

# New calculations & techniques for NLO EW

Facilitating Precision Physics at the LHC

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GEFÖRDERT VOM



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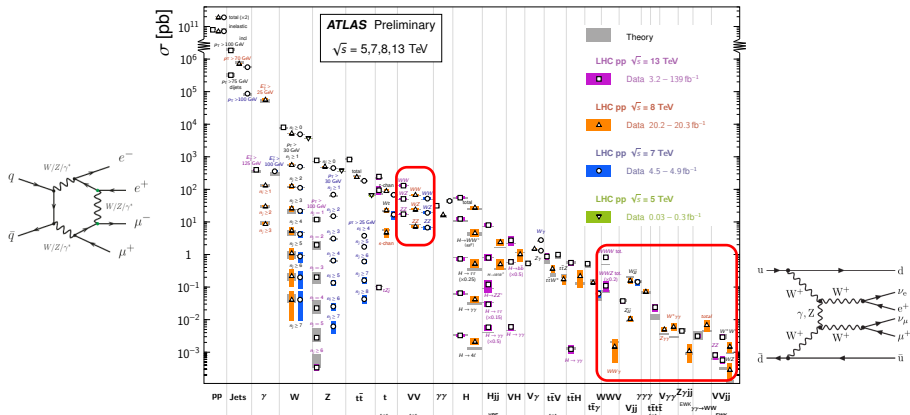
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# Scrutinizing the Standard Model: multi-boson production

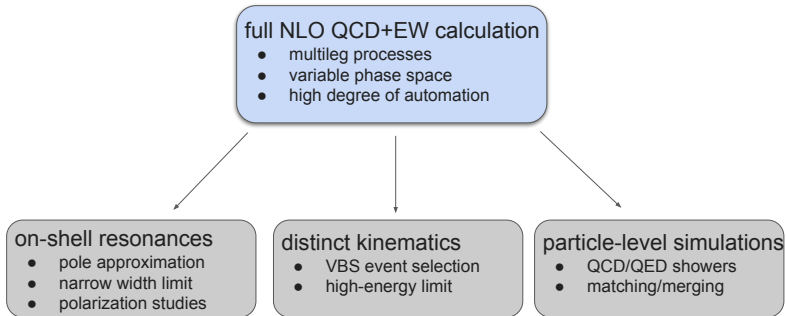
Standard Model Production Cross Section Measurements

Status: February 2022



- rare & subtle electroweak signal processes probing EWSB
- triple-, quartic gauge-boson couplings
- longitudinal polarisation modes of massive gauge bosons

# Accounting for (dominant) electroweak corrections



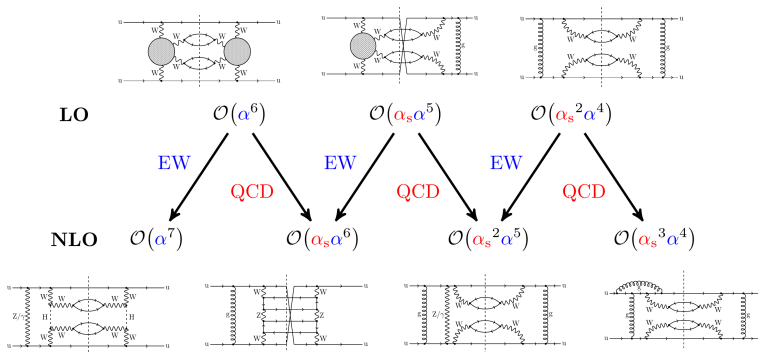
- EW one-loop and QED real emission amplitudes needed, e.g. RECOLA [Denner *et al.*], OPENLOOPS [Pozzorini *et al.*]
- QED infrared subtraction terms (dipole/FKS)  
     $\rightsquigarrow$  real weak-boson radiation excluded
- frameworks to accomplish full calculations, e.g. MG5\_aMC [Frederix *et al.*], POWHEG [Nason *et al.*], SHERPA [Bothmann *et al.*]
- invoke QCD/QED showers for particle-level predictions  
    HERWIG [Bellm *et al.*], PYTHIA [Bierlich *et al.*], SHERPA

## state-of-the-art: full NLO calculation for $2 \rightarrow 6$ processes

- full NLO QCD & EW corrections and QCD–EW interferences  
 $\rightsquigarrow$  crucial benchmark for approximation schemes

- consider **like-sign  $W$ -boson scattering**:  $pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$

[Dittmaier et al. JHEP 11 (2023) 22] [Biedermann et al. JHEP 10 (2017) 124]



## state-of-the-art: $pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$ at full NLO

[Dittmaier et al. JHEP 11 (2023) 22] [Biedermann et al. JHEP 10 (2017) 124]

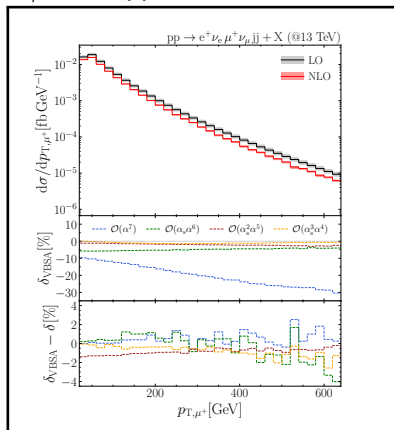
- consider **VBS event selection cuts**, in particular

$$M_{j_1 j_2} > 500 \text{ GeV}, |y_{j_1} - y_{j_2}| > 2$$

- full off-shell calculation vs. VBS/DPA approximations

	Order	Result [fb]	$\delta$ [%]	Scale uncertainty
LO	$\mathcal{O}(\alpha^6 \alpha_s^0)$	1.24597(5)	-7.7%	9.9%
	$\mathcal{O}(\alpha^5 \alpha_s^1)$	0.051133(3)	-14.0%	17.7%
	$\mathcal{O}(\alpha^4 \alpha_s^2)$	0.18649(2)	-22.2%	31.6%
	sum	1.48359(5)	-9.8%	12.1%
	NLO	$\mathcal{O}(\alpha^7 \alpha_s^0)$	-0.1747(5)	-11.8%
$\mathcal{O}(\alpha^6 \alpha_s^1)$		-0.0902(8)	-6.1%	
$\mathcal{O}(\alpha^5 \alpha_s^2)$		-0.00017(19)	0.0%	
$\mathcal{O}(\alpha^4 \alpha_s^3)$		-0.0033(7)	-0.2%	
sum		-0.268(1)	-18.1%	
LO+NLO	sum	1.215(1)	-4.0%	1.5%

- sizeable NLO corrections
- VBS/DPA within few %
- $\mathcal{O}(\alpha^7)$  dominate tails  
 $\rightsquigarrow$  Sudakov logarithms



## state-of-the-art: $pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$ at full NLO

[Denner, Pellen, Schönherr, S. to appear]

- consider **inclusive triple- $W$**  phase space, in particular

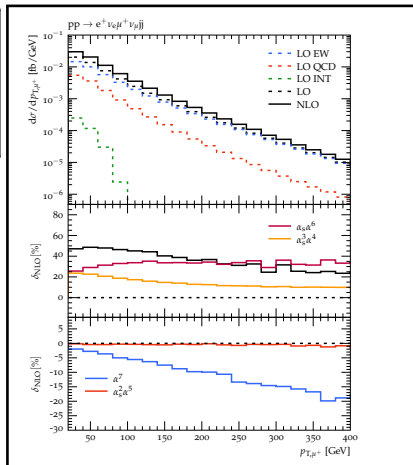
$$M_{j_1 j_2} < 160 \text{ GeV}, \quad |y_{j_1} - y_{j_2}| < 1.5 \quad \text{[inspired by ATLAS 2201.13045]}$$

orders	$\mathcal{O}(\alpha^6)$	$\mathcal{O}(\alpha_s \alpha^5)$	$\mathcal{O}(\alpha_s^2 \alpha^4)$	sum
$\sigma_{\text{LO}}[\text{fb}]$	0.78549(9)	0.00732(1)	0.25925(3)	1.05206(9)
$\sigma/\sigma_{\text{LO}}^{\text{sum}}[\%]$	74.7	0.7	24.6	100

orders	$\mathcal{O}(\alpha^7)$	$\mathcal{O}(\alpha_s \alpha^6)$	$\mathcal{O}(\alpha_s^2 \alpha^5)$	$\mathcal{O}(\alpha_s^3 \alpha^4)$	sum
$\delta\sigma[\text{fb}]$	-0.035(1)	0.305(1)	-0.0032(3)	0.2260(3)	0.493(2)
$\delta\sigma/\sigma_{\text{LO}}^{\text{sum}}[\%]$	-3.4	29.0	-0.30	21.5	46.9

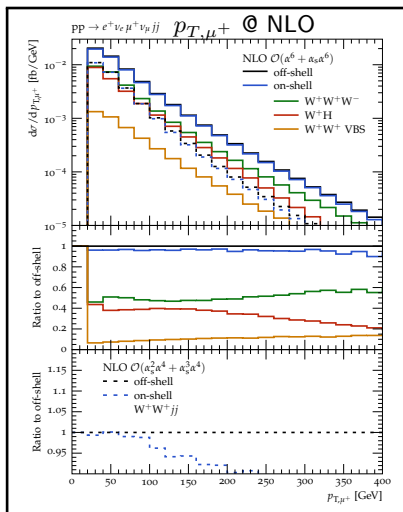
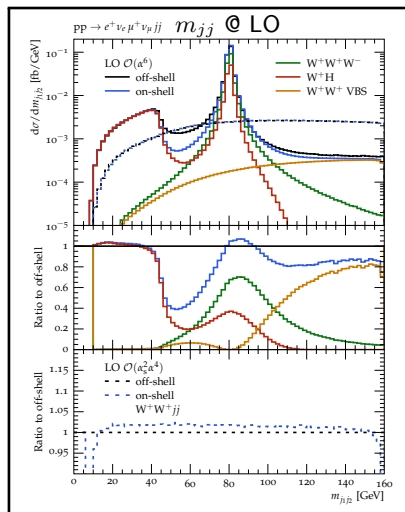
- many  $\mathcal{O}(\alpha^6)$  contributions  
 $WWW, WH, WZ, \text{VBS}$
- $\delta_{\text{NLO}} = +47\%$ , largest  
 $\mathcal{O}(\alpha_s \alpha^6)$  &  $\mathcal{O}(\alpha_s^3 \alpha^4)$
- $\mathcal{O}(\alpha^7)$  sizeable in tails  
 $\rightsquigarrow$  Sudakov logarithms



## state-of-the-art: $pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$ at full NLO

[Denner, Pellen, Schönherr, S. to appear]

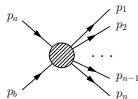
- full off-shell calc vs. incoherent sum of on-shell channels



## universal high-energy enhancements

- consider EW one-loop amplitudes in high-energy limit, where

$$s_{ij} \equiv (p_i + p_j)^2 \sim s \gg M_W^2 \quad \forall i, j$$



- amplitude factorization, dominance of scale-ratio logarithms

$$\mathcal{M}_1 \propto \mathcal{M}_0 \times \left( \delta^{\text{DL}} + \delta^{\text{SL}} \right)$$

$$\delta^{\text{DL}} \sim \frac{\alpha}{4\pi} \log^2 \left( \frac{|s_{ij}|}{M_W^2} \right) \quad \delta^{\text{SL}} \sim \frac{\alpha}{4\pi} \log \left( \frac{|s_{ij}|}{M_W^2} \right)$$

- algorithm to construct NLL EW corrections [Denner, Pozzorini '01]
- recent revisitations, refinements and new implementations

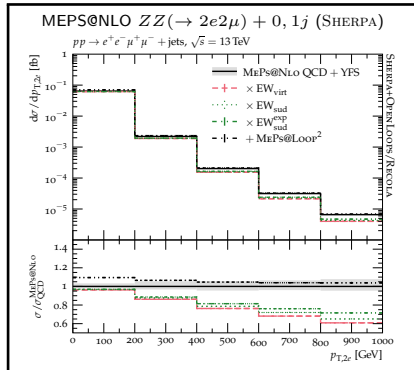
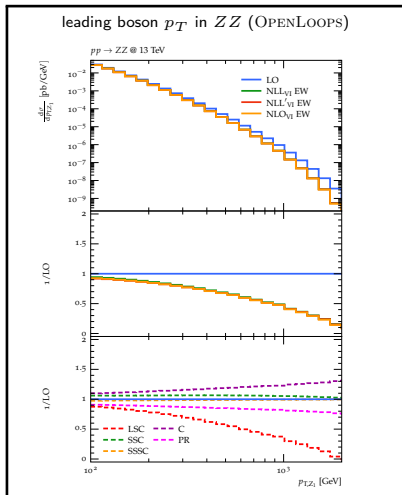
SHERPA, MG5\_aMC & OPENLOOPS

[Bothmann, Napoletano '20, Bothmann et al. '22] [Pagani, Zaro '22, Pagani et al. '23] [Lindert, Mai '23]



# Taming the tails: EW Sudakov logarithms

- extensive validation for OPENLOOPS [Lindert, Mai 2312.07927]
- comparison to NLO<sub>VI</sub> EW approximation [Kallweit et al. '15]
- ↪ used in SHERPA MEPS@NLO approach [Bothmann et al. JHEP 06 (2022) 131]



↪ MG5\_aMC Timea Vitos (Thu)

- NLL resummation in SCET<sub>EW</sub> [Denner, Rode 2402.10503]

## predicting vector-boson polarization fractions $f_{\text{pol}}$

- consider decay of on-shell massive gauge boson ( $m_{q/l} = 0$ )  
↪ use pole approximation, i.e. on-shell projections, or NWA

$$\mathcal{M}^{\text{tot}} \approx \sum_{\lambda=L,\pm} \mathcal{M}_{\lambda}^{\text{fac}} = \frac{i}{p^2 - M_V^2 + i\Gamma_V M_V} \sum_{\lambda=L,\pm} \mathcal{M}_{\lambda}^{\text{prod}}(\tilde{p}) \mathcal{M}_{\lambda}^{\text{dec}}(\tilde{p})$$

- consider inclusive & fiducial phase spaces  
↪ residual **interference contribution** when fiducial cuts

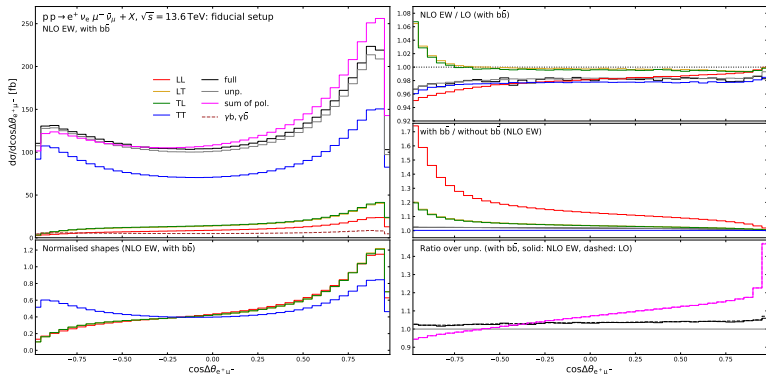
$$|\mathcal{M}_{\text{res}}^{\text{tot}}|^2 = \sum_{\lambda=L,\pm} |\mathcal{M}_{\lambda}^{\text{fac}}|^2 + \sum_{\lambda \neq \lambda'} \mathcal{M}_{\lambda}^{\text{fac}} \mathcal{M}_{\lambda'}^{*\text{fac}}$$

- seek for differential distributions with  $\lambda = L$  enhancements  
↪ for use in experimental template fits  
↪ note,  $f_{\text{pol}}$  frame dependent, e.g. lab or diboson rest frame  
↪ **more on polarizations in Rene Poncelet's talk (Thu)**

## NLO EW for polarized $pp \rightarrow W^+(\rightarrow e^+\nu_e)W^-(\rightarrow \mu^-\bar{\nu}_\mu)$

[Denner et al. PLB 850 (2024) 138539] [Dao, Le EPJC 84 (2024) 3]

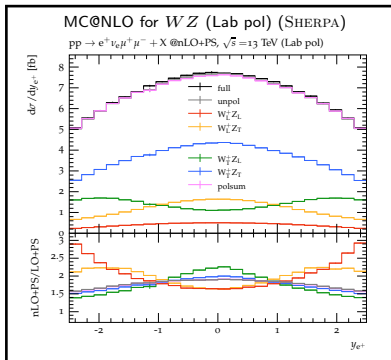
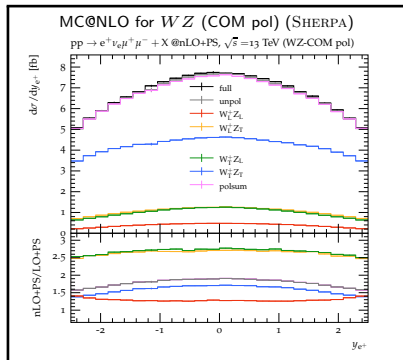
- full calc & DPA on-shell projection (valid for  $\sqrt{\hat{s}} > 2M_W$ )
- polarization states at amplitude level, fiducial cuts  
 $\rightsquigarrow$  non-vanishing interference contributions
- allow for  $\gamma\gamma$ ,  $b\bar{b}$  &  $\gamma b$  (full calc only) initial states  
 $\rightsquigarrow$  contributing differently for  $LL$ ,  $TT$ ,  $LT/TL$



## particle-level predictions for polarized bosons

[Hoppe, Schönherr, Siegert JHEP 04 (2024), 001] [Pelliccioli, Zanderighi EPJC 84 (2024) 1]

- implementations in SHERPA (NWA) & POWHEG (DPA)
- restrict to QCD corrections at (N)LO and QCD parton shower
- SHERPA utilizes its spin-correlated decay model [Höche et al. '15]
  - ↪ event weights for different polarizations/frames on-the-fly
  - ↪ (currently) assume virtual QCD amplitude as unpolarized



## accounting for (dominant) NLO EW corrections

- full NLO SM calculations for  $2 \rightarrow 6/7$  processes
  - ↪ numerous contributing (non-)resonant channels
  - ↪ corrections strongly dependent on phase-space selections
  - ↪ validity tests for approximation schemes
- automation of NLL EW Sudakov corrections in generators
  - ↪ SHERPA, MG5\_aMC, OPENLOOPS
- predictions for polarised resonant vector bosons
  - ↪ NLO QCD EW corrections for diboson channels
  - ↪ NLO QCD+PS in POWHEG and SHERPA

