# The NLL accurate parton shower Alaric in Sherpa

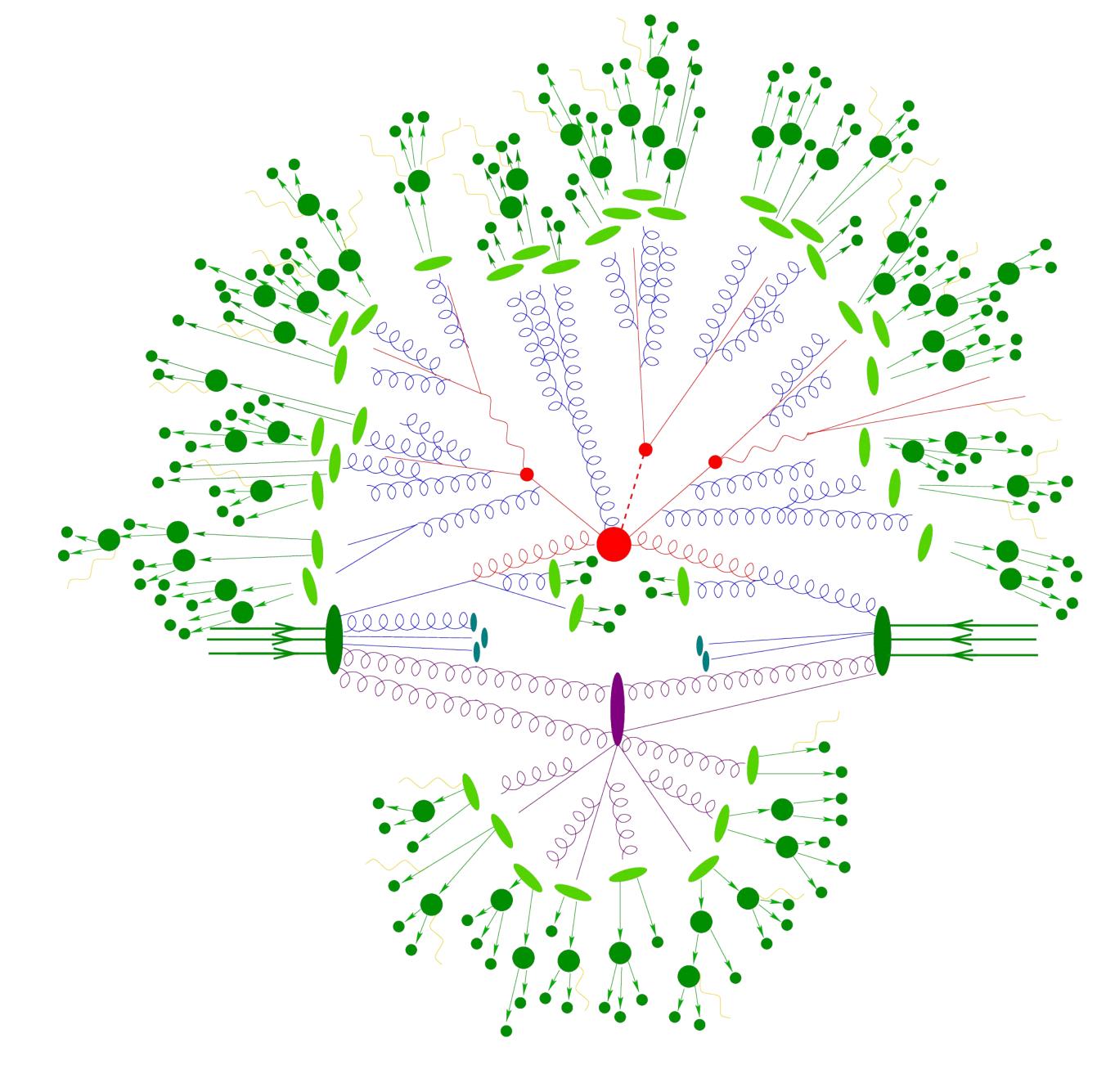
25th MCnet meeting 2023, 24 April 2023

[arXiv:2208.06057]

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#### colliders for theorists

- Event simulation factorised into
  - Hard Process
  - Parton Shower
  - Underlying event
  - Hadronisation
  - QED radiation
  - Hadron Decays



# A Logarithmically Accurate Resummation In C++

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#### This Talk:

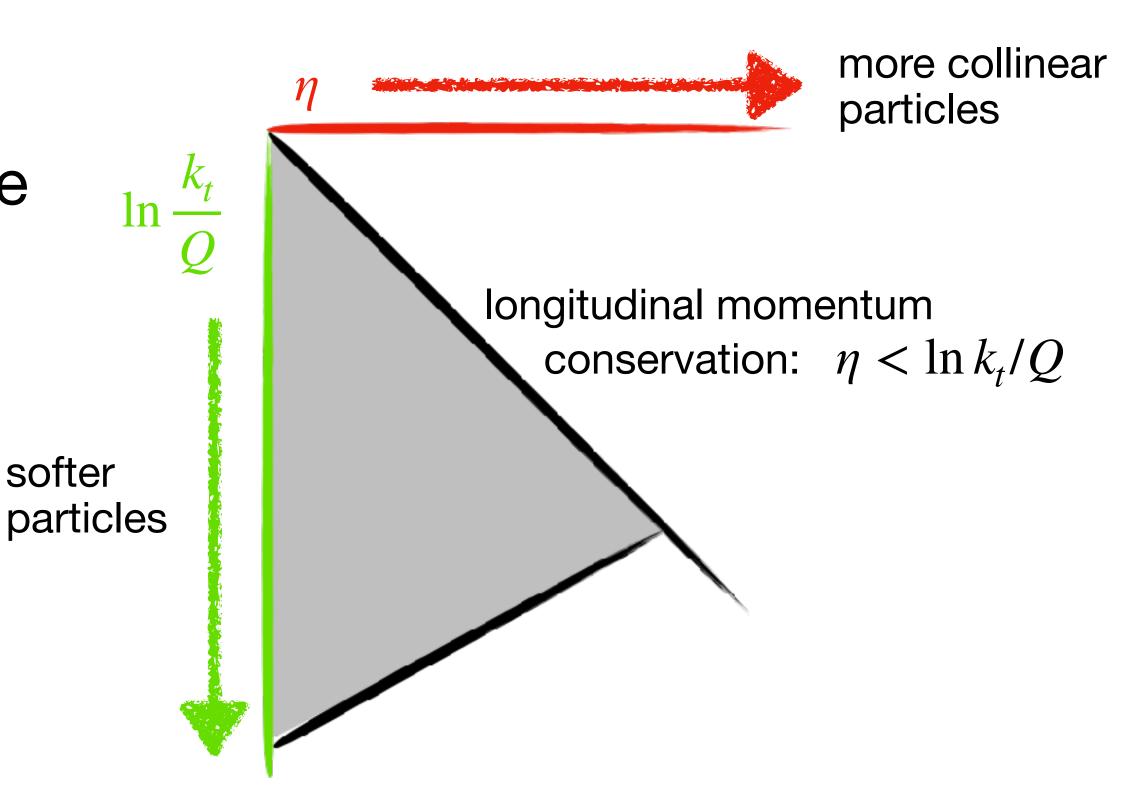
#### Why?

- parton showers resum large logs ~ NLL, but open questions on actual accuracy
- starting work towards NNLL → probably better resolve this first
- recent formal discussion → current dipole showers need reworking

[Dasgupta, Dreyer, Hamilton, Monni, Salam '18]

# parton showers - Cliff notes version

- no-emission probability (sudakov factor)
- $\sim \exp \left[-\int_{t_0}^{t_1} \frac{dk_t}{k_t} dz \frac{\alpha_S}{2\pi} P(z)\right]$
- splitting kernels P(z) captures soft and collinear limits of matrix elements
- fill phase space ordered in evolution variable  $(k_t, \theta, q^2, ...) \Rightarrow \text{here } k_t \text{ ordered shower}$
- generate new final state after emission according to recoil scheme



# splitting of Eikonal

$$\frac{p_i p_k}{(p_i p_j)(p_j p_k)} = \frac{1}{E_j^2} \frac{1 - \cos \theta_{ik}}{(1 - \cos \theta_{ij})(1 - \cos \theta_{jk})} \equiv \frac{W_{ik,j}}{E_j^2}$$

naive implementation leads to soft double counting need to split into ij and kj collinear terms [Marchesini, Webber '88]

#### Option 1:

$$W_{ik,j} = \tilde{W}_{ik,j}^{i} + \tilde{W}_{ki,j}^{k} , \quad \text{where} \quad \tilde{W}_{ik,j}^{i} = \frac{1}{2} \left( \frac{1 - \cos \theta_{ik}}{(1 - \cos \theta_{ij})(1 - \cos \theta_{jk})} + \frac{1}{1 - \cos \theta_{ij}} - \frac{1}{1 - \cos \theta_{jk}} \right)$$

• e.g. Angular ordered shower, downside: problems with NGLs

#### Option 2: follow [Catani, Seymour '97]

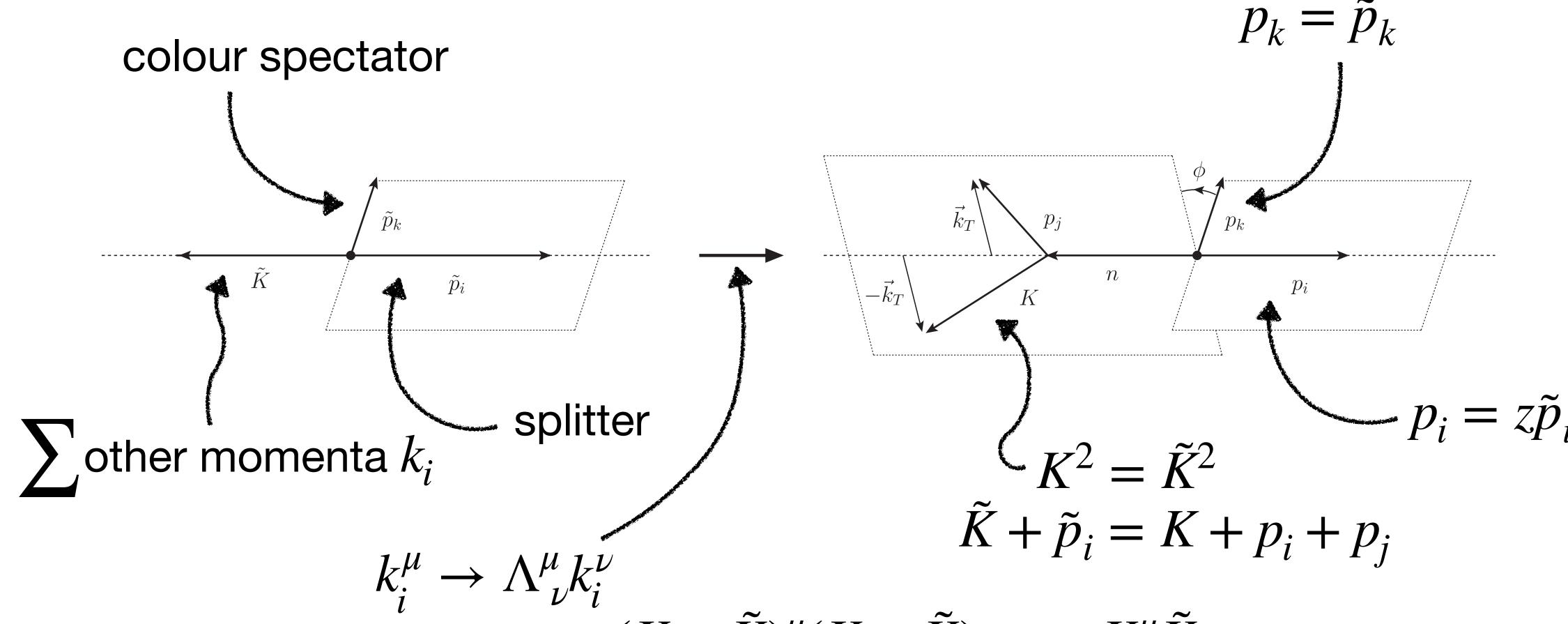
$$W_{ik,j} = \bar{W}_{ik,j}^i + \bar{W}_{ki,j}^k$$
, where  $\bar{W}_{ik,j}^i = \frac{1 - \cos \theta_{ik}}{(1 - \cos \theta_{ij})(2 - \cos \theta_{ij} - \cos \theta_{jk})}$ 

• full phase space coverage, splitting functions remain positive definite

# kinematics - global recoil scheme

Before splitting:

After splitting:



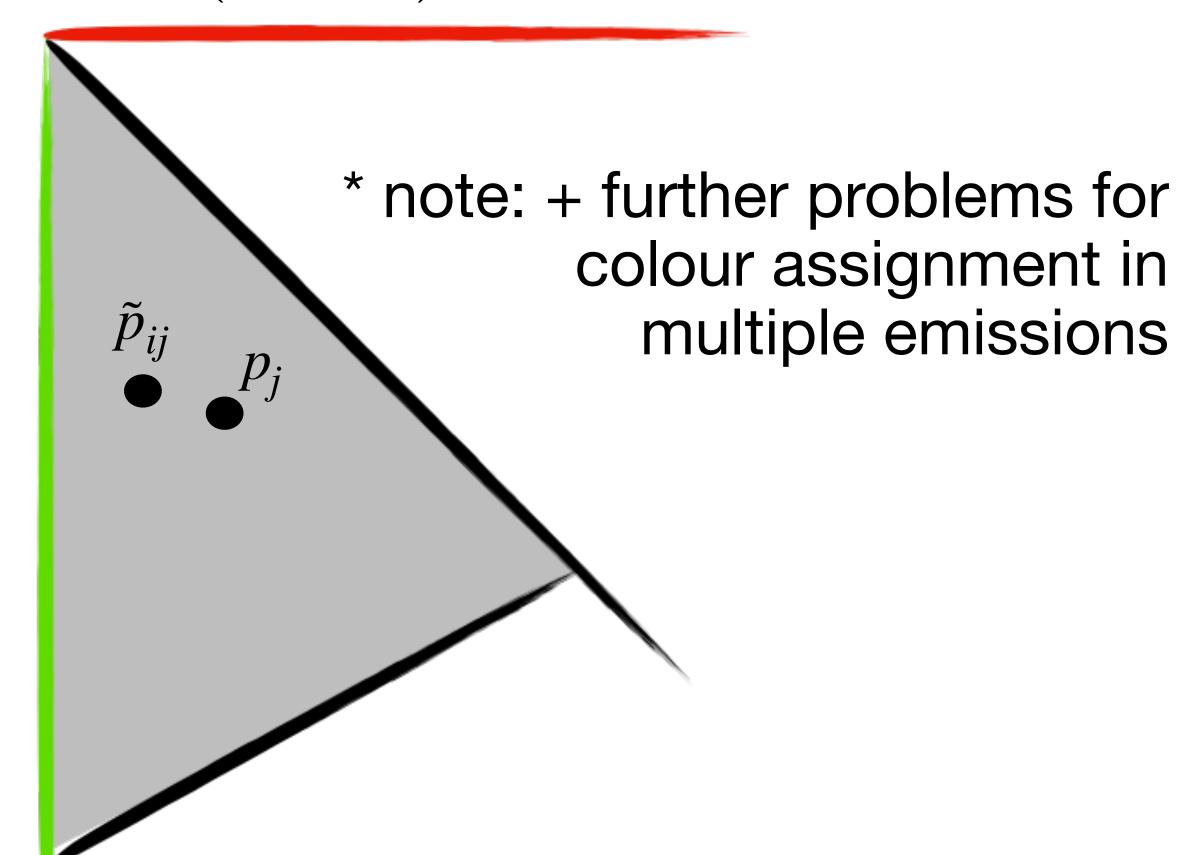
[Catani, Seymour '97] 
$$\Lambda^{\mu}_{\ \nu} = g^{\mu}_{\ \nu} - \frac{(K + \tilde{K})^{\mu}(K + \tilde{K})_{\nu}}{K \cdot \tilde{K} + \tilde{K}^{2}} + 2 \frac{K^{\mu} \tilde{K}_{\nu}}{\tilde{K}^{2}} \ \to \ \Lambda^{\mu}_{\ \nu} \tilde{K}^{\nu} = K^{\mu}$$

## effect of recoil on accuracy

- question: do recoil effects indeed vanish in soft limit (i.e.  $\rho \to 0$ )?\* [Dasgupta,Dreyer,Hamilton,Monni,Salam '18]
- consider situation where we first emit  $\tilde{p}_{ij}$  from  $p_a$ ,  $p_b$ , then emit  $p_j$ ,  $\tilde{p}_{ij} \rightarrow p_i$ ,  $p_j$
- transverse momentum of  $p_i$  will be  $\sim k_t^{ij} + k_t^j$

$$\Rightarrow \frac{\Delta k_t^{ij}}{k_t^{ij}} \to \frac{\rho k_t^j}{\rho k_t^{ij}} = \mathcal{O}(1)$$

$$p_i = z\tilde{p}_{ij} + (1-z)y\tilde{p}_k + k_{\perp}$$
  
 $p_j = (1-z)\tilde{p}_{ij} + zy\tilde{p}_k - k_{\perp}$   
 $p_k = (1-y)\tilde{p}_k$ .



# analytic proof of accuracy

$$\Lambda^\mu_{~\nu}(K,\tilde K)=g^\mu_\nu+\tilde K^\mu A_\nu+X^\mu B_\nu$$
 vanishes in soft limit

work out 
$$ho o 0$$
 limit:

$$\text{work out } \rho \to 0 \text{ limit:} \quad A^{\nu} \xrightarrow{\rho \to 0} 2 \, \frac{\tilde{K}X}{\tilde{K}^2} \, \frac{\tilde{K}^{\nu}}{\tilde{K}^2} - \frac{X^{\nu}}{\tilde{K}^2} \,, \qquad \text{and} \qquad B^{\nu} \xrightarrow{\rho \to 0} \frac{\tilde{K}^{\nu}}{\tilde{K}^2}$$

$$B^{\nu} \stackrel{\rho \to 0}{\longrightarrow} \frac{K^{\nu}}{\tilde{K}^2}$$

apply to soft momentum  $p_i$ :

$$\frac{\Delta p_l^{0,3}}{p_l^{0,3}} \sim \rho^{1-\max(\xi_i, \xi_j)}$$

$$\frac{\Delta p_l^{1,2}}{p_l^{1,2}} \sim \rho^{(1-\xi_l)(\max(\xi_i,\xi_j)-\xi_l)}$$

compare to 
$$\Delta k_t \sim \mathcal{O}(1) \Rightarrow \frac{\Delta k_t}{k_t}$$
 from local dipole scheme

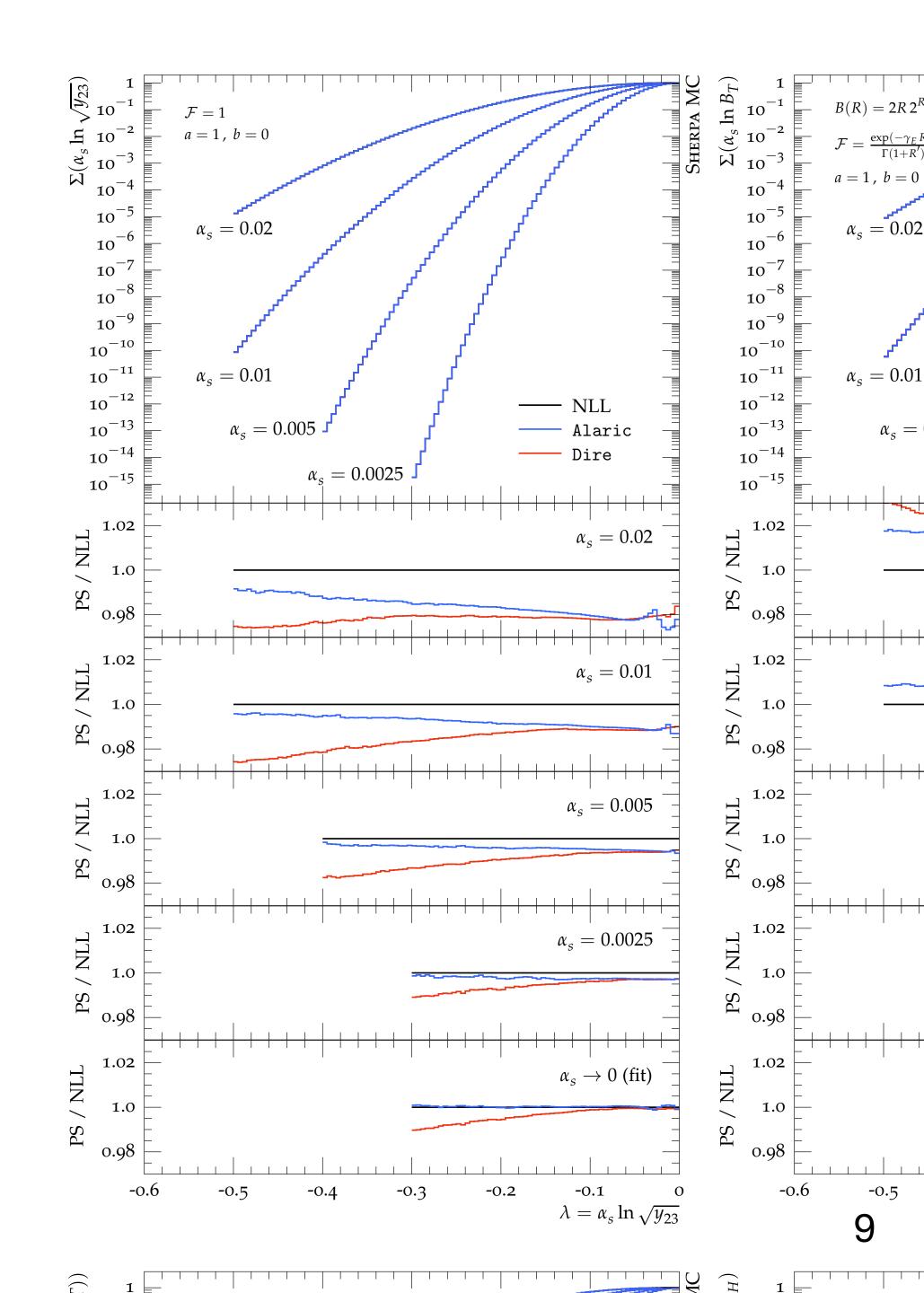
### numerical validation

• Limit  $\alpha_{\scriptscriptstyle S} \to 0$  with  $\lambda = \alpha_{\scriptscriptstyle S} L = {\rm const.}$  of

$$\frac{\Sigma^{\text{Shower}}}{\Sigma^{\text{NLL}}} \sim \exp\left(f_{\text{Shower}}^{LL} - Lg_1(\alpha_s^n L^n)\right) \\ \times \exp\left(f_{\text{Shower}}^{NLL} - g_2(\alpha_s^n L^n)\right) \\ \times \exp\left(\mathcal{O}(\alpha_s^{n+1} L^n)\right) \\ \rightarrow 1 \quad \text{if shower reproduces}$$

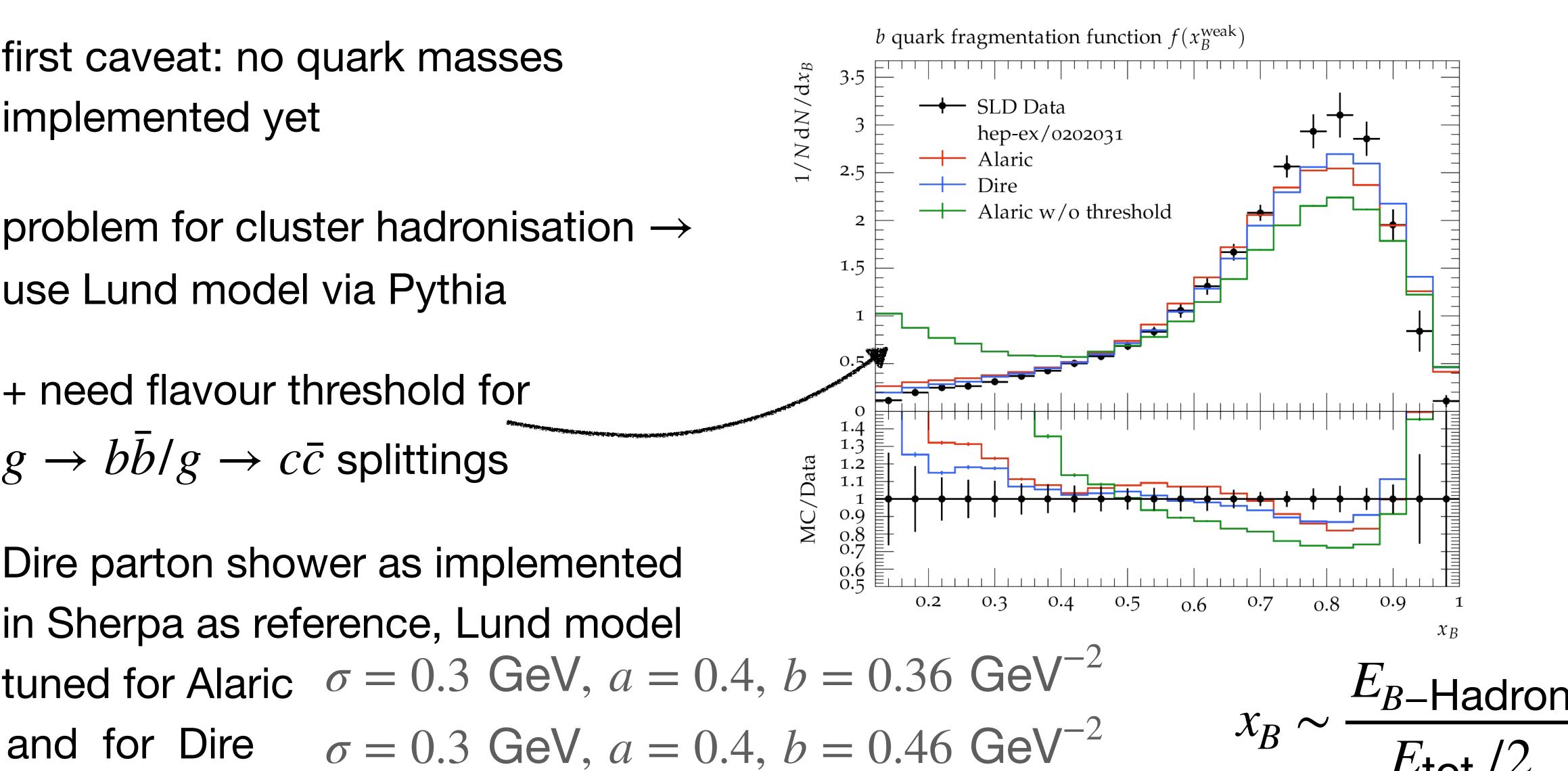
LL, NLL logs

• Observable: jet resolution  $y_{23}$  in Cambridge jet measure,  $\mathscr{F}=1\to \text{only largest}$  emission matters, check that additional shower emissions vanish

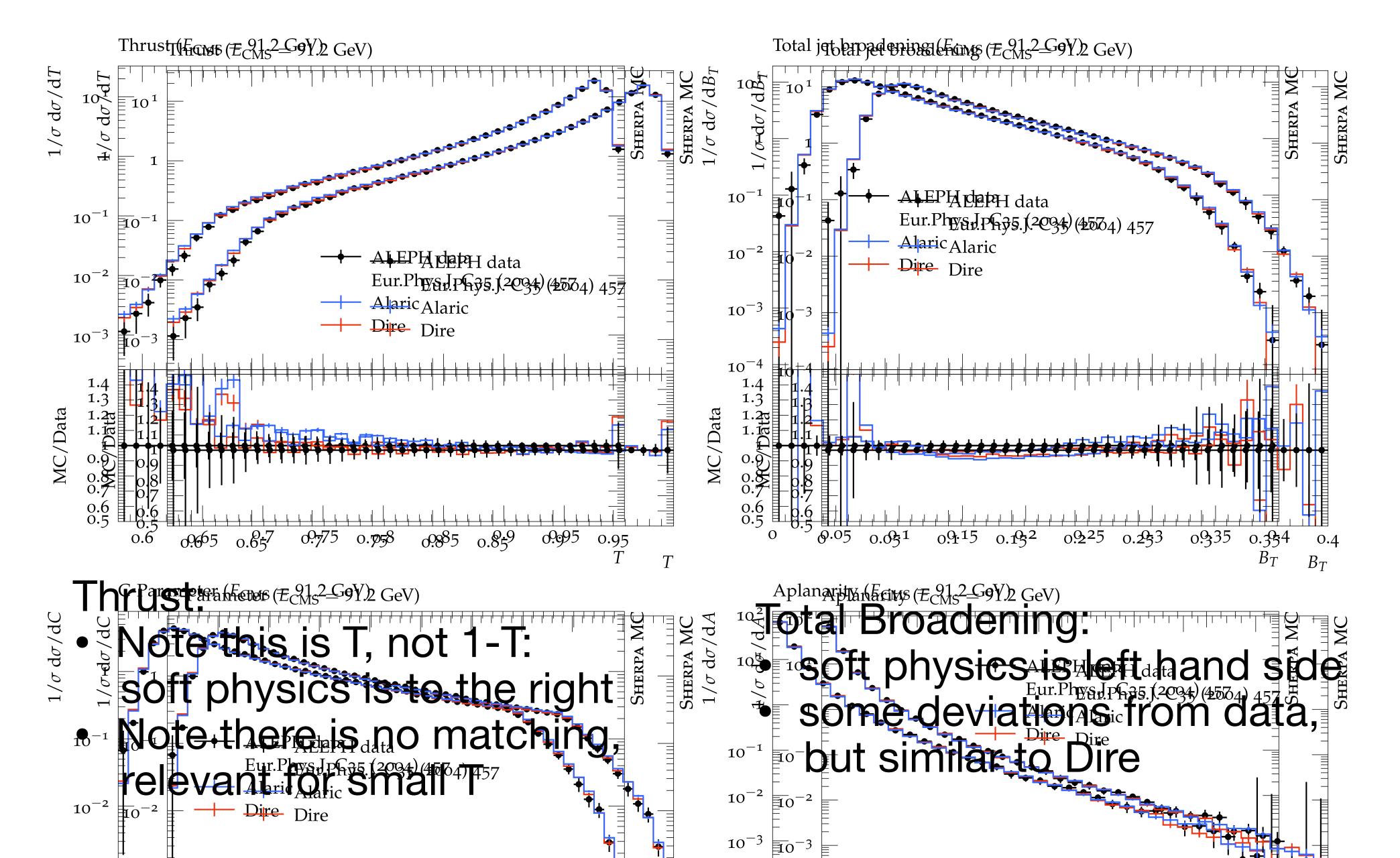


# pheno, details and b fragmentation

- first caveat: no quark masses implemented yet
- problem for cluster hadronisation → use Lund model via Pythia
- + need flavour threshold for  $g \to bb/g \to c\bar{c}$  splittings
- Dire parton shower as implemented in Sherpa as reference, Lund model tuned for Alaric  $\sigma = 0.3$  GeV, a = 0.4, b = 0.36 GeV<sup>-2</sup>

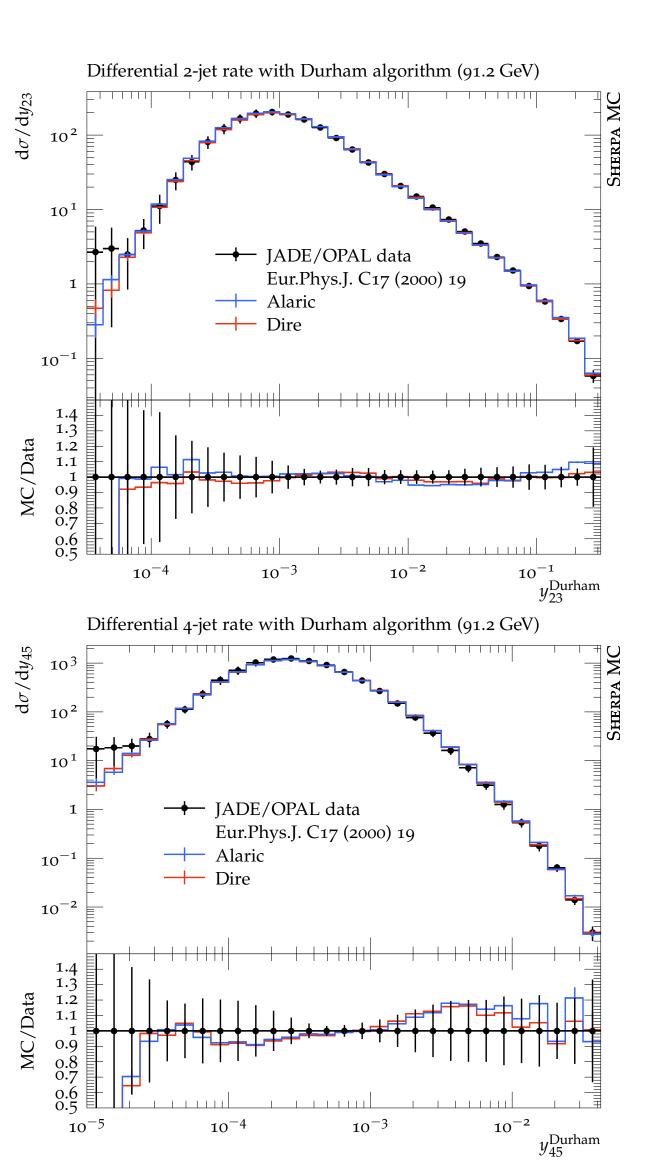


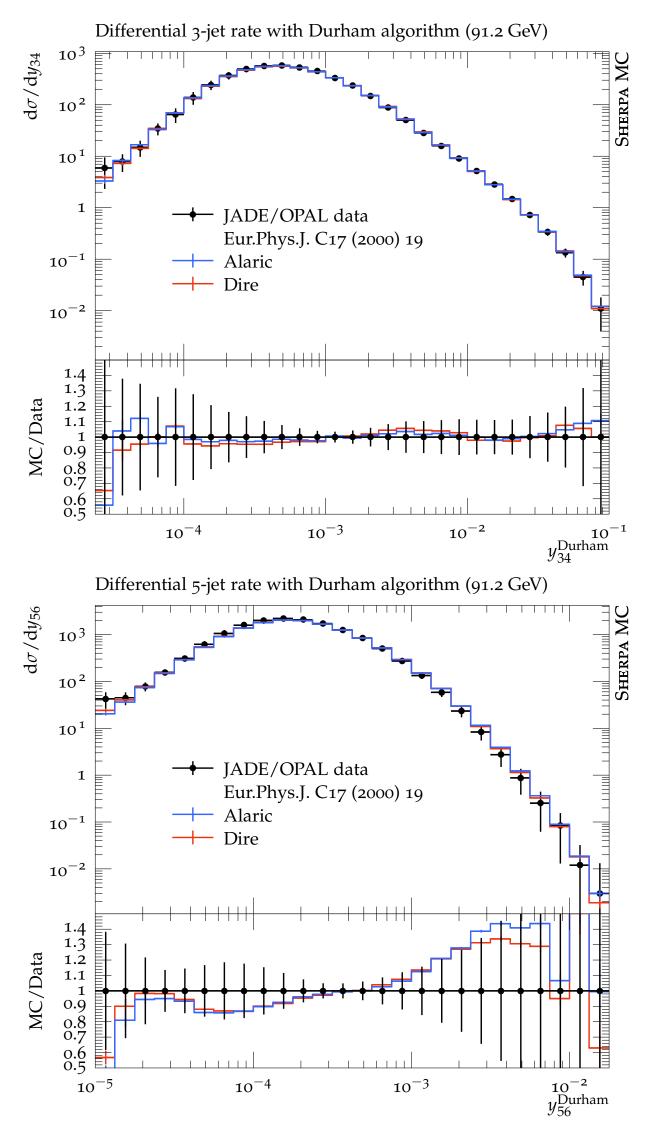
# pheno, LEP observables



## pheno, LEP observables

- Durham resolution scales  $y_{n,n+1} \sim k_t^2/Q^2$
- higher Born multiplicities → sensitivity to multiple emissions increased
- again, note no matching/merging involved

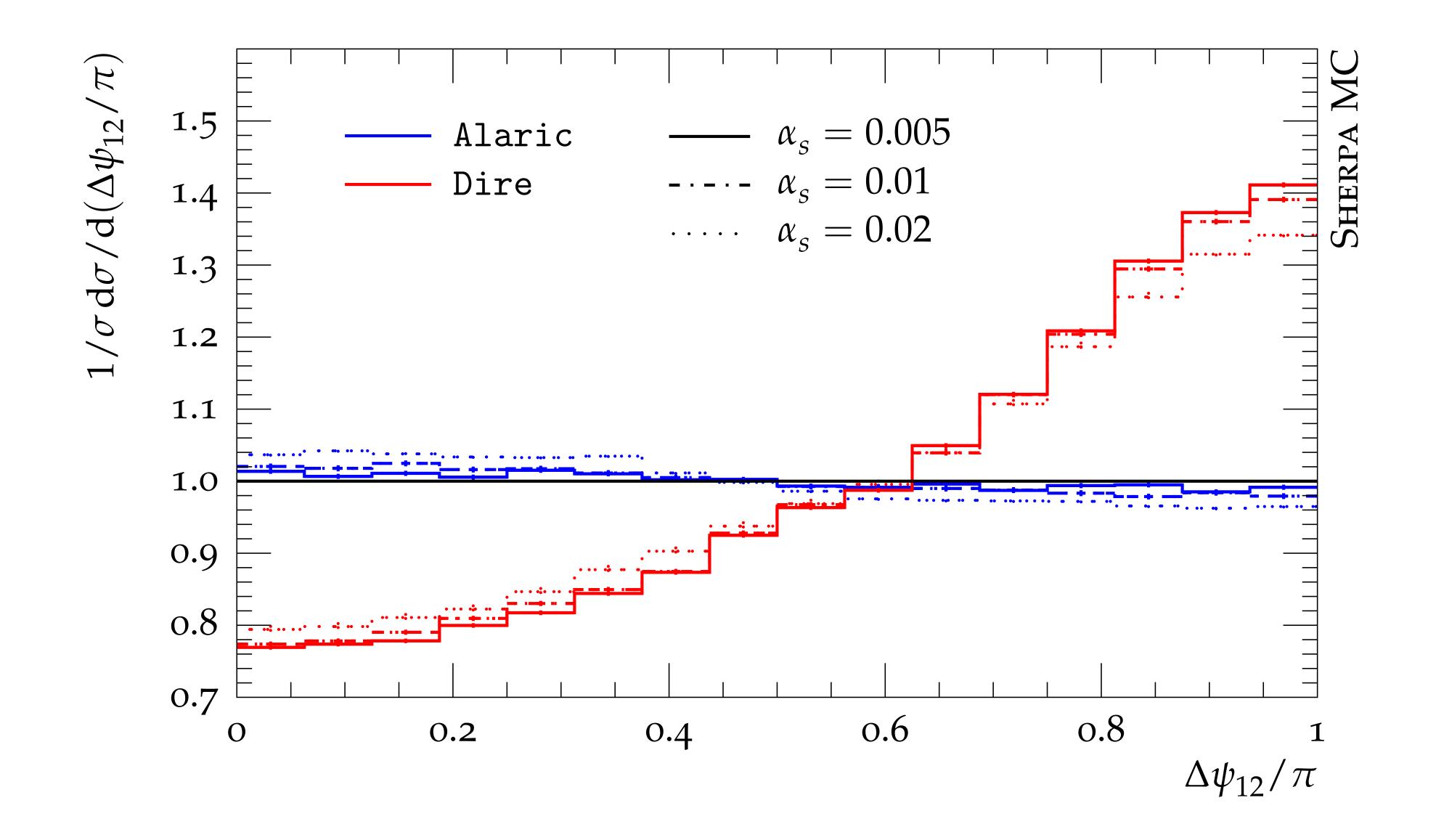




## A Logarithmically Accurate Resummation In C++

- NLL resummation in CAESAR formalism as definition and validation of parton shower accuracy
- New parton shower Alaric
  - partial fractioning of eikonal → positive definite splitting function with full phase space coverage
  - global kinematics scheme enables analytic proof of NLL accuracy
     + numerical validation
  - included in Sherpa framework and first pheno results

# Backup



### Alaric numerical validation

