^{\text{HVP,LO}}$ represents a major uncertainty in the e^+e^- data-driven method for SM prediction
- MUonE: a new approach for $\alpha_{\mu}^{\text{HVP,LO}}$ **via $\mu - e$ scattering**
 - An **independent determination of $\Delta\alpha_{\text{had}}$ for the first time**
 - A **high-precision experiment**; lots of hardware & software developments
 - We are now analyzing 2023 data demonstrative for $\Delta\alpha_{\text{lep}}$
 - Promising test lead us to **the first physics run in 2025 and full run for 2028+**

50+ people from over 9 countries



CERN
Exp-Th

<https://web.infn.it/MUonE/>



INFN +Univ. (Bologna,
Milano-Bicocca, Padova,
Pavia, Perugia, Pisa, Trieste)
Exp-Th



Imperial College (London),
Liverpool U. *Exp-Th*
Durham U.



Krakow IFJ Pan
Exp



Cornell U.,
Northwestern U.,
Regis U.,
Virginia U.
Exp



Budker Inst.
(Novosibirsk)
Exp

**The MUonE
Collaboration**



Demokritos INPP
(Athens) *Exp-Th*



Shanghai
Jiao Tong U.
Exp



PSI (Villigen),
U.Zürich, ETH Zürich
Th



Mainz U.,
Max-Planck Inst.
Exp-Th

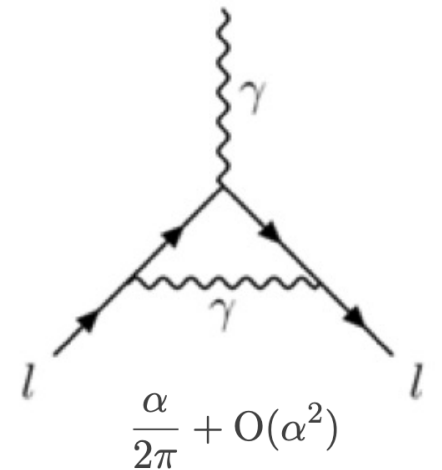
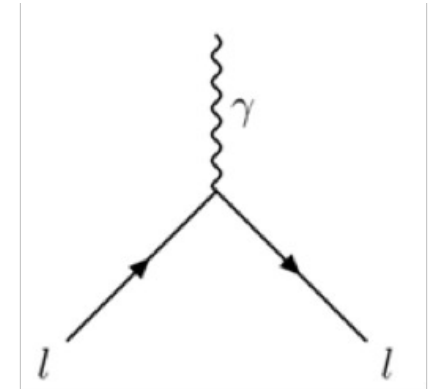
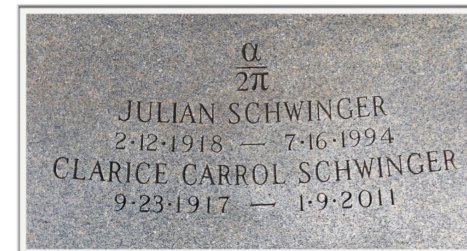
+ other involved theorists from: New York City Tech (USA), Vienna U. (A)

Backup

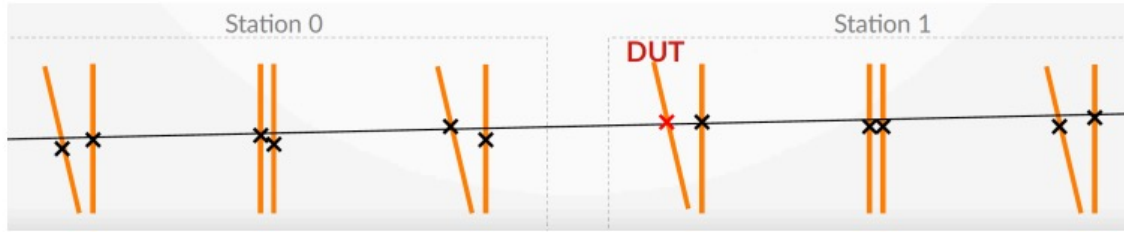
Muon $g - 2$

- The anomalous magnetic moment of the muon:
 - Magnetic moments **precess** in a magnetic field $\vec{\mu} = g \frac{e}{2m} \vec{S}$
 - g - factor quantifies interaction strength
- Interactions with virtual particles cause g to deviate from 2 ($g > 2$). **Muon magnetic anomaly** is defined as:

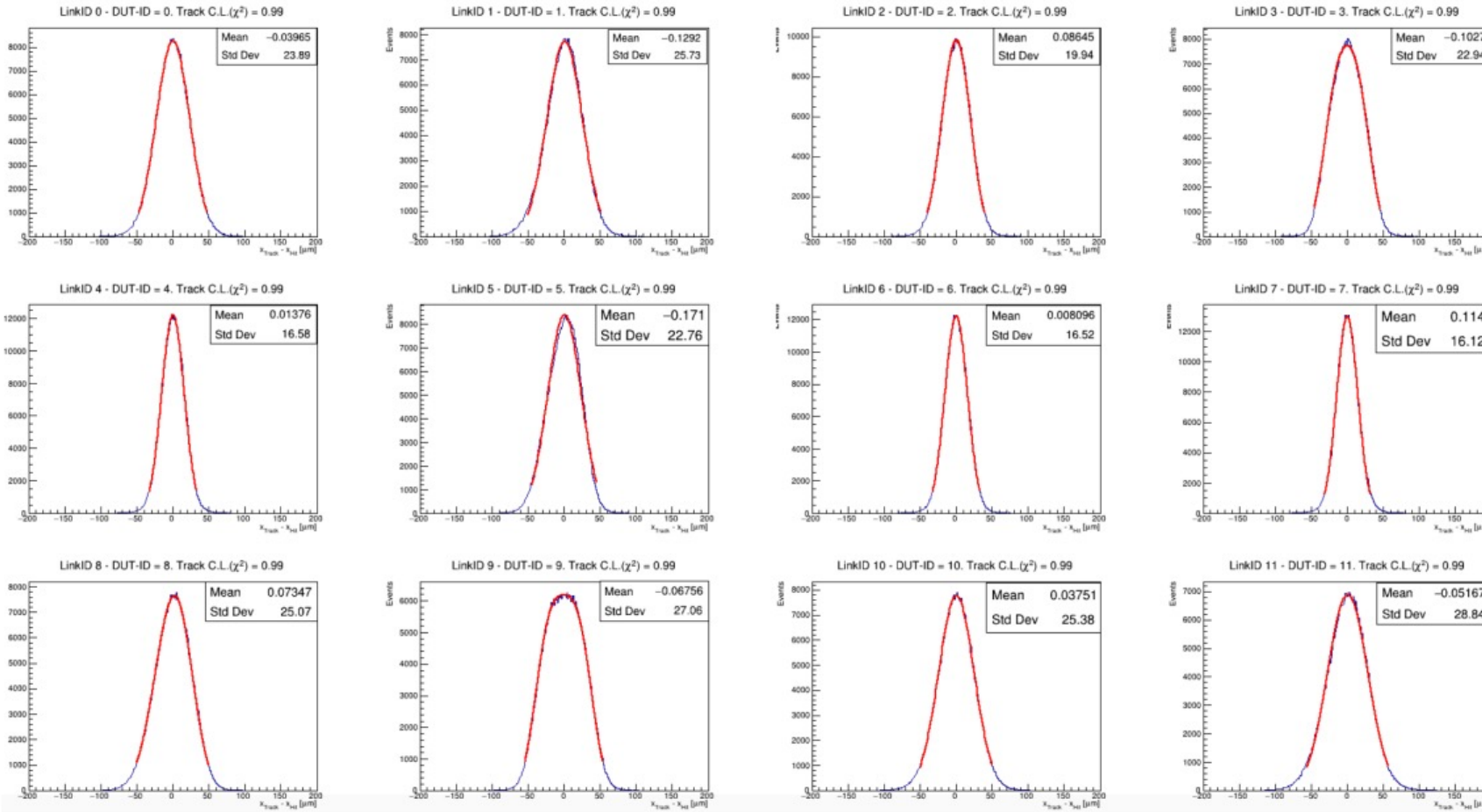
$$a_{\mu} = \frac{g - 2}{2}$$



Real Data Alignment - Resolution



The tracker is aligned with passing beam muons leaving one hit in all the 12 detector modules



three coordinates aligned per each module:

Strip local position (local X)

Rotation angle around the Z axis

Orthogonal coordinate (local Y)

Unbiased residuals on the tracker modules after the alignment: RMS consistent with expected resolution

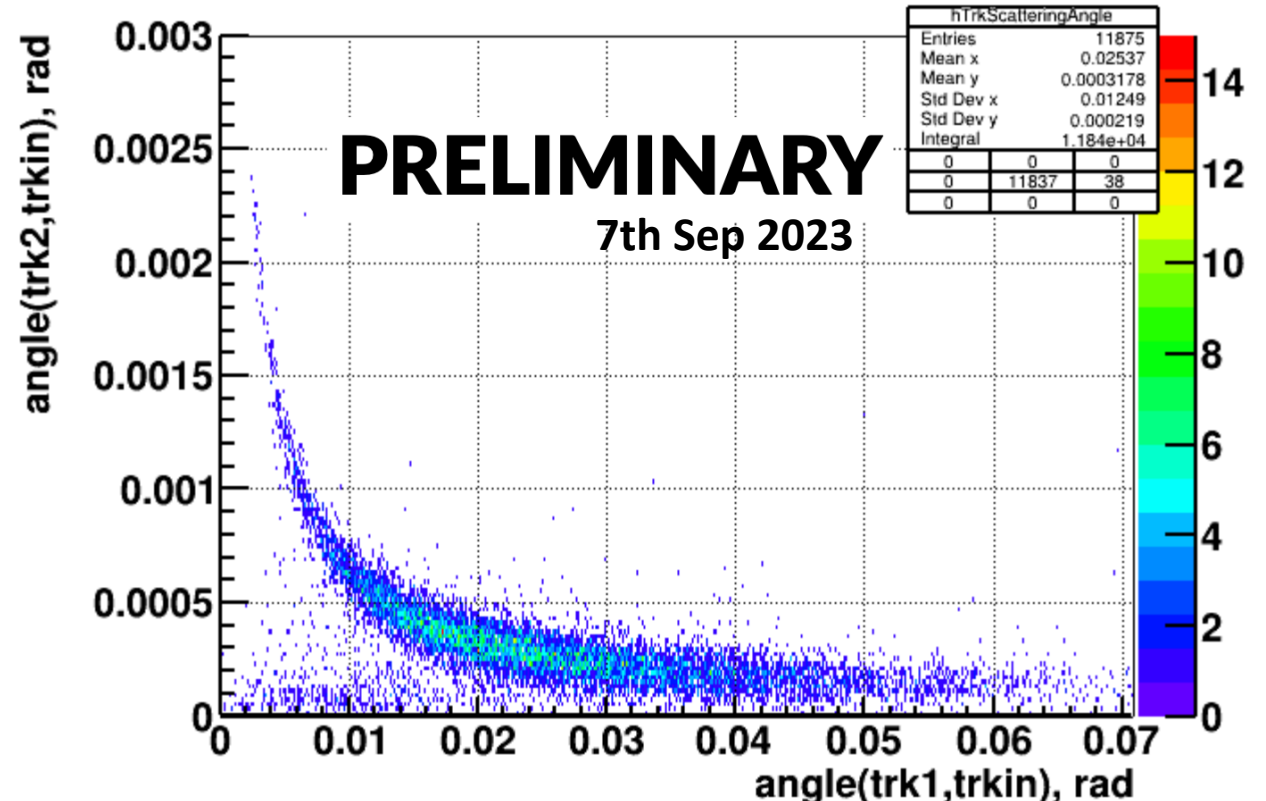
On-going development to include the metrology measurements as starting point

Results from test run 2023



Preliminary result on scattering events!

- Runs with a 3-cm target installed
- N single muons 2.9×10^8 in used sample (assuming no hit loss and overlap)
- One track in the 1st station + 2 tracked in the 2nd station
- Chi2/ndf track cut < 5
- Zvtx selection applied after selecting two outgoing tracks within the target position

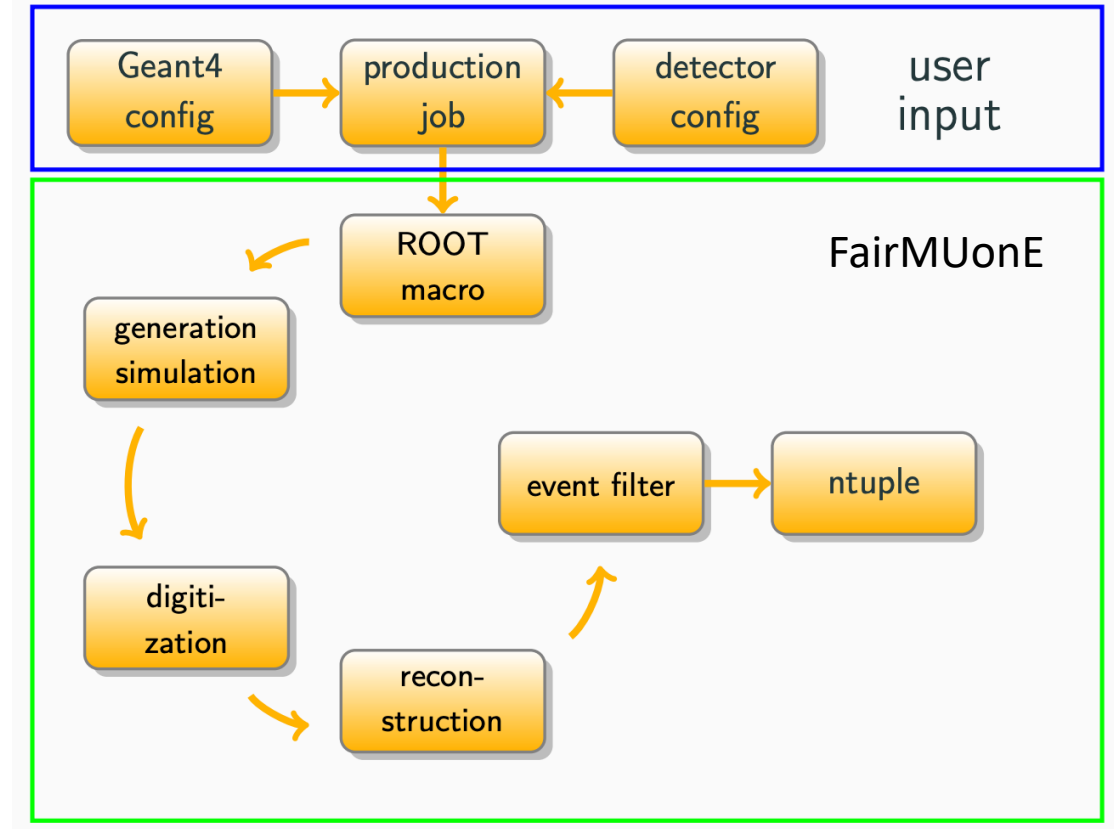
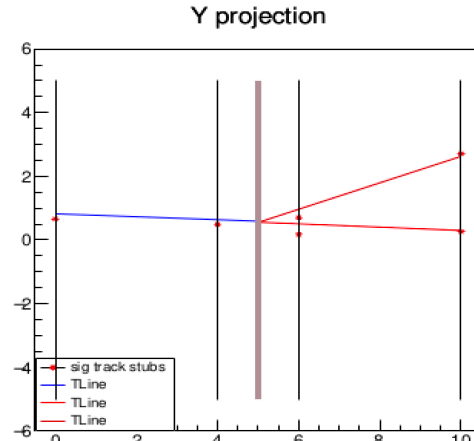
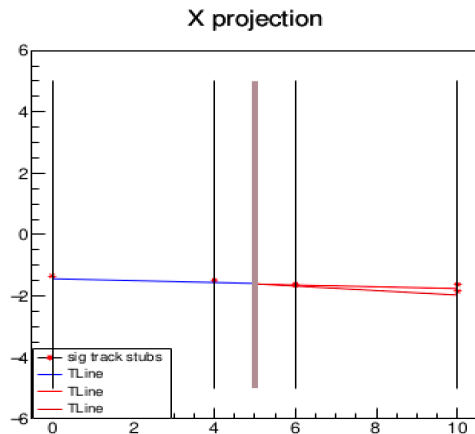


Elastic Scattering Analysis

'FairMUonE' Package



- The package developed dedicated to MUonE
- Both simulation and track reconstruction in the same package
- Digitization of tracker & calo are implemented



Elastic Scattering Analysis

Template Fit



- Extracting $\Delta\alpha_{had}(t)$ through a **template fit** to the (θ_e, θ_μ) distribution

- $\Delta\alpha_{had}$ parameterization (**K, M**):
$$\Delta\alpha_{had}(t) = KM \left\{ -\frac{5}{9} - \frac{4M}{3t} + \left(\frac{4M^2}{3t^2} + \frac{M}{3t} - \frac{1}{6} \right) \frac{2}{\sqrt{1 - \frac{4M}{t}}} \ln \left| \frac{1 - \sqrt{1 - \frac{4M}{t}}}{1 + \sqrt{1 - \frac{4M}{t}}} \right| \right\}$$

- ‘Lepton-like’ parameterization
- K: related to α_0 and the electric charge of the lepton in the loop (had: quarks colour charge)
- M: related to the **squared mass of the particle** in the loop $(m_l^2, m_\mu^2, m_\tau^2)$
- In the hadronic parameterization, K & M don’t have real physical meaning

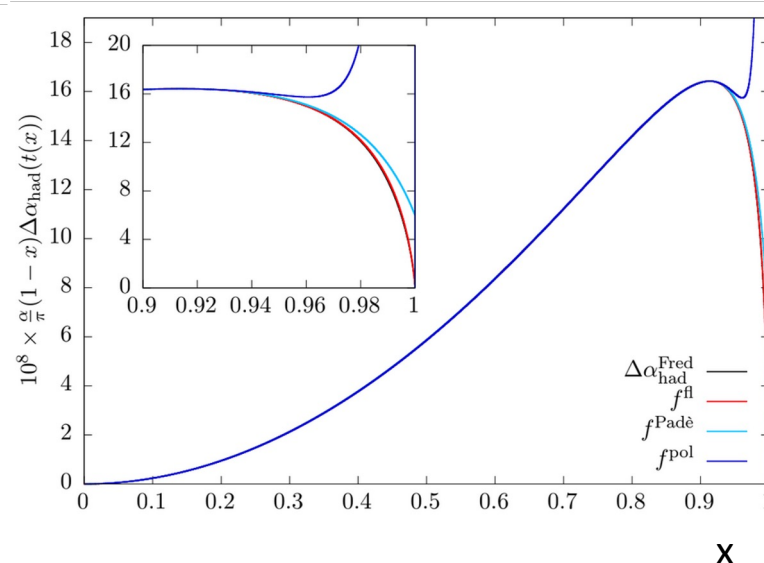
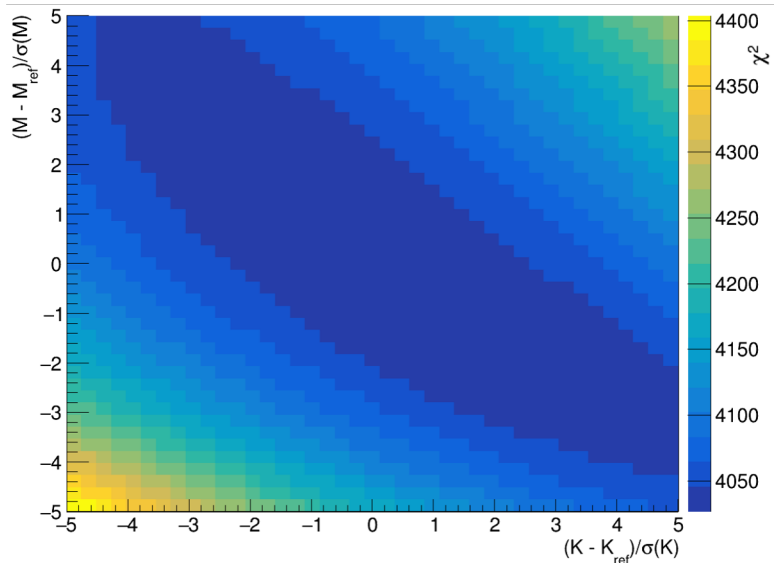
Elastic Scattering Analysis

Template Fit



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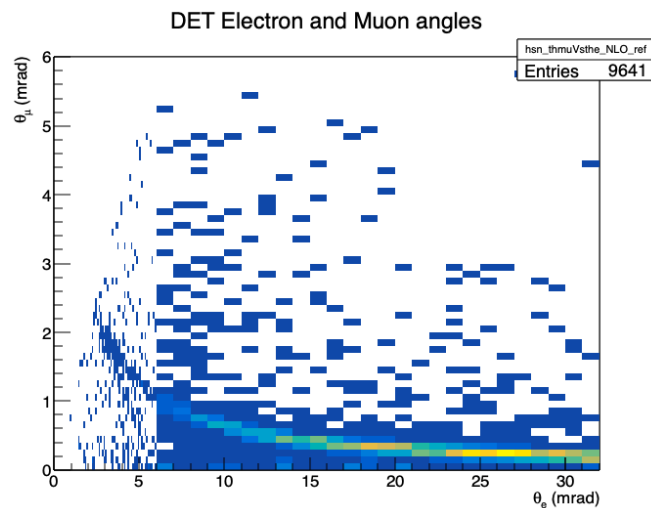


Preliminary template fit:

- Luminosity: $1.5 \times 10^4 \text{ pb}^{-1}$
- 4×10^{12} elastic events with $E_e > 1 \text{ GeV}$ ($\theta_e < 32 \text{ mrad}$)
- Input a_μ^{HLO} : 688.6×10^{-10}
- Fitted a_μ^{HLO} : $(688.8 \pm 2.4) \times 10^{-10}$
- 0.35% statistical error

Test of template fit for $\Delta\alpha_{lep}$

- Input about 1e4 MC events into the template fit
 - 3cm_HitSharing1_NoAlignment_Alpha2
 - Passing 'default_gold_angles_aco_zvtx' to fast simulation, do reweighting and generates 40 templates
 - Usual trick: use the **same MC set** for the pseudodata and the templates. Smear the pseudodata according to the expected statistics to make it independent of the templates

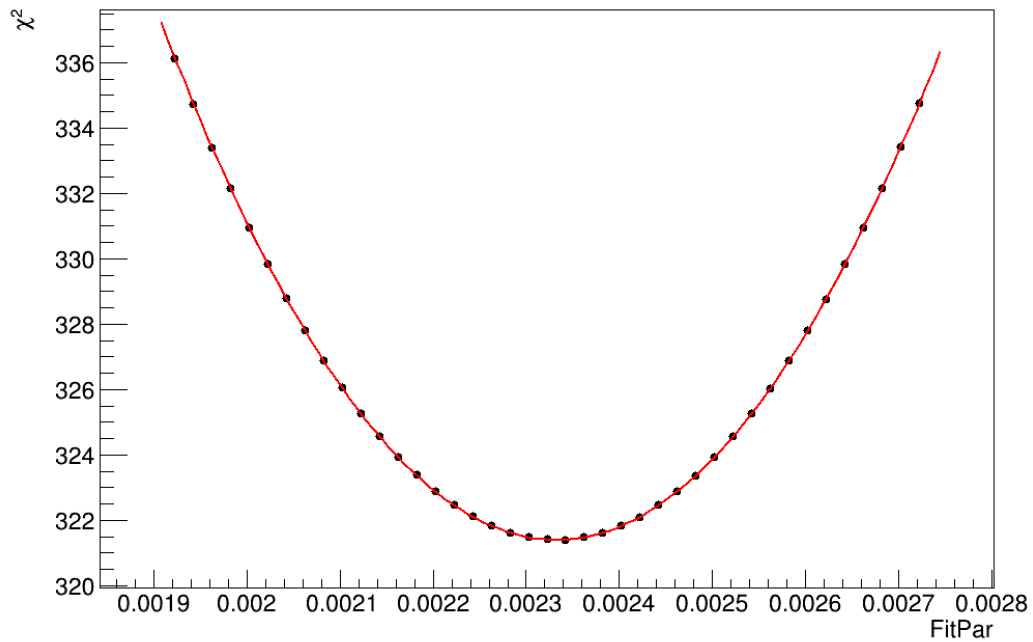


Template fit parameters:

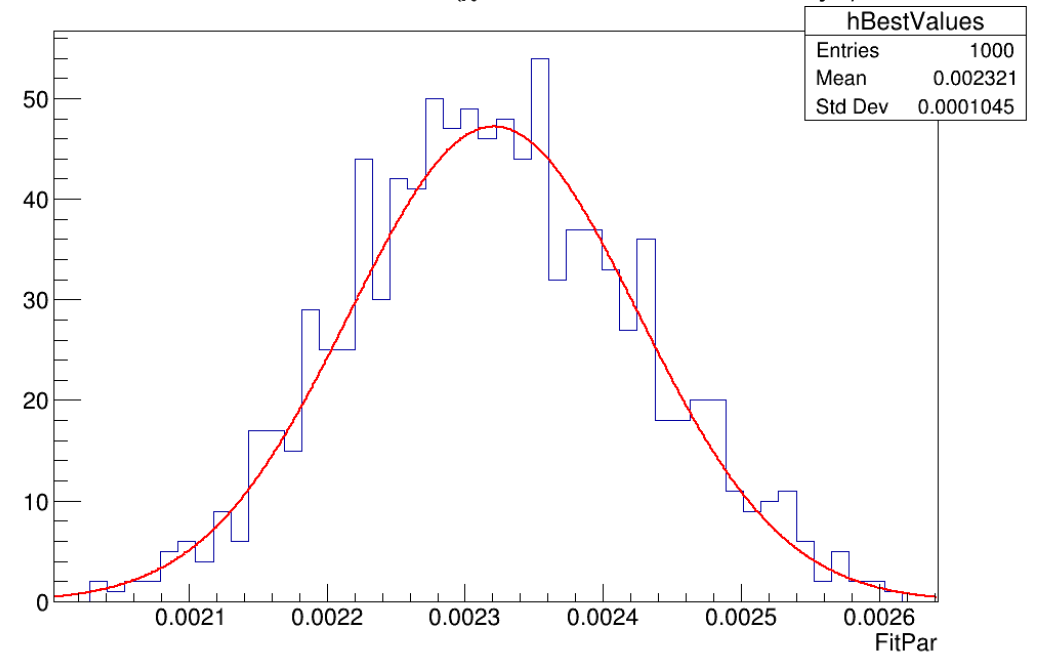
- Kref = 0.0023223 +/- 8e-05
- Mref = 0.000511 +/- 0
- Sigma limit = 5
- Sigma step = 4
- Weights normalization: 1345.26 μb

Test of template fit for $\Delta\alpha_{lep}$

FitPar template fit



FitParBest distribution (χ^2 minimization of 1000 toys)



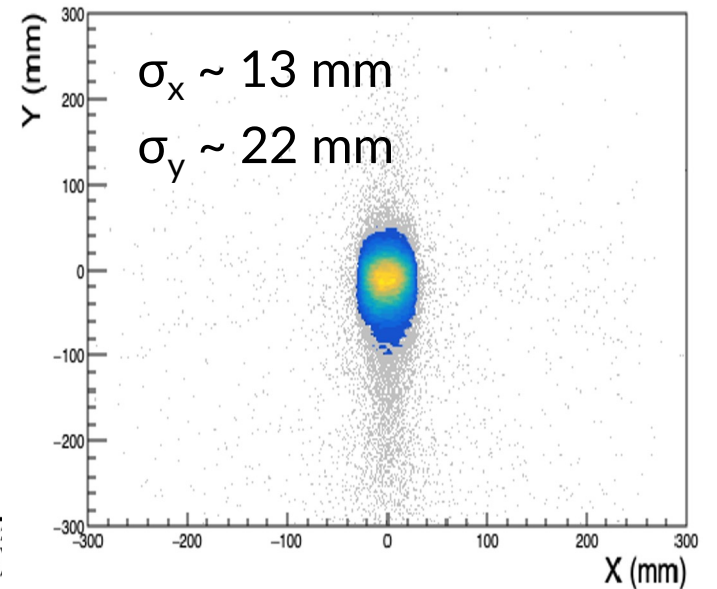
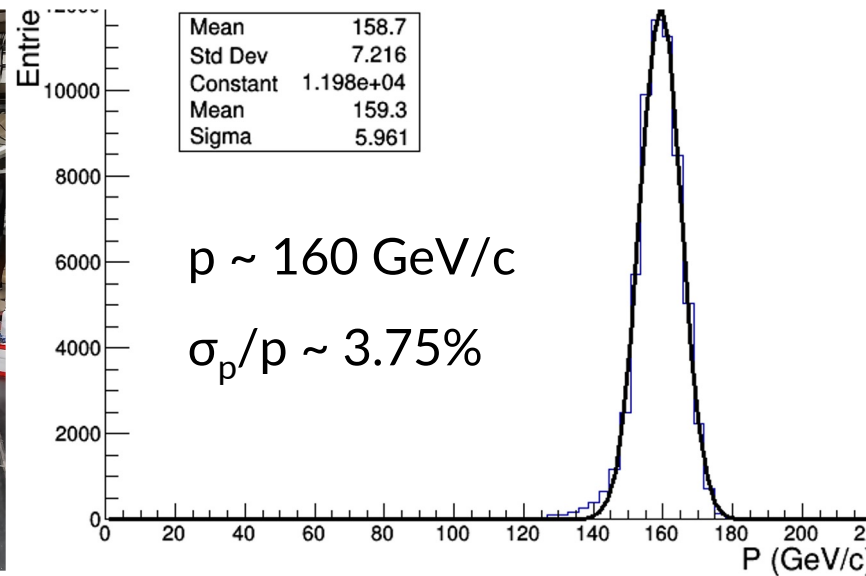
Fited best $K = 0.00232086 \pm 0.000104678$
(~4.4%, but it doesn't mean much!)

Test run 2023

Muon (M2) beam-line at CERN Prévessin site



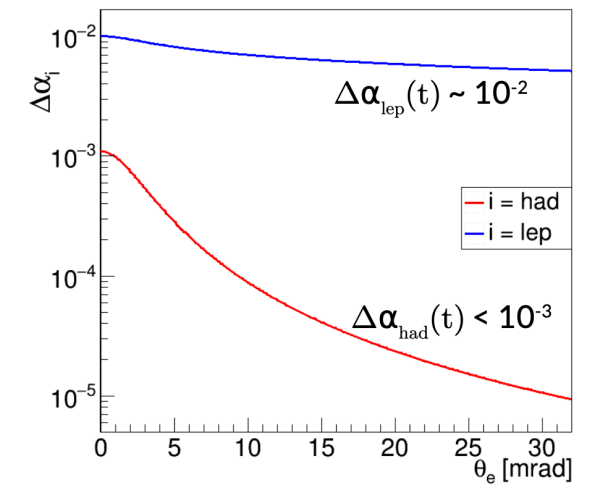
- CERN North Area M2: upstream of the COMPASS detector
 - Maximum 50 MHz ($2\text{-}3 \times 10^8 \mu^+/\text{spill}$) for 10^{12} 400 GeV/c incident protons



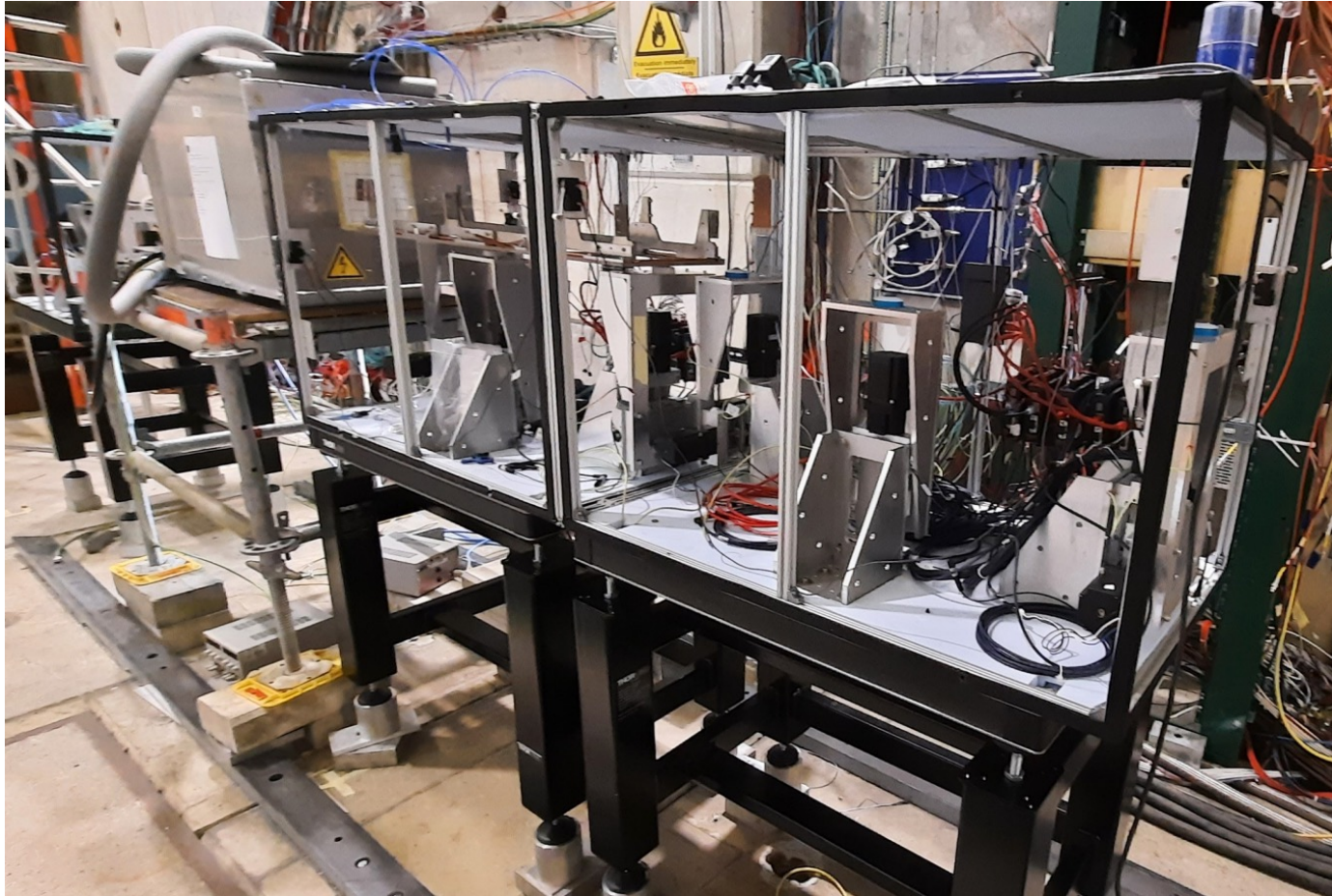
Test run 2023



- 21 Aug – 17 Sep
- 2 stations (pre-tracker + target + tracker) + ECAL
- Expected luminosity: $\sim 1 \text{ pb}^{-1}$
 - $\sim 10^{12}$ μ accumulated on target with $\sim 2.5 \times 10^8$ elastic events $E_e > 1 \text{ GeV}$
- **Goals:**
 - Engineering stability & detectors performance
 - Background study
 - Reconstruction & prompt analysis
 - **Demonstration measurement of $\Delta\alpha^{\text{LEP}}$ with a few % precision!**

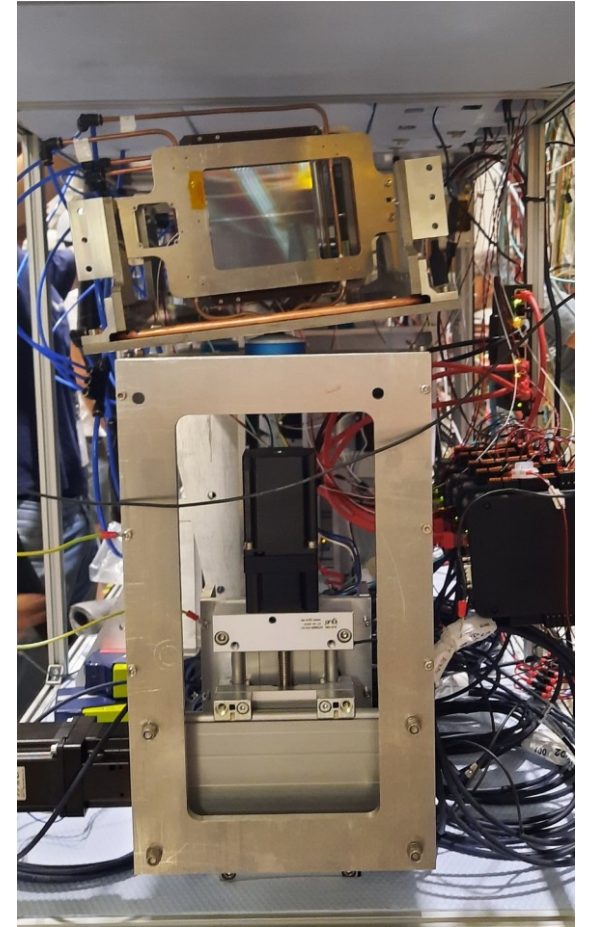


Test run 2023

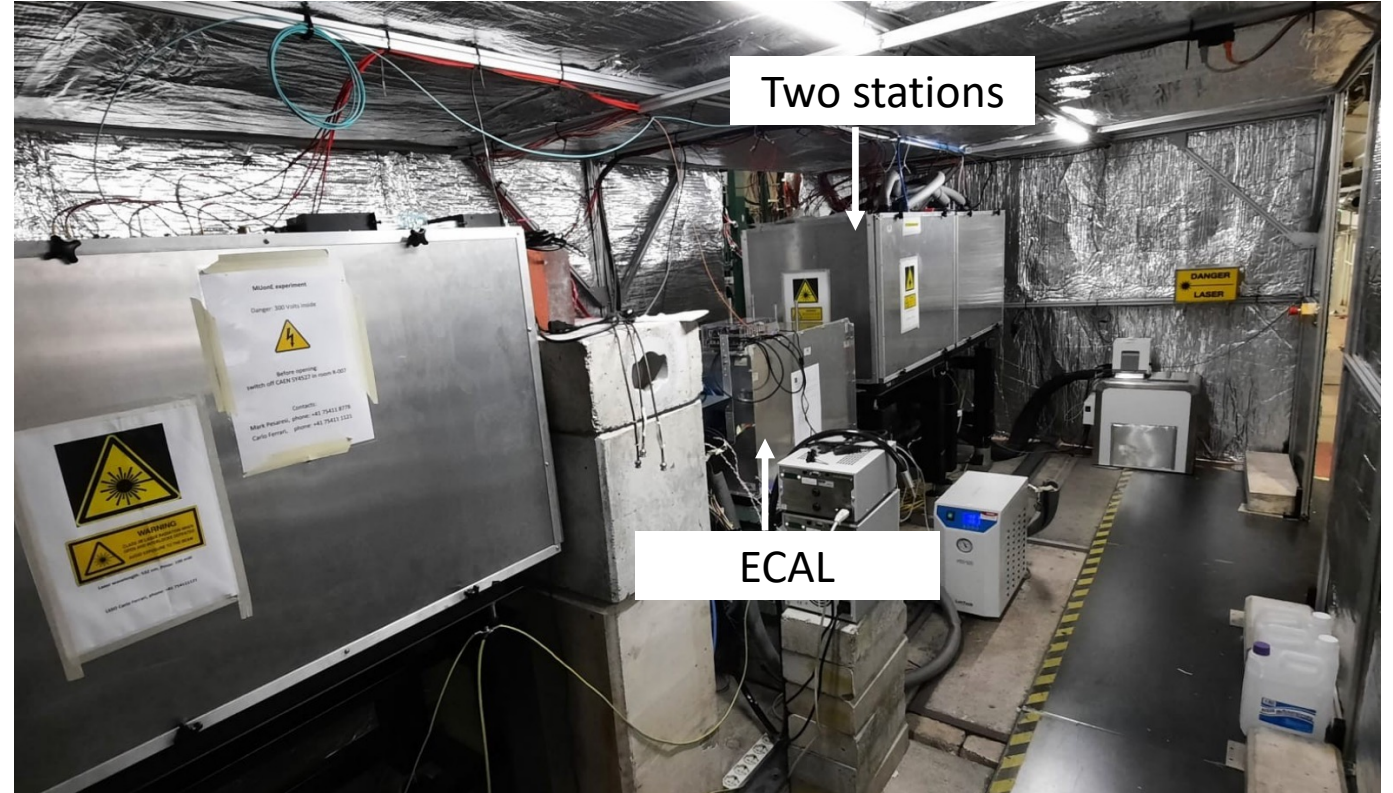


← Two stations

2S module →



Test run 2023

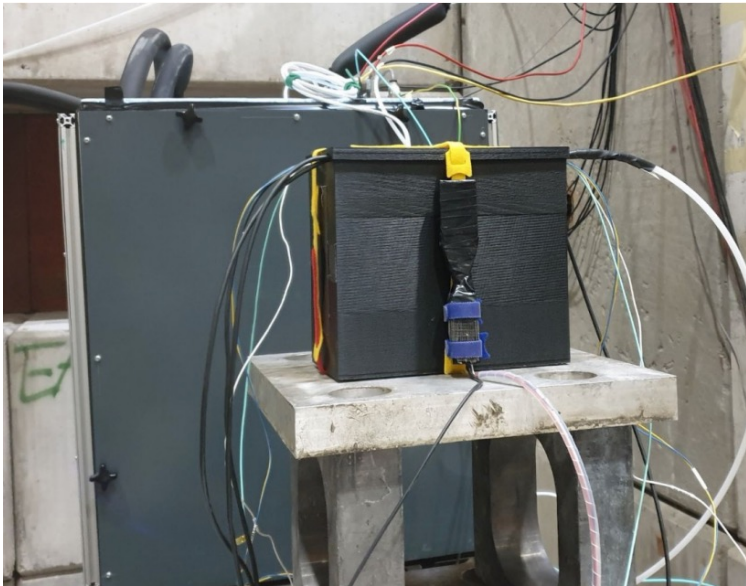


Test runs

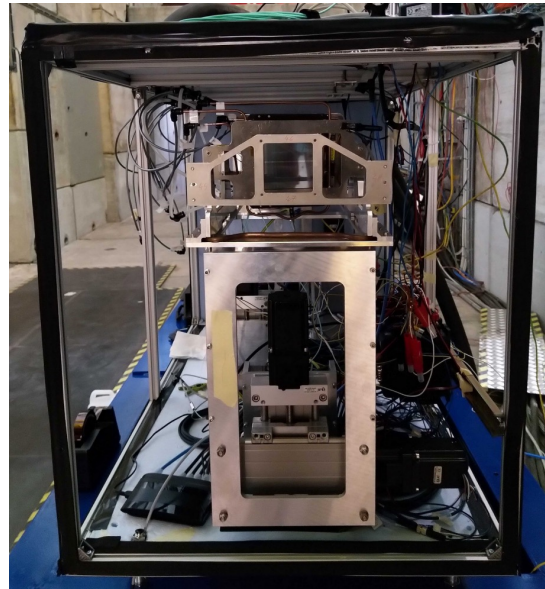
2021, 2022 and 2023



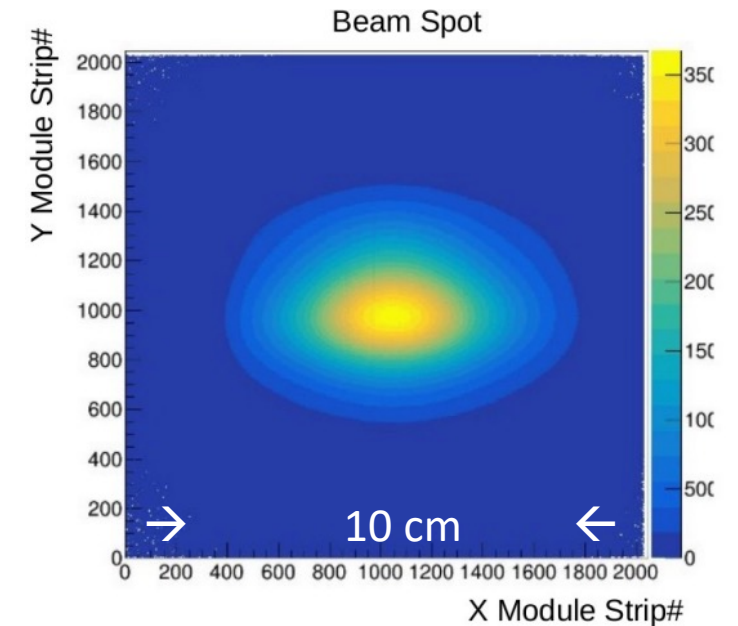
- Intense Beam Test activities with detector in real beam conditions



2S module firstly tested on Nov 2021



1 full station (6 modules) + ECAL in the proposed MUonE location, Oct 2022

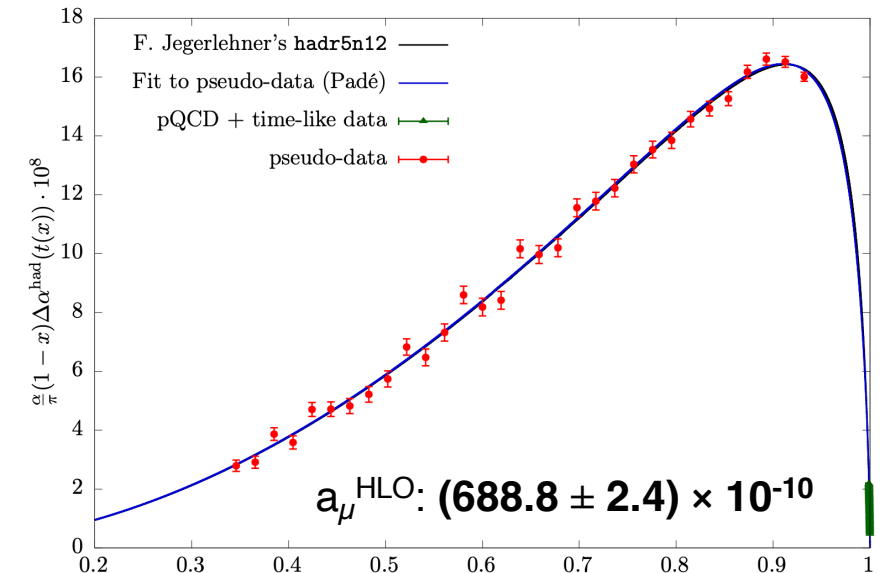


Systematic Effects

General Considerations



- The main challenge of the MUonE is the control of systematic effects at the same level of the stat precision
 - **~0.3%** statistical accuracy on $a_\mu^{\text{HVP,LO}}$
 - Competitive with dispersive data-driven method
 - **3 years data-taking** with full stations \rightarrow 4E12 events
 - Estimated **10 ppm** systematic uncertainty



Systematic Effects

General Considerations

$$R_{\text{had}} = \frac{d\sigma_{\text{data}}(\Delta\alpha_{\text{had}})}{d\sigma_{\text{MC}}(\Delta\alpha_{\text{had}} = 0)} \sim 1 + 2\Delta\alpha_{\text{had}}(t)$$

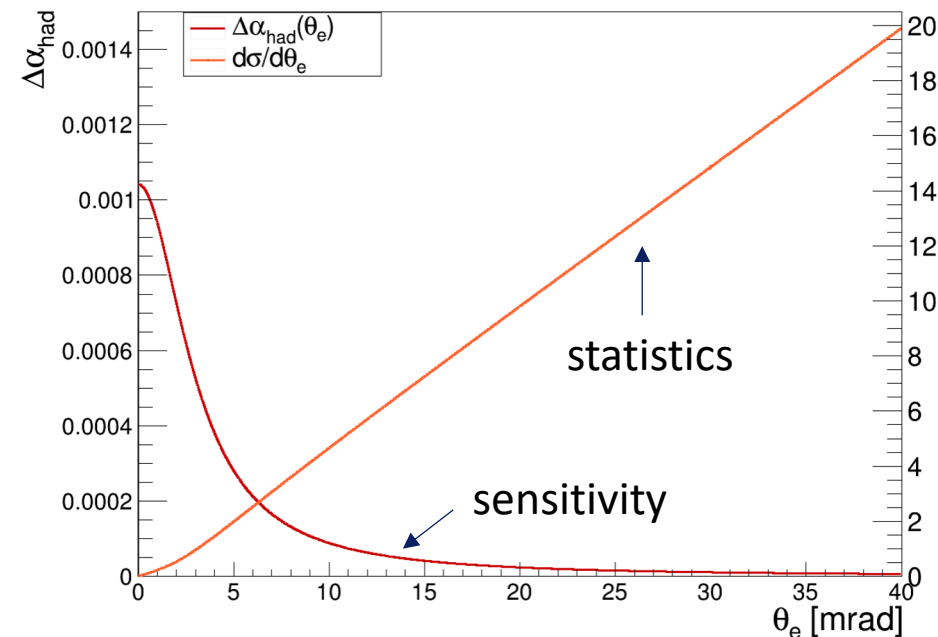
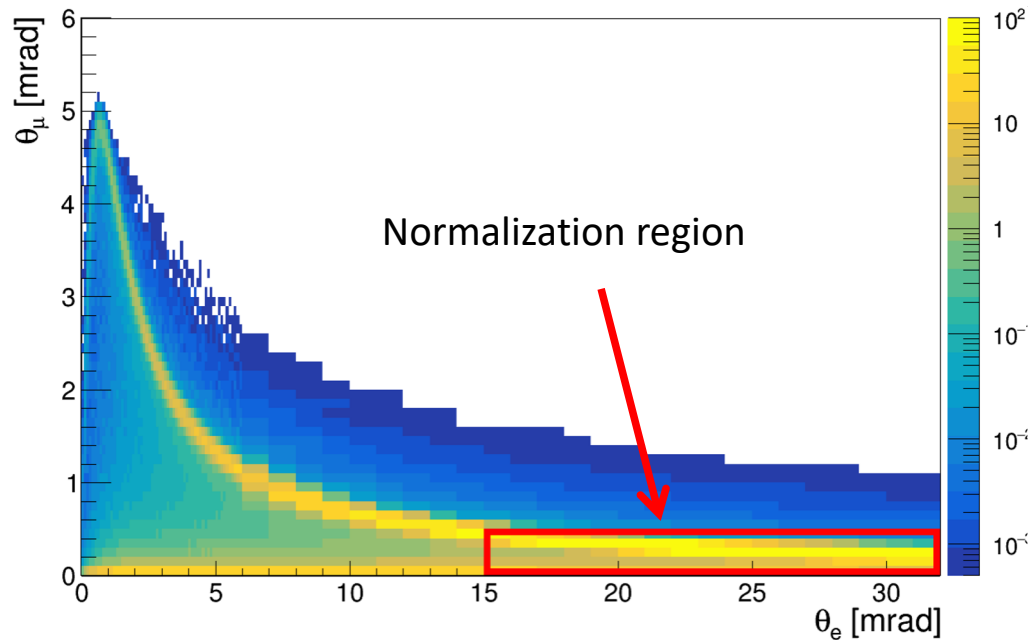
- Theory input: MC generator of radiative contributions at **NNLO** level
- Experimental requirements:
 - Uniform detection efficiency (modules, across all angular range)
 - Precise alignment (10 μm longitudinally)
 - Main sources:
 - **Multiple-scattering** (accuracy of 1%)
 - Angular resolution (a few %)
 - Beam energy
 - ...

Systematic Effects

Strategy



- Main systematics have large effects in **the normalization region**.
- Large statistics but not sensitivity to Δa_{had}

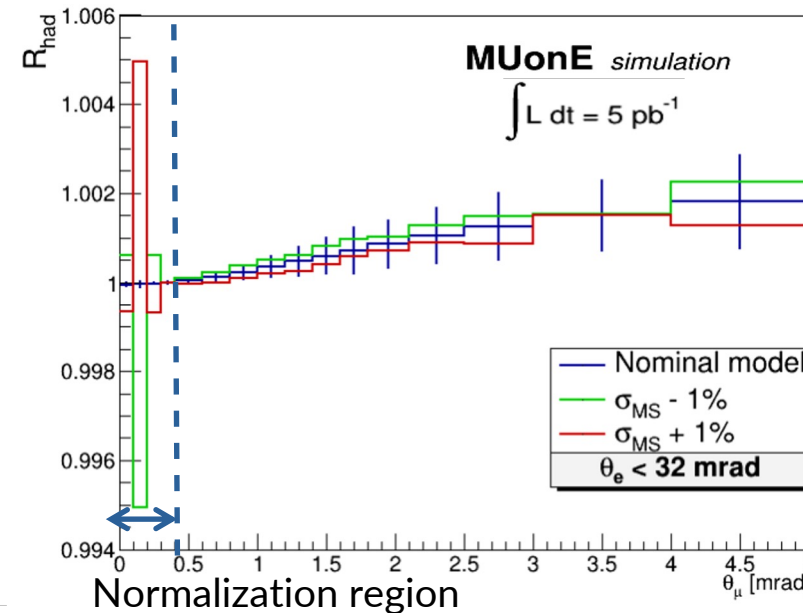
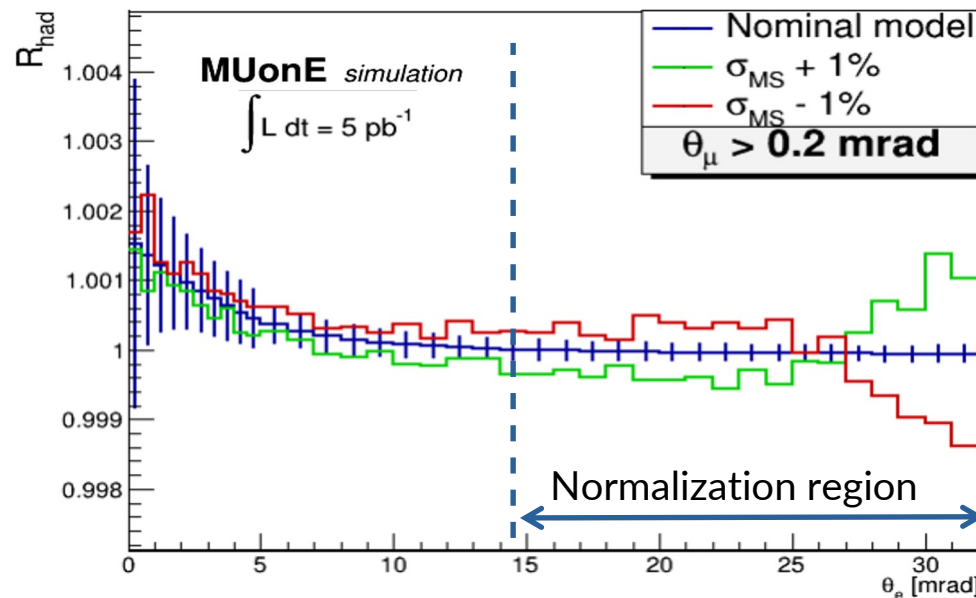


Systematic Effects



① Multiple Scattering

- Effect of $\alpha \pm 1\%$ error on the multiple scattering core width
- Previously studied in a Beam Test in 2017 with 12–20 GeV electrons on the 8-20 mm Carbon targets: [G. Abbiendi et al JINST \(2020\) 15 P01017](#)

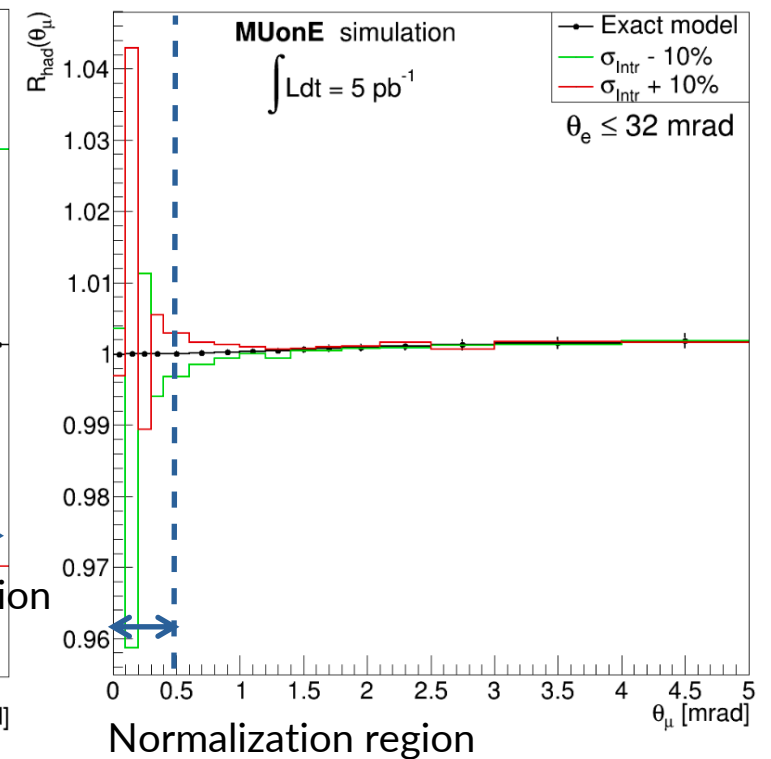
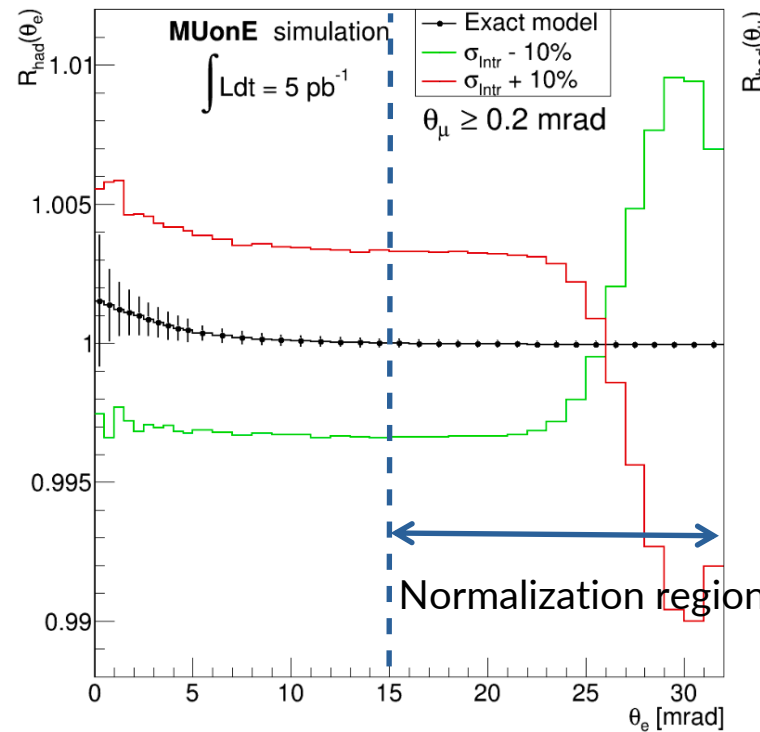


Systematic Effects

② Angular Intrinsic Resolution



- 2S modules resolution (from beam test): 8-11 μm
- An effect of a $\pm 10\%$ error on the angular intrinsic resolution

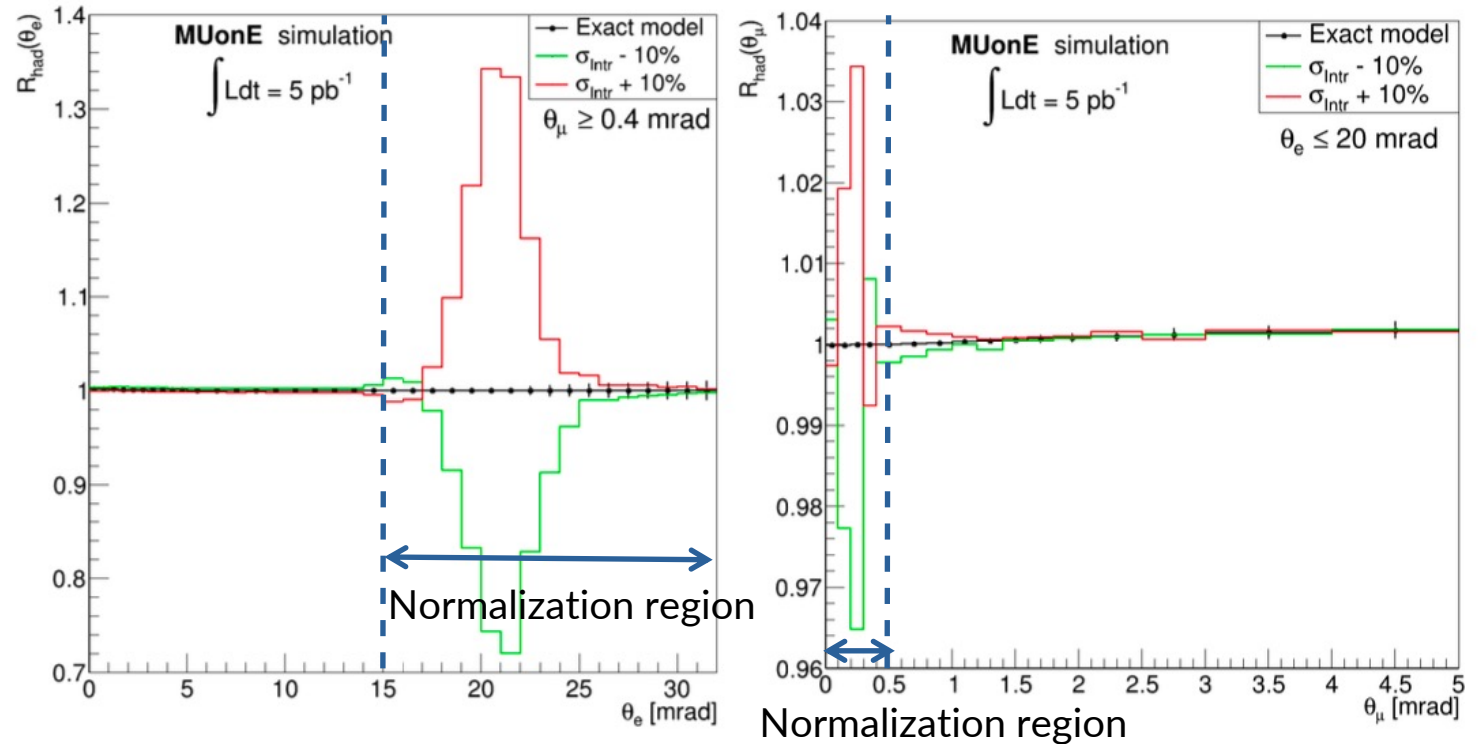


Systematic Effects

② Angular Intrinsic Resolution



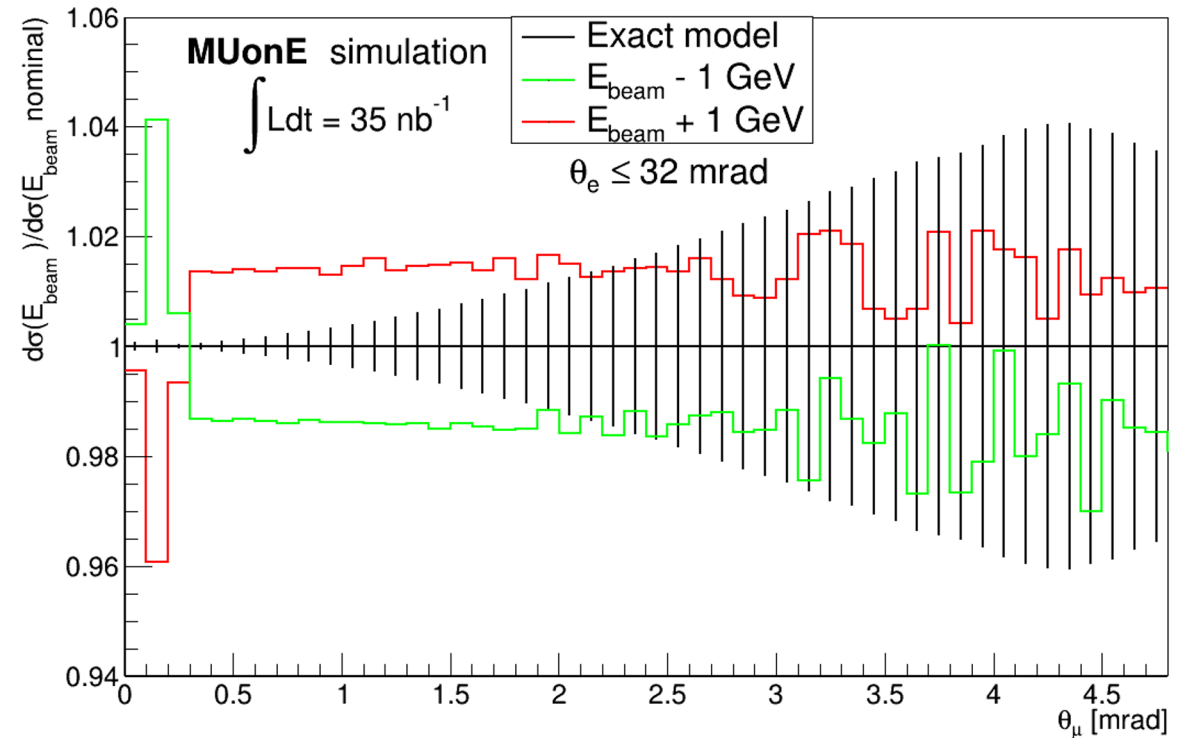
- 2S modules resolution (from beam test): 8-11 μm
- An effect of a $\pm 10\%$ error on the angular intrinsic resolution
- $\theta_\mu > 0.4 \text{ mrad}$ ($\theta_e < 20 \text{ mrad}$) gives better normalization region



Systematic Effects

③ Muon Beam Energy

- Accelerator provides E_{beam} with $O(1\%)$ precision (~ 1 GeV) \rightarrow goal of **10 ppm** in the differential cross section
- The effect can also be seen in a quick data taking (\sim hours) for calibration

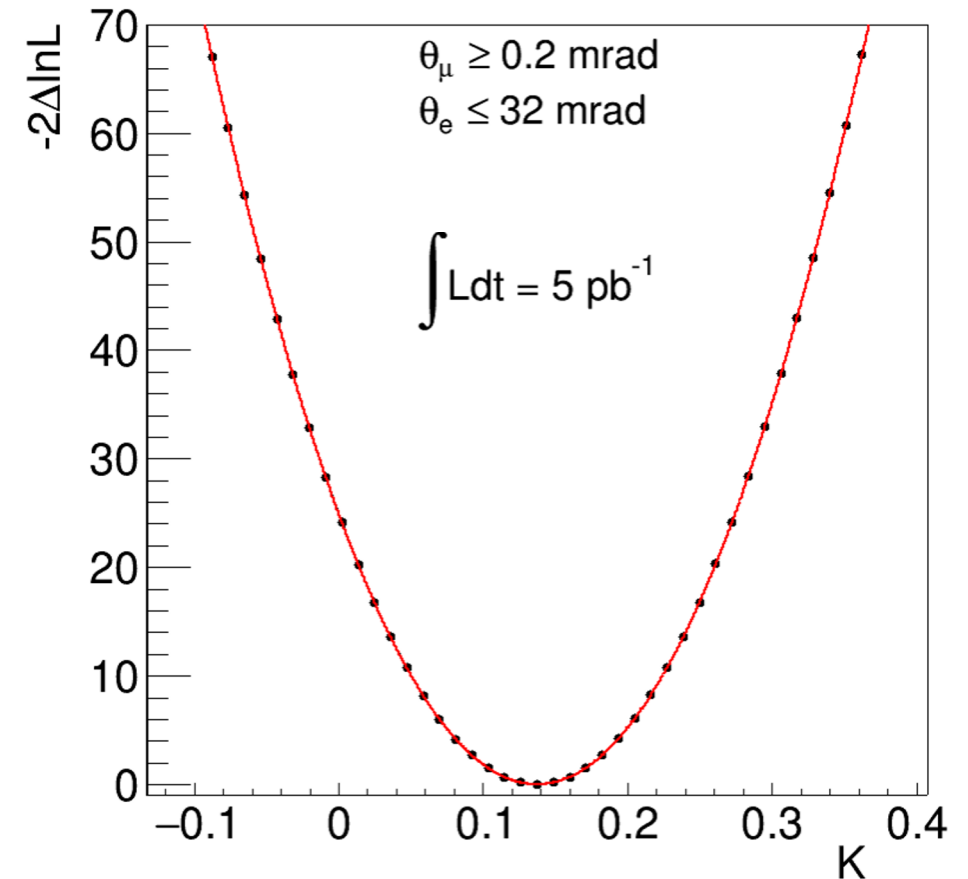


Systematic Effects



④ Residual Systematics: the 'Combine' Tool

- Include **residual systematics as nuisance parameters** in a fit with signal.
- We can adjust the distortions in the shape of the differential cross section due to the residual systematics
 - **Combine tool** performs a likelihood fit to the nuisance parameters for each template
 - The profile likelihood as a function of K
 - Best fit value of K is determined by parabolic interpolation among the template points.
 - Nuisance parameters values for $K = K_{\text{best_fit}}$



Systematic Effects

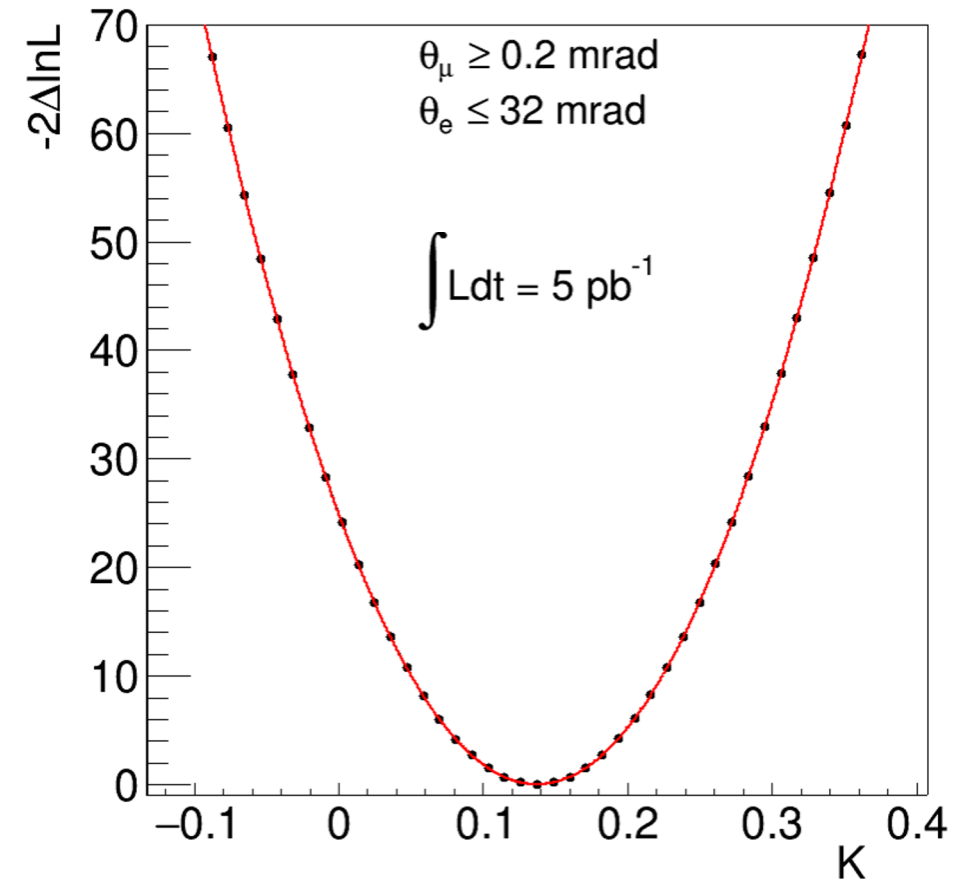


④ Residual Systematics: the 'Combine' Tool

- Include **residual systematics as nuisance parameters** in a fit with signal.
- We can adjust the distortions in the shape of the differential cross section due to the residual systematics

Selection cuts	Fit results
	$K = 0.133 \pm 0.028$
	$\mu_{\text{MS}} = (0.47 \pm 0.03)\%$
$\theta_e \leq 32 \text{ mrad}$	$\mu_{\text{Intr}} = (5.02 \pm 0.02)\%$
$\theta_\mu \geq 0.2 \text{ mrad}$	$\mu_{\text{E}_{\text{Beam}}} = (6.5 \pm 0.5) \text{ MeV}$
	$\nu = -0.001 \pm 0.003$

(Input shifts identified correctly)



Open to new ideas!

- Tracker (2S module?), Calorimeter
 - Efficiency, pile-up, ...
- Mechanics

- A new method to extract a_μ^{HLO} using the same MUonE data
- Software developments (systematic effects, prompt data analysis, computing...)
- ...
- Working towards **TDR next year** → an important milestone
- New collaborators & ideas are welcome!

Alternative method to extract a_μ^{HLO}



a_μ^{HLO} can be written as the sum of 4 terms:

$$a_\mu^{\text{HLO}} = a_\mu^{\text{HLO}(I)} + a_\mu^{\text{HLO}(II)} + a_\mu^{\text{HLO}(III)} + a_\mu^{\text{HLO}(IV)}$$

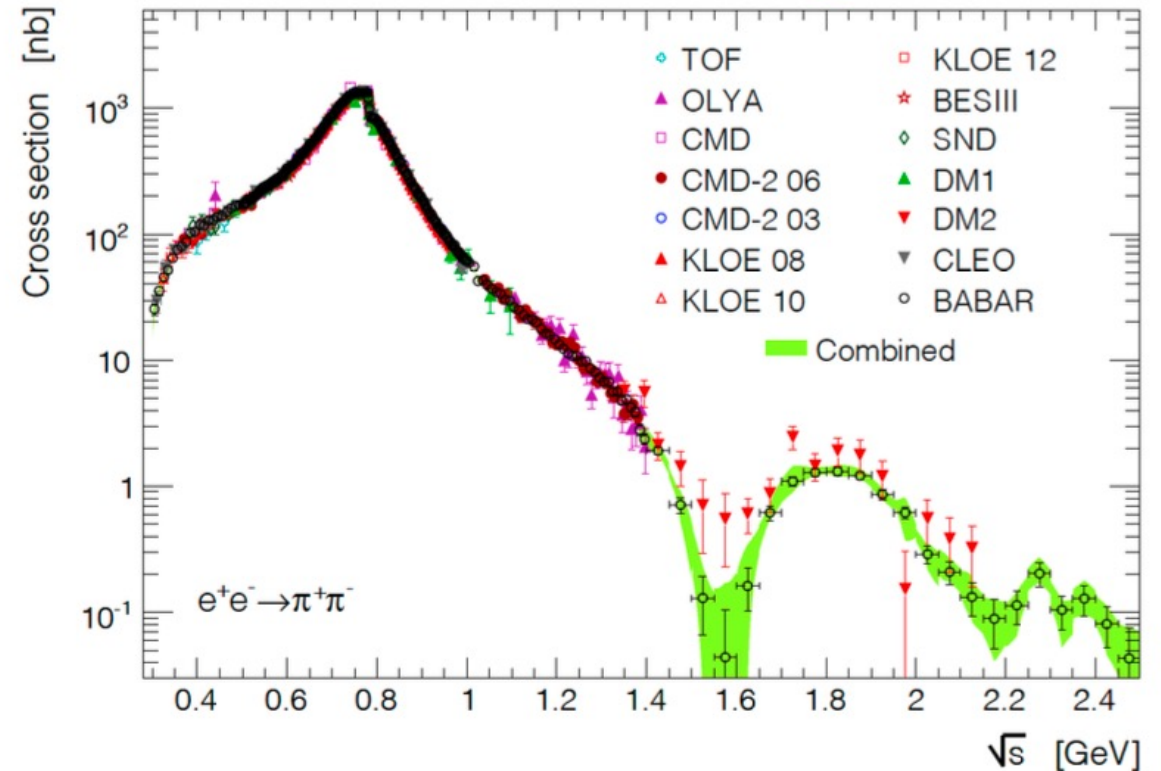
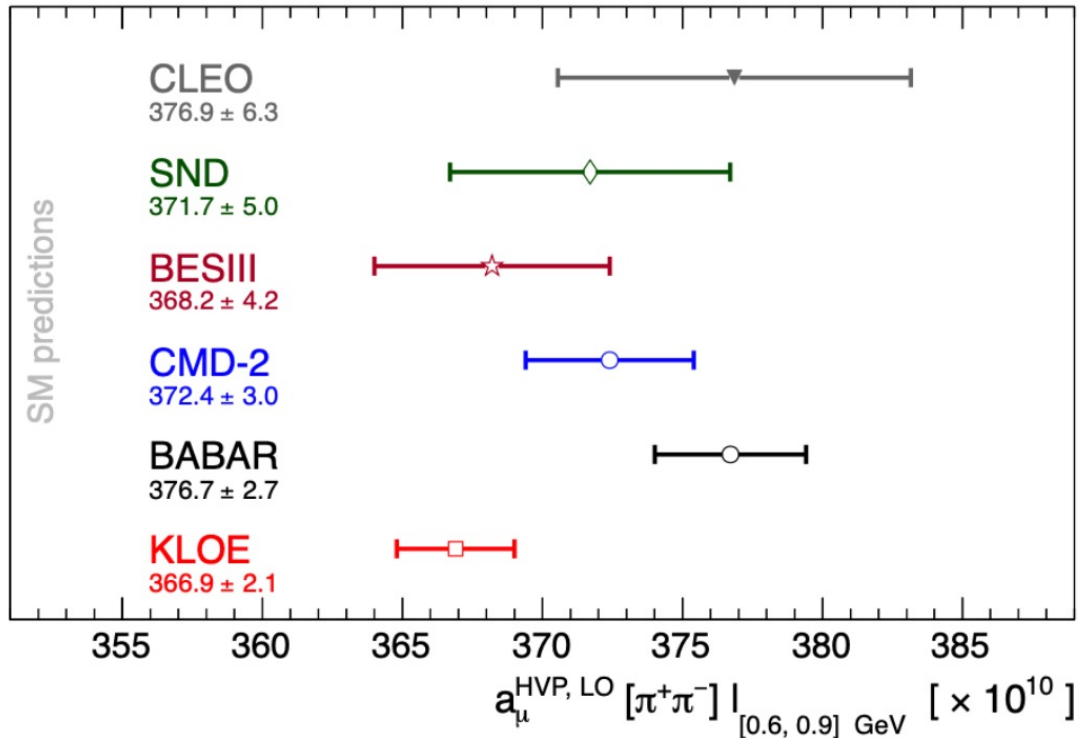
MUonE	$a_\mu^{\text{HLO}(I)} = -\frac{\alpha}{\pi} \sum_{n=1}^3 \frac{c_n}{n!} \frac{d^{(n)}}{dt^n} \Delta\alpha_{had}(t) \Big _{t=0}$	~99% of a_μ^{HLO}
Time-like data and pQCD	$a_\mu^{\text{HLO}(II)} = \frac{\alpha}{\pi} \frac{1}{2\pi i} \oint_{ s =s_0} \frac{ds}{s} c_0 s \Pi_{had}(s) \Big _{\text{pQCD}}$	~1% of a_μ^{HLO}
	$a_\mu^{\text{HLO}(III)} = \frac{\alpha^2}{3\pi^2} \int_{s_{th}}^{s_0} \frac{ds}{s} [K(s) - K_1(s)] R(s)$	
	$a_\mu^{\text{HLO}(IV)} = \frac{\alpha^2}{3\pi^2} \int_{s_0}^{\infty} \frac{ds}{s} [K(s) - \tilde{K}_1(s)] R(s)$	

11

[Talk at Bern, 8th Sep by GV](#)

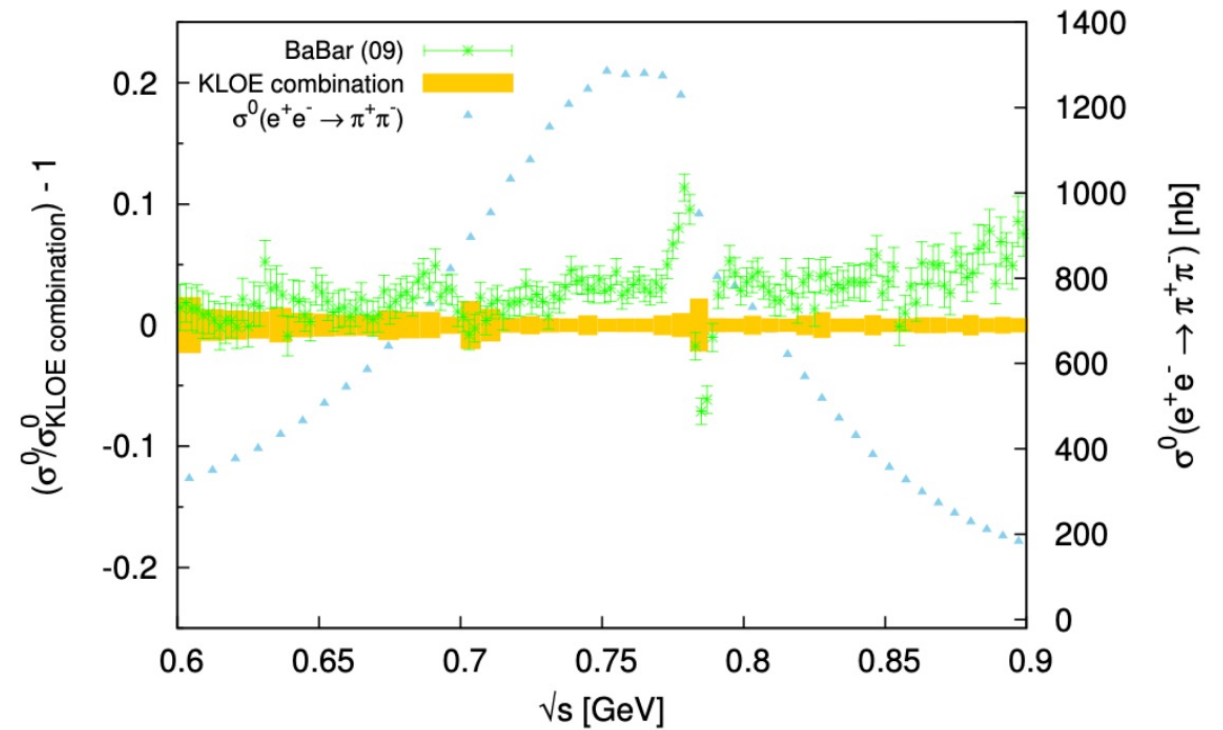
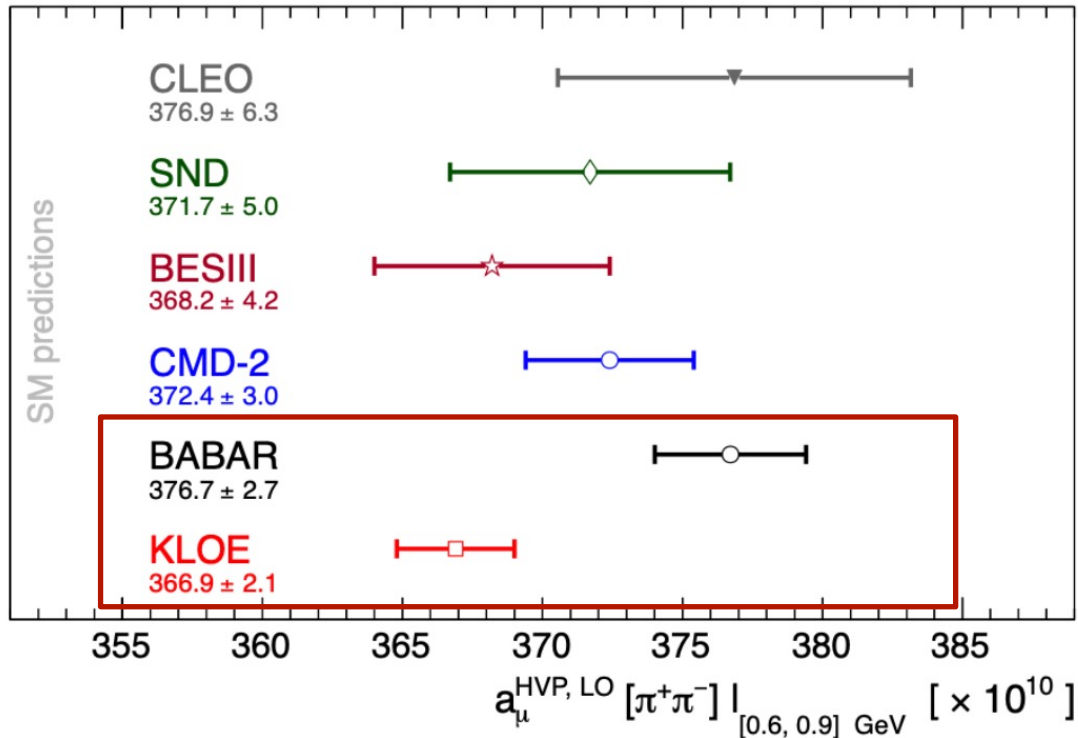
Muon $g - 2$ Puzzle

$e^+e^- \rightarrow \pi^+\pi^-$ Channel



Muon $g - 2$ Puzzle

$e^+e^- \rightarrow \pi^+\pi^-$ Channel



- The discrepancy between BABAR and KLOE needs to be understood

Track Reconstruction



Production loop – reconstruction – algorithm

- 2D tracks reconstructed in X and Y projections
 - seeding with hit pairs
 - additional hits assigned based on distance from track
 - track refitted until no new hits can be added
 - clones with same sets of hits removed
 - [trivial hit pairing with intended detector setup](#)
- 3D tracks reconstructed from all pairs of X and Y tracks
 - stereo hits assigned based on distance
 - tracks with no stereo hits must have at least 3 X and Y hits
 - [only tracks with stereo hits allowed with intended detector setup](#)
 - tracks fitted and sorted based on χ^2/ndf
 - shared hits removed from worse tracks
 - if adaptive fitter enabled, Kalman filter is ran on tracks
- linking based on deposited charge
 - full digitization → no direct matching
 - 3 tracks with highest deposits assigned to each stub, sorted
 - reconstructed track linked to track with highest weighted sum
- for each target, all possible vertices are reconstructed
 - if enabled, also adaptive vertices
- signal vertices
 - single incoming and two outgoing tracks required (fixed number)
 - z position fixed in the middle of the target
 - kinematic fit with tracks restricted to an interaction point
 - modifies track parameters → improved θ angle resolution
- adaptive fitter
 - implemented for alignment using pions
 - only outgoing tracks required (at least 2, variable)
 - seeding based on distance in target, window size to be optimized
 - doesn't modify tracks, assigns Tukey weights instead
 - fits vertex position, including z

The digitization algorithm

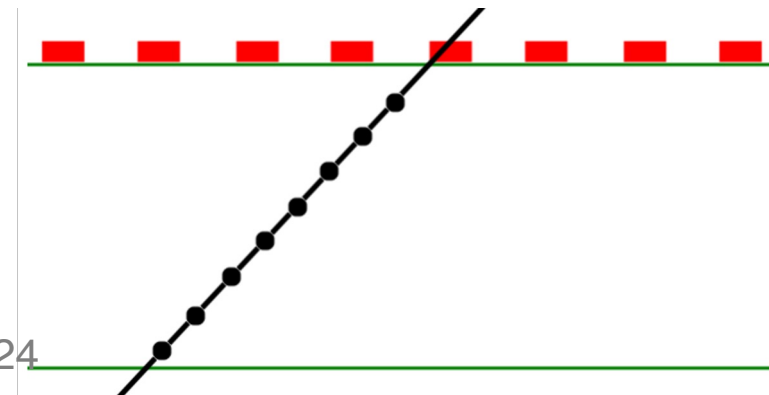
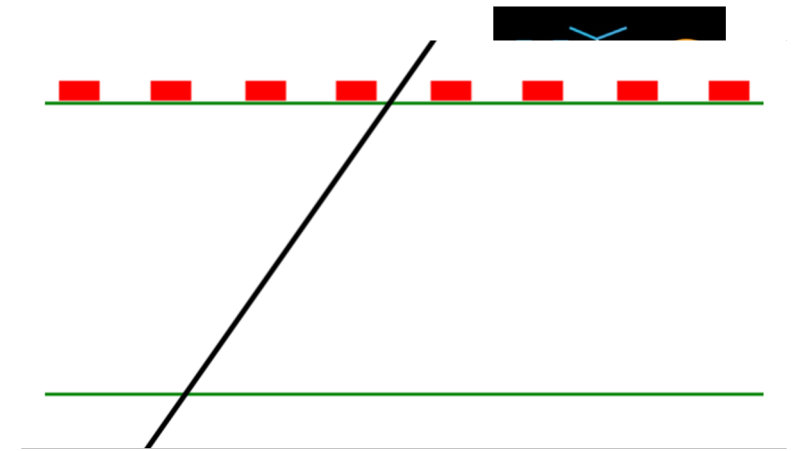
1) Primary ionization

- Start from the trajectory of a particle in a Si sensor + energy deposit.

- The trajectory is sampled into ionization points (10 μm steps). An even fraction of the total energy deposit is associated to each point.

- The fraction of energy deposit is converted into a charge

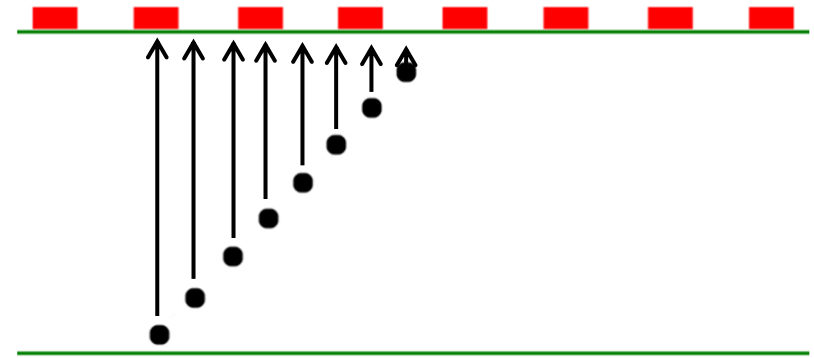
20/04/2024 $(Q = E_{\text{dep}}/3.6 \text{ eV}).$



The digitization algorithm

2) Drift

- The ionization points are drifted on the sensitive surface of the Si.
- A Gaussian charge diffusion model is applied to the ionization points.

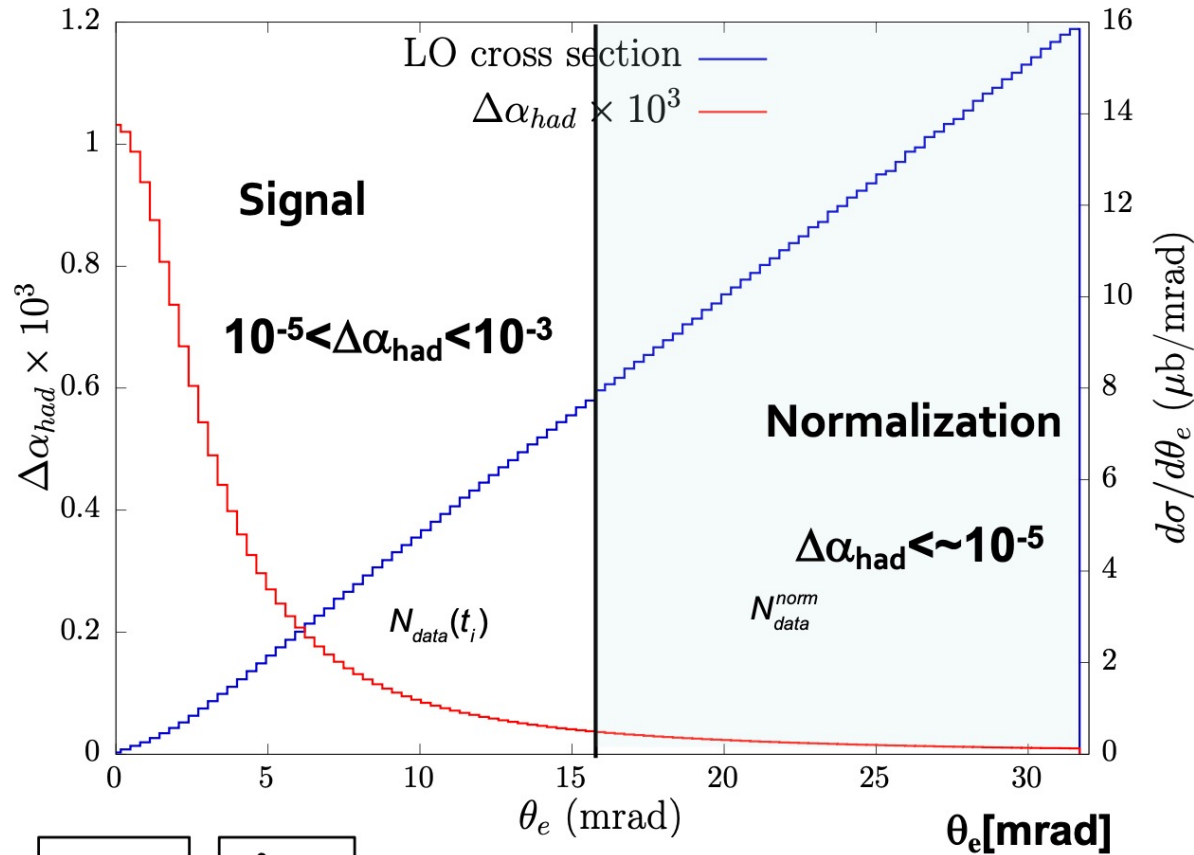


$$\sigma_{drift} \propto \sqrt{\text{drift distance}}$$

3) Induce signal

- The ionization point is expanded to a 2D cloud. The dimension depends on the drift distance.
- The total amount of charge in each strip is obtained by adding contribution from all the particles.

MUonE : signal/normalization region



$$\frac{N_{data}(t_i)}{N_{MC}^0(t_i)} = \frac{N_{data}(t_i)}{N_{data}^{norm}} \times \frac{\sigma_{MC}^{0,norm}}{\sigma_{MC}^0(t_i)} \sim 1 - 2(\Delta\alpha_{lep}(t_i) + \Delta\alpha_{had}(t_i))$$

Ratio of data $N_{signal}(t)/N_{normalization}$

Ratio of the theoretical cross section (with no VP)

a_μ^{HLO} at 0.3% → These two ratios should be known at 10^{-5}